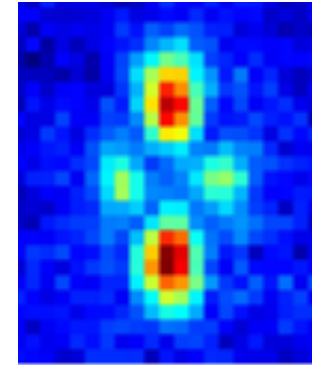
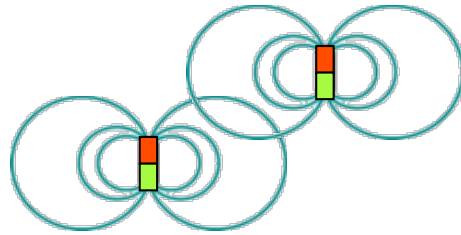
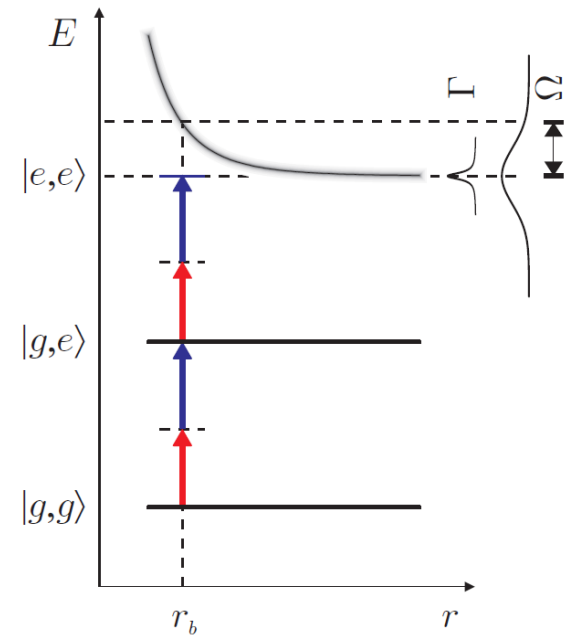
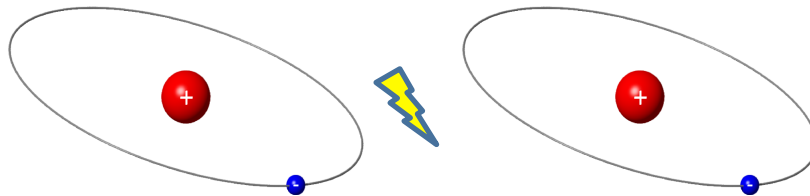


# Lecture I: (magnetic) dipolar gases

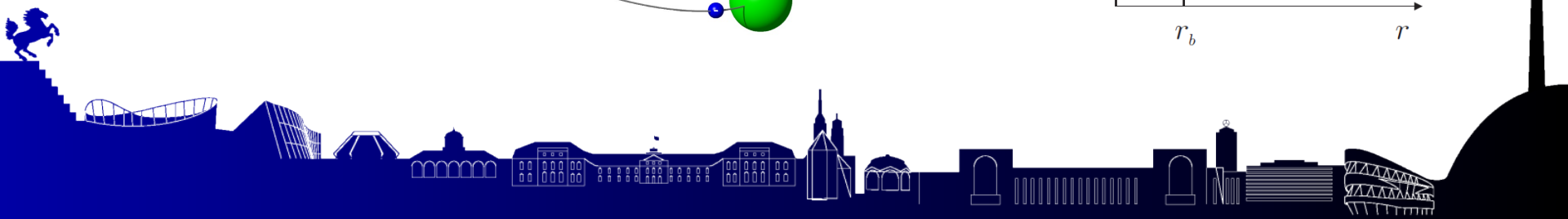
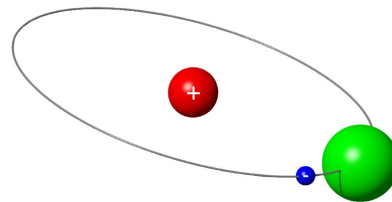


# Lecture II: Rydberg Rydberg interaction



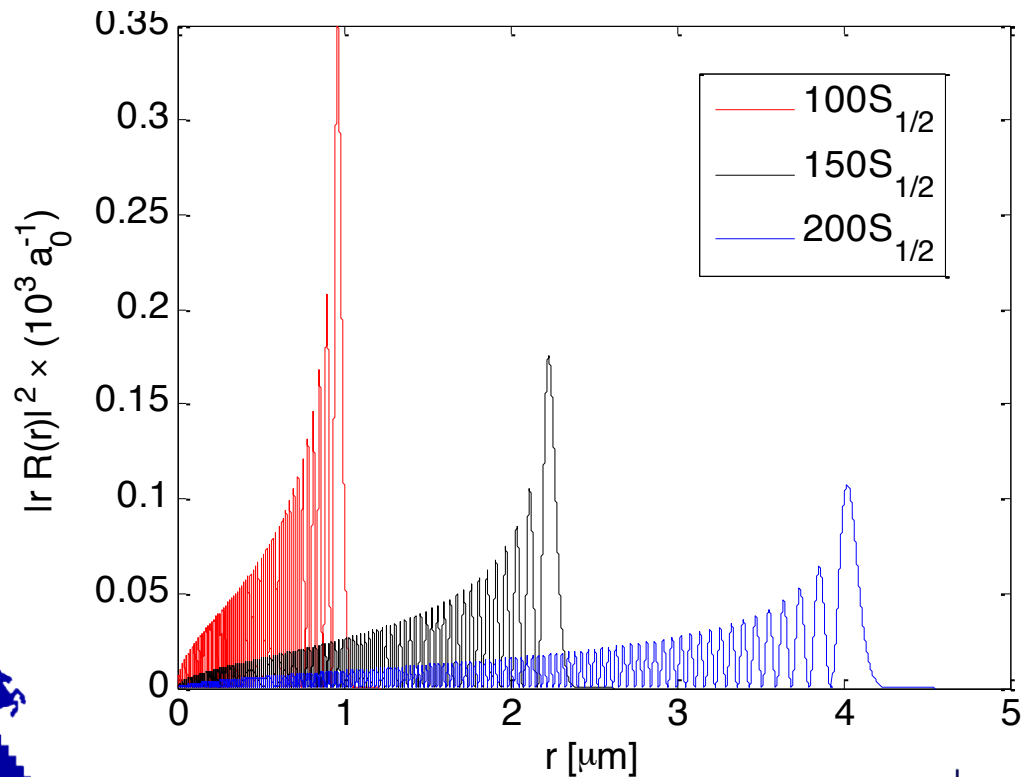
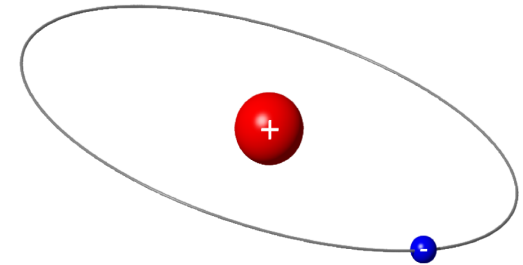
# Lecture III : Rydberg ground state interaction

dimer:



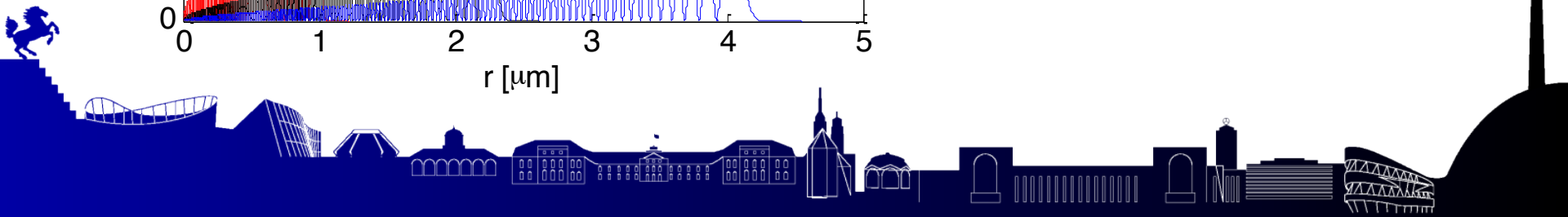
# Rydberg atoms - Size

quantity	scaling	100S-state of $^{87}\text{Rb}$
radius	$\propto n^2$	$\sim 1 \mu\text{m}$

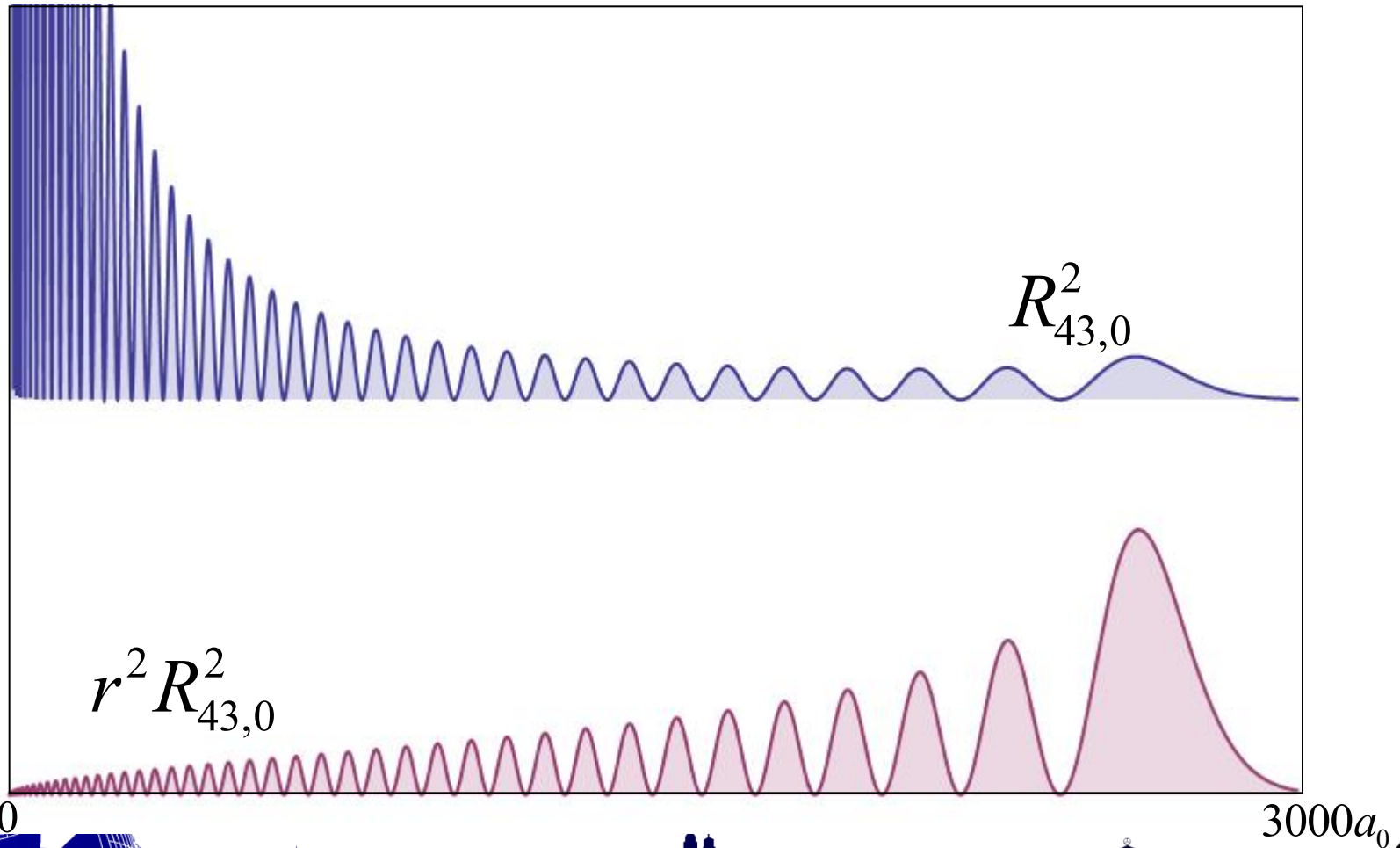


Size of Rydberg atom  $> 1 \mu\text{m}$

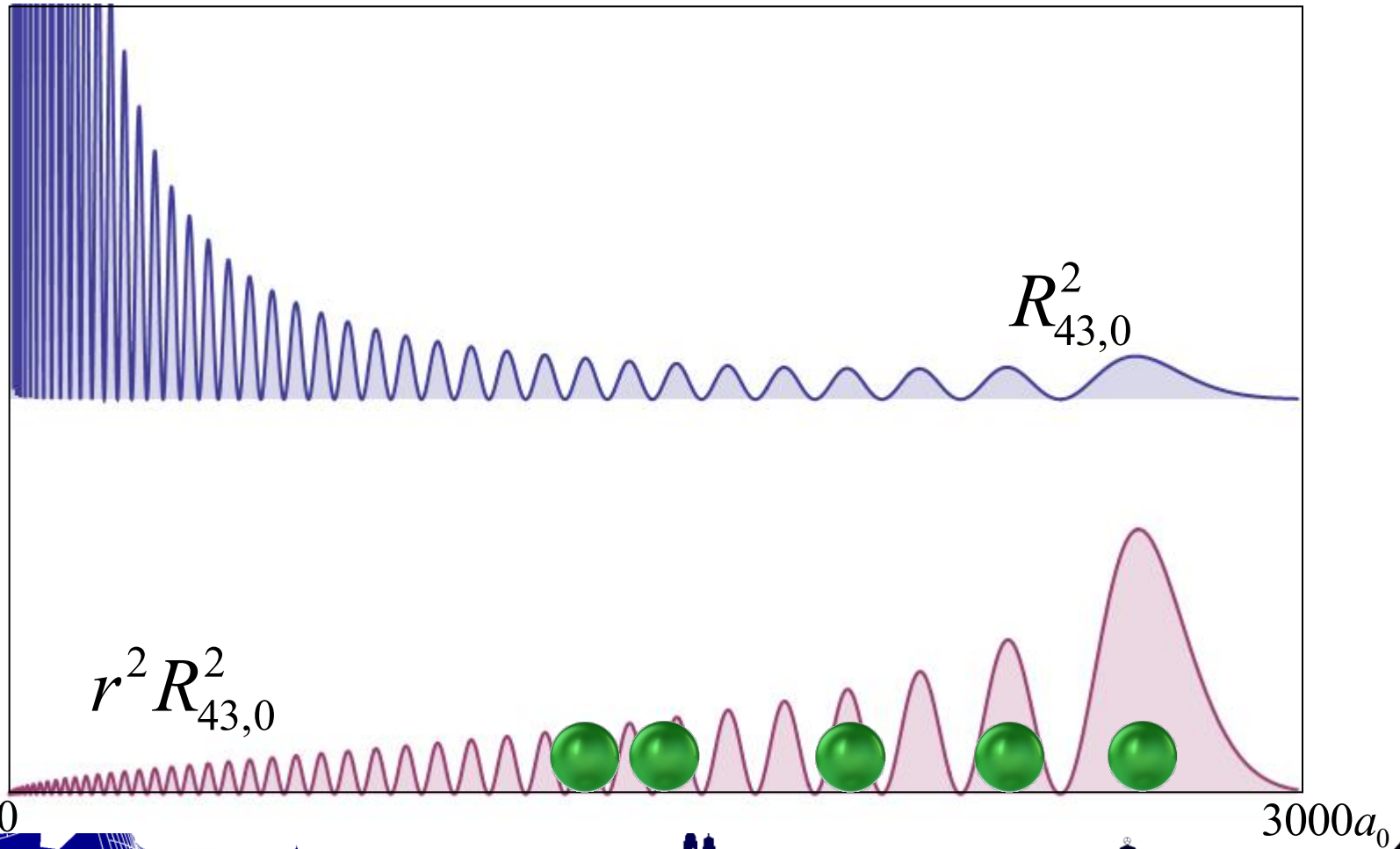
for  $n > 100$



# Rydberg electron interacting with ground state atoms

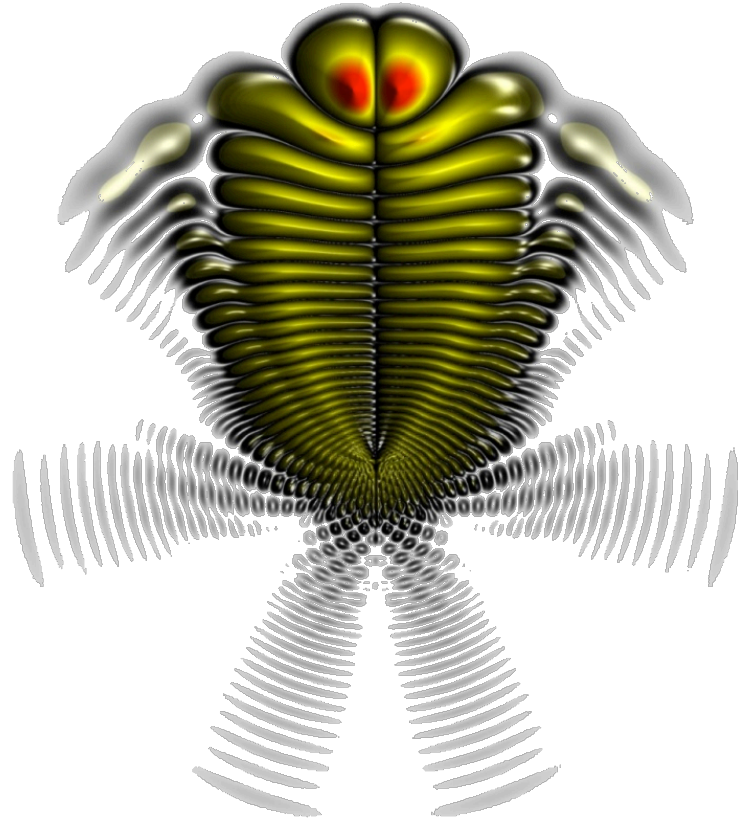


# Rydberg electron interacting with ground state atoms



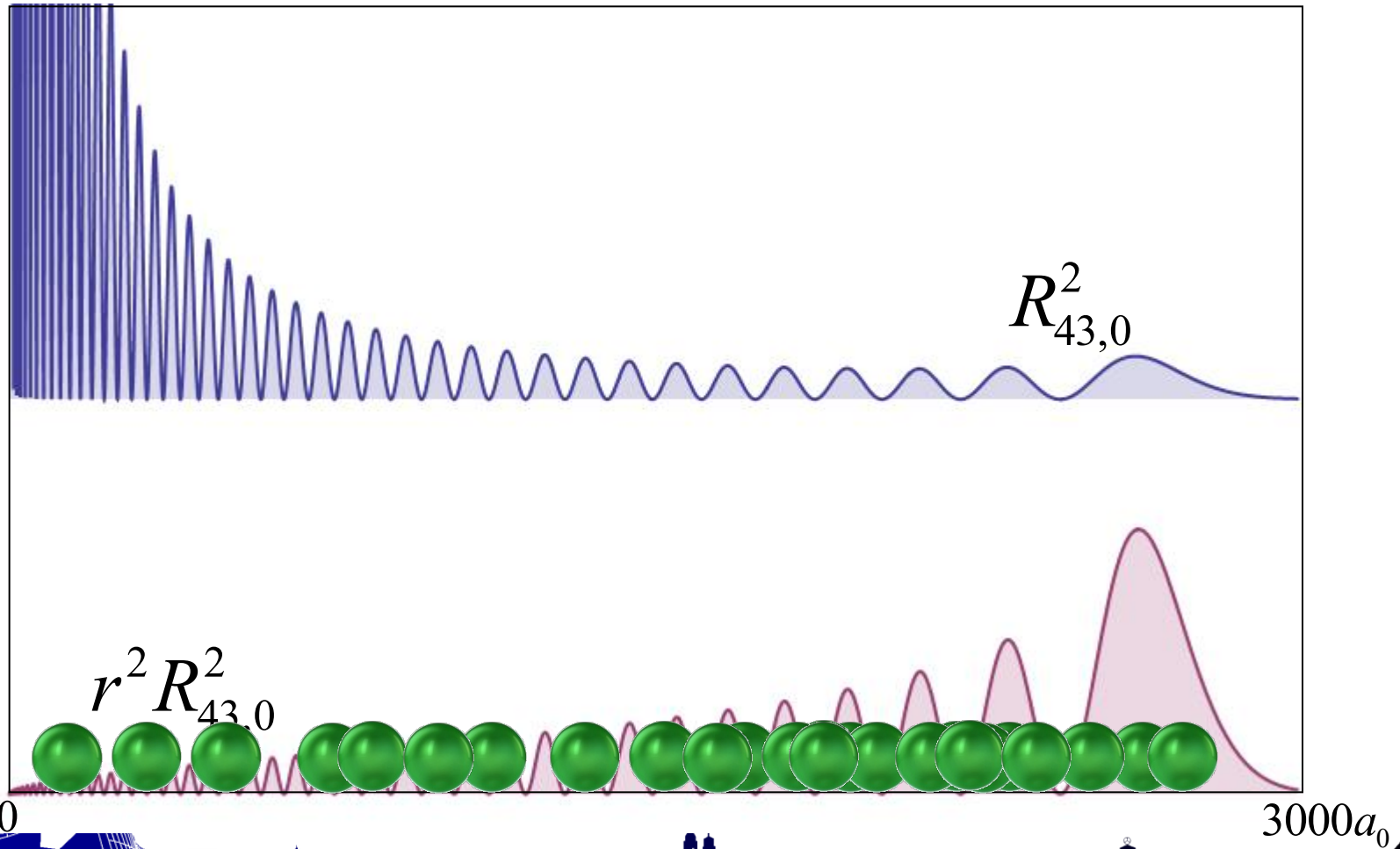
# Ultracold Rydberg Chemistry

- Giant molecules

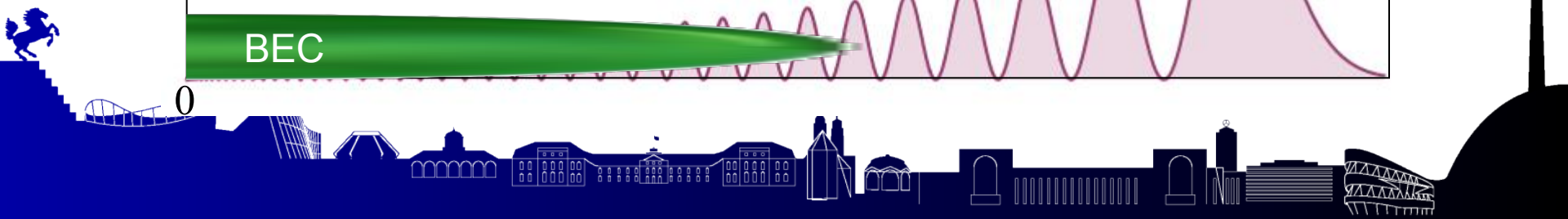
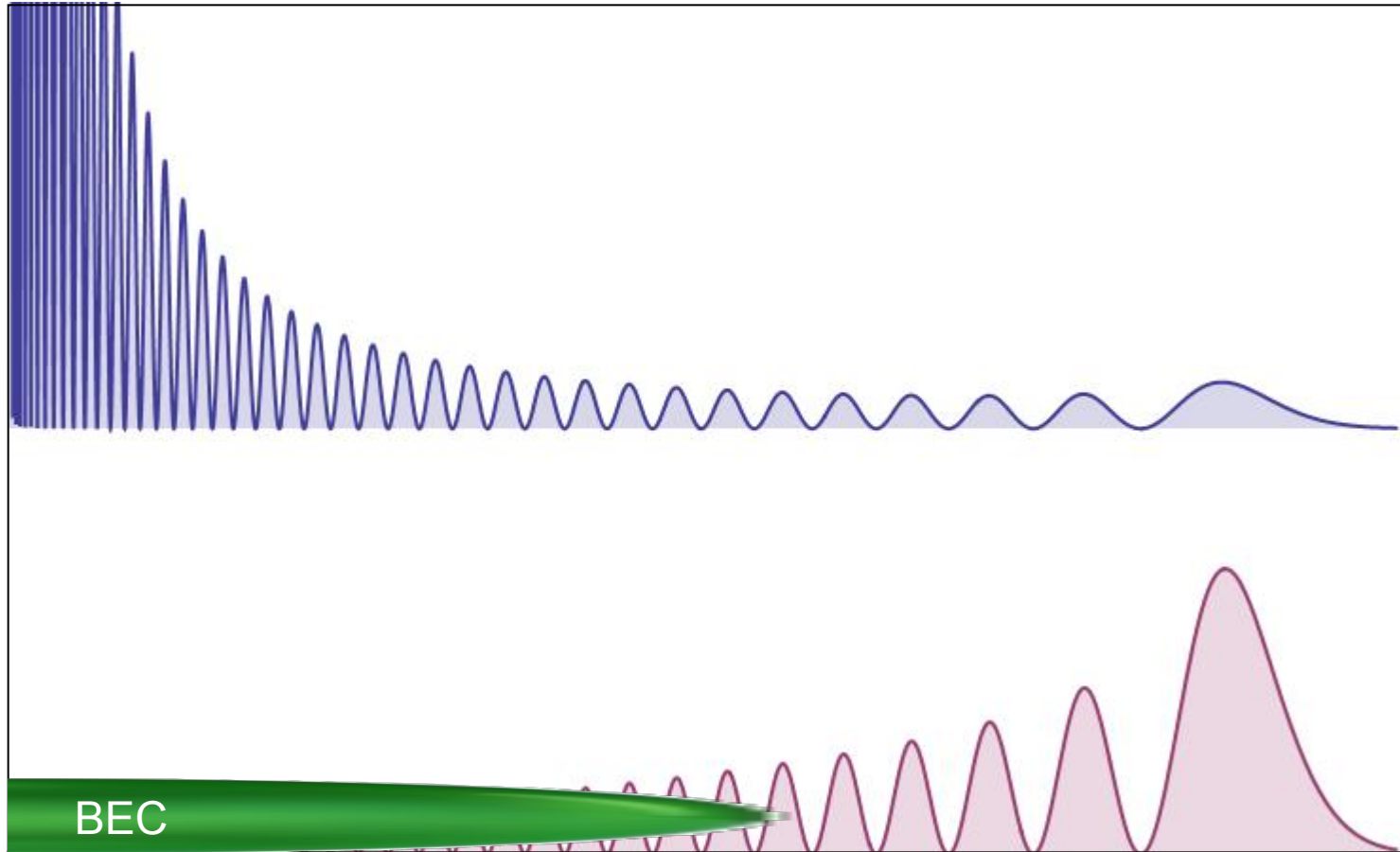


Two or few-body physics

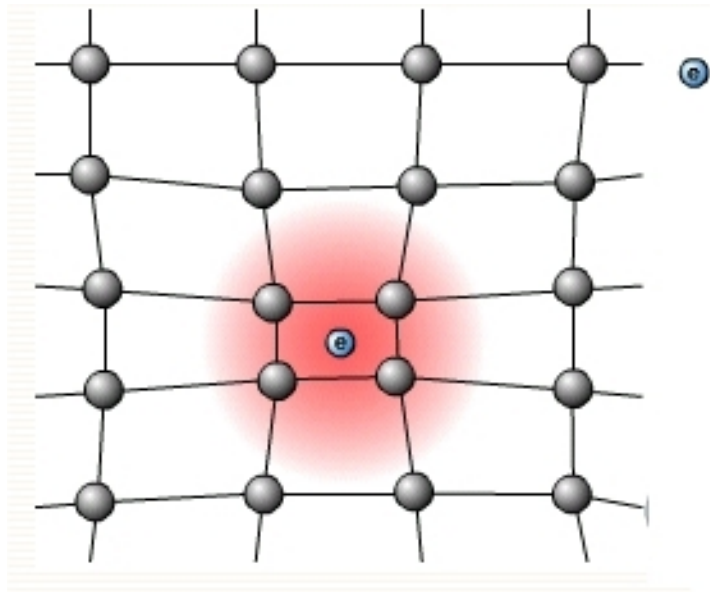
# Rydberg electron interacting with ground state atoms



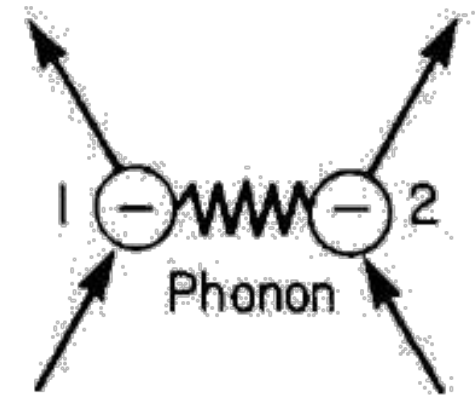
# Ultimately: one electron bound by a charged BEC



# Single electron in a quantum gas



electron phonon coupling



Cooper pairs

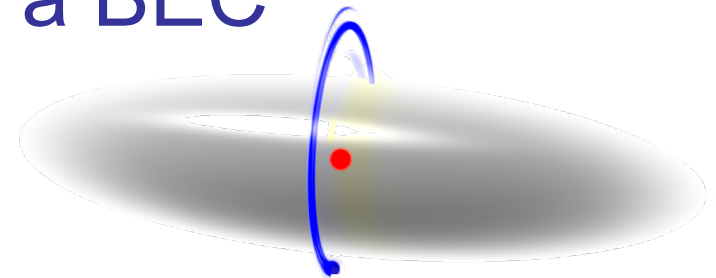
**Many**-body physics



# Outline



- History of Rydberg atoms in dense gases
- How Rydberg electrons catch atoms
- Single Rydberg electron in a BEC



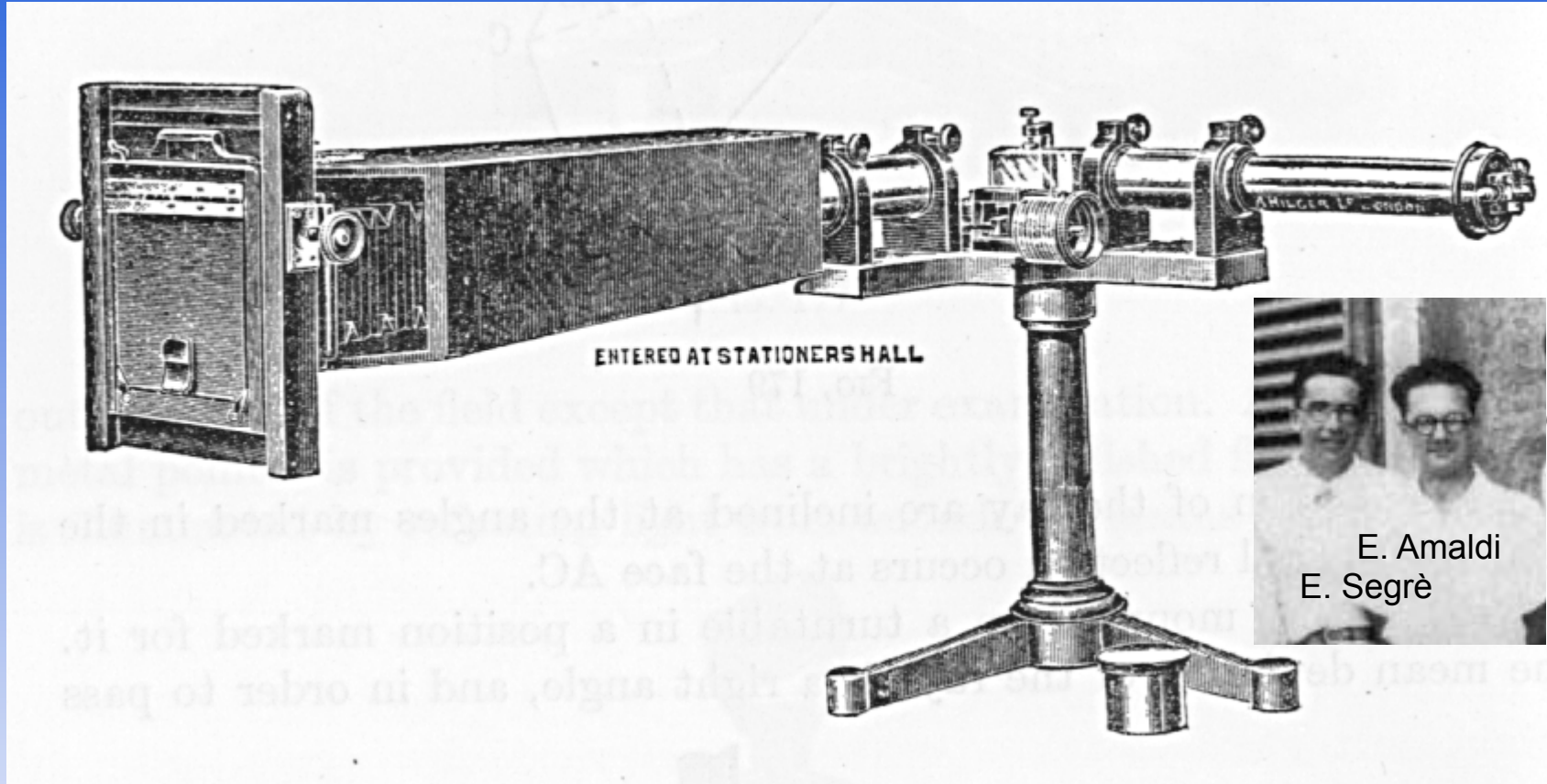


## The group of Rome

Oscar D'Agostino  
Emilio Segrè,  
Edoardo Amaldi  
Franco Rasetti  
Enrico Fermi



# History of Rydberg atoms in dense gases

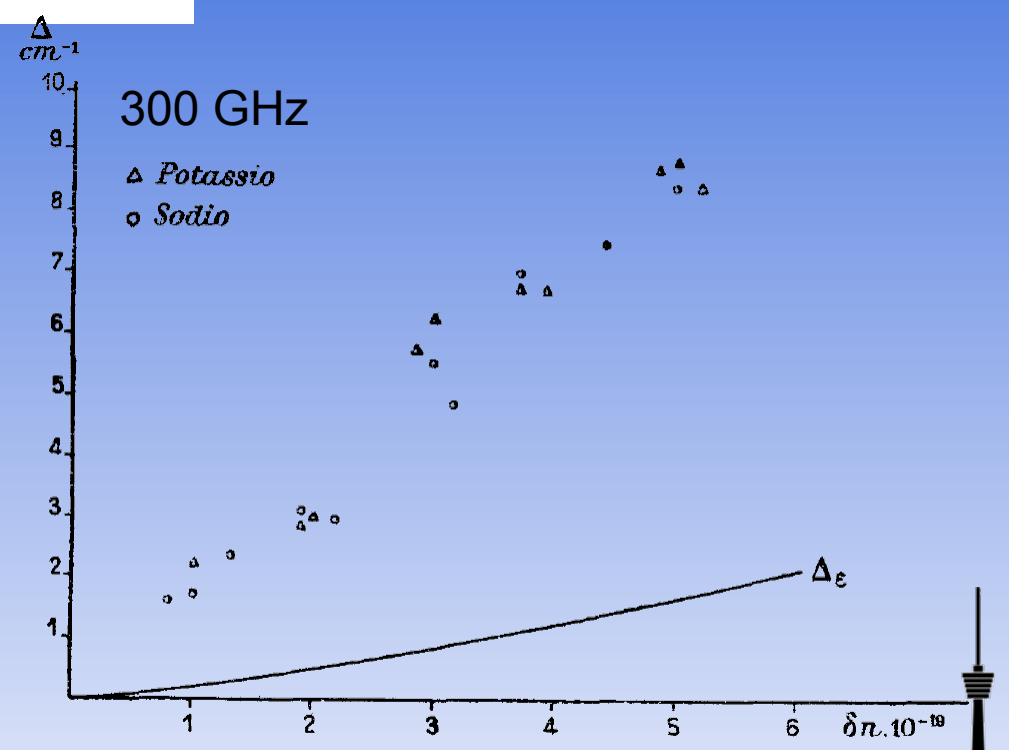
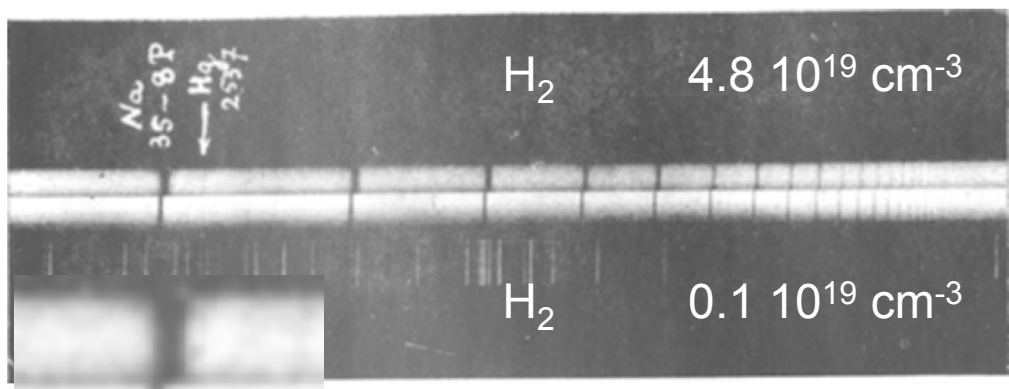


Hilger Ltd., London UK



# EFFETTO DELLA PRESSIONE SUI TERMINI ELEVATI DEGLI ALCALINI

Nota di E. AMALDI ed E. SEGRÈ (\*)



$H_2$	...	4,80	$cm^{-1}$	$\nu$
$N_2$	...	0,00	»	
$He$	...	5,15	»	$\nu$
$A$	...	11,60	»	$r$

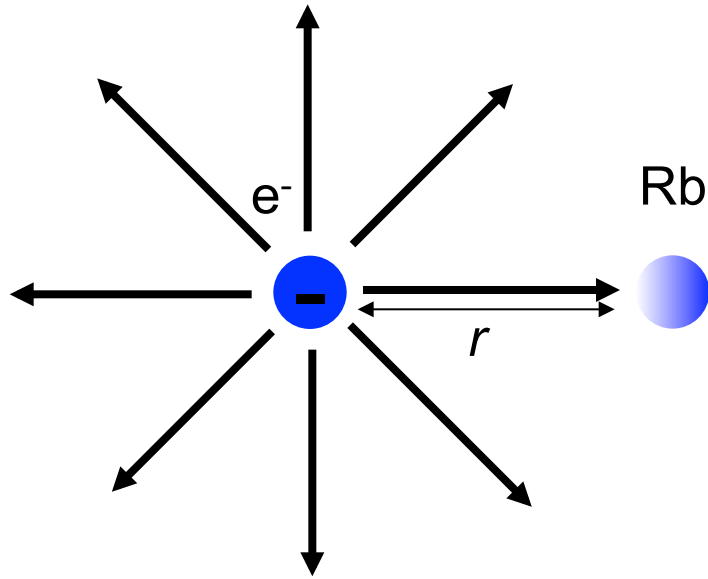
Fig. 3

Spostamento medio delle righe in funzione della concentrazione di  $H_2$

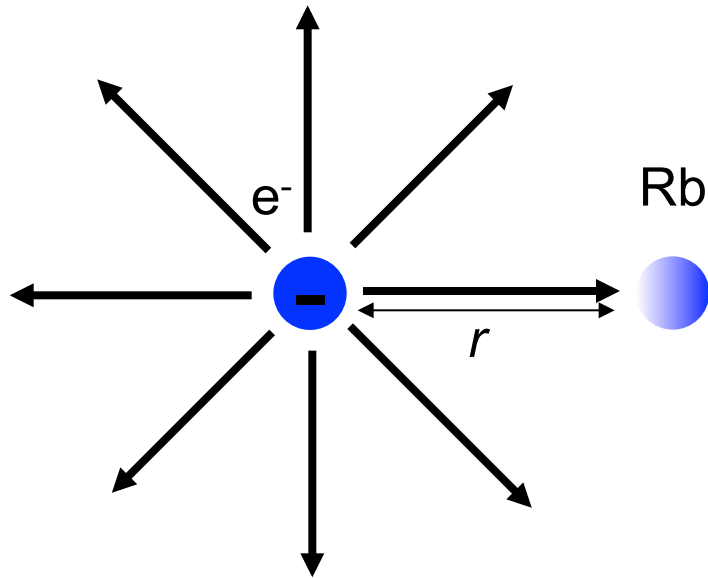
E. Amaldi, E. Segre: Nature **133**, 141 (1934), Nuovo Cimento **11**, 145 (1934)



# Interaction between a charge and a polarizable atom



# Interaction between a charge and a polarizable atom



$$\begin{aligned} V(r) &= -\vec{d} \cdot \vec{E} \\ &= -\frac{1}{2} \alpha \vec{E} \cdot \vec{E} \\ &= -\frac{1}{(4\pi\epsilon_0)^2} \frac{\alpha q^2}{2r^4} = -\frac{\alpha}{2r^4} \end{aligned}$$



# Interaction between a charge and a polarizable atom

$$V_{pseudo}(r) = 2\pi a_s \delta(r)$$

$$V(r) = -\frac{\alpha}{2r^4}$$

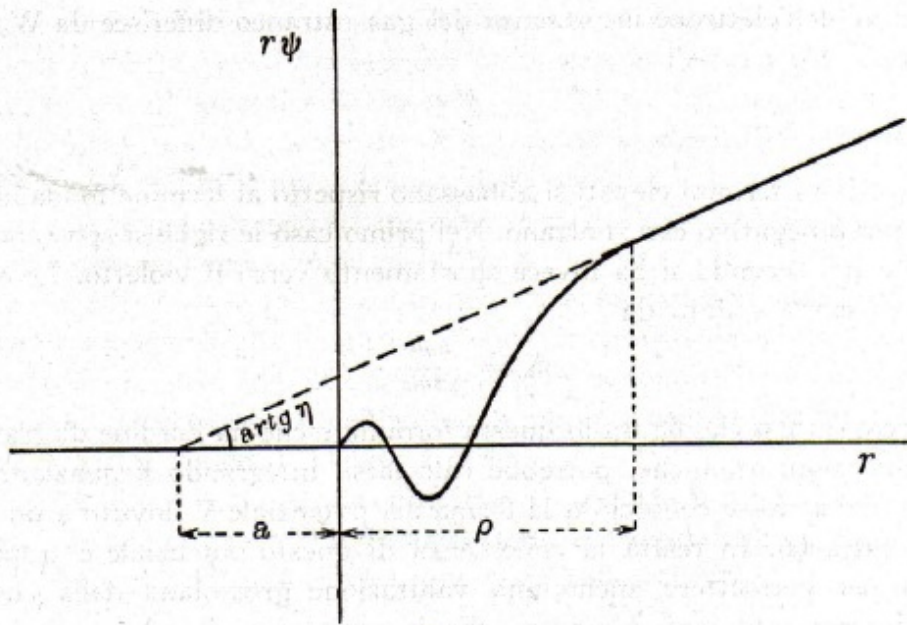


Fig. 1.

E. Fermi: Nuovo Cimento 11, 157 (1934)



# Interaction between a charge and a polarizable atom

$$V_{pseudo}(r) = 2\pi a_s \delta(r)$$

$$V(r) = -\frac{\alpha}{2r^4}$$

range of interaction

$$E_{kin}(r^*) = E_{pot}(r^*)$$

$$\frac{\hbar^2}{2\mu r^{*2}} = \frac{1}{(4\pi\epsilon_0)^2} \frac{\mu\alpha q^2}{2r^{*4}}$$

SI

a.u.

$$r^* = \sqrt{\frac{\mu\alpha q^2}{(4\pi\hbar\epsilon_0)^2}} = \sqrt{\alpha} \approx 18a_0$$

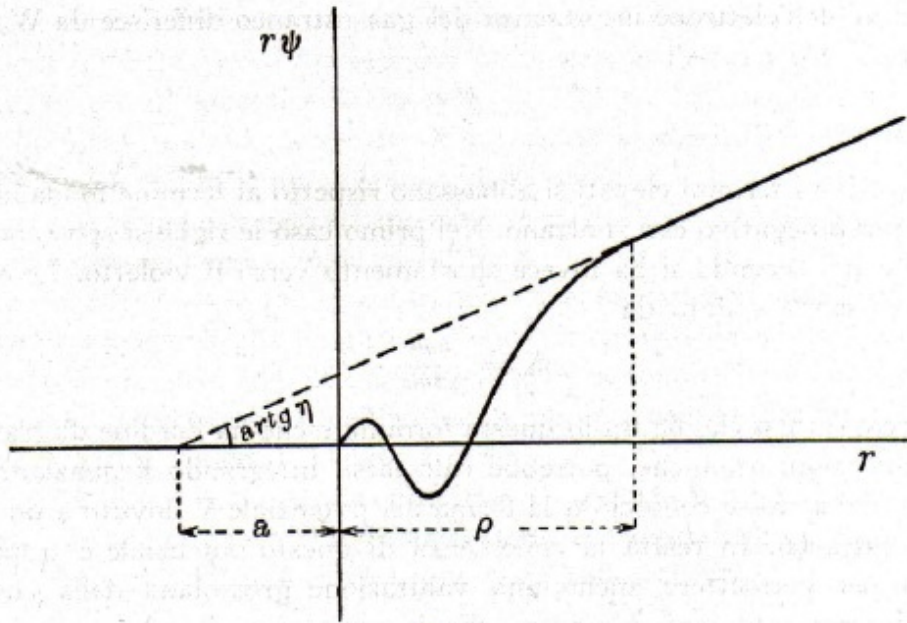


Fig. 1.

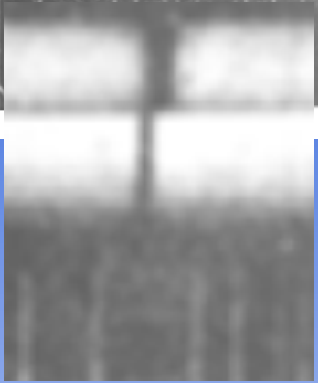
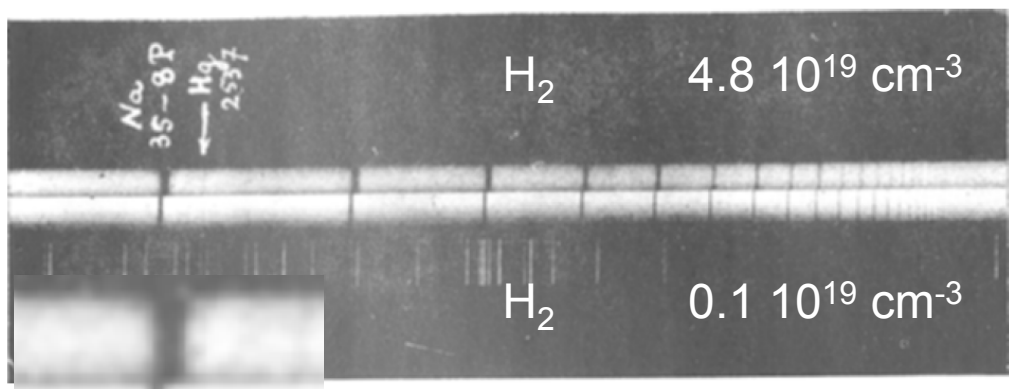
E. Fermi: Nuovo Cimento 11, 157 (1934)





# EFFETTO DELLA PRESSIONE SUI TERMINI ELEVATI DEGLI ALCALINI

Nota di E. AMALDI ed E. SEGRÈ (\*)



$H_2$	. . . . .	4,80 $cm^{-1}$	$\nu$
$N_2$	. . . . .	0,00	»
$He$	. . . . .	5,15	» $\nu$
$A$	. . . . .	11,60	» $r$

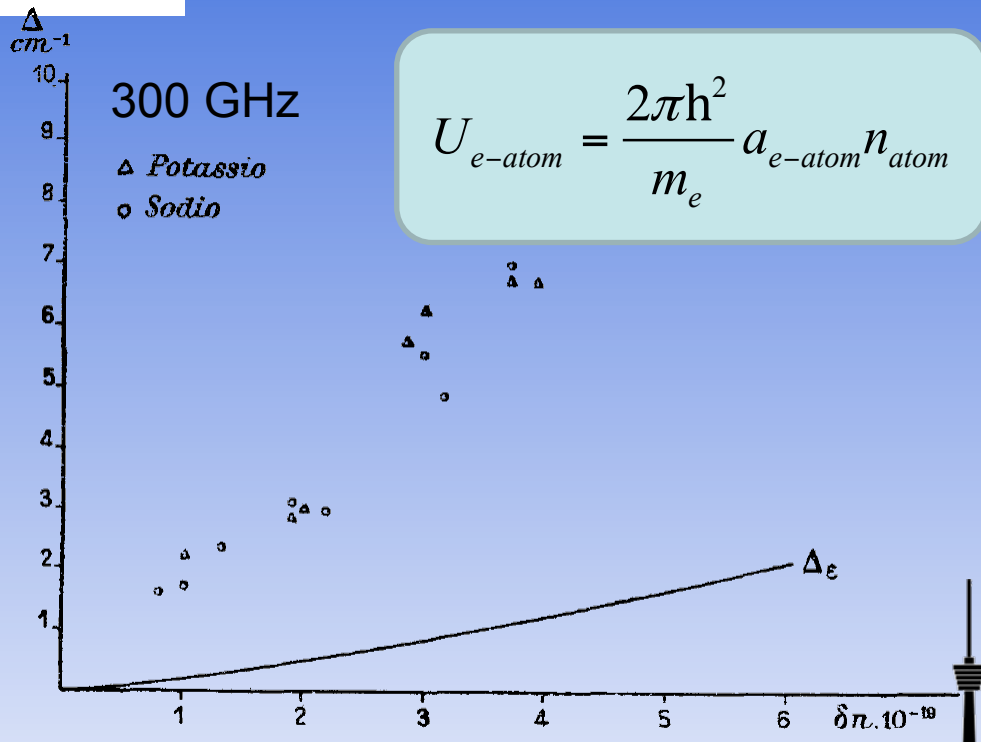


Fig. 3

Spostamento medio delle righe in funzione della concentrazione di  $H_2$

E. Amaldi, E. Segre: Nature **133**, 141 (1934), Nuovo Cimento **11**, 145 (1934)



# Verschiebung von hohen Serienlinien des Natriums und Kaliums durch Fremdgase, Berechnung der Wirkungsquerschnitte von Edelgasen gegen sehr langsame Elektronen.

Von Chr. Fichtbauer, P. Schulz und A. F. Brandt in Rostock.

Mit 4 Abbildungen. (Eingegangen am 30. Juni 1934.)

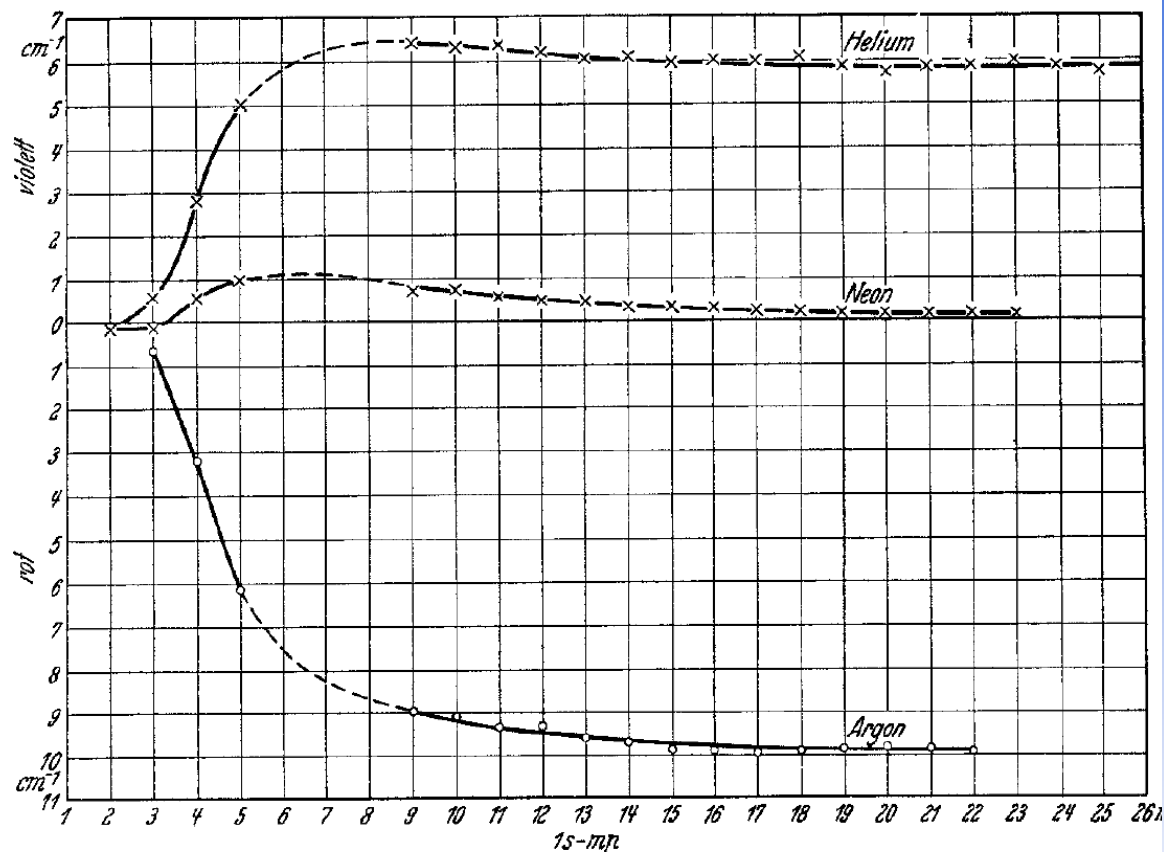
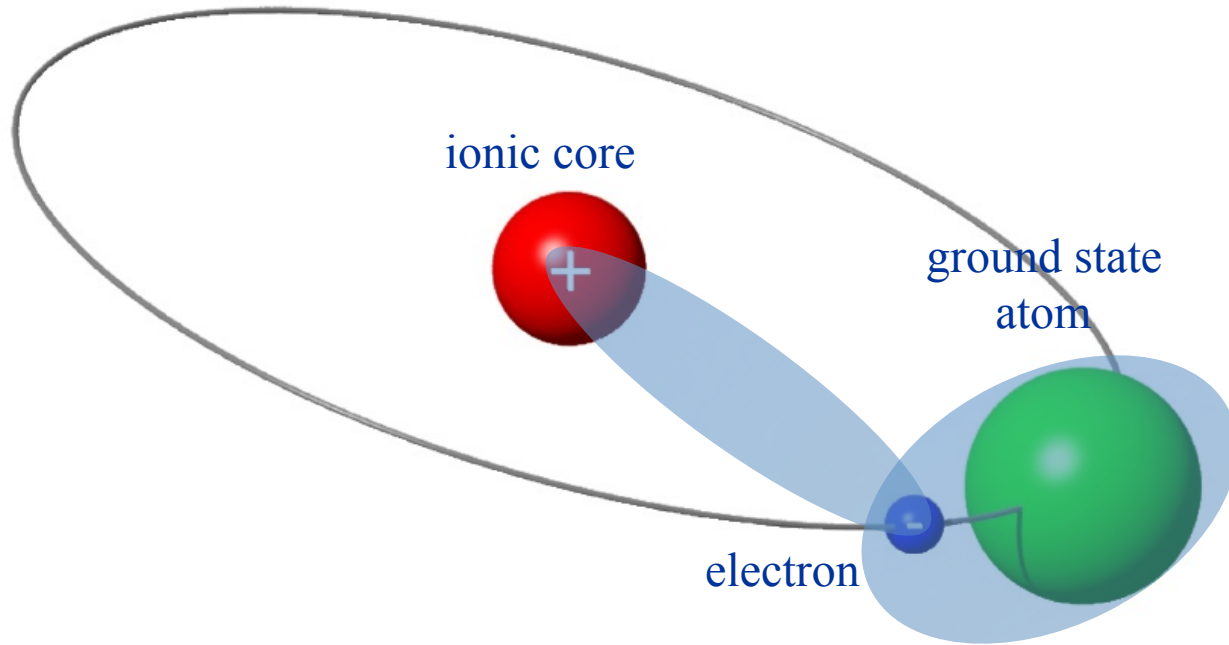


Fig. 4. Gesamtverlauf der Verschiebung bei 0° und 1 Atm. für die Cäsiumhauptserie.

$$U_{e\text{-atom}} = \frac{2\pi h^2}{m_e} a_{e\text{-atom}} n_{\text{atom}}$$



# interacting Rydberg electron



Effect on ground state atom?



# Creation of Polar and Nonpolar Ultra-Long-Range Rydberg Molecules

Chris H. Greene

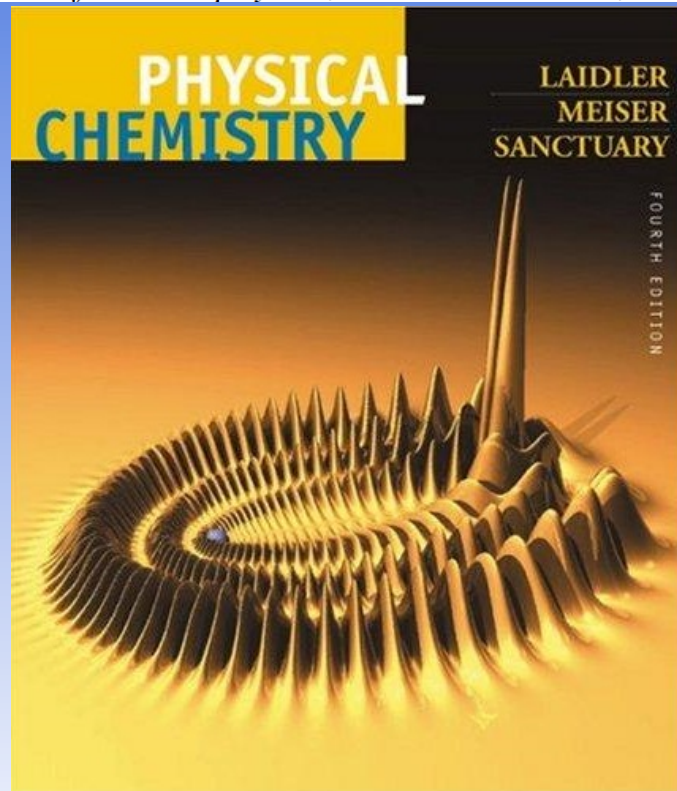
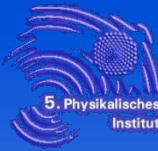
*Department of Physics and JILA, University of Colorado, Boulder, Colorado 80309-0440*

A. S. Dickinson\*

*JILA, University of Colorado, Boulder, Colorado 80309-0440*

H. R. Sadeghpour

*ITAMP, Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, Massachusetts 02138*



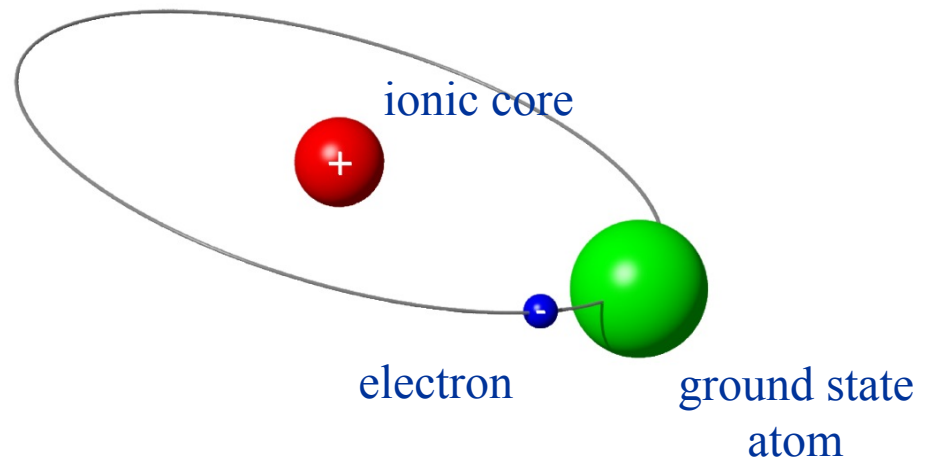
PRL **85**, 2458 (2000)



# density/pressure shift

atom effects electron

$$U_{e-atom} = \frac{2\pi\hbar^2}{m_e} a_{e-atom} n_{atom}$$



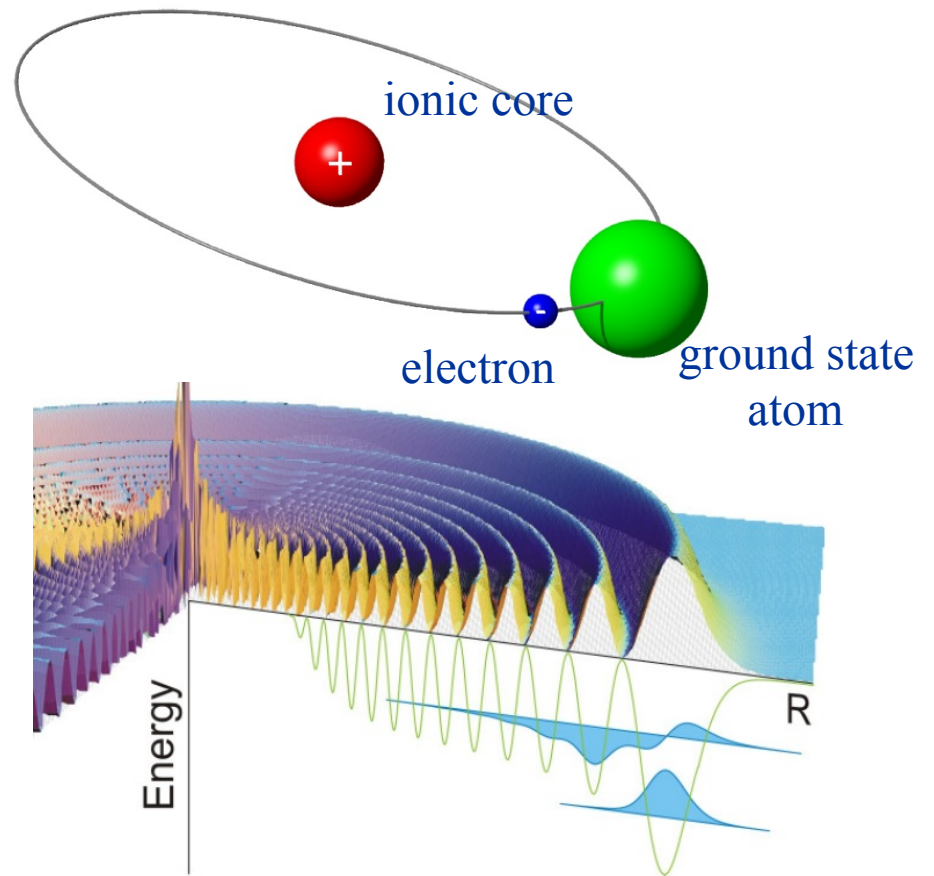
- E. Fermi, Nuovo Cimento **11**, 157 (1934).
- E. Amaldi, E. Segrè, Nuovo Cimento **11**, 145 (1934)
- A. Omont, J. Phys. France **38**, 1343 (1977)
- I. Fabrikant, J. Phys. B **19**, 1527 (1986).



# „Trilobite“ molecules

electron effects atom

$$U_{e\text{-atom}} = \frac{2\pi\hbar^2}{m_e} a_{e\text{-atom}} n_e$$

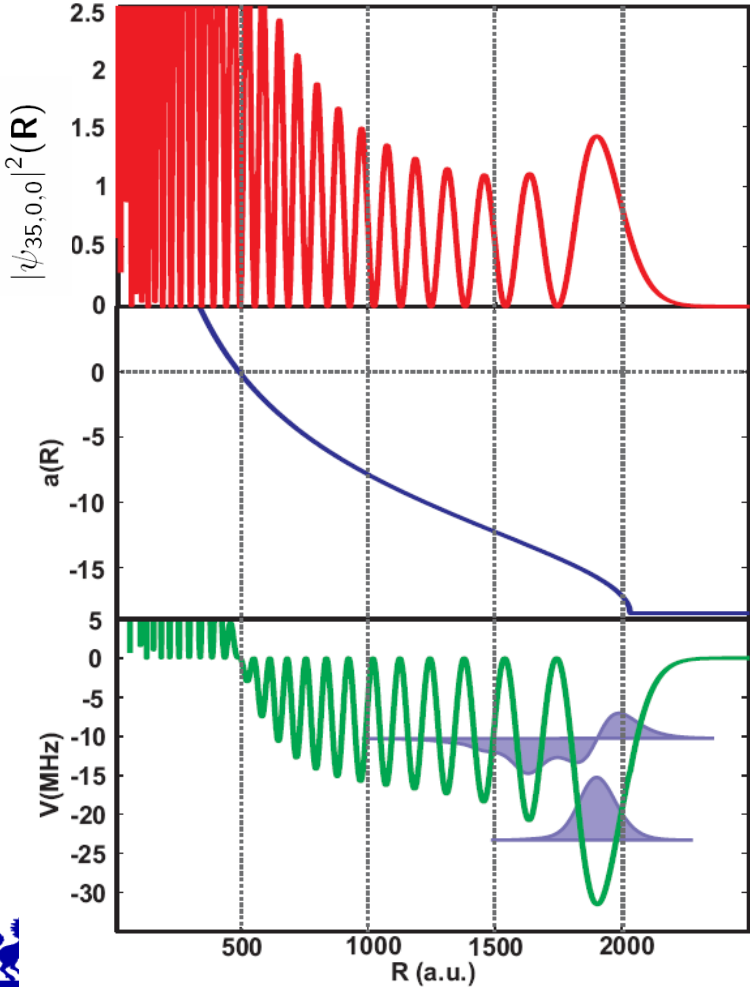
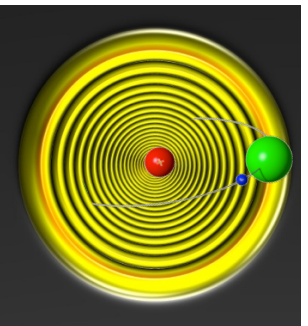


- E. Fermi, Nuovo Cimento **11**, 157 (1934).
- E. Amaldi, E. Segrè, Nuovo Cimento **11**, 145 (1934)
- A. Omont, J. Phys. France **38**, 1343 (1977)
- I. Fabrikant, J. Phys. B **19**, 1527 (1986).
- C. Greene et al. PRL **85**, 2458 (2000)



# Fermi-Greene Model

single channel



probability density

$$|\psi_{35,0,0}|^2(\mathbf{R})$$



energy-dependent scattering length

$$a[k(R)] = a_0 + \frac{\pi\alpha}{3}k(R)$$



molecular potential

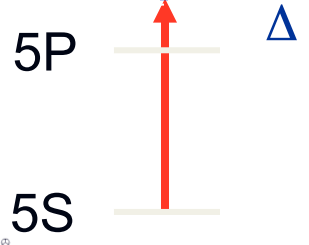
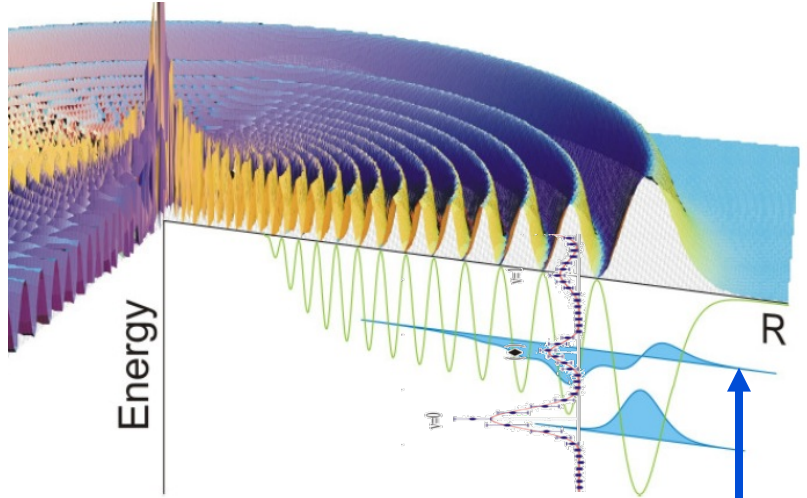
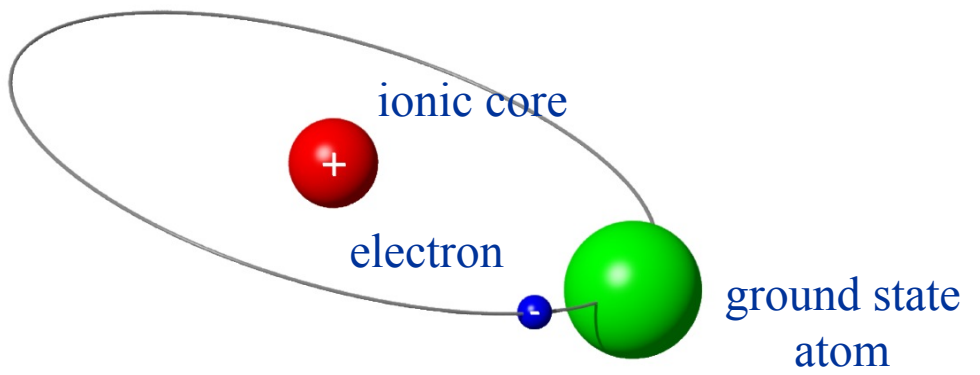
$$V_0(\mathbf{R}) = 2\pi a[k(\mathbf{R})] |\Psi_{35,0,0}(\mathbf{R})|^2$$



# „Trilobite“ molecules

electron effects atom

$$U_{e-atom} = \frac{2\pi\hbar^2}{m_e} a_{e-atom} n_e$$

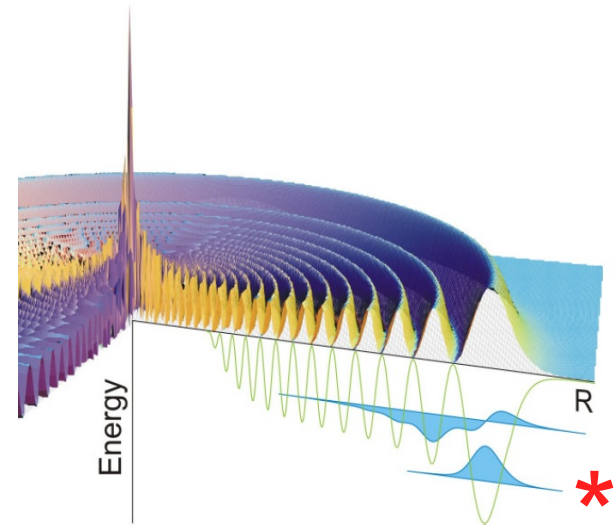
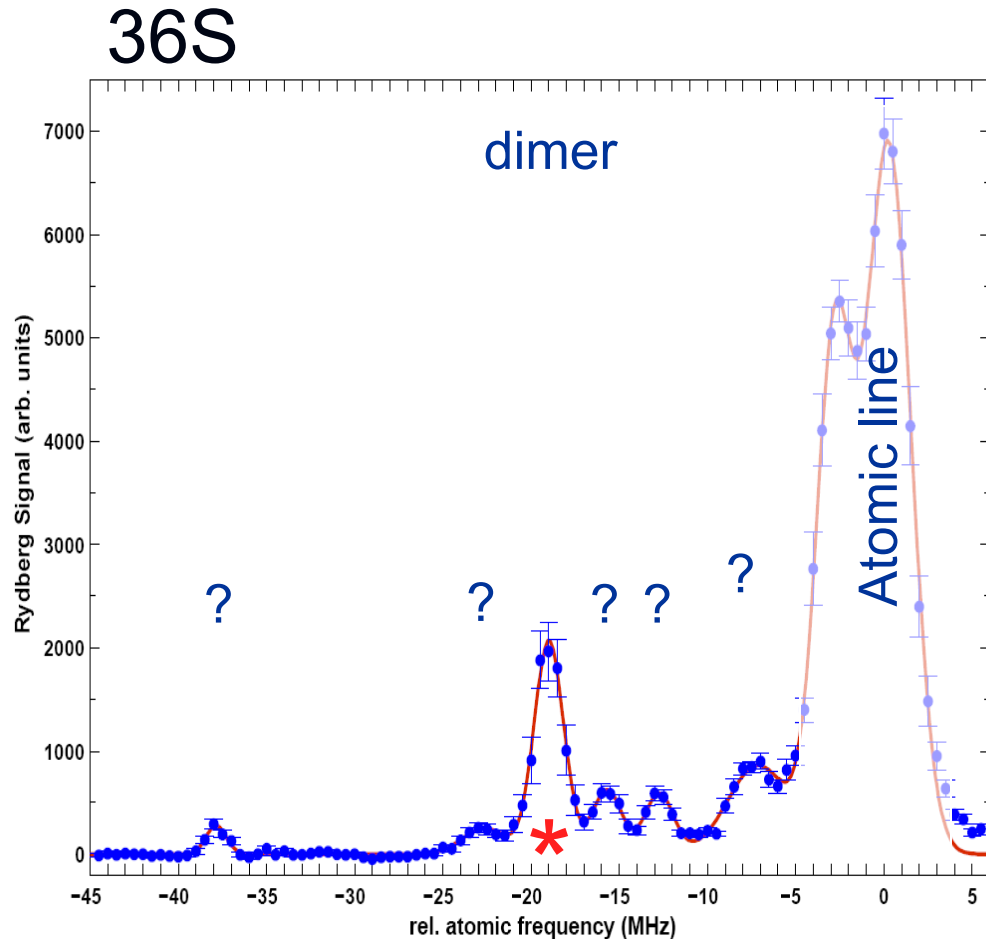


V. Bendkowsky, B. Butscher, J. Nipper,  
J. P. Shaffer, R. Löw, TP,  
*Nature* **458**, 1005 (2009)





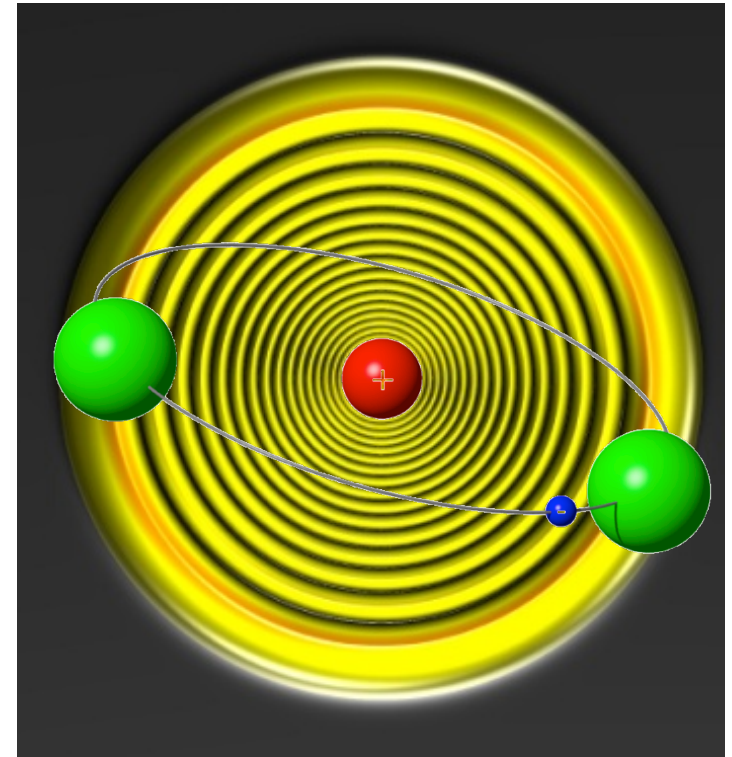
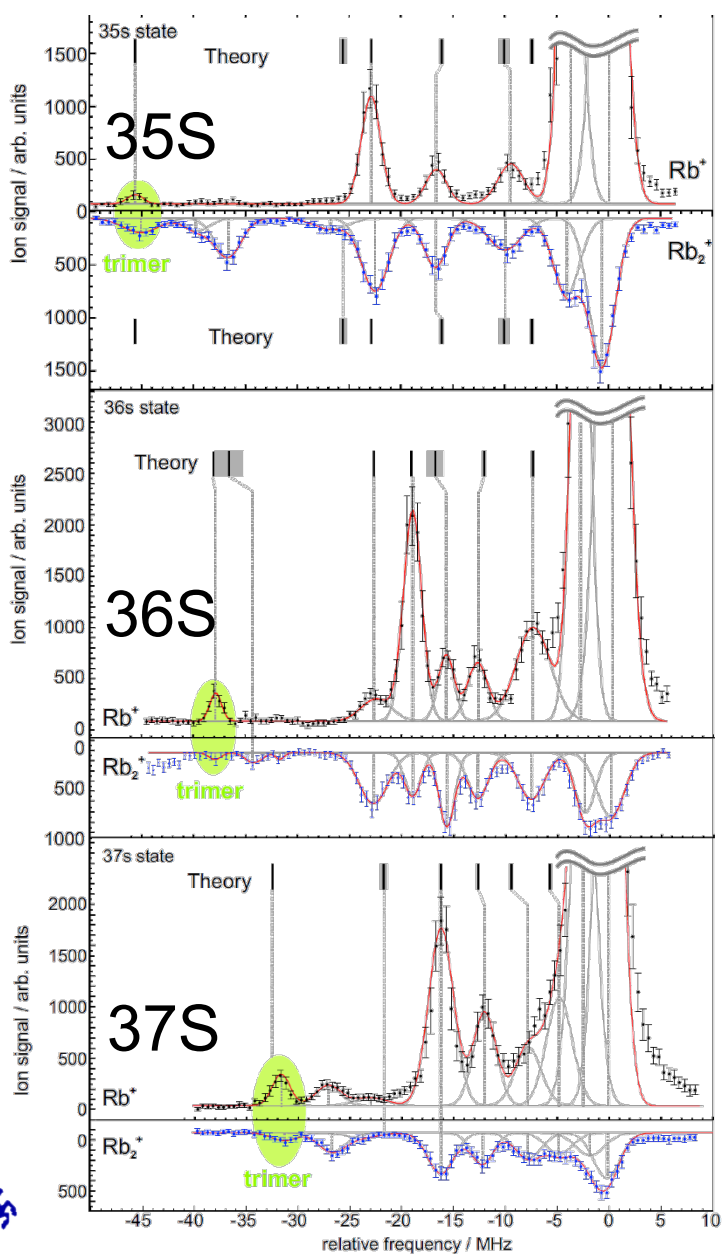
# rich molecular spectra



\* molecule bound by s wave scattering



# Ultralong-range trimers

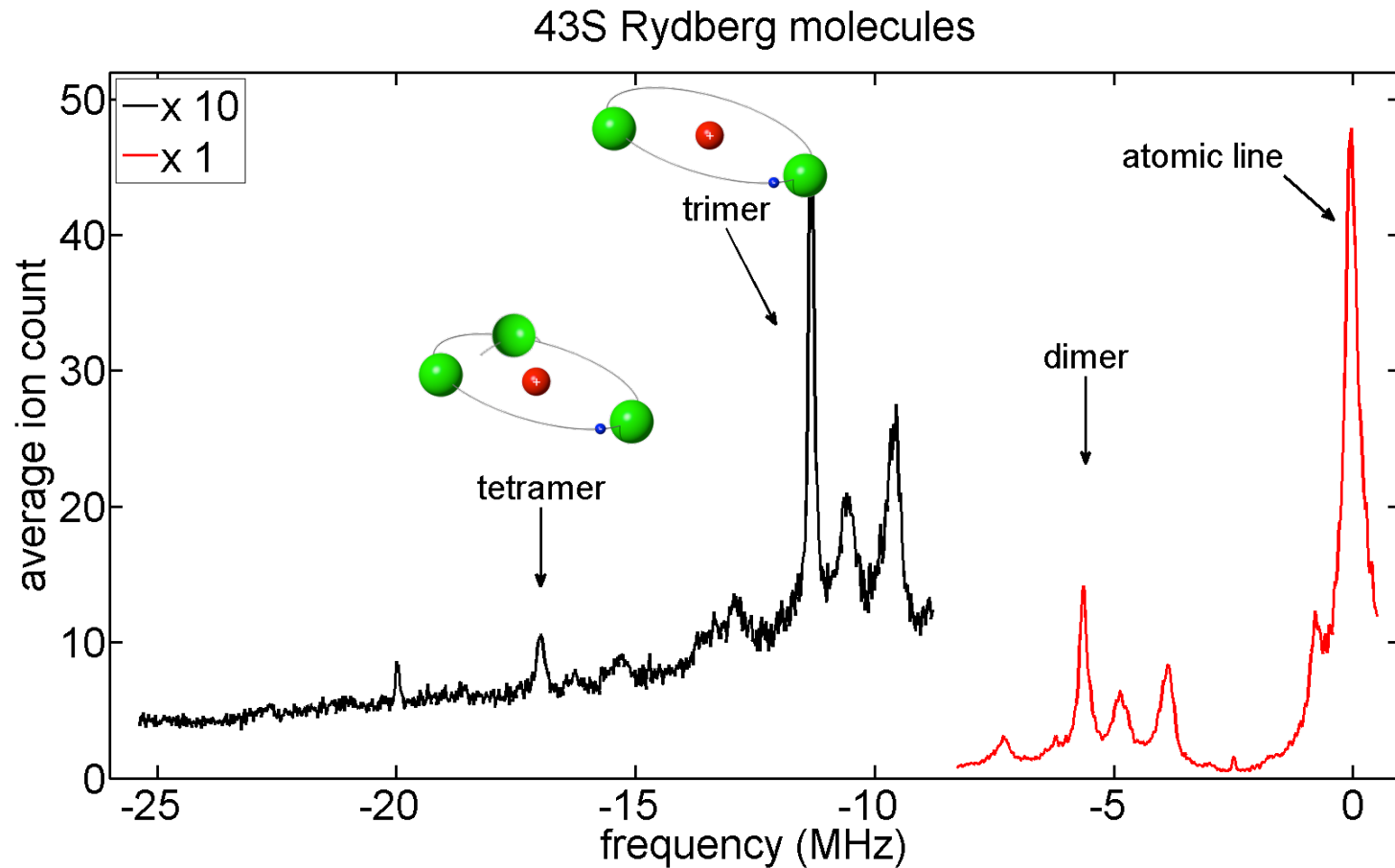


3 body photoassociation

PRL105, 163201 (2010)



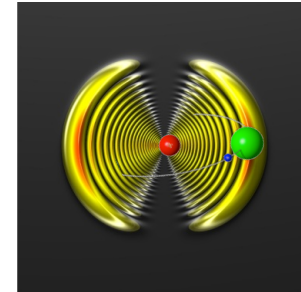
# Ultralong-range trimers, and tetramers and...



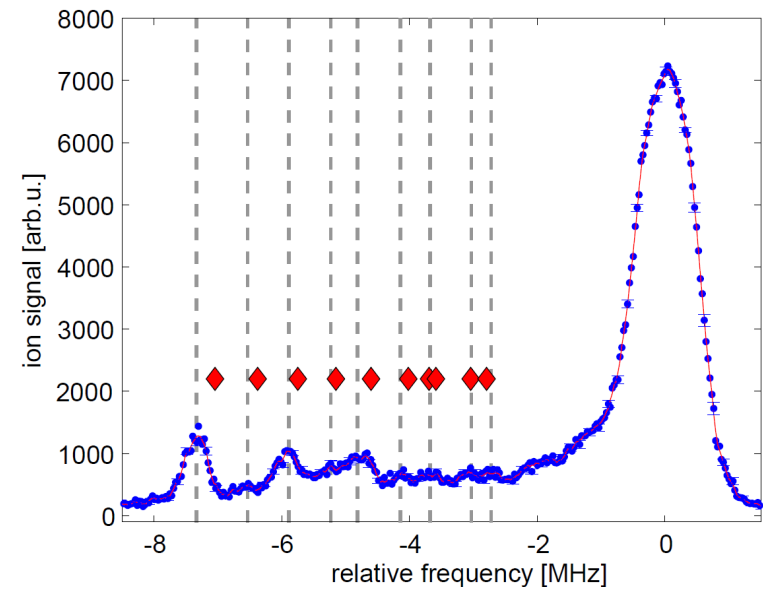
# Increase $l$ :

## D state molecules show **rovibrational** states...

42  $D_{5/2}$  state



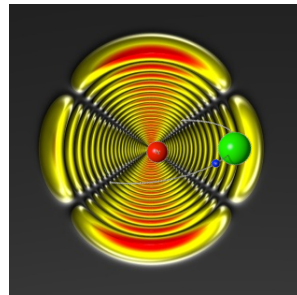
$m_J = 5/2$



A. Krupp, M. Kurz, P. Schmelcher et al.  
arXiv:1401.4111 (2014) accepted in PRL

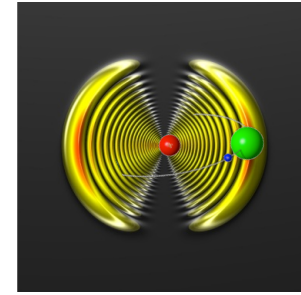
# Increase $l$ :

## D state molecules show **rovibrational** states...

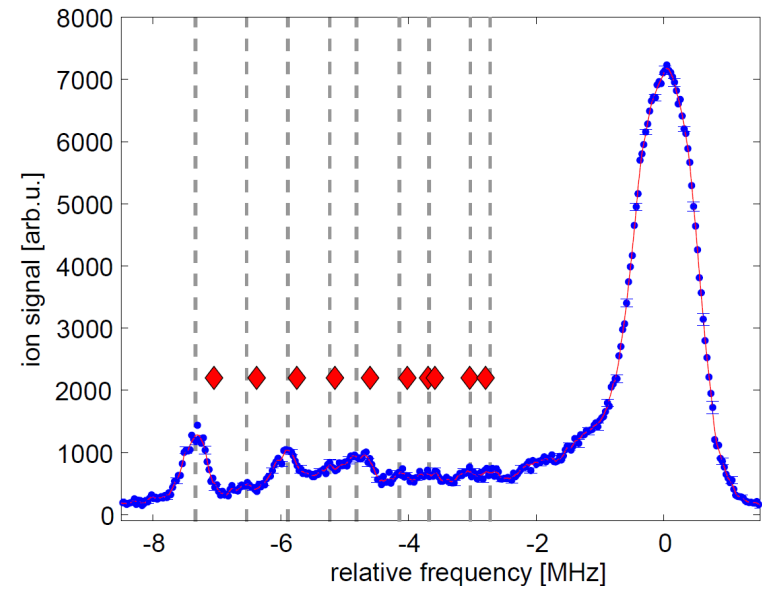
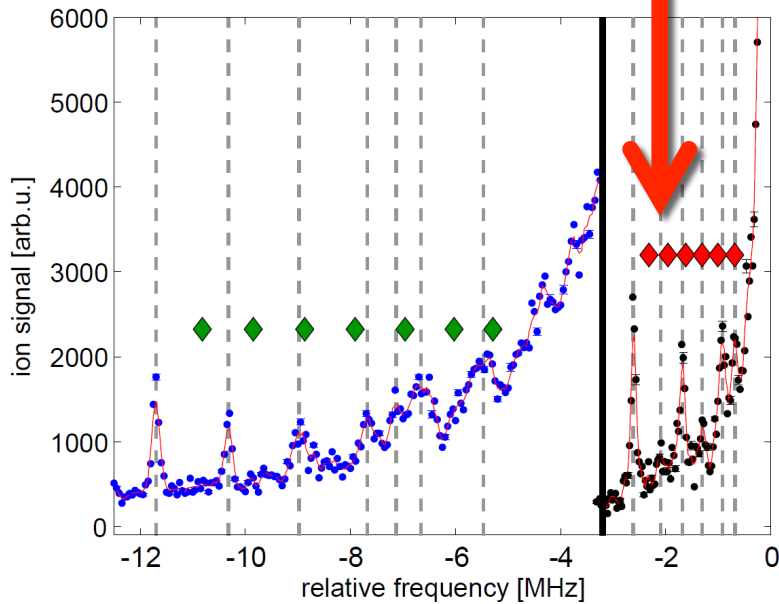


$m_J = 1/2$

42  $D_{5/2}$  state



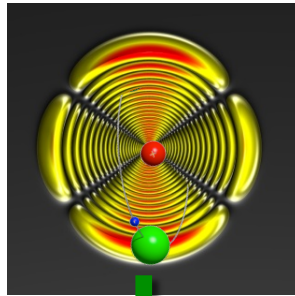
$m_J = 5/2$



A. Krupp, M. Kurz, P. Schmelcher et al.  
arXiv:1401.4111 (2014) accepted in PRL

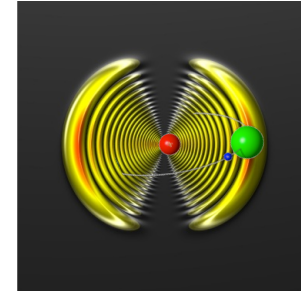
# Increase $l$ :

## D state molecules show **rovibrational** states...

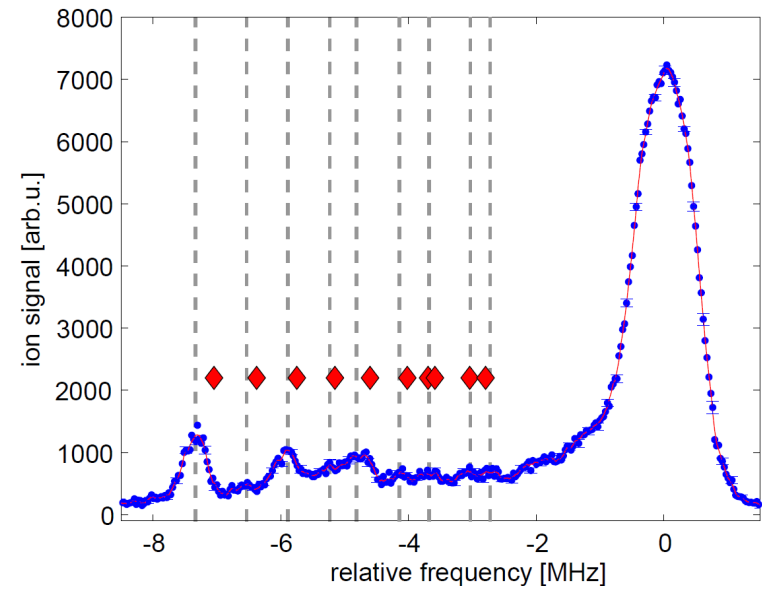
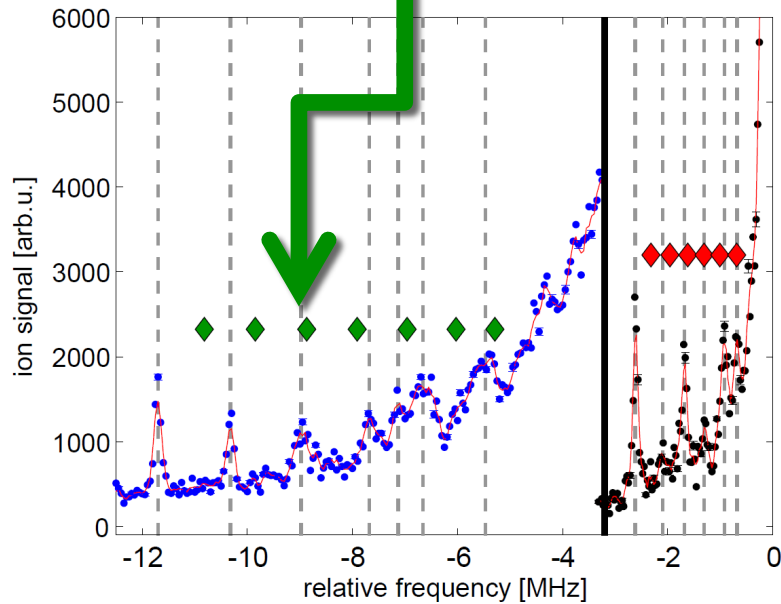


$m_J = 1/2$

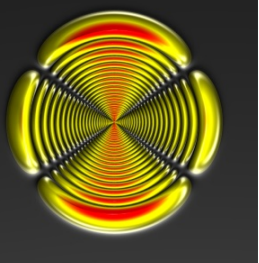
42  $D_{5/2}$  state



$m_J = 5/2$

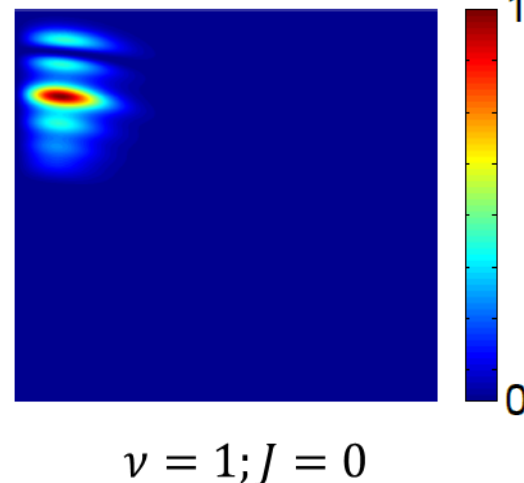
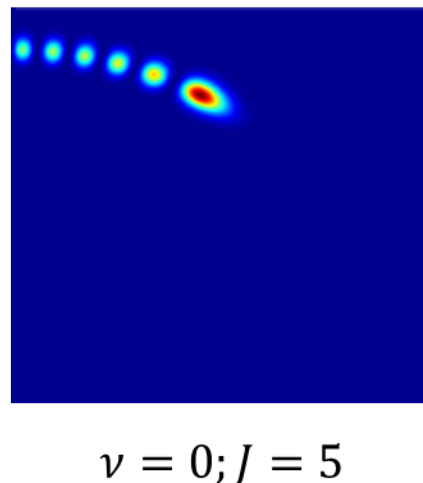
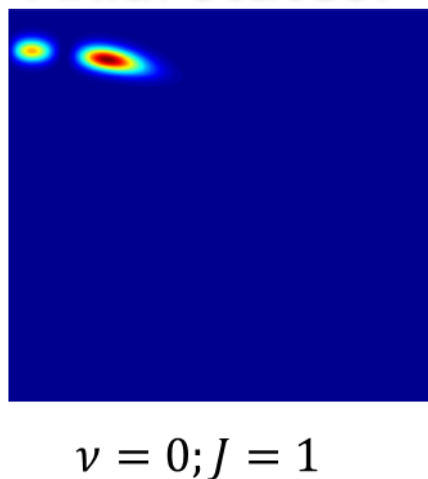
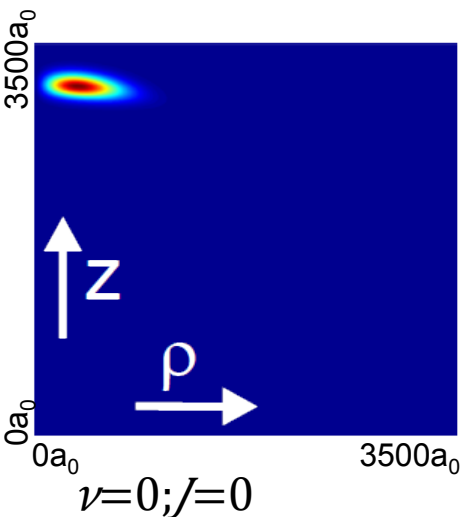


A. Krupp, M. Kurz, P. Schmelcher et al.  
arXiv:1401.4111 (2014) PRL 2014

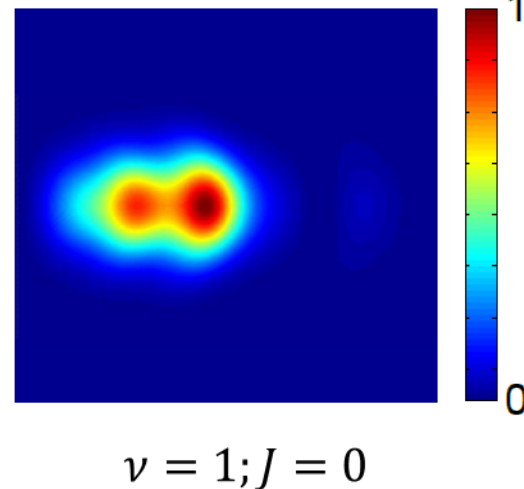
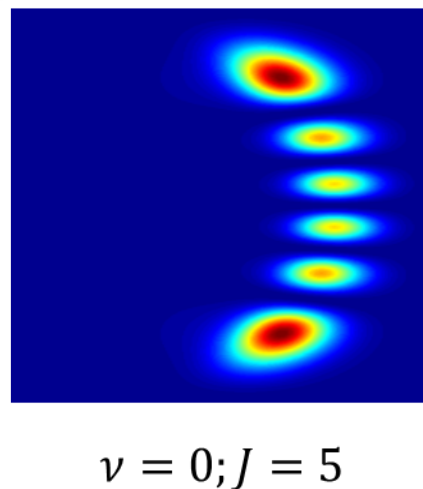
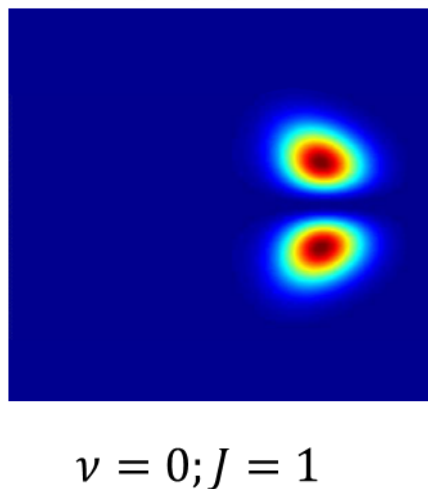
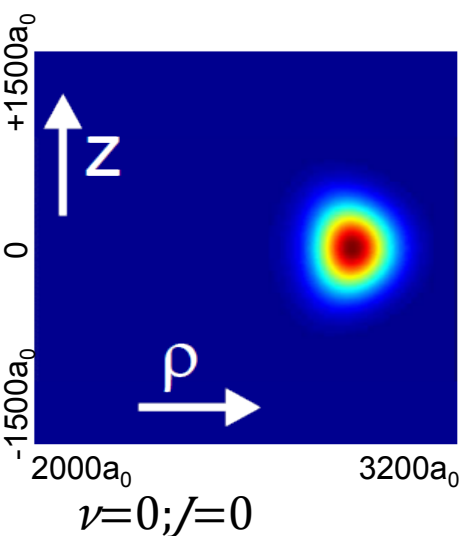


# Scaled rovibrational probability densities

Axial states:



Toroidal states:

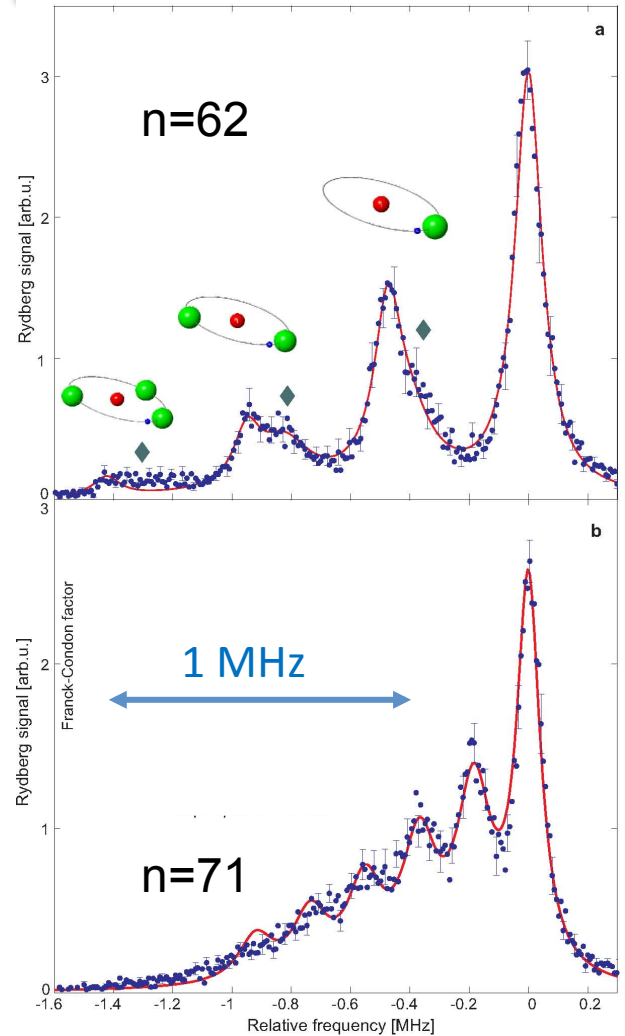


# Going higher in n:

**dimers, trimers, tetramers, pentamers ...**

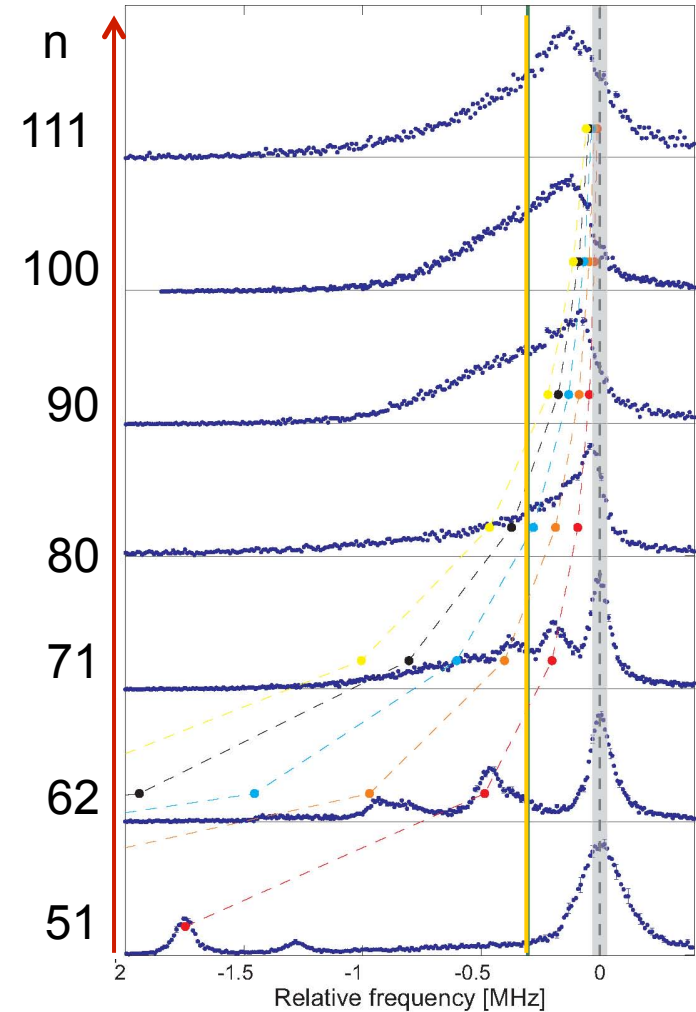
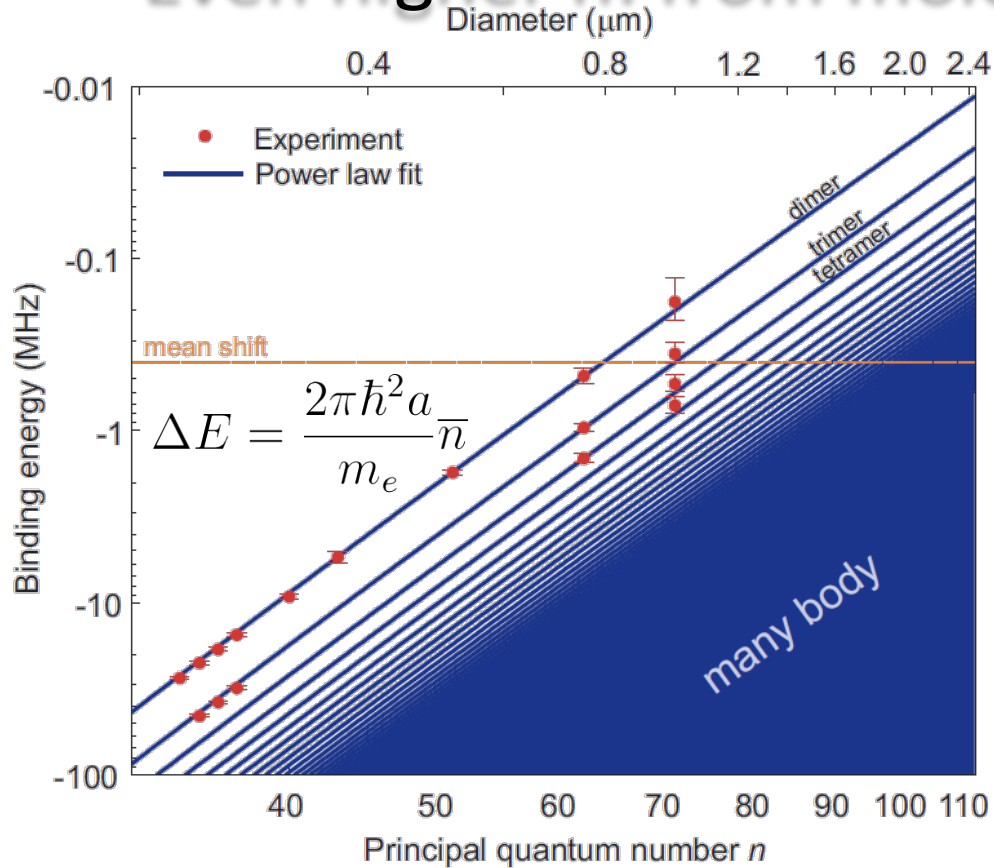
Binding energy scales with principal quantum number

$$V_{\text{mol}}(\vec{R}) = \frac{2\pi\hbar^2 a}{m_e} |\Psi(\vec{R})|^2 \sim n^{-6}$$





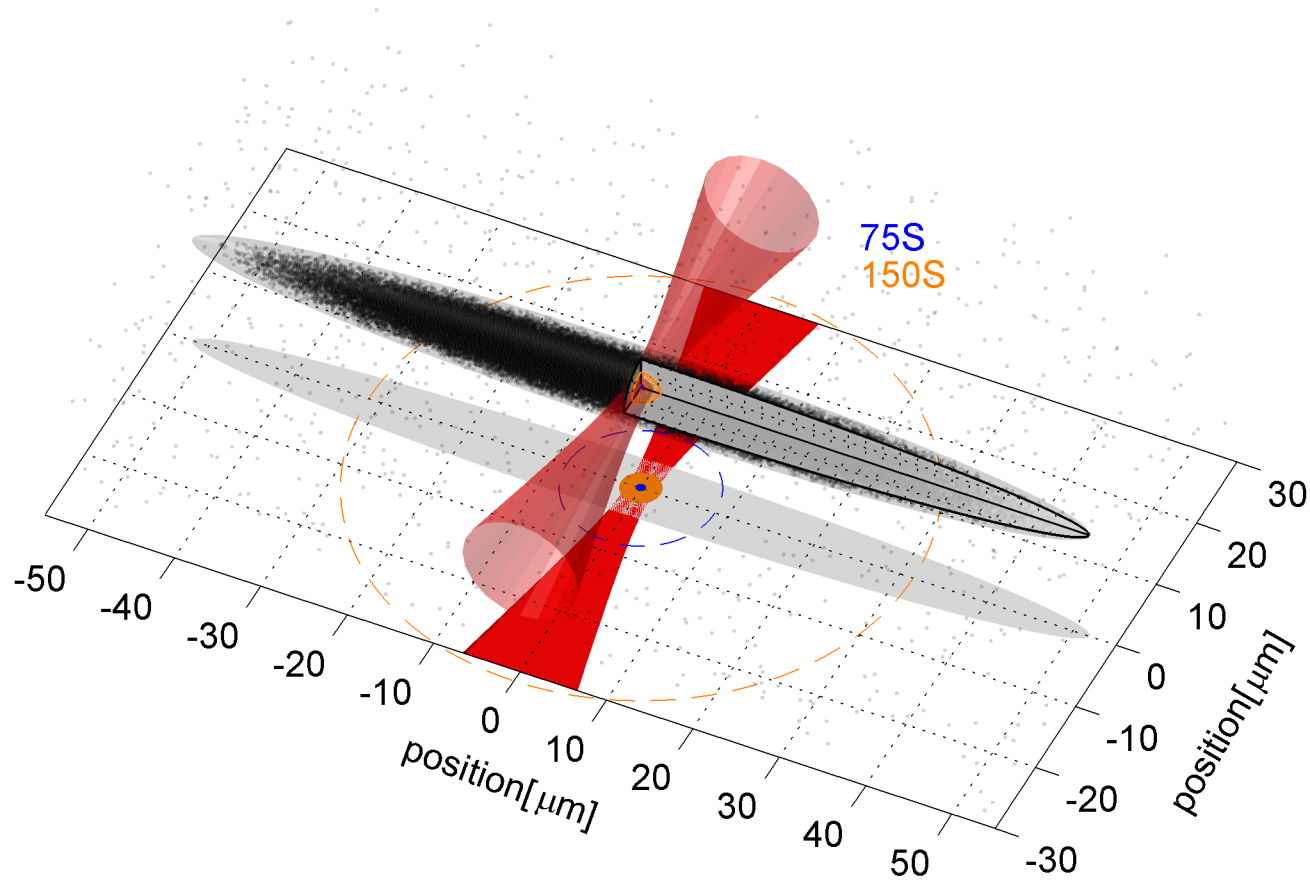
# Even higher n: from molecules to mean shift



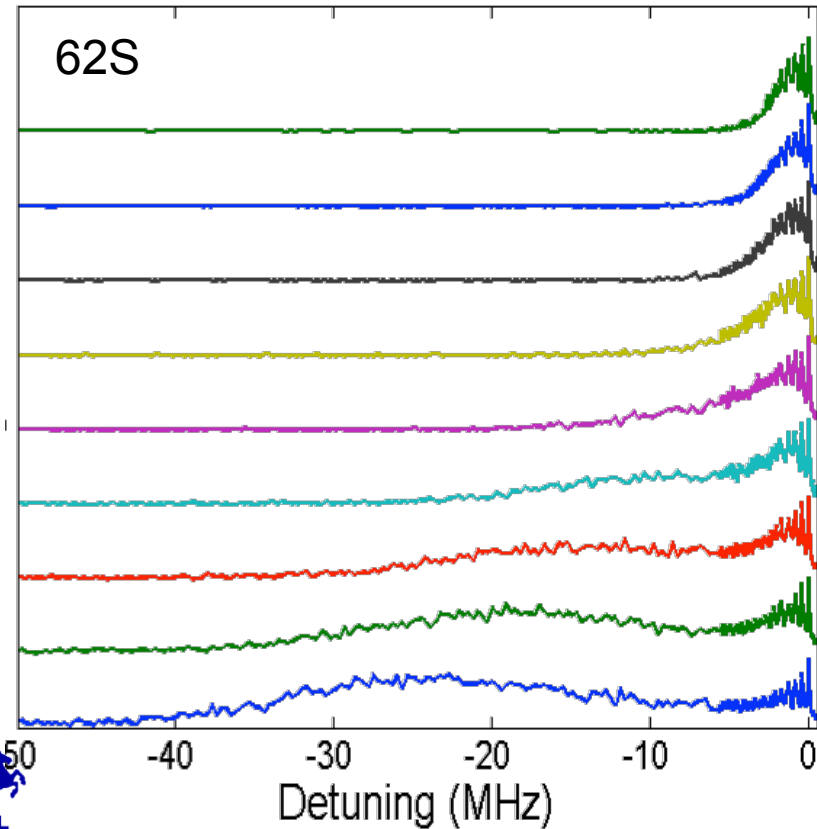
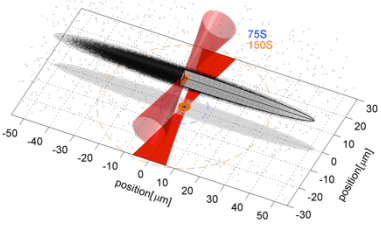
A. Gaj, A. T. Krupp, J. B. Balewski,  
 R. Löw, S. Hofferberth, and T. Pfau  
 Nature Comm. In press



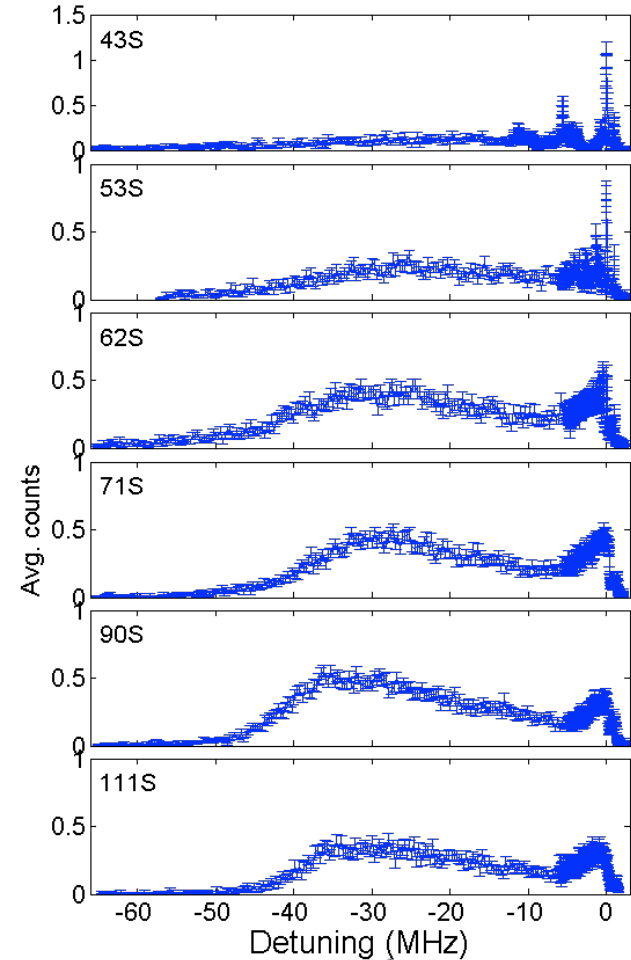
# In situ Rydberg spectroscopy setup



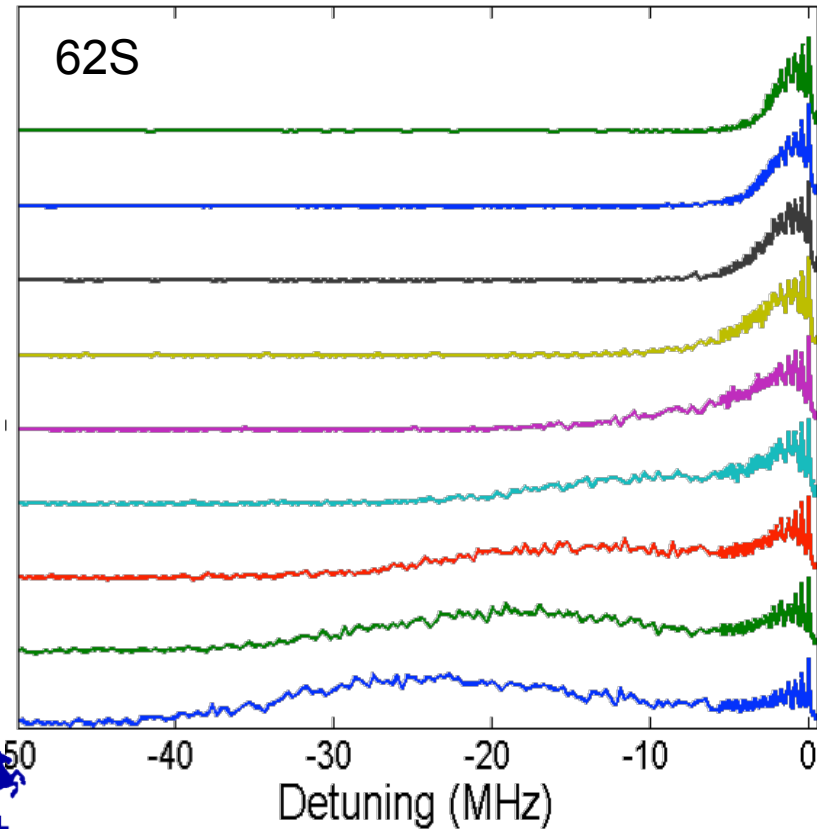
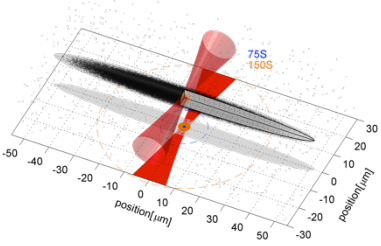
# Increase density: Rydberg spectroscopy in a BEC



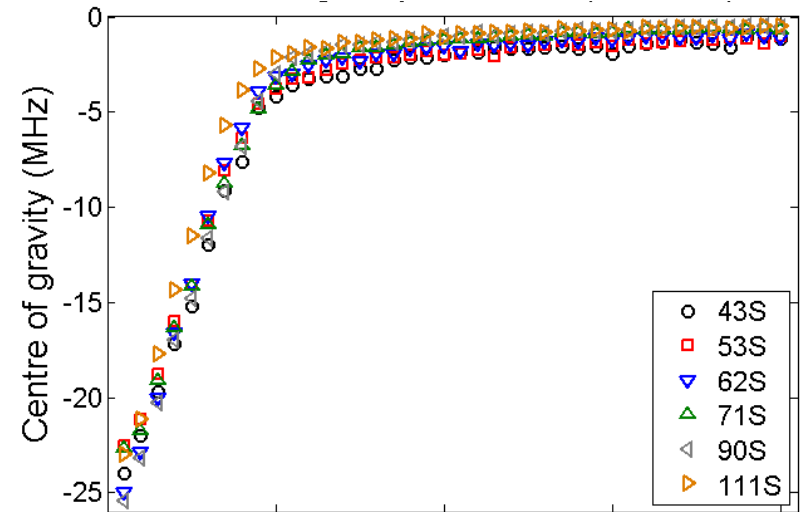
## BEC Spectra



# Increase density: Rydberg spectroscopy in a BEC



## BEC Spectra



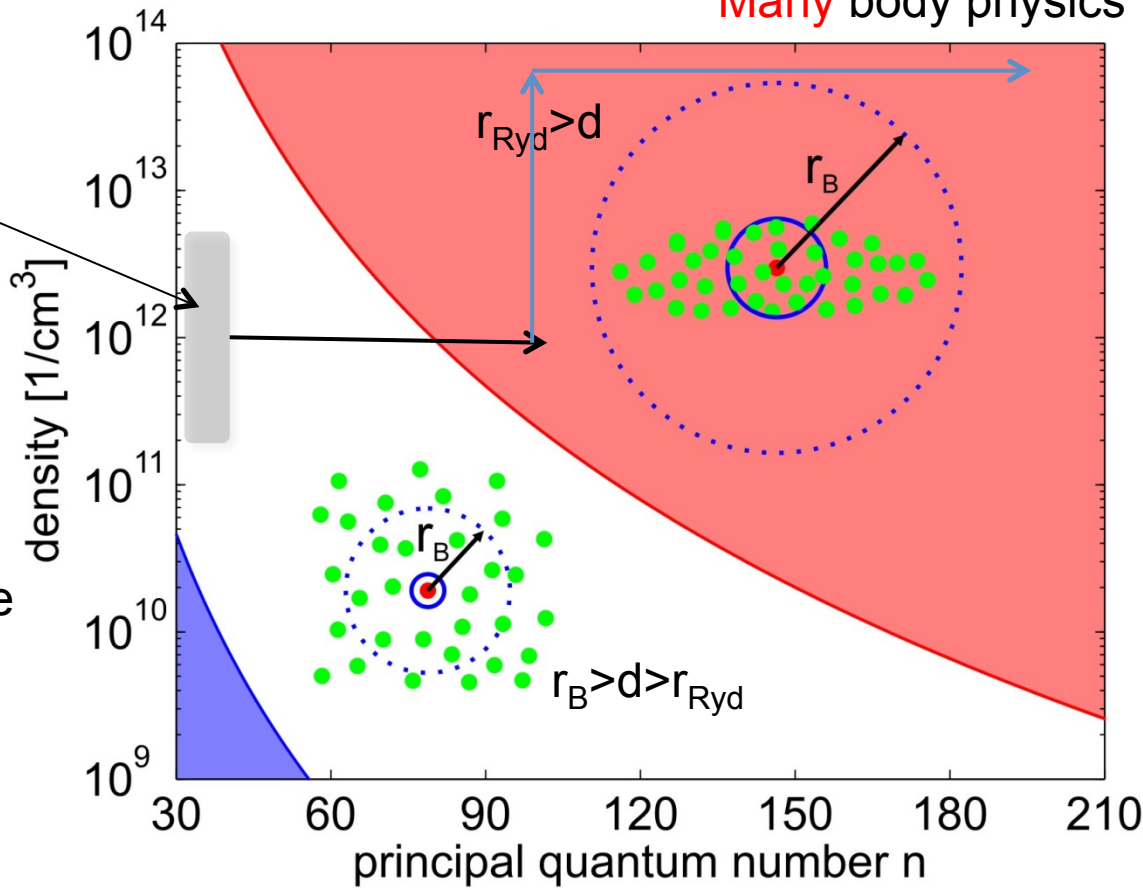
$T \ll T_c$  ←  $T > T_c$



# Length scales

probability to find an atom inside Rydberg electron wavefunction small, but finite!  
**Few** body physics

**Many** body physics

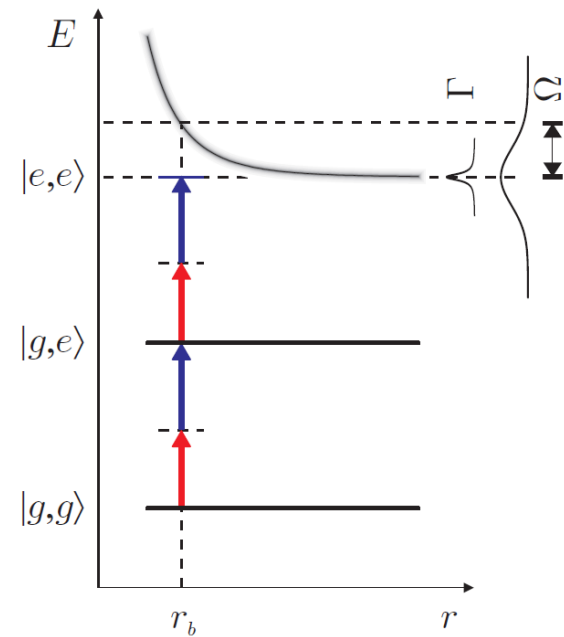
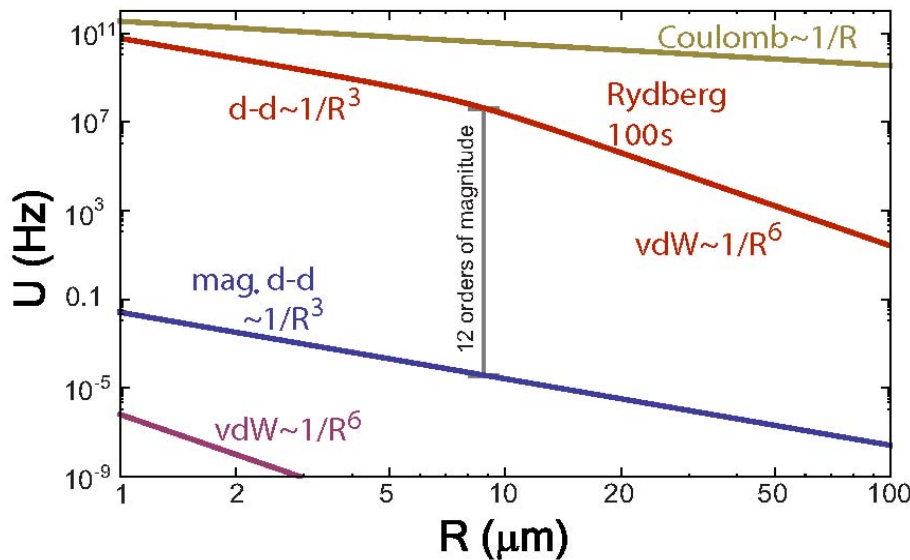
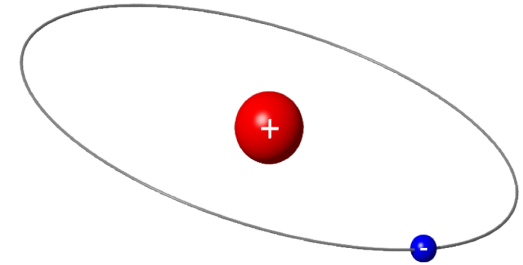


- d: mean particle distance
- $r_B$ : blockade radius
- $r_{Ryd}$ : size of electron orbit



# Rydberg atoms - Blockade

quantity	scaling	100S-state of $^{87}\text{Rb}$
lifetime	$\propto n^3$	1.24 ms
Polarizability	$\propto n^7$	$6.245 \text{ GHz (V/cm)}^{-2}$
Van der Waals $C_6$	$\propto n^{11}$	$-3.89 \times 10^{23} \text{ a.u.}$



M. Saffman et al., Rev. Mod. Phys. 82, 2313 (2010)

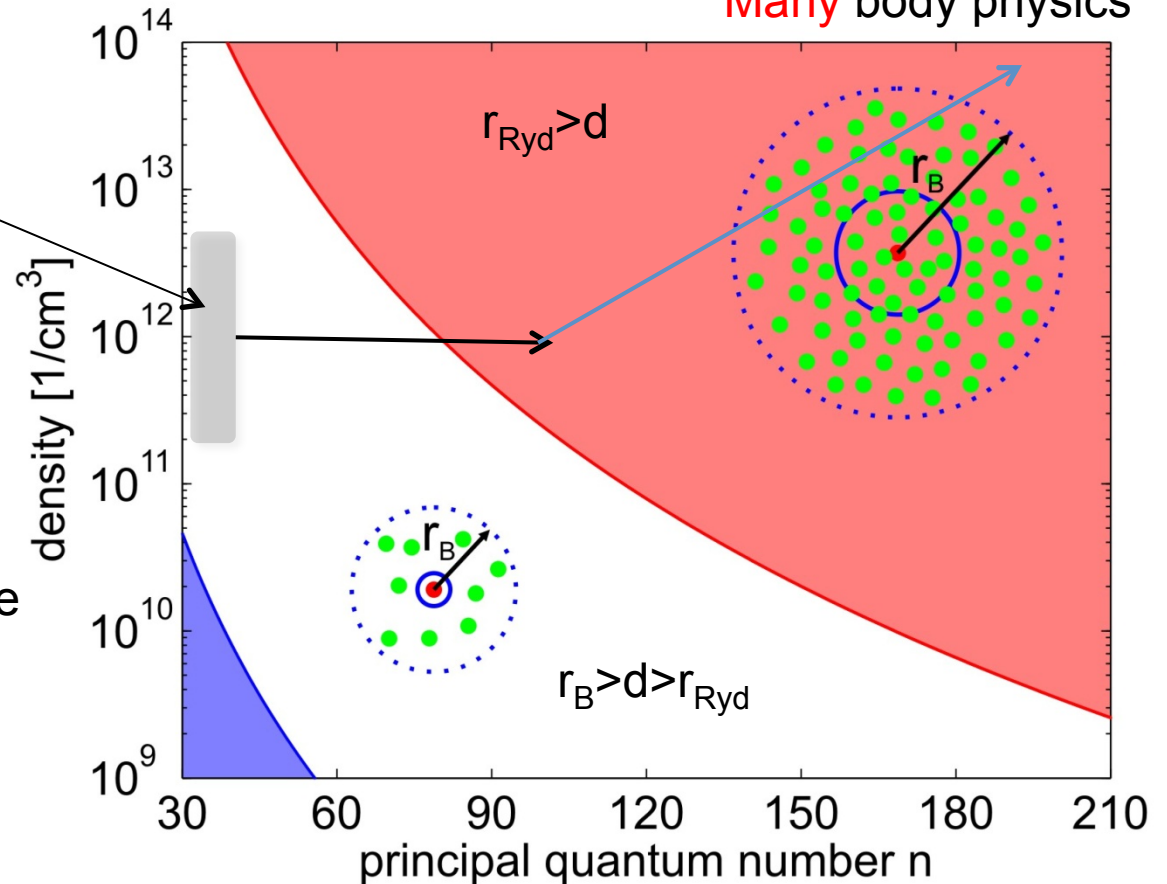


# Rydberg atoms in dense gases

Many body physics

probability to find an atom  
inside Rydberg electron  
wavefunction small, but finite!

Few body physics



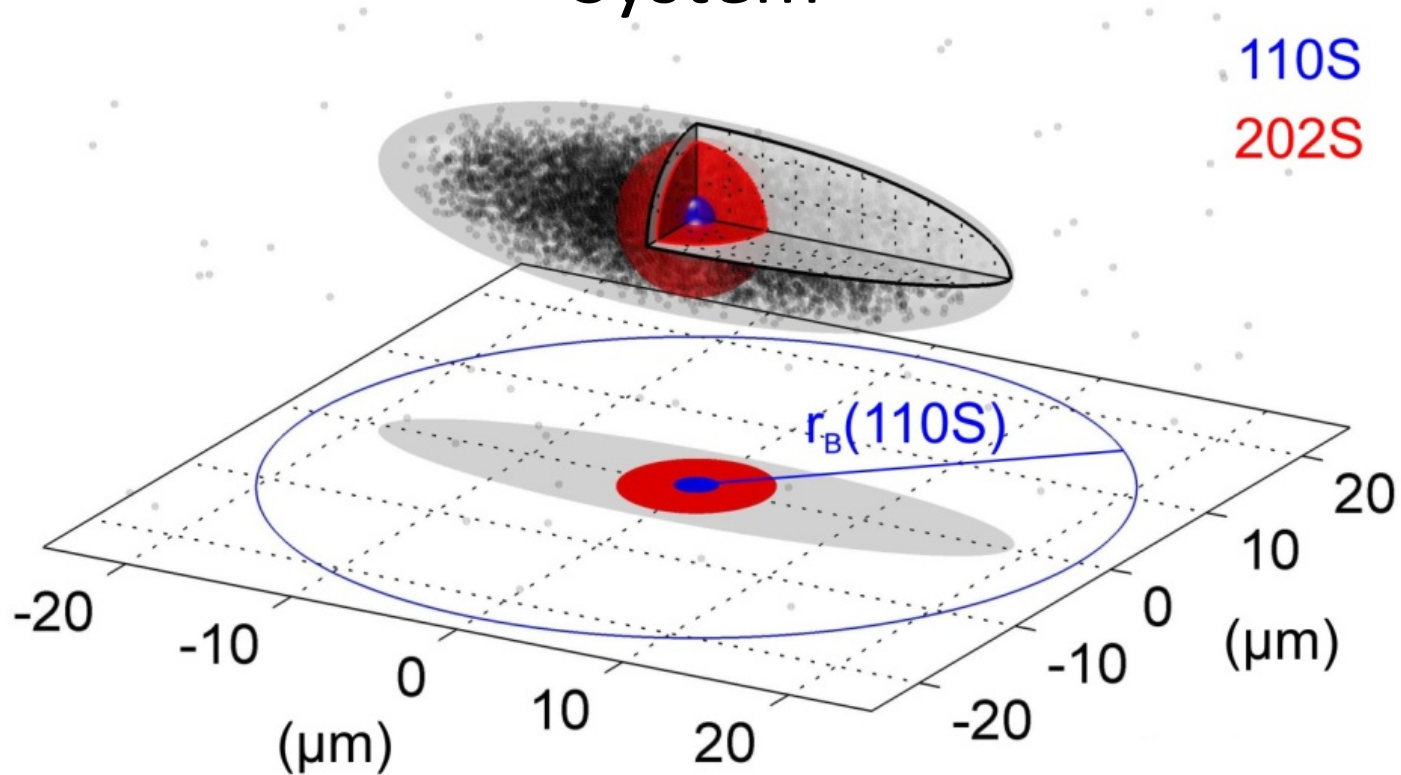
$d$ : mean particle distance

$r_B$ : blockade radius

$r_{\text{Ryd}}$ : size of electron orbit



# System



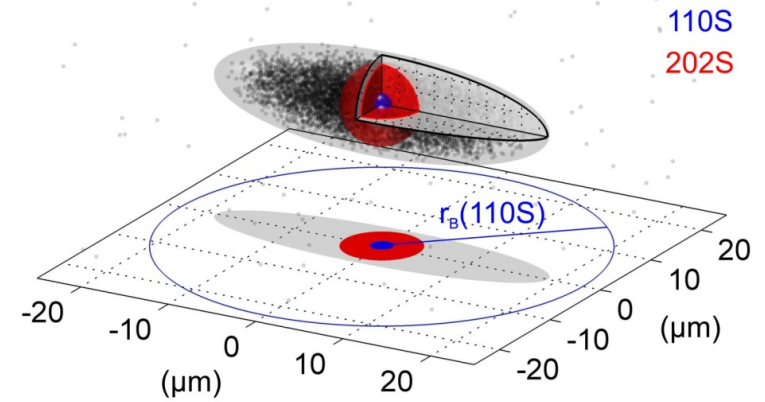
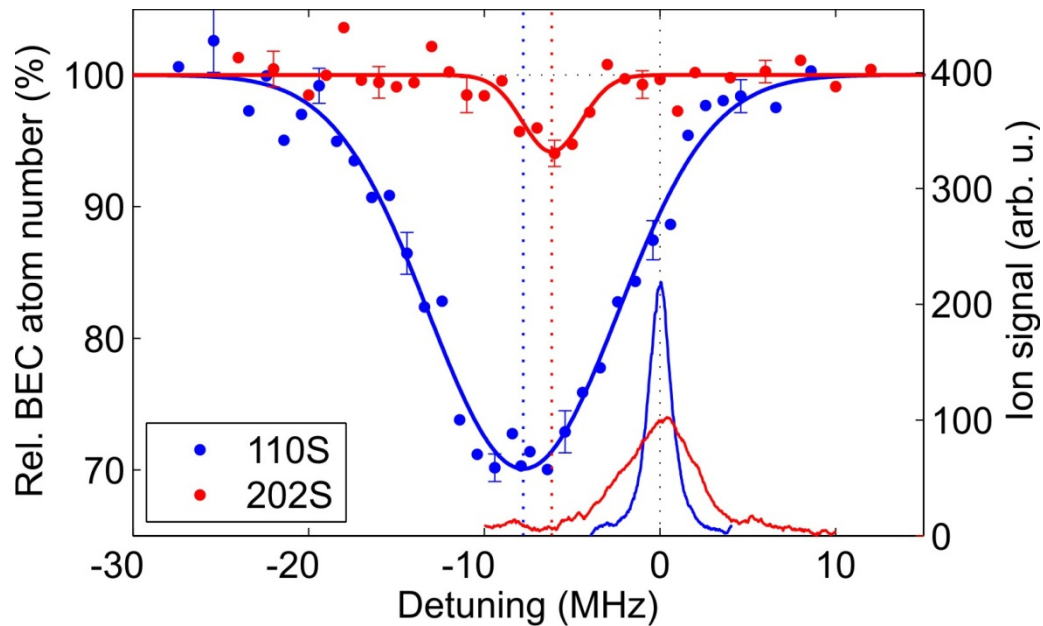
Rydberg: 1.2  $\mu\text{m}$  radius / 4.2  $\mu\text{m}$  radius

BEC:  $8 \cdot 10^4$  atoms, 5 / 18  $\mu\text{m}$  radial / axial TF-radius

$\Rightarrow$  700 / 30000 atoms inside Rydberg atom



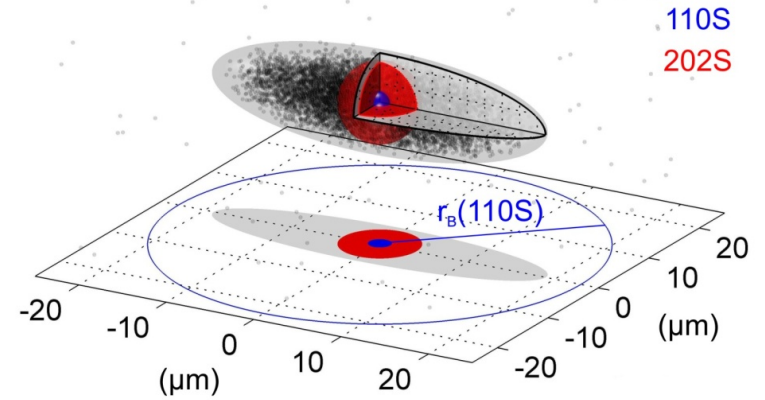
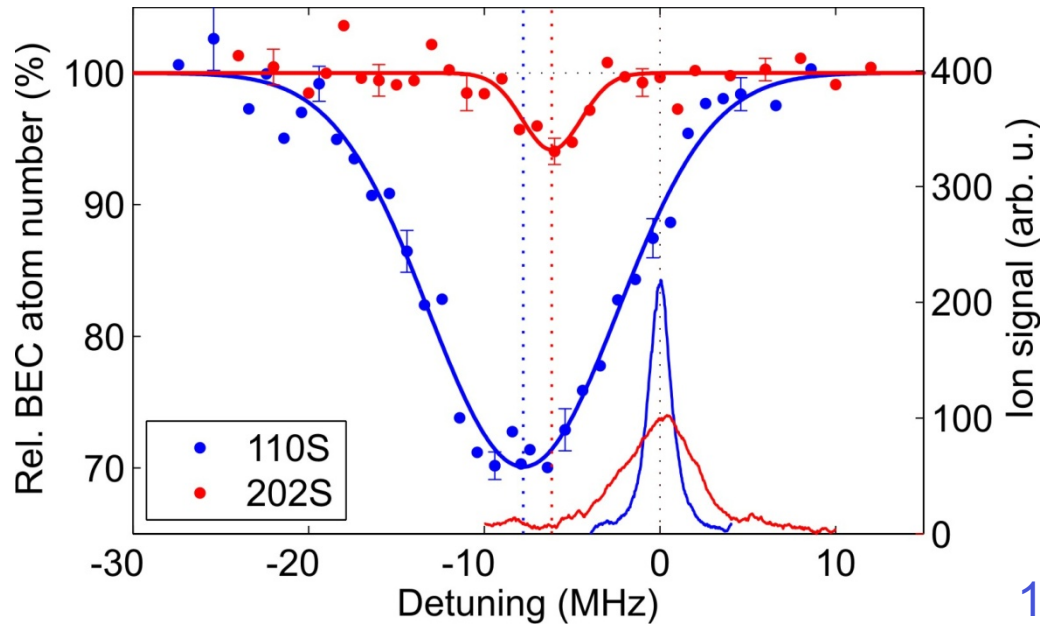
# Effect of BEC on single Rydberg electron



⇒ effect on Rydberg: lineshift  $\sim 10$  MHz



# Effect of single electron on BEC



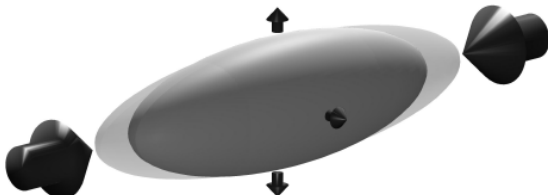
110S ~ 700 atoms inside  
~ 50 atoms lost pp

202S ~ 30000 atoms inside  
~ 7 atoms lost pp

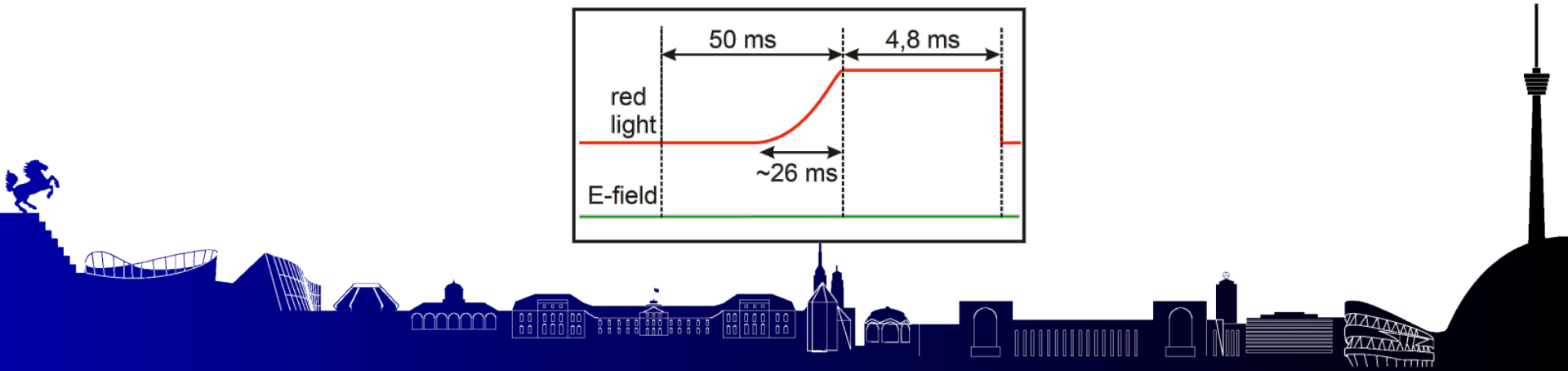
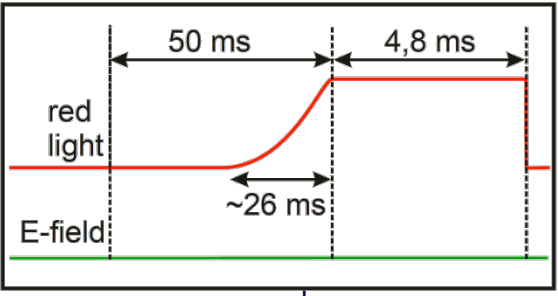
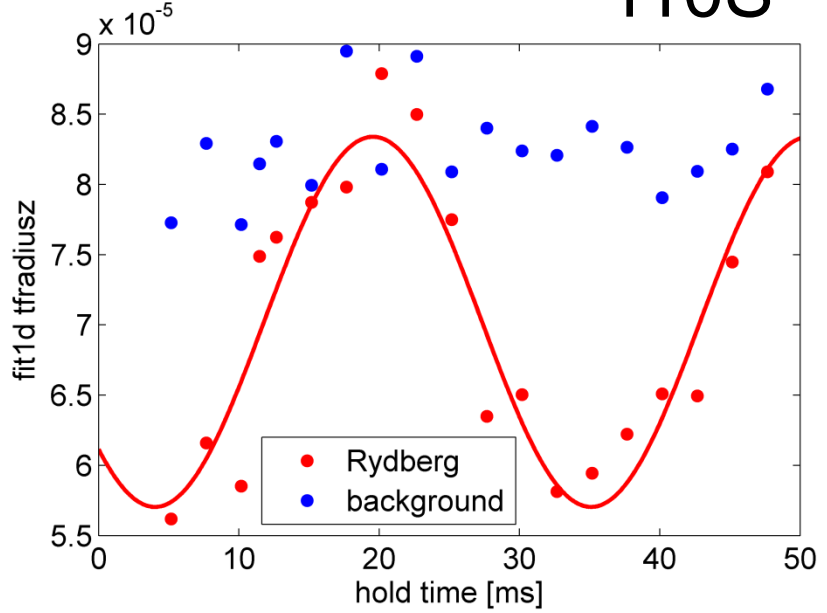
⇒ effect on Rydberg: lineshift ~10 MHz



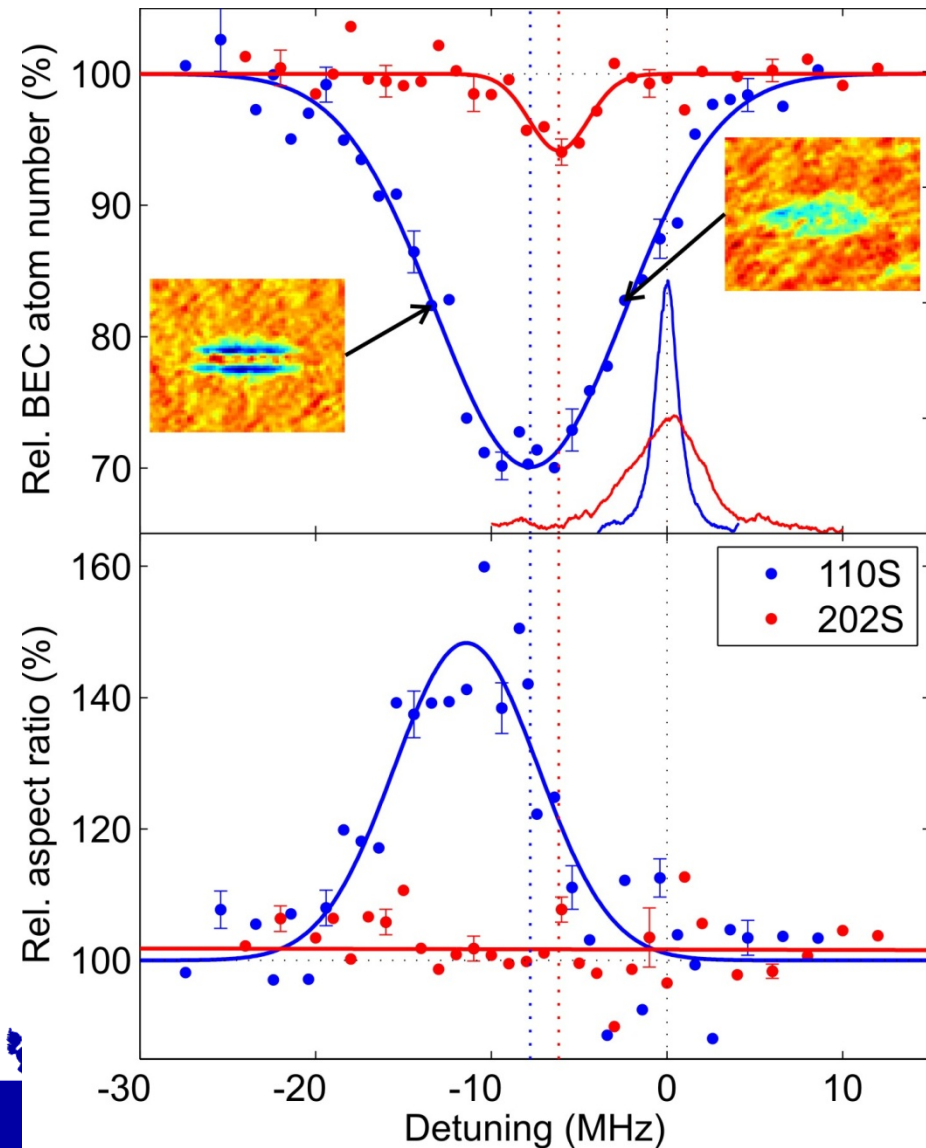
# Rydberg electron sets BEC in motion



110S



# Effect of single electron on BEC

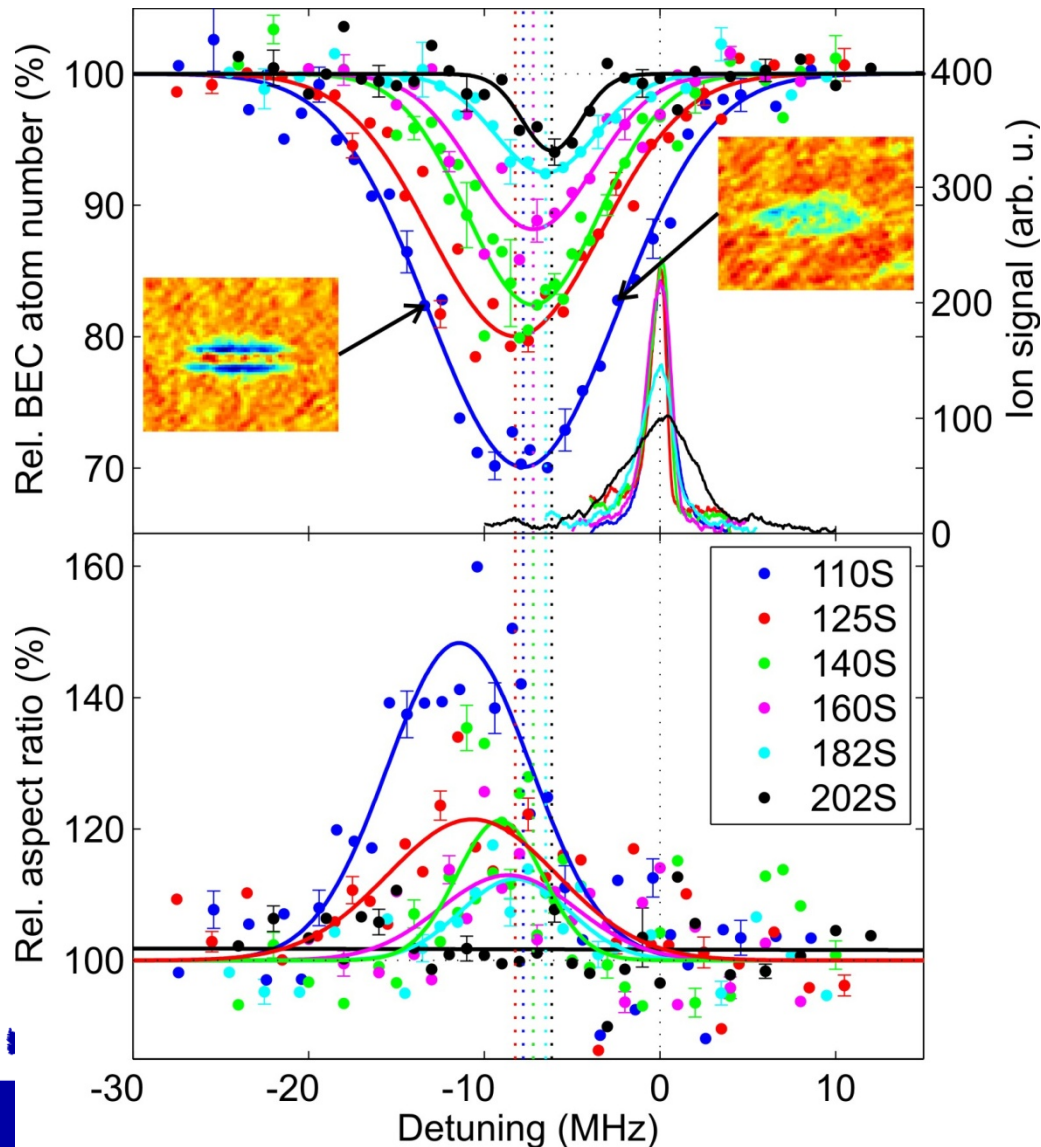


110S ~ 700 atoms inside  
~ 50 atoms lost pp  
**strong mechanical effects**

202S ~ 30000 atoms inside  
~ 7 atoms lost pp  
**no mechanical effects**



# Effect of single electron on BEC

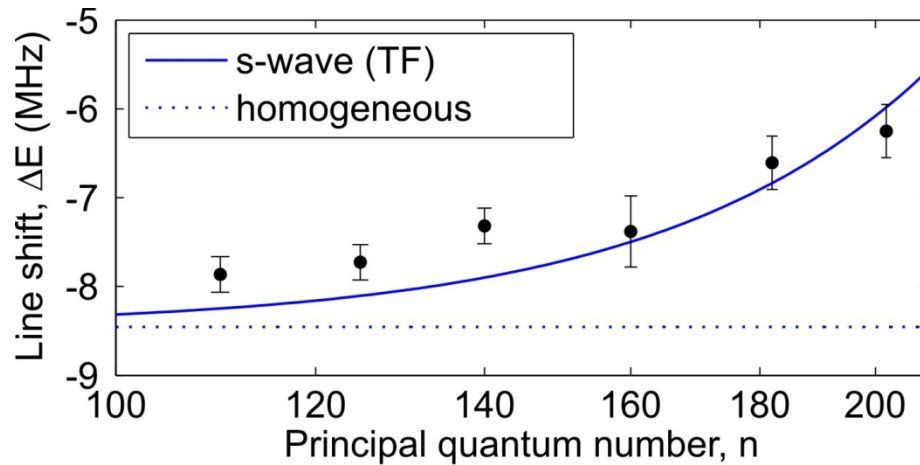


110S ~ 700 atoms inside  
~ 50 atoms lost pp  
**strong mechanical effects**

202S ~ 30000 atoms inside  
~ 7 atoms lost pp  
**no mechanical effects**

J.B. Balewski, A.T. Krupp, A.Gaj, D. Peter,  
H. P. Büchler, R. Löw,  
S. Hofferberth and T. Pfau,  
[Nature, 502, 664 \(2013\)](#)

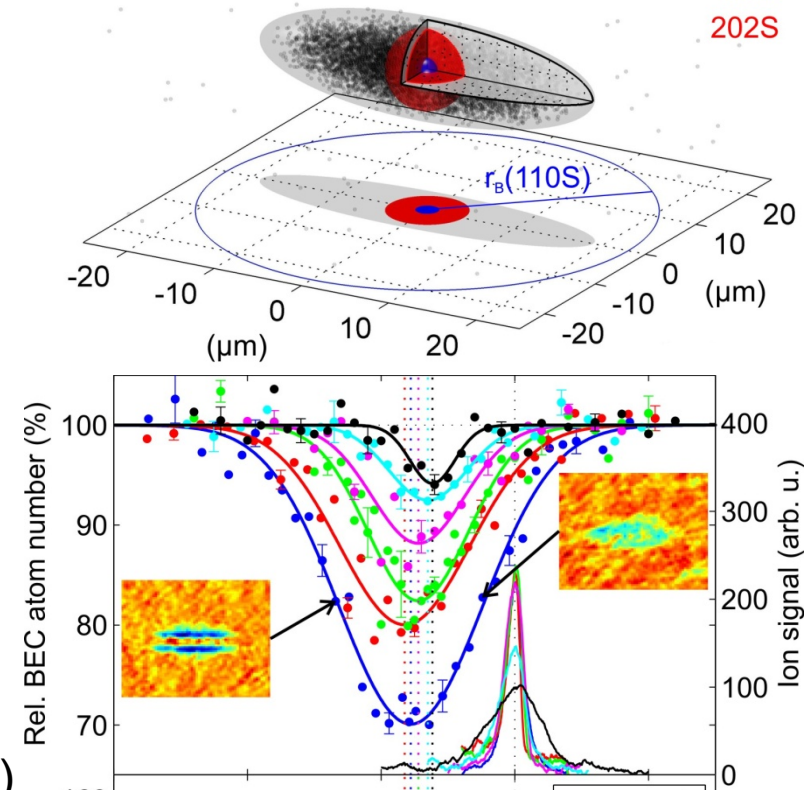
# Line shift



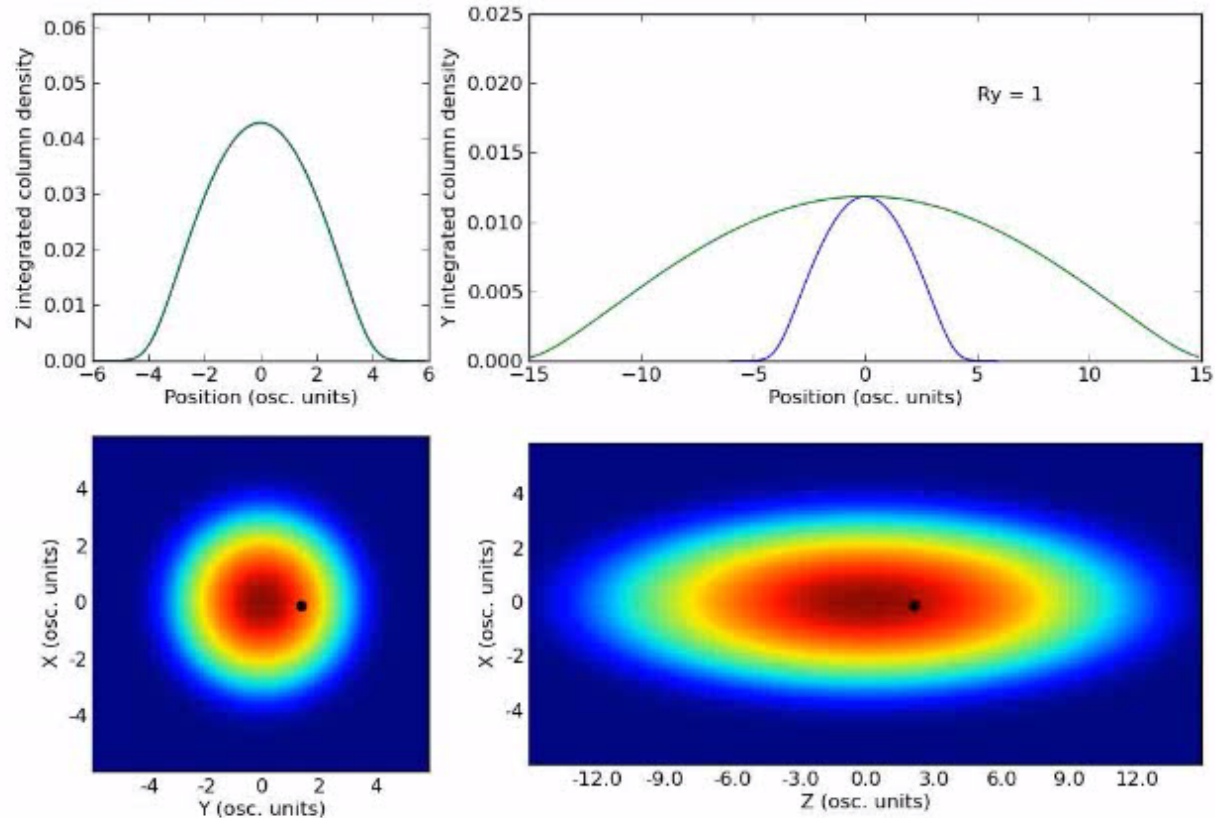
- line shift depending only on mean density  $\bar{n}$ :

$$\Delta E = \frac{2\pi\hbar^2 a}{m_e} \bar{n} \quad (\text{cf. Amaldi, Segrè, 1934})$$

- density not homogeneous (Thomas-Fermi)



# Solving GP equation for our parameters



T. Karpiuk, M. Brewczyk, K. Rzążewski



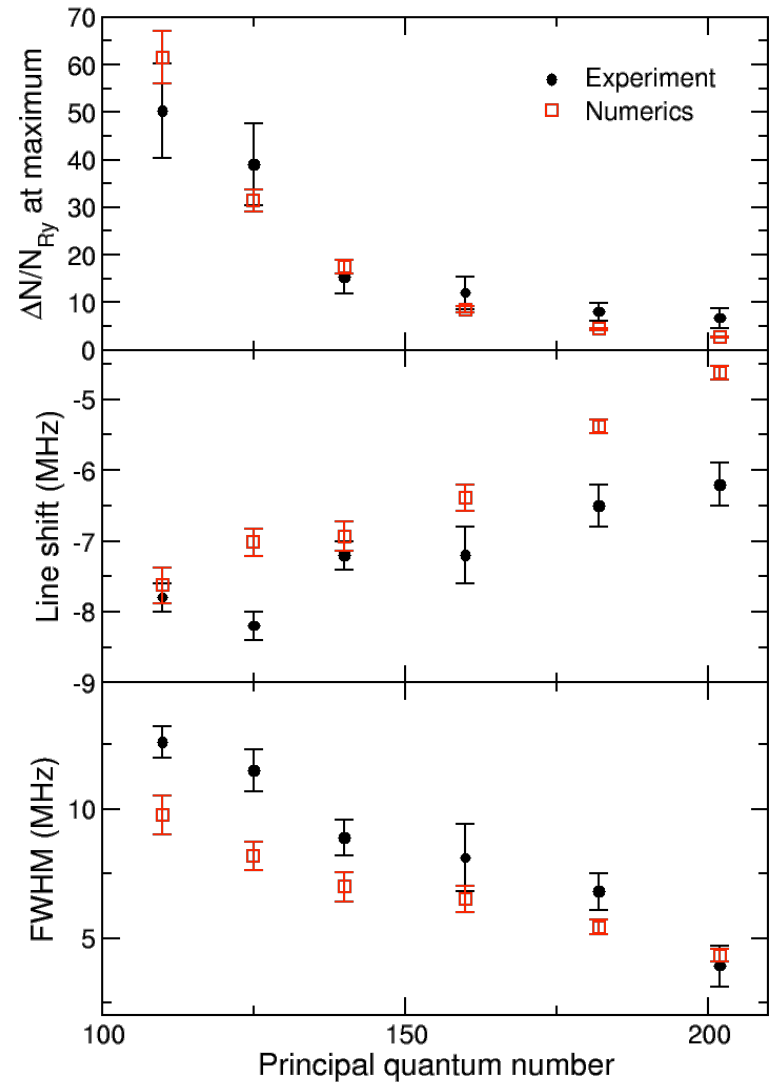
# Loss after ToF – numerics

collaboration with Tomasz Karpiuk, Mirosław Brewczyk and Kazimierz Rzążewski (Warsaw, Poland) arXiv: 1402.6875

## Methods:

- Monte-Carlo simulation of excitation process
- time evolution of Gross-Pitaevskii equation for BEC
- Classical field approximation to extract atom loss

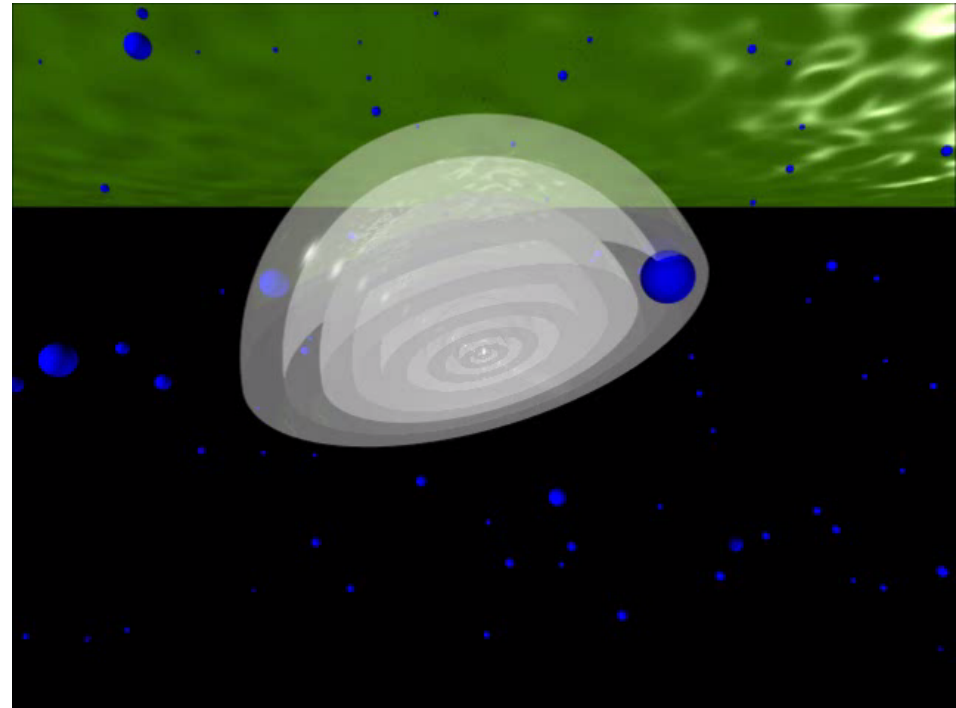
PRA 81, 013629 (2010)





# Combining high Rydberg states and BEC

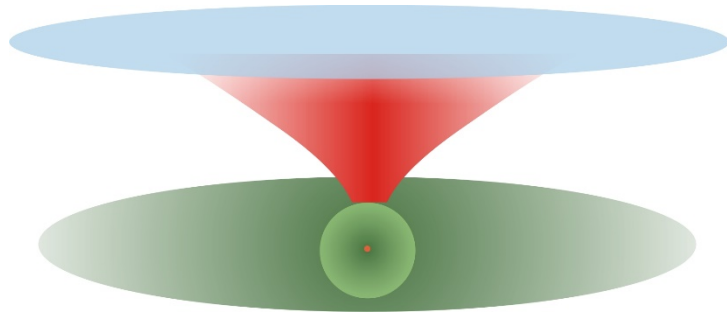
- Rydberg core serves as  $e^-$  - trap
- Rydberg blockade allows only one **single electron**
- **quasifree electron in pure state**
  - 700-30.000 atoms within wavefunction



⇒ strong coupling of charged impurity to **BEC excitations**



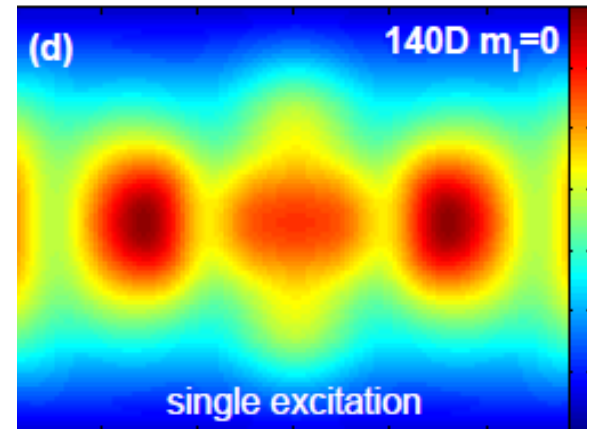
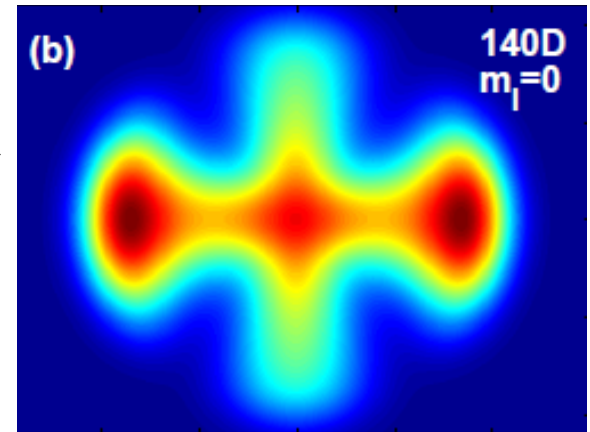
# Wavefunction<sup>2</sup> imaging of single electrons



Excite single Rydberg atom

$$\int |\Psi(\mathbf{r})|^2 dz$$

BEC as contrast agent  
(GP simulation)



T. Karpiuk, M. Brewczyk, K. Rzażewski, J. B. Balewski,  
A. T. Krupp, A. Gaj, M. Schlagmüller, R. Löw, S. Hofferberth, and T. Pfau  
["Detecting and imaging single Rydberg electrons in a Bose-Einstein condensate"](#)

arXiv:1402.6875

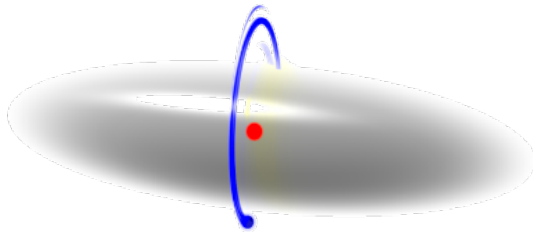


# Ion – BEC interaction?

new approach to prepare a single ion in a BEC?

Idea 1:

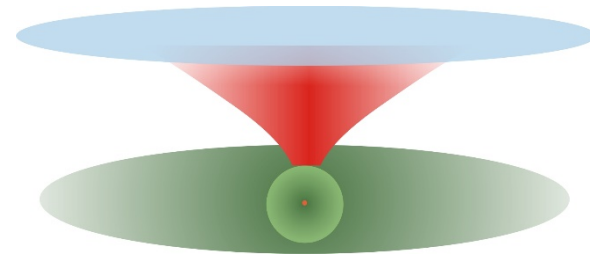
high  $n$  circular ( $l \gg 0$ ) state



electron outside the BEC shields ion

Idea 2:

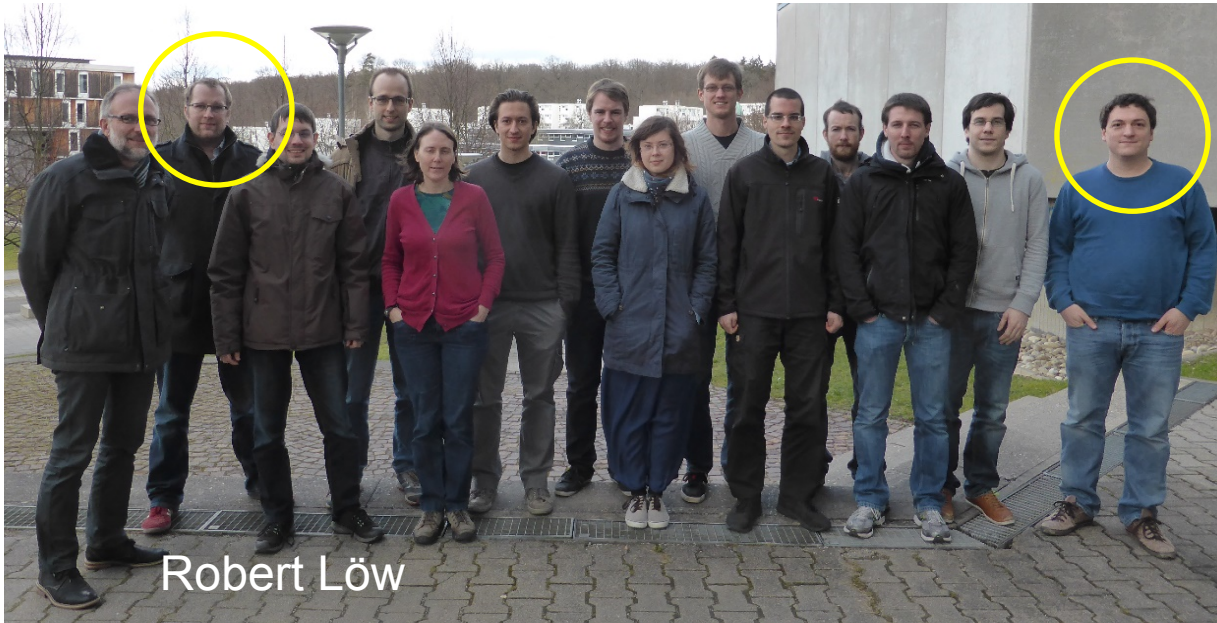
hold ion in optical trap



„magic“ wavelength (430nm) ODT for ion



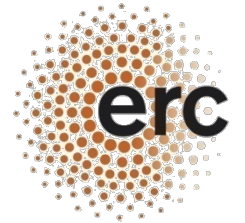
# The COLD Rydberg team



Robert Löw

W Li, T Pohl, JM Rost  
ST Rittenhouse, HR Sadeghpour,  
D Peter, HP Büchler,  
K Rzażewski, M Brewczyk  
M. Kurz, P. Schmelcher

Sebastian Hofferberth: Rydberg quantum optics



CO.CO.MAT

SFB/TRR 21

