

### The definition of the kelvin in the new SI

# Michael de Podesta

Varenna 216 6<sup>th</sup> July2016





# How will you know what the temperature is in 2018?

# Michael de Podesta

Varenna 216 6<sup>th</sup> July2016



How will you know what the temperature is next year?

1. What's the point?

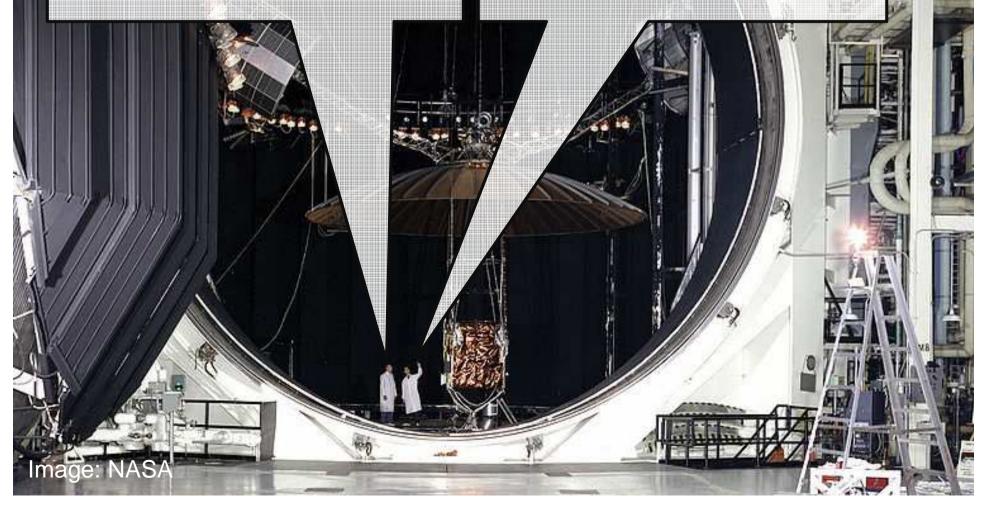
2. The new SI

3. The new kelvin

4. What was the point again?

### I measured the temperature of the antenna to be 148.4 K

Is that correct? On NPL-SAT-1 wasn't it 168 K in 2007?



### **Temperature Measurement Matters**

We need the temperature measurement system to be:

- Stable
  - Enables comparability over time
- Consistent
  - Enables comparability over distance and across boundaries

#### Additionally the system should:

- Not be too complicated or expensive
  - So that people actually use it
- Provide measurement uncertainty required
  - Subject to the historical trend to always make things better!
- Be reasonably close to thermodynamic temperature

The SI kelvin disseminated through the ITS-90 provides all this already!

# So why are we re-defining the kelvin?

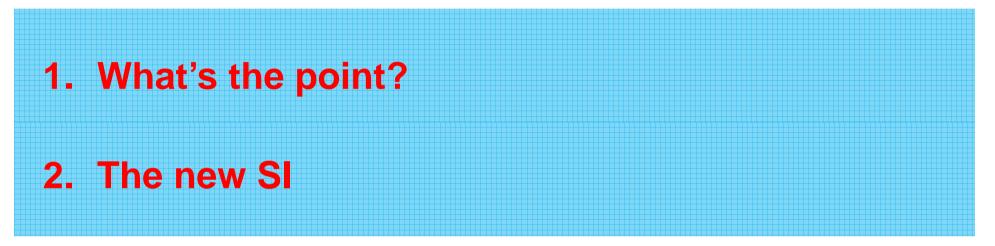
- The International System of Units (the SI) is built on the MKSA system
- MKSA = metre-kilogram-second-ampere
  - What's the difference?
  - The SI has 'People who care'
- The SI is astonishingly successful
  - But all complex structures need maintenance of their foundations
  - After all the work
    - Not much to 'show': except confidence in the structure



The kelvin re-definition is not about solving a problem we have today.

It is about building a system of measurement for an unknown future

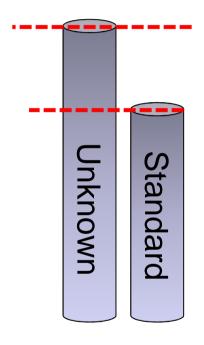
How will you know what the temperature is next year?



- 3. The new kelvin
- 4. What was the point again?

### Measurement is...

### Quant Cotive arison...

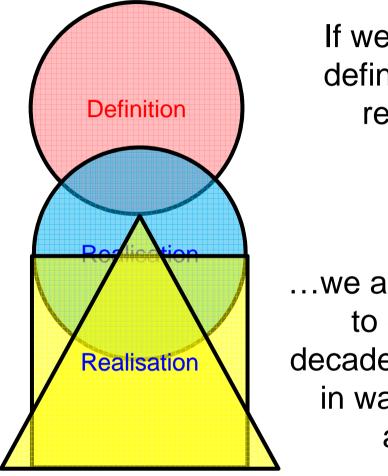


# ...of an unknown quantity with a standard quantity

Historically the definition of a standard was also its realisation.

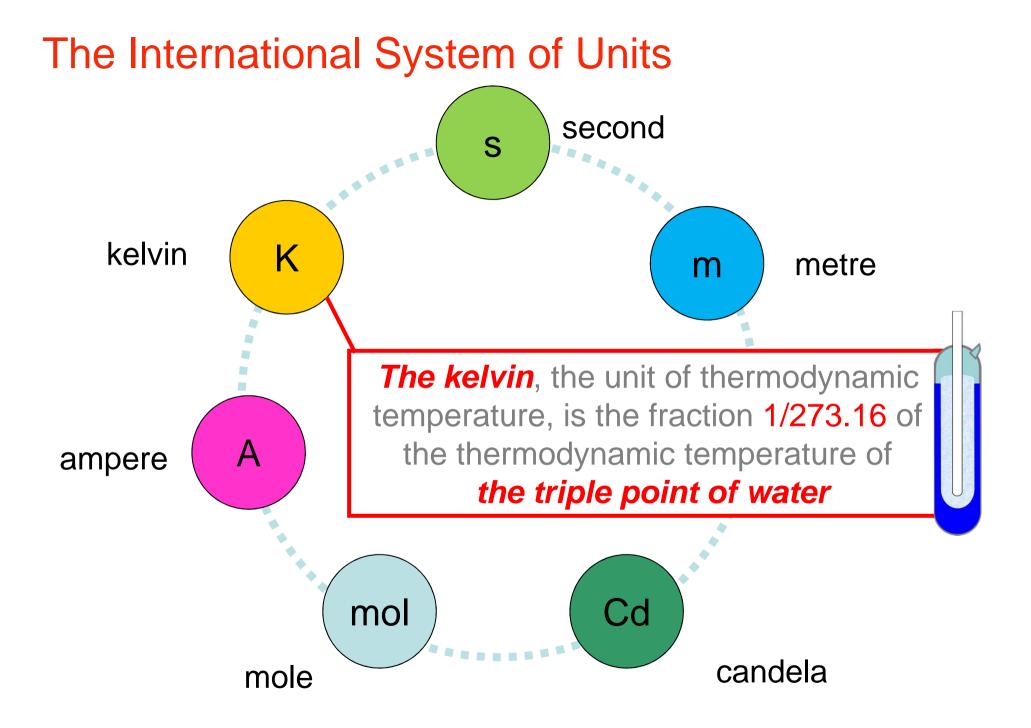
## **Definitions and Realisations**

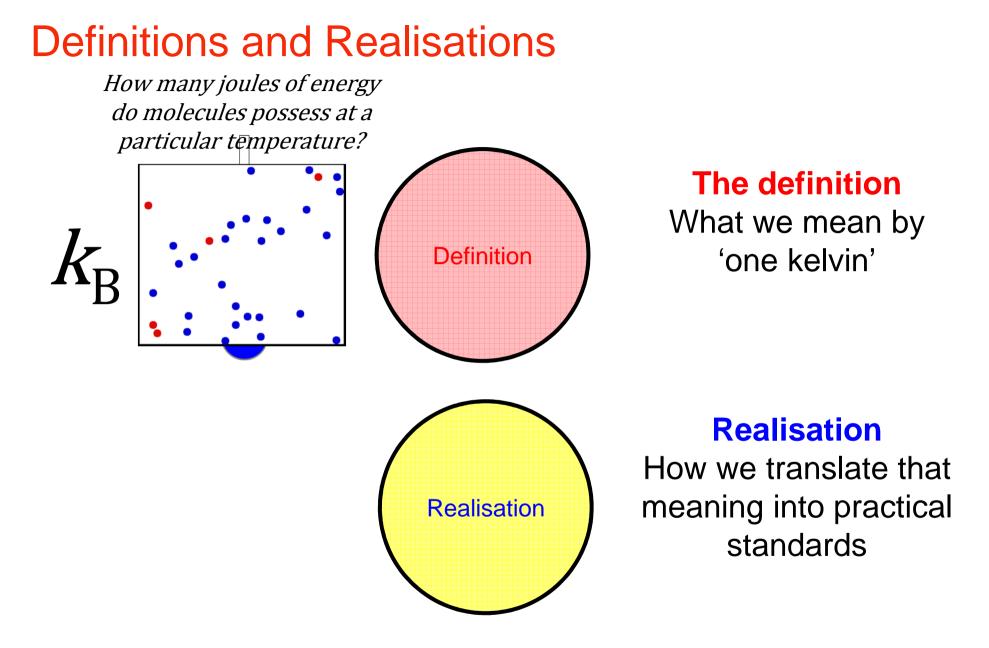
Traditionally unit definitions include some part of their preferred mode of realisation

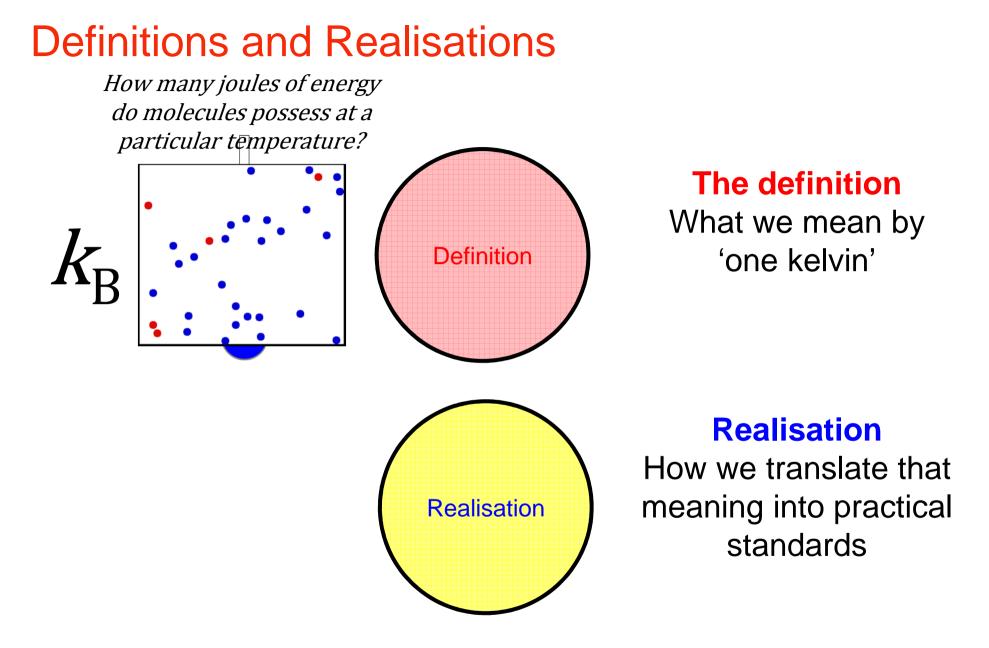


If we separate the definition from the realisation...

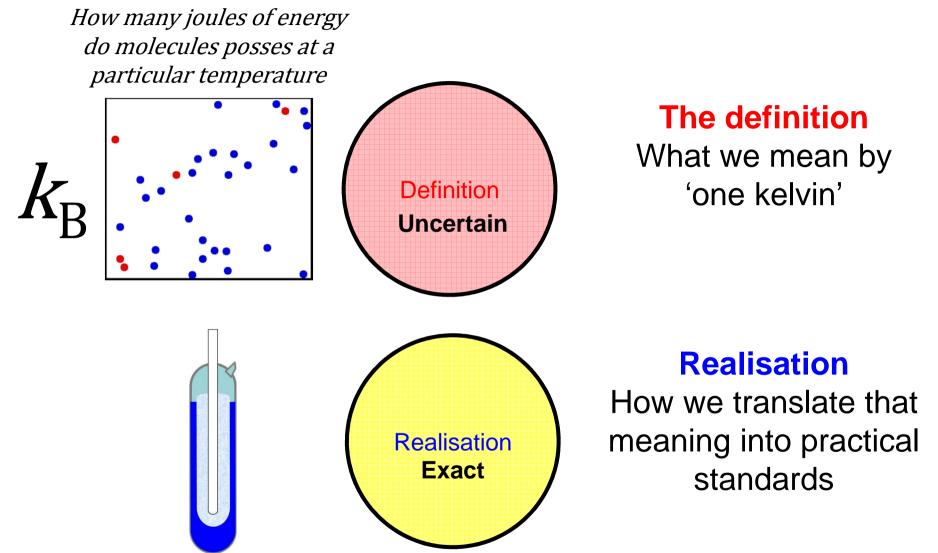
...we allow realisations to evolve over decades and centuries in ways we cannot anticipate







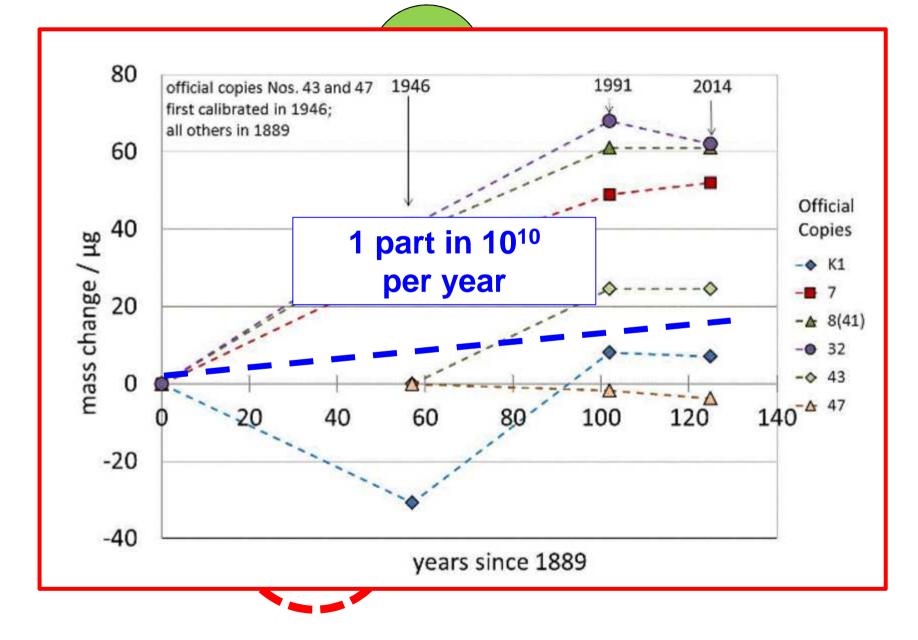
### **Definitions and Realisations and Uncertainty**



### **The International System of Units**

#### The Current International System of Units second S \*\*\*\*\*\* kelvin K metre m **Units differ** dramatically in the concepts required for their definition and kg kilogram A ampere realisation mol cd candela mole

### **The Current International System of Units**

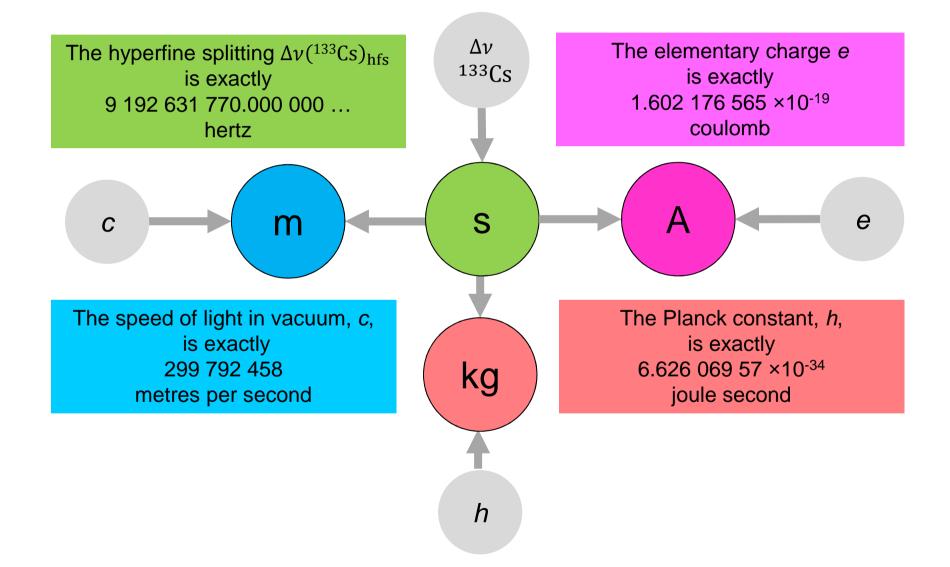


### Unit Status...

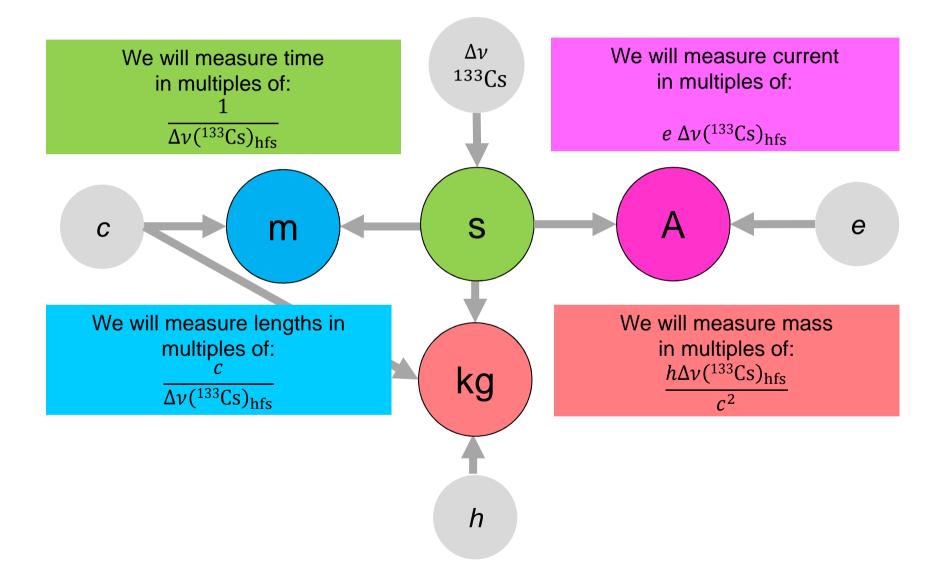
Unit	Problems with the definition?
Second	Successful: May need updating for new atomic transition
Metre	Successful
Kilogram	Unsatisfactory. The International Prototype is drifting!
Ampere	Unsatisfactory. Since 1990 realisations of the ampere (and volt and ohm) are using the new SI definitions!
Candela	Adequate
Mole	Successful: But definition linked to mode of realisation
Kelvin	Successful: But definition linked to mode of realisation No link to the unit definitions for energy

### The 'Core' Units

# The NEW International System of Units... ...is the system of units in which...



### So in future...



## The core of the 'New SI'...

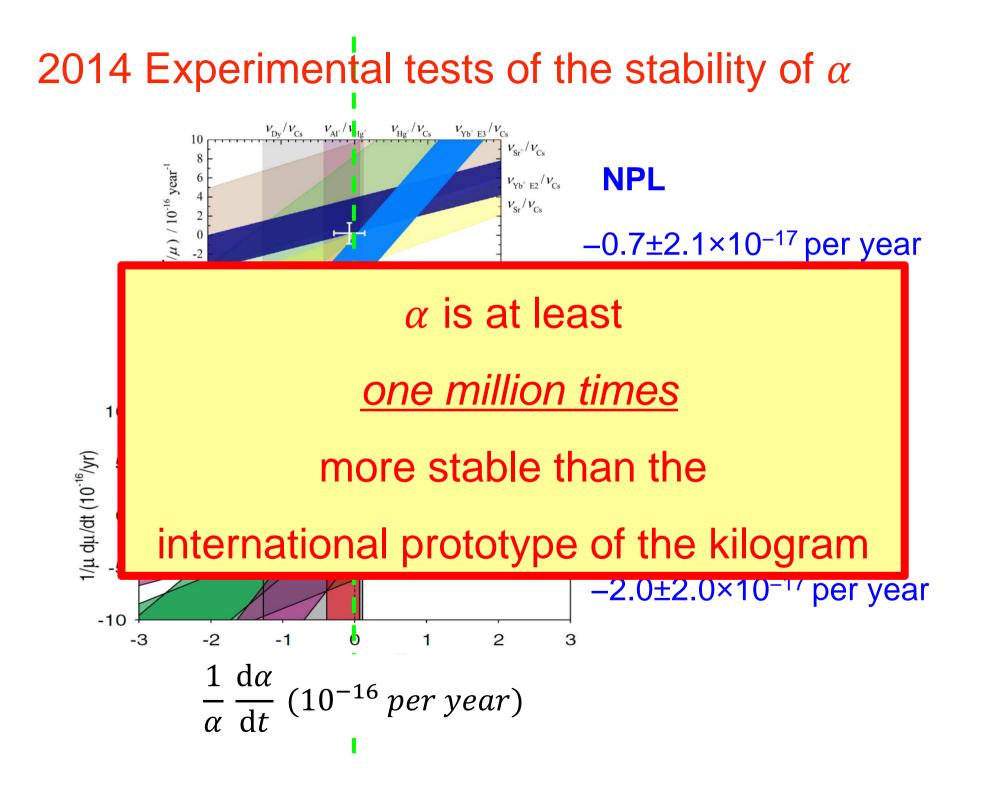
• Based on our belief that *c*, *h* and *e* have not changed for a long time

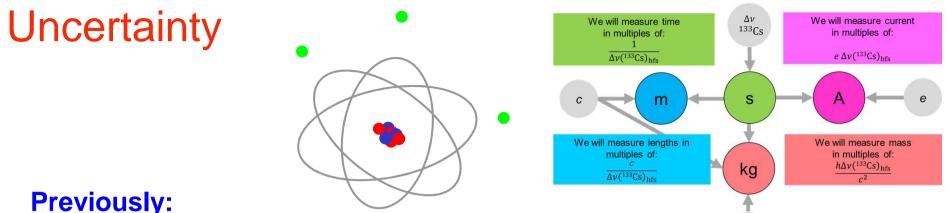
$$\alpha = \frac{e^2}{hc}$$

• The stability of the  $\alpha$  can be measured using atomic clocks

Improved Limit on a Temporal Variation of mp/me from Comparisons of Yb+ and Cs Atomic Clocks N. Huntemann, B. Lipphardt, Chr. Tamm, V. Gerginov, S. Weyers, and E. Peik *Physical Review Letters* **113**, 210802 2014 – Published November 17, 2014

Frequency Ratio of Two Optical Clock Transitions in Yb+171 and Constraints on the Time Variation of Fundamental Constants
R. M. Godun, P. B. R. Nisbet-Jones, J. M. Jones, S. A. King, L. A. M. Johnson, H. S. Margolis, K. Szymaniec, S. N. Lea, K. Bongs, and P. Gill *Physical Review Letters* 113, 210801 2014 – Published November 17, 2014





#### **Previously:**

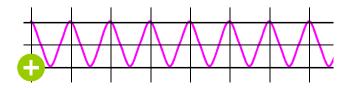
- We scaled our measurement system to human-scale artefacts
- 'Constants' needed to be measured and so had measurement uncertainty

#### In this conception of the SI

- We scale our measurement system to 'natural constants'
- The constants in the unit *definitions* have no uncertainty.

#### This is not magic or trickery!

It simply places the measurement uncertainty in a part of the traceability chain where it can be reduced without requiring a unit re-definition.

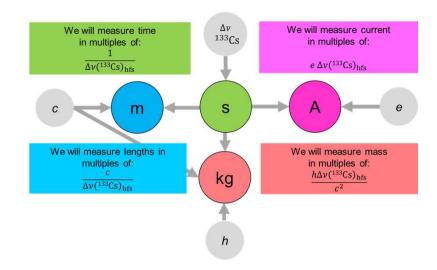


### Abstraction

#### The new definitions are more abstract.

Improves the longevity of the definitions

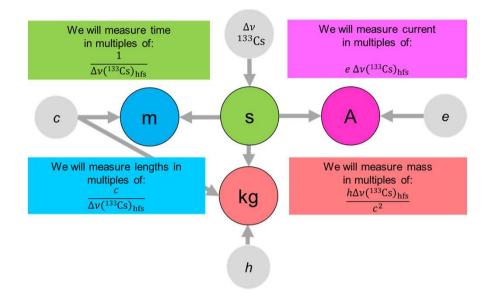
How do we explain how fixing h defines a unit of mass?



The ampere is that constant current which, if maintained in two straight parallel conductors of infinite length, of negligible circular cross-section, and placed 1 metre apart in vacuum, would produce between these conductors a force equal to  $2 \times 10^{-7}$  newton per metre of length.

How do we explain how this defines a unit of electric current?

# Summary

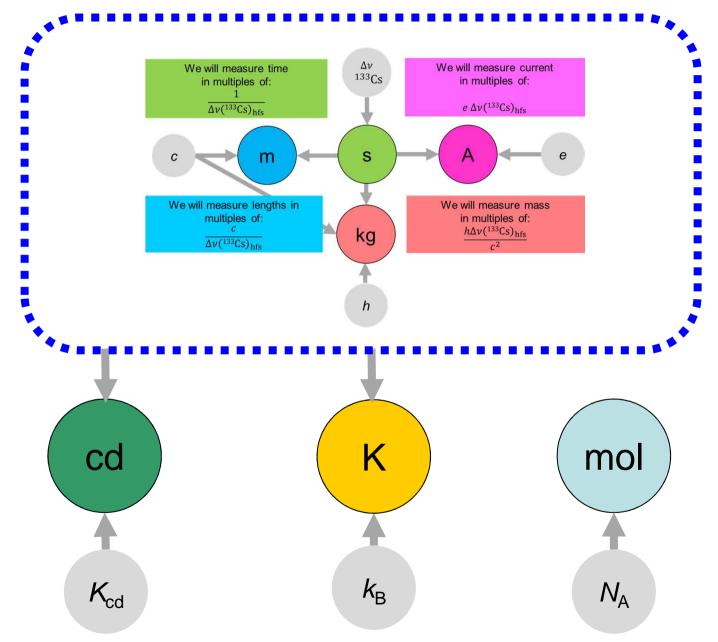


#### The definitions of 'core units' in the new SI are extremely satisfactory:

- They simply specify 'natural constants'
- Their abstraction leads to the possibility of improvement in the technology of realising the units without affecting the definition.
- The long-standing 'Ampere problem' is resolved
- The 'Kilogram problem' is resolved. Just.

### The 'Non-Core' Units

### There are three non-core units in the new SI...



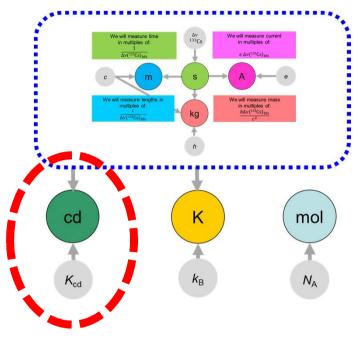
### The 'new' candela...

### Key concept is unchanged.

 $K_{cd}$  is simply re-stated as an 'explicit constant'

The luminous efficacy,  $K_{cd}$ , for monochromatic radiation of frequency 540 × 10<sup>12</sup> Hz is exactly 683 when it is expressed in the SI units cd·sr/W = Im/W

The unique feature of the candela is that it is linked to human perceptions which are likely to vary from person to person.



## The 'new' mole...

Redefinition is a consequence of the kilogram re-definition.

Previously:

• The number of atoms in 12 g of <sup>12</sup>C

Proposed:

- We will measure term
   av(1^2/GS))00
   We will measure term

   av(1^2/GS))00
   av(1^2/GS))00
   av(1^2/GS))00

   We will measure terms
   av(1^2/GS))00
   av(1^2/GS))00

   We will measure terms
   by av(1^2/GS))00
   av(1^2/GS))00

   Cold
   By av(1^2/GS))00
   By av(1^2/GS))00

   For av(1^2/GS))00
   By av(1^2/GS))00
   By av(1^2/GS))00
- $N_A$  elementary entities where  $N_A = 6.022 \ 141 \ 29 \ \times 10^{23} \ exactly$
- Recognises that Chemistry is about <u>stoichiometry</u>, not mass
- What was previously a definition of the mole a weighing procedure now becomes a technique for realising the mole.

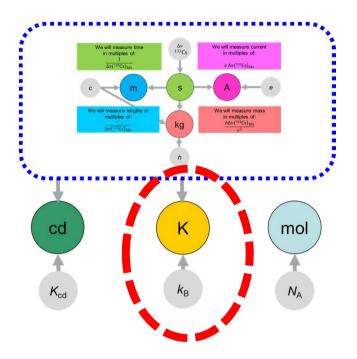
# The kelvin...

Redefinition links kelvin to the concept of molecular energy

Previously:

• *T*<sub>TPW</sub> = 273.16 K <u>exactly</u>

Proposed:



- $k_{\rm B} = 1.380\ 648\ 52 \times 10^{-23}$  joules per kelvin <u>exactly</u>
- $N_A \times k_B = R = 8.31445986$  joules per kelvin per mole <u>exactly</u>
  - Recognises the statistical mechanical nature of temperature
  - Temperature measurements no longer tied to  $T_{\text{TPW}}$

## The 'New' SI

- Builds the SI on the most stable things we know:
  - Natural Constants
- Removes uncertainty from *definitions* of the units:
  - There will always be uncertainties in how units are realised.
- Corrects problems with:
  - Kilogram
  - Ampere
- Consequences for:
  - mole

Why are we re-defining the kelvin?

How will you know what the temperature is next year?

### 1. What's the point?

2. The new SI

3. The new kelvin

4. What was the point again?

The definition of the kelvin in the new SI

### Rationale

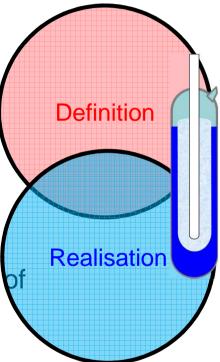
Implementation

Implications

# What was the alternative?

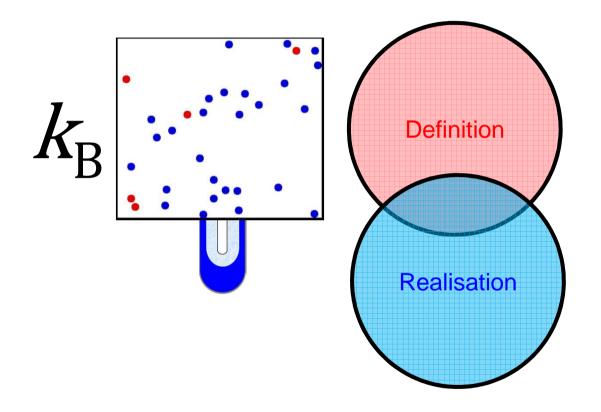
To define the kelvin in the same style as the rest of the new SI

- We <u>could</u> have used the explicit constant definition to re-state
  - "*T*<sub>TPW</sub> = 273.16 K exactly"
- If we had chosen that:
  - Then nothing would change.
  - No separation between definition and realisation.
  - In the context of the new SI, it implies  $T_{\text{TPW}}$  is fundamental to what we *mean* by temperature
  - No possibility of ever improving beyond realise-ability  $T_{\rm TPW}$ 
    - Inhibits possible technological or theoretical progress, especially at temperature extremes.
  - No connection to the rest of the SI and the concept of Energy



#### The choice to base the kelvin on a defined value of $k_{\rm B}$ is profound:

- It creates a 'modern' unit definition.
- It acknowledges underlying molecular reality.



### Why has this taken so long?

## **Thermal pioneers**

- Anders Celsius (1710) and Daniel Gabriel Fahrenheit (1724)
  - Allowed people to investigate the world
  - Thermometers were useful
- Jean-Rantiste Jeenh Fourier (1807 1820)

### No consensus on what thermometers measured!

- Theory of Free and Perfectly Elastic Molecules in a State of Motion
- James Clerk Maxwell (1859-1866)
- Ludwig Boltzmann (1866)

• The kinetic theory of gases

- Josiah Willard Gibbs(1901)
- John Tyndall (1865)
  - Wrote the textbook: "Heat: a mode of motion"
- John Baptiste Perrin (1926)
  - Nobel prize for finally demonstrating the existence of atoms



Jean Baptiste Joseph Fourier

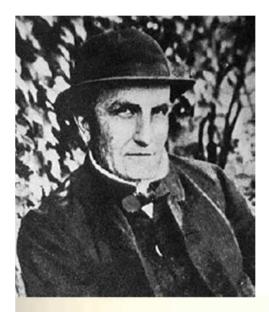
## Analytical Theory of Heat

PRIMARY causes are unknown to us; but are subject to simple and constant

Newton comprised the system of the universe. It is recognised that the same principles regulate all the movements of the stars, their form, the inequalities of their courses, the equilibrium and oscillations of the seas, the harmonic vibrations of the air and sonorous bodies, the transmission of light, capillary actions, the

But whatever may be the range of mechanical theories, they do not apply to the effects of heat. These make up a special order of phenomena which cannot be explained by the principles of motion and equilibrium.

Preliminary Discourse But whatever may be the range of mechanical theories, they do not apply to the effects of heat. These make up a special order of phenomena, which cannot be explained by the principles of motion and equilibrium. We have for a long time been in possession of ingenious instruments adapted to measure many of these effects; valuable observations have been collected; but in this manner partial results only have become known, and not the mathematical demonstration of the laws which include them all.



John James Waterston (1845)

On the Physics of Media that are Composed of Free and Perfectly Elastic Molecules in a State of Motion

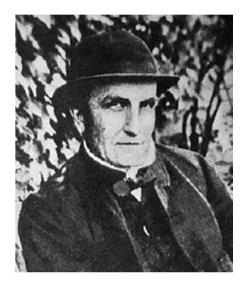
# PHILOSOPHICAL TRANSACTIONS.

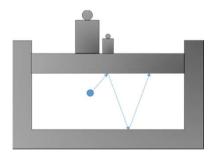
I. On the Physics of Media that are Composed of Free and Perfectly Elastic Molecules in a State of Motion.

By J. J. WATERSTON.

Communicated by Captain BEAUFORT, R.N., F.R.S., &c.

Received December 11, 1845,-Read March 5, 1846.





To have a proper conception of what the medium is that forms the subject of ... we must imagine a vast multitude of small particles of matter, perfectly alike in every respect

...the condition of the multitude ... that form the medium may be likened to the familiar appearance of a swarm of gnats in a sunbeam.

motor than their comments hall -

...The quality of perfect elasticity being common to all the particles, the original amount of *vis viva* ...of the whole multitude must forever remain the same... as unchanged as the matter that is associated with it.

The medium must in this way become endowed with a permanent state of elastic energy, or disposition to expand, uniformly sustained in every part and communicating to it the physical character of an elastic fluid.

Pages 6 & 7

## **JJ Waterston's Predictions**

Waterston shows that a medium of this kind:

- Would obey the laws of Mariott, Dalton and Gay-Lussac
- The Vis Viva (Kinetic Energy) would be 'like Temperature' i.e.  $k_{\rm B} = 1$
- Vis Viva would equally distributed, even amongst molecules of differing

### "The paper is nothing but nonsense"

Referee 1845

- Calculates the 'mechanical equivalent of heat' (measured by Joule)
- States that the 'Absolute Zero' of temperature (~-480 °F) is when the vis

viva of molecules is zero

"The omission to publish it at the time was a misfortune which probably retarded the subject by 10 to 15 years."

Commentary by Lord Rayleigh in 1896

#### John Tyndall

HEAT

CONSIDERED AS

1865.

laht of translation is reserved

### HEAT: a Mode of Motion 1865

ng

#### PREFACE

- ▲ M In the following Lectures I have endeavoured to bring the rudiments of a new philosophy within the reach of a person of ordinary intelligence and culture.
- The first seven Lectures of the course deal with thermometric heat; its generation and consumption in mechanical processes; the determination of the mechanical equivalent of heat; the conception of heat as molecular motion; the application of this conception to solid, liquid and gaseous forms of matter; to expansion he and combustion; to specific and latent heat and to ry calorific conduction.

the possible sources of his energy; the relation of this energy to terrestrial forces, and to vegetable and animal life.

My aim has been to rise to the level of these questions

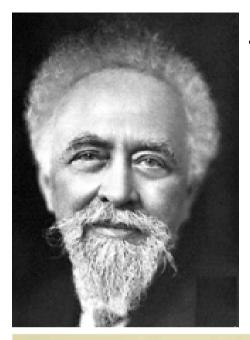
Josiah Willard Gibbs

### Elementary Principles in

In the present state of science, it hardly seems possible to frame a dynamic theory of molecular action...

the attempt to frame hypotheses concerning the constitution of material bodies, we pursue statistical inquiries as a branch of rational mechanics. In the present state of science, it seems hardly possible to frame a dynamic theory of molecular nation, which shall embrance the phenomeno of thermody

Even if we confine our attention to the phenomena distinctively thermodynamic, we do not escape difficulties in as simple a matter as the number of degrees of freedom of a diatomic gas. It is well known that while theory would assign to the gas six degrees of freedom per molecule, in our experiments on specific heat we cannot account for more than five. *Certainly, one is building on an insecure foundation who rests his work on hypotheses concerning the constitution of matter.* 



#### Jean Baptiste Perrin

### Nobel Prize for Physics 1926

"for his work on the discontinuous structure of matter, and especially for his discovery of sedimentation equilibrium".

92

Equating these two expressions we have a relation

 $f[a, a', a'', \ldots] \equiv g[b, b', b'', \ldots],$ 

where only evident realities enter, and which expresses a profound connection between two phenomena at first sight completely independent, such as the transmutation of radium and the Brownian movement. For example, if we compare the law of the distribution of the energy A of dark radiation as a function of the wave-length (No. 41) and the law of rarefaction of a uniform emulsion as a function of gravity (No. 14), we perceive that these two laws are not independent and that the one is connected to the other by the conation

The discovery of such relationships marks the point where the underlying reality of molecules becomes a part of our scientific consciousness.

scientific consciousness.

#### BROWNIAN MOVEMENT AND MOLECULAR REALITY.

BY M. JEAN PERRIN (Professeur de Chimie Physique, Faculté des Sciences, Université de Paris.)

TRANSLATED FROM THE

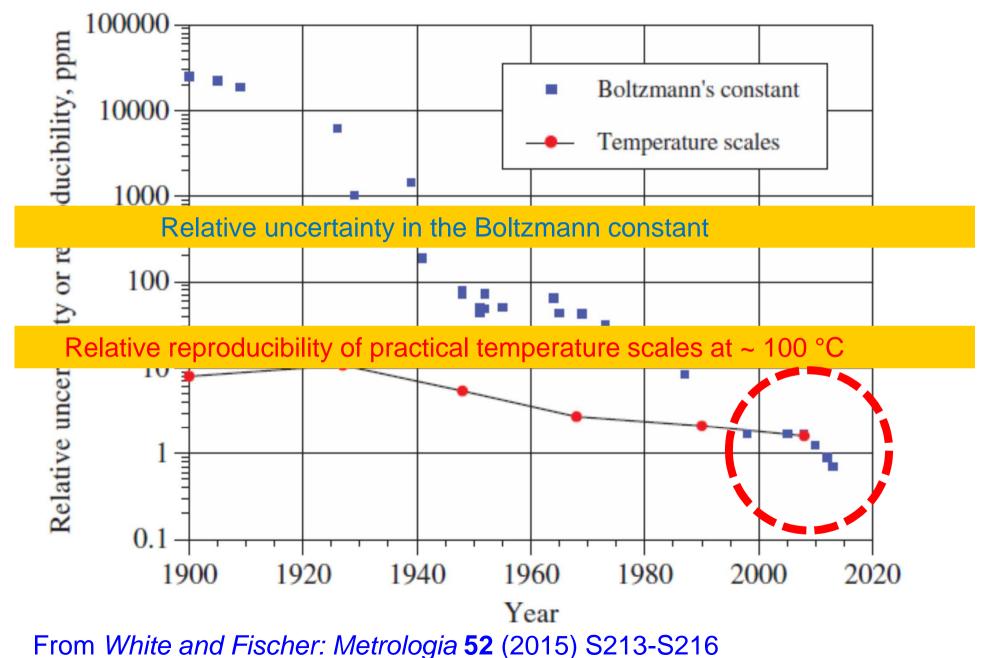
ANNALES DE CHIMIE ET DE PHYSIQUE, 8<sup>me</sup> SERIES, September 1909,

BY F. SODDY, M.A., F.R.S.

Not only are our ideas clearer...

We have progressed experimentally...

## We have (slowly) got better at measuring $k_{\rm B}$



## Why has this taken so long?

### Historically...

- Temperature measurement became important for science and engineering before we understood what we were measuring!
- The need for reproducible measurements was more important than the link to statistical mechanics

#### Now...

- We accept the existence of atoms,
- We define the SI in terms of fundamental constants,
- We accept the validity of statistical mechanics
- We have (slowly) become better at measuring  $k_{\rm B}$
- But in metrological terms, there have been very few opportunities to revise our previous scepticism.
- (ITS-1927, ITS-1948, IPTS-1968, ITS-1990)

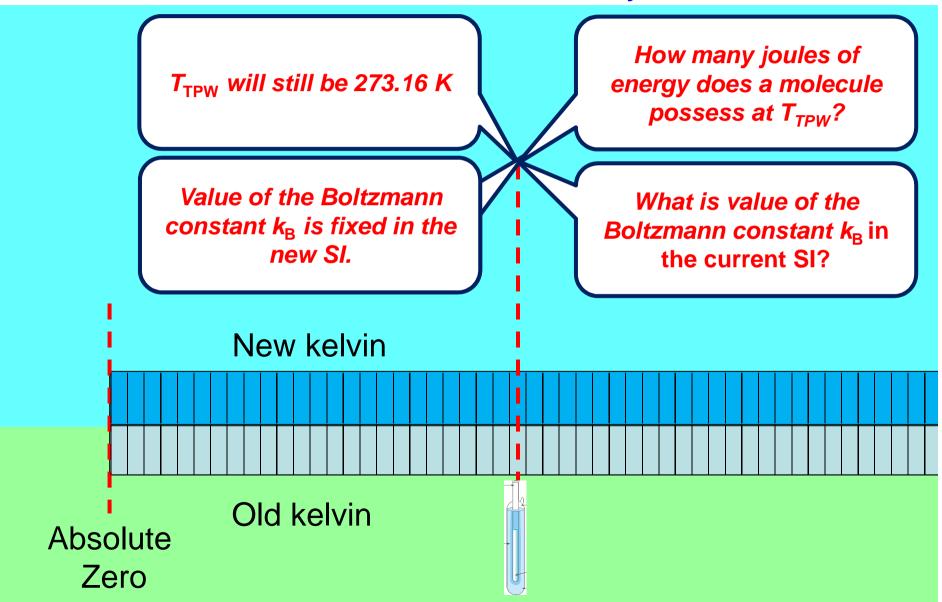
### Rationale

## Implementation

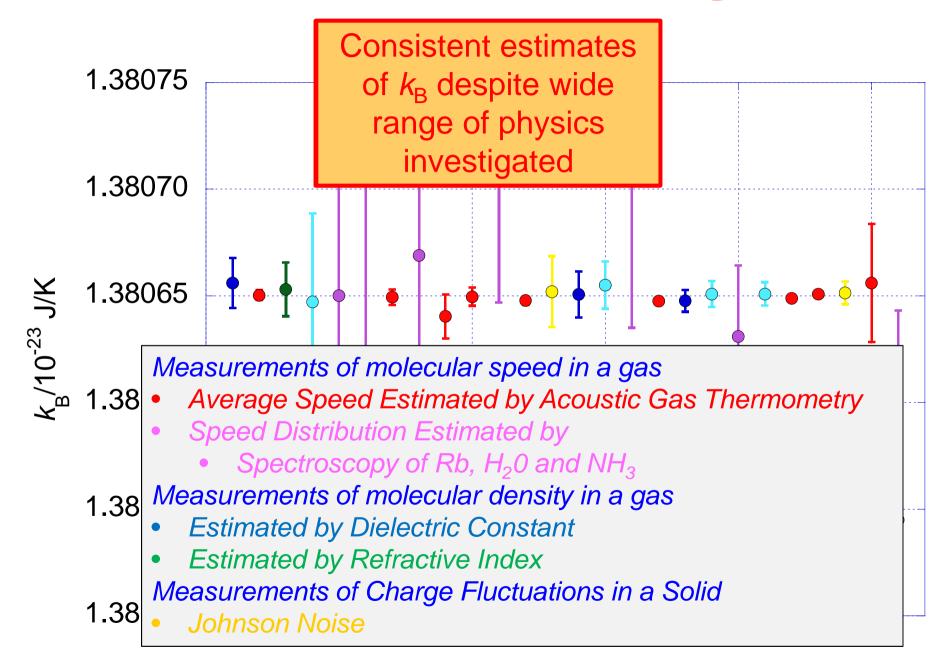
Implications

## Changing from old to new

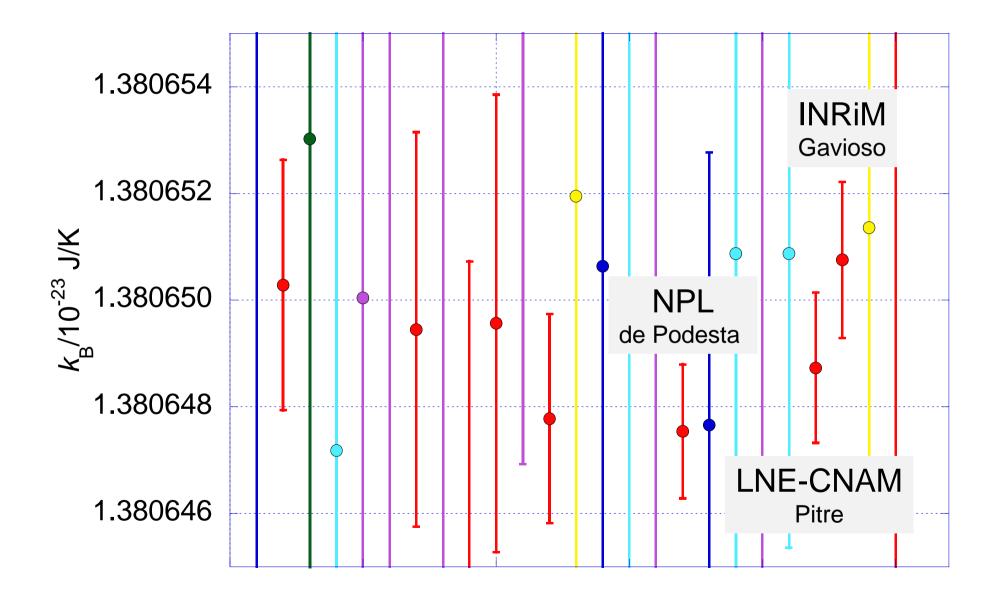
• We want the size of the kelvin to stay the same:



## How do we know we have the right $k_{\rm B}$ ?

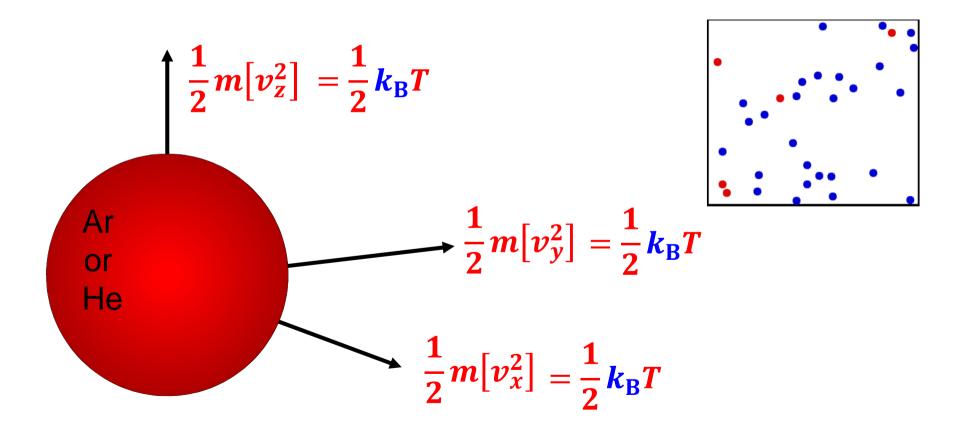


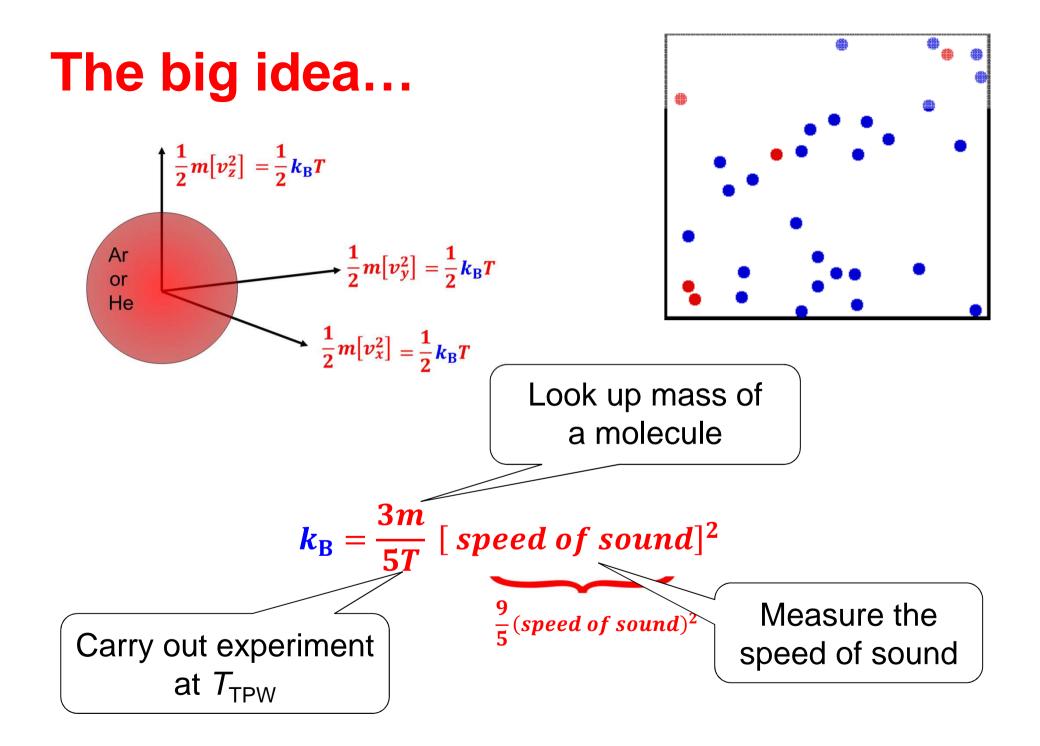
## How do we know we have the right $k_{\rm B}$ ?



## Molecular motion is simple in a gas

- We can approach 'ideal gas' conditions at low pressure
- In an ideal gas the internal energy is just the kinetic energy of the molecules





## CCT Task Group on the SI...

...requests CODATA to make its final adjustment of the value of the Boltzmann constant only when the following two conditions are met:

1. The relative standard uncertainty of the adjusted value of  $k_{\rm B}$  is less than  $1 \times 10^{-6}$ 

CODATA 2010 relative uncertainty equal to  $9.1 \times 10^{-7}$ . CODATA 2014 relative uncertainty equal to  $5.7 \times 10^{-7}$ .

2. The determination of  $k_{\rm B}$  is based on at least two fundamentally different methods, of which at least one result for each shall have a relative standard uncertainty less than 3 × 10<sup>-6</sup>.

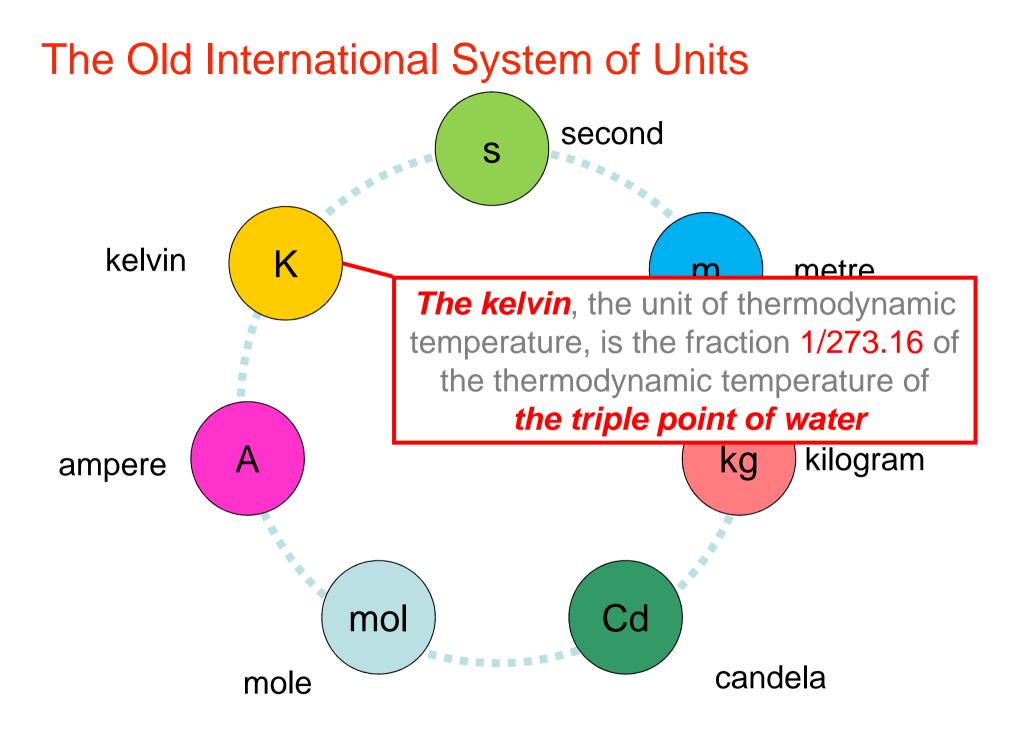
Not yet achieved.

But results expected before 2017

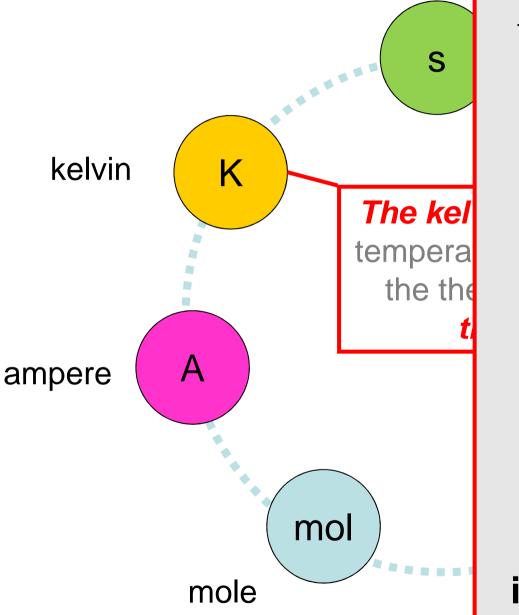
### Rationale

Implementation

Implications



### The Old International System of Units



<u>Every</u> temperature measurement is a quantitative comparison of

the 'level of molecular jiggling'

in the target with

the 'level of molecular jiggling'

in a triple-point cell

### The International System of Units

**Every** temperature measurement is a The kel quantitative tem comparison of Boltzmar kelvin K  $k_{\rm B} = 1.38$ the 'level of molecular jiggling' kel  $T_{\text{TPW}}$  will still be a era useful reproducible in the target with the temperature The SI Joule But it will not *define* (defined in terms of what we mean the product  $h\Delta v$ ) by 'one degree' 

, le n f

## **Triple point of water**



<u>Every</u> temperature measurement is a quantitative comparison of

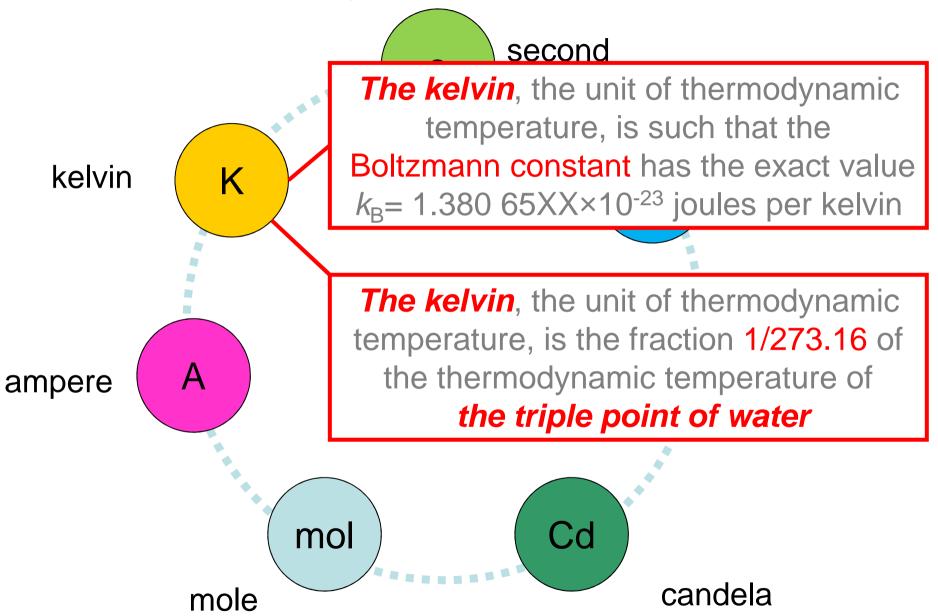
the 'level of molecular jiggling'

in the target with

the 'level of molecular jiggling'

in a triple-point cell

## The International System of Units



## **Triple point of water**



*T*<sub>TPW</sub> will still be a useful reproducible temperature

But it will not <u>define</u> what we mean by 'one degree' <u>Every</u> temperature measurement is a quantitative comparison of

the 'level of molecular jiggling'

in the target with

The SI Joule (defined in terms of the product  $h\Delta v$ )

## For temperature dissemination..

### Immediately

- No consequences
- ITS-90 will still be based on the triple point of water
- The uncertainty in  $T_{\text{TPW}}$  (likely to be ~140 µK) will increase the thermodynamic uncertainty of all  $T_{90}$  estimates
  - But this is tiny compared to the known errors in  $T_{90}$
- No impacts expected

## For Fundamental thermometry 'close' to $T_{\text{TPW}}$

#### **Currently**:

- We estimate  $T_{unknown}$  as a ratio to  $T_{TPW}$ , which is 'known' exactly.
- $u(T_{\text{TPW}})$  is then the uncertainty of realisation ~ 40  $\mu$ K (k = 1)

#### In future:

- Traceability to the joule is more complex than traceability to  $T_{\text{TPW}}$
- Now the value of  $T_{TPW}$  is itself uncertain with an uncertainty (after redefinition) of close to 140  $\mu$ K making a quadrature sum ~146  $\mu$ K

#### For example:

- At 303 K in our recent measurements of  $T T_{90}$ 
  - *u*(*T*) was ~ 150 µK.
  - u(T) will increase to ~ 205  $\mu$ K.

#### But notice that.:

- The uncertainty of any product  $k_{\rm B}T$  or RT is unaffected
- Unlikely to have any major significance

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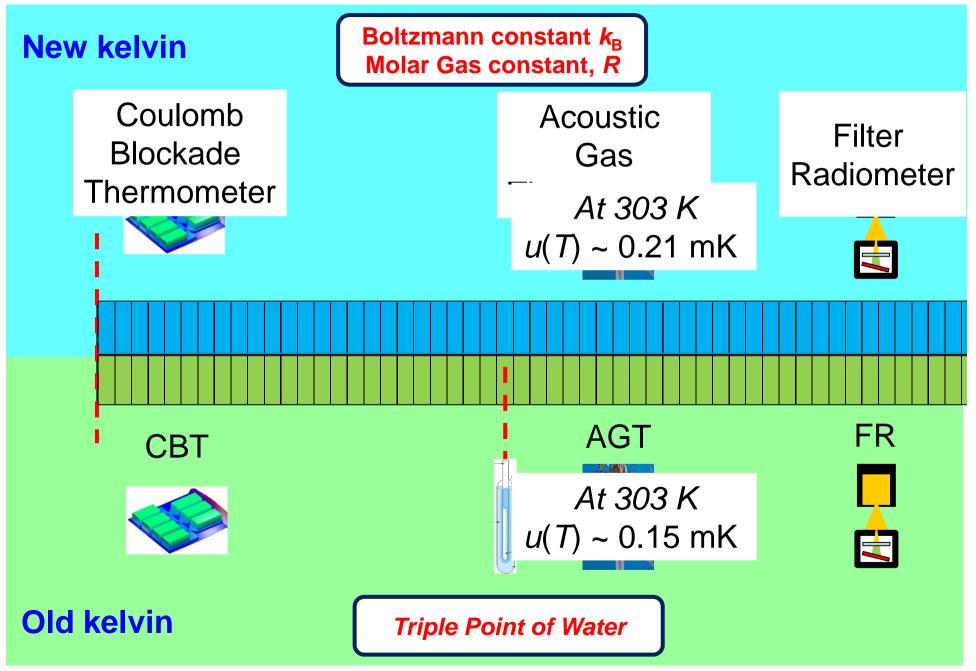
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#### But notice that:

- The uncertainty of any product  $k_{\rm B}T$  or RT is unaffected
- Unlikely to have any major significance

## For Fundamental thermometry



# For primary thermometry $T >> T_{TPW}$

#### **Currently two routes to traceability via Planck Law**

Traceability to	
kelvin	electrical power
$T_{\text{unknown}}$ deduced from a spectral radiance ratio to (say) $T_{\text{Cu}}$ .	T <sub>unknown</sub> deduced from absolute spectral radiance (W sr <sup>-1</sup> m <sup>2</sup> )

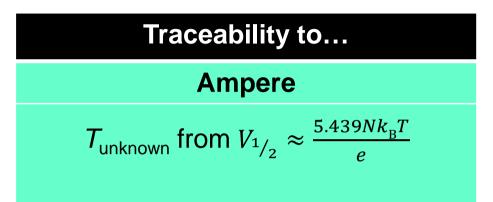
#### In future

Traceability to	
kelvin	electrical power
u(T <sub>unknown</sub> ) will be <i>increased</i>	u(T <sub>unknown</sub> ) will be <i>decreased</i>
(negligibly) by an additional	(negligibly) by an removal of
140 $\mu$ K ( $k = 1$ ) of uncertainty in $T_{TPW}$ .	uncertainty in $k_{\rm B}$ .

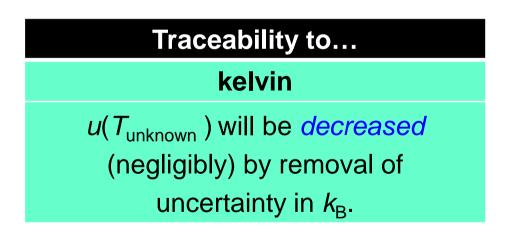
• Unlikely to have any major significance

## For primary thermometry $T << T_{TPW}$

#### For example, Coulomb Blockade Thermometer



In future

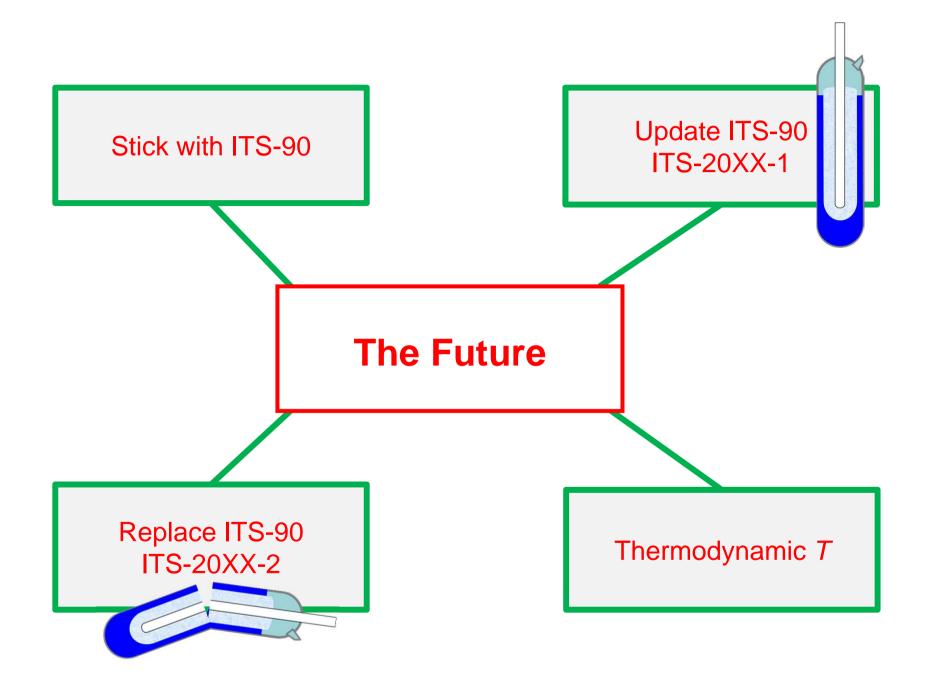


• Unlikely to have any major significance

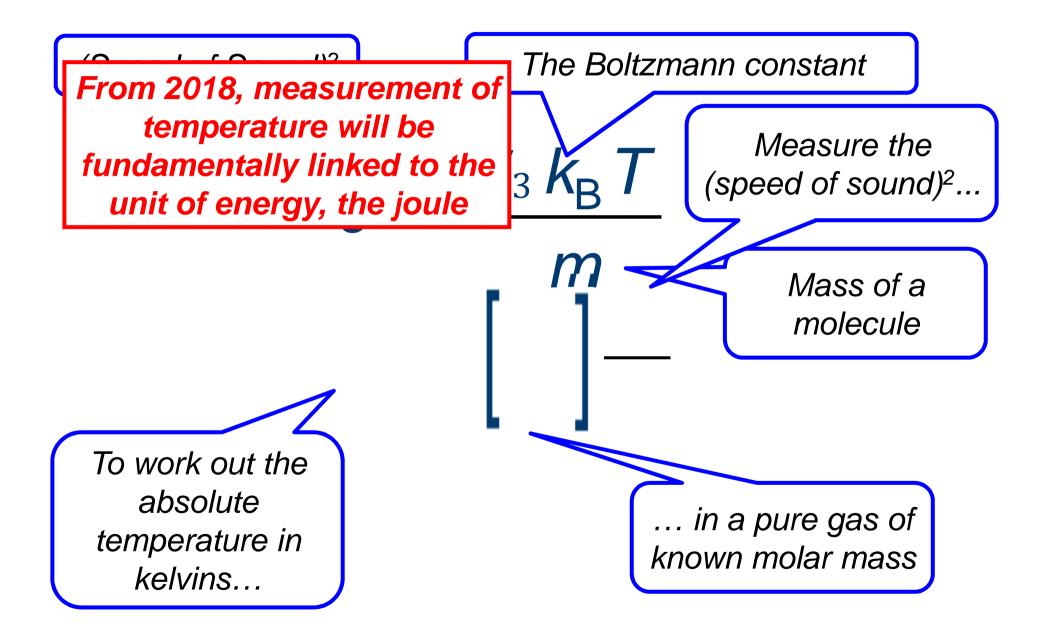
Rationale

Implementation

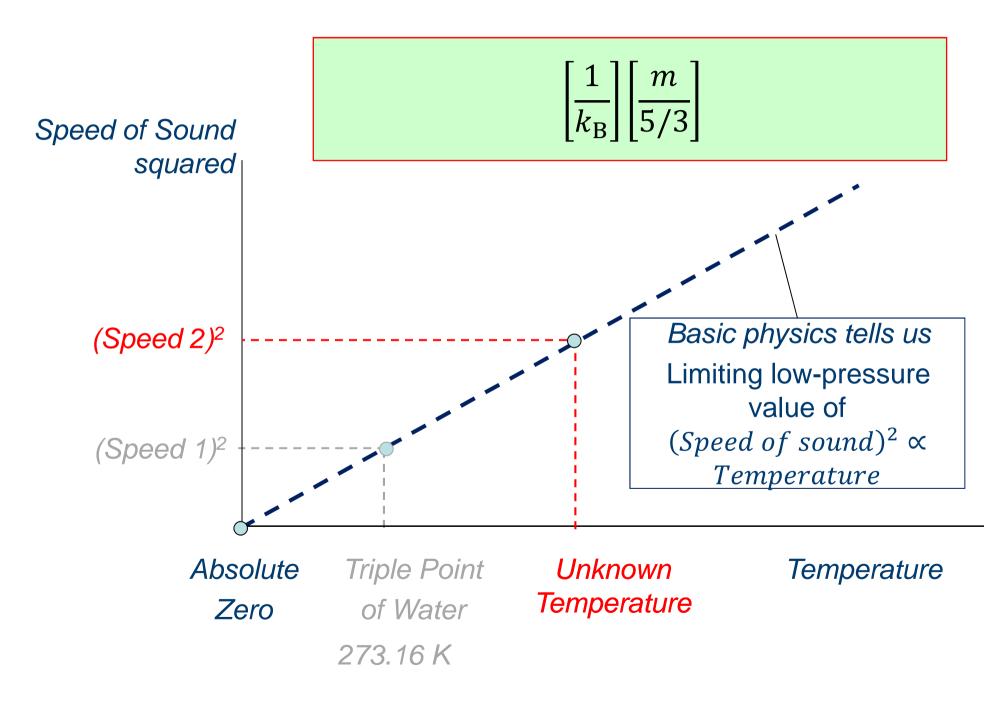
### **Longer Term Implications**



## Thermometry after 2018



### How to work out an unknown temperature after 2018



## **Practical** Thermodynamic Thermometers?

- An atom-perfect nano-structured material with an artificially engineered electrical conductivity or tunnelling characteristic.
- Computers of sufficient power to model the electrical resistivity of a metal or semiconductor from first principles.
  - SPRT or thermistor would become a *primary* instrument.
- Photonic crystal interferometers with the possibility of primary selfcalibration.
- Acoustic resonators that could act as super-accurate references cheaper and more reliable than an SPRT.
  - Possible lower uncertainty than  $T_{90}$
- Practical Johnson Noise Thermometer
- Something else that we can't imagine!

All these devices are conceivable. In 100 years time they may even be likely

## The Distant Future...

- Everyone is happy ③
- Everything is perfect ③
- Thermodynamic Thermometers are used in every NMI!
- Practical Thermodynamic Thermometers will be here 'soon'
- A new fixed-point is sent to three NMIs
  - Thermodynamic thermometer A in PBT reads 34.234 °C Thermodynamic thermometer B in NLP reads 35.111 °C
  - Thermodynamic thermometer C in NSIT reads 33.123°C

In a world of thermodynamic thermometers, we still need the equivalent of ITS-90 to enable reliable comparisons

For thermometery, it is almost always more important to agree on the temperature, than to be 'right' 'Cooking' is more important than 'science'! How will you know what the temperature is next year?

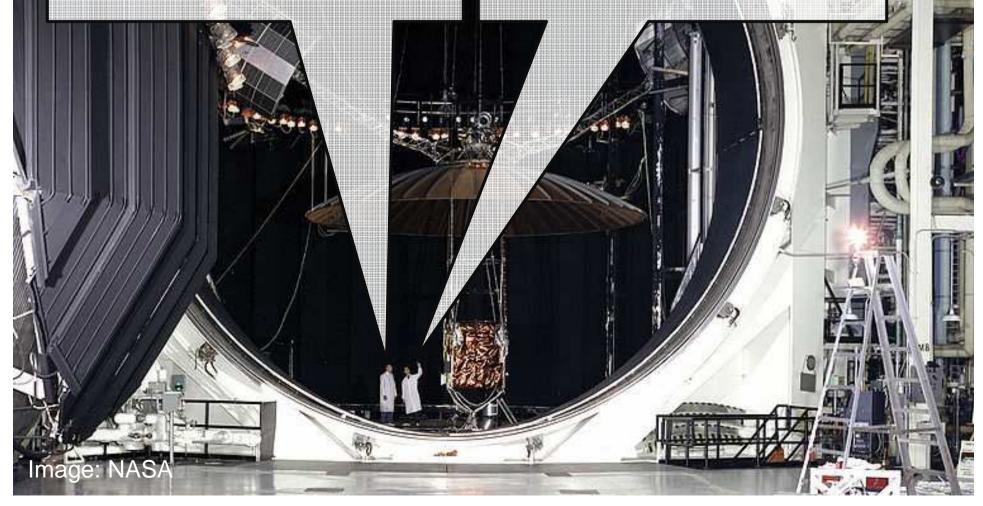
- 1. What's the point?
- 2. The new SI

3. The new kelvin

4. What was the point again?

### I measured the temperature of the antenna to be 148.4 K

Is that correct? On NPL-SAT-1 wasn't it 168 K in 2007?



## Summary

### The kelvin redefinition:

- Fits well within the new model of the SI
- Separates what we mean by 'one kelvin', from how we realise it.
- Does not solve any problems we have today.
- Paves the way for future developments.

#### In short term:

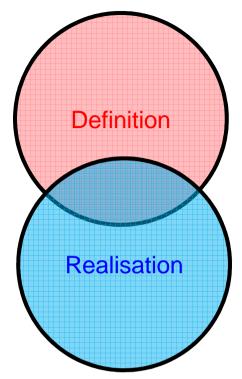
 No negative consequences because of the widespread use of ITS-90

### In the medium term :

• Questions about role and design of a replacement for ITS-90

#### In the distant future:

- People will look back and ask why it took so long.
- But they will probably still be using something like ITS-90!

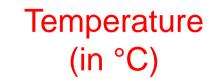


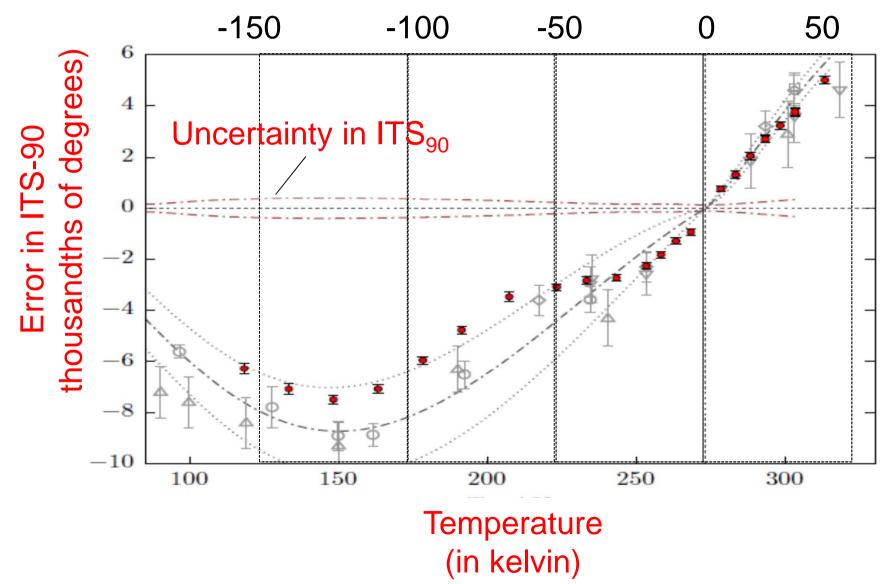
## **Precision Measurement...**

# ...brings the world into focus

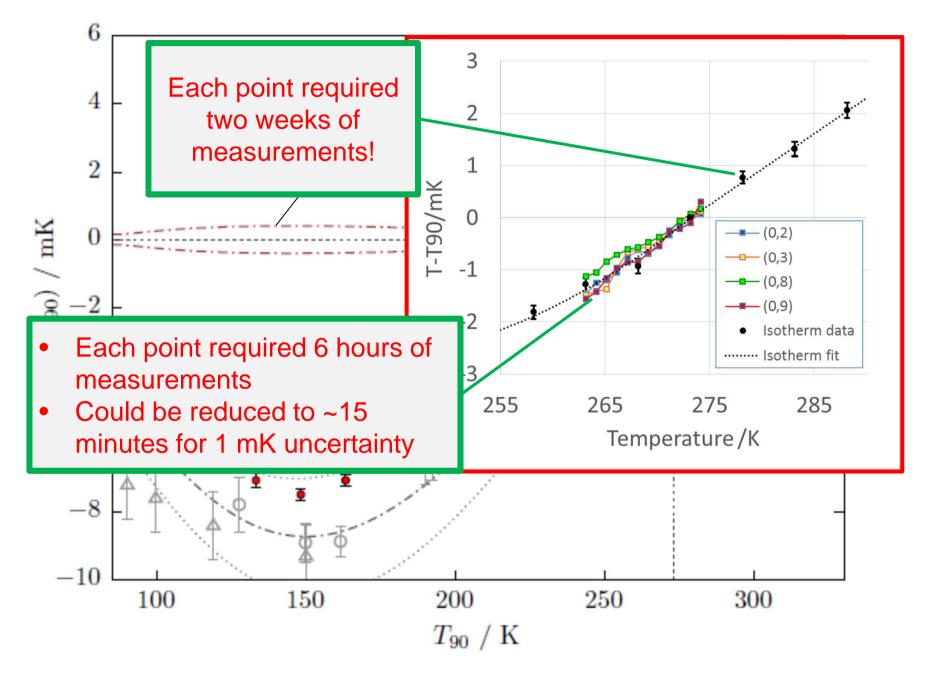
Thank you

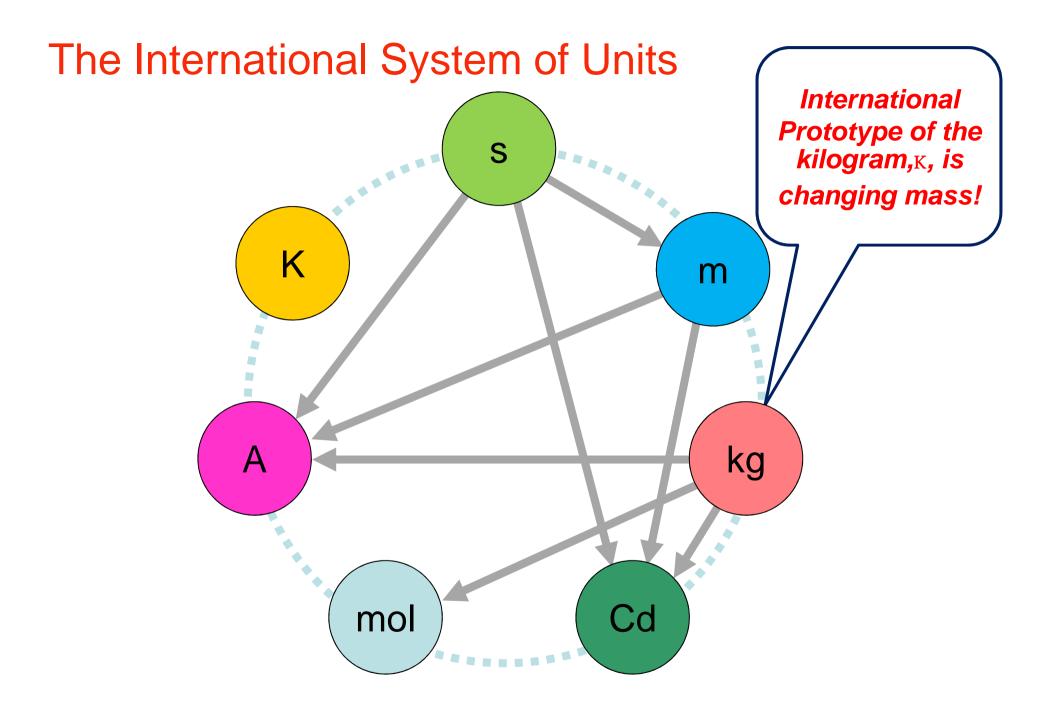
## **Errors in ITS-90**





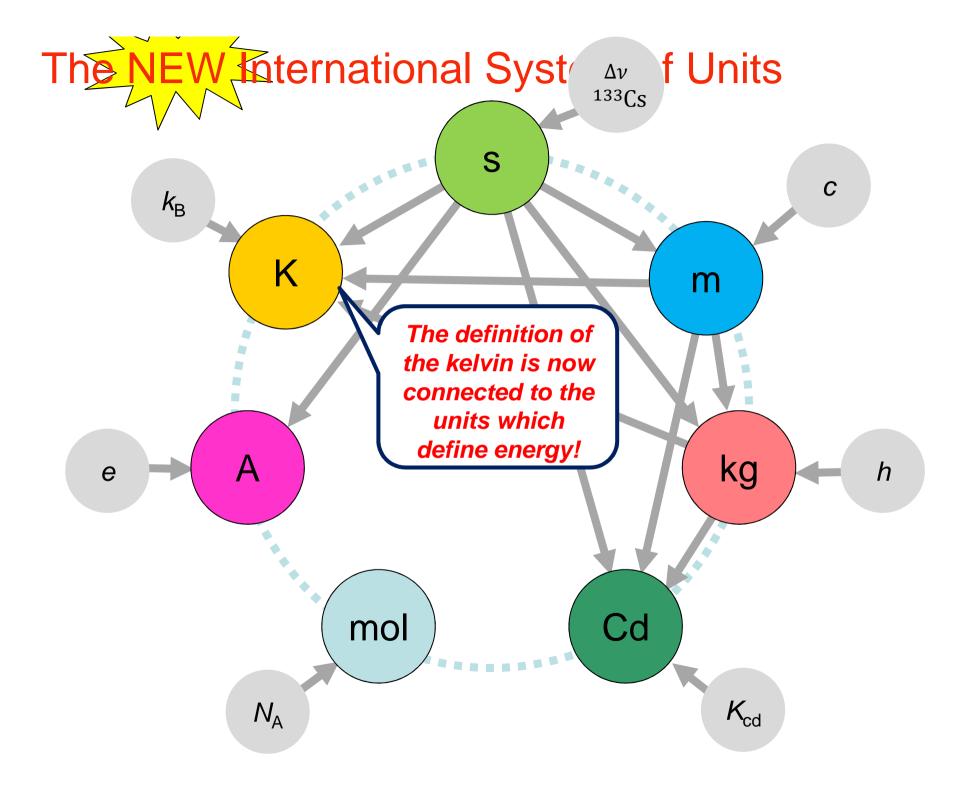
## $T - T_{90}$ showing only uncertainty in T

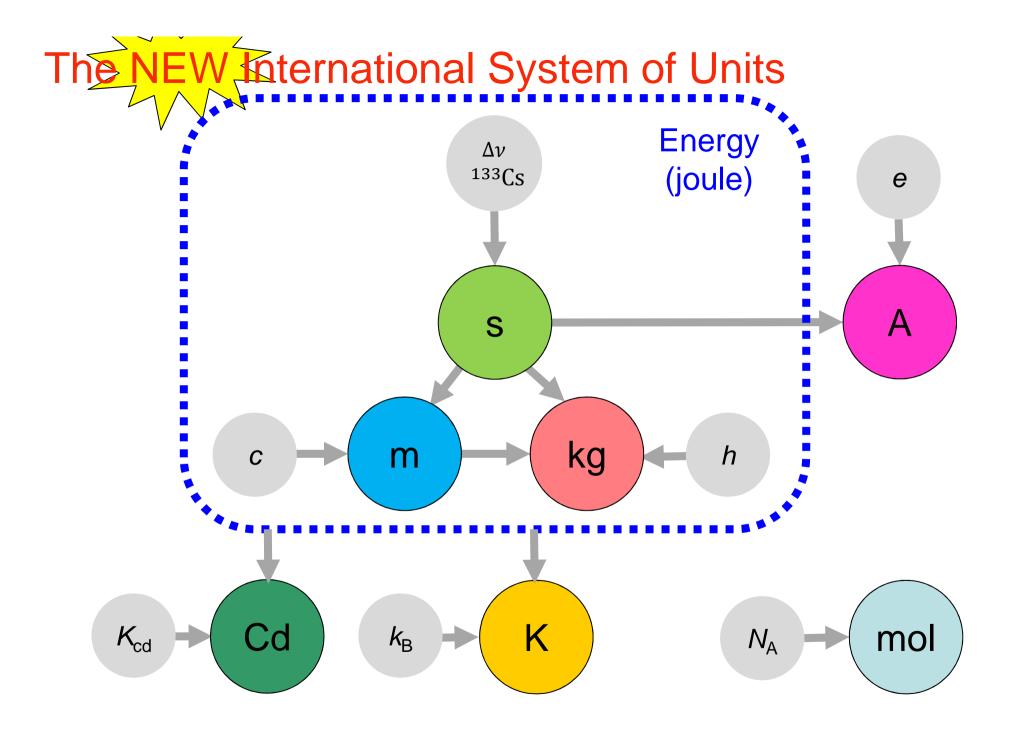


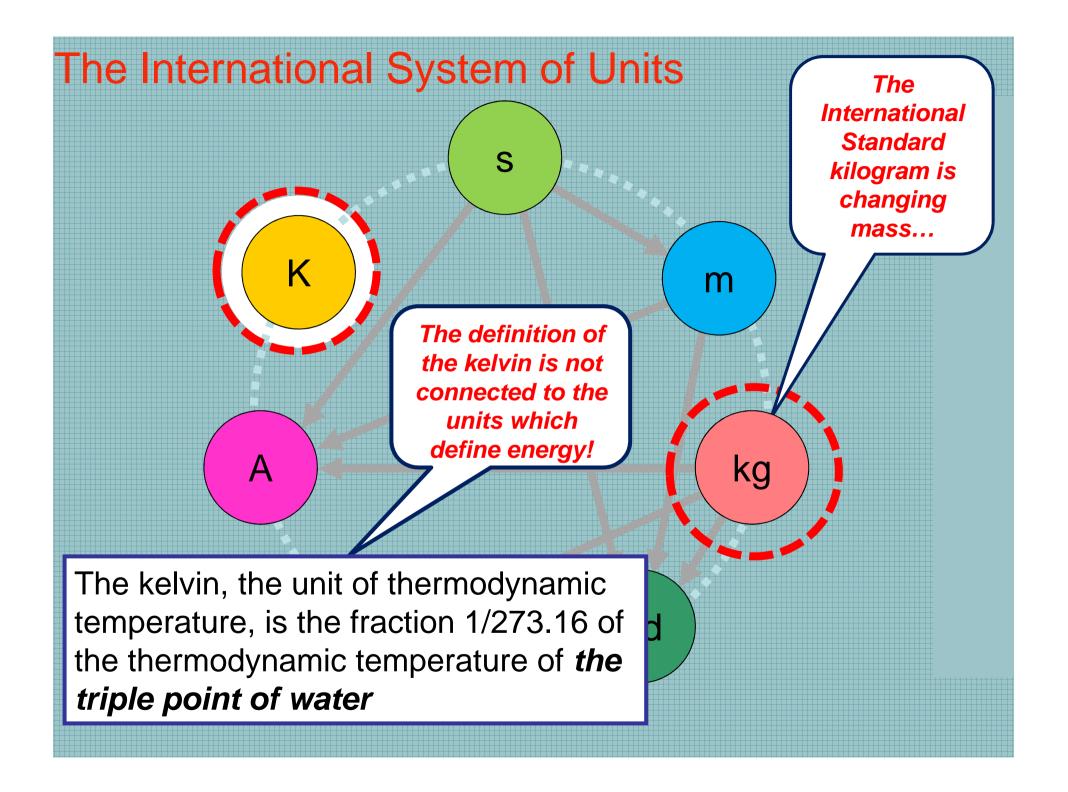


### The NEW International System of Units

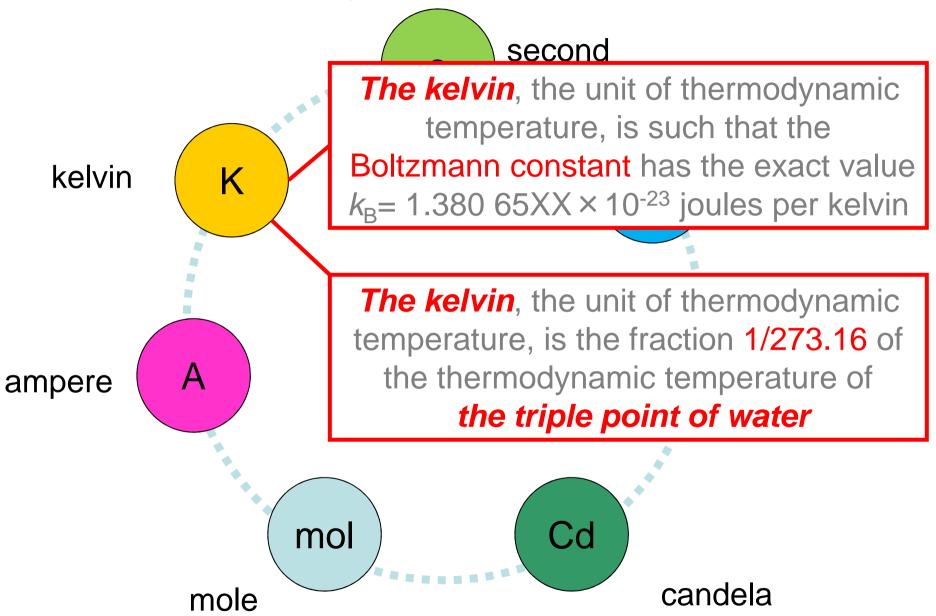




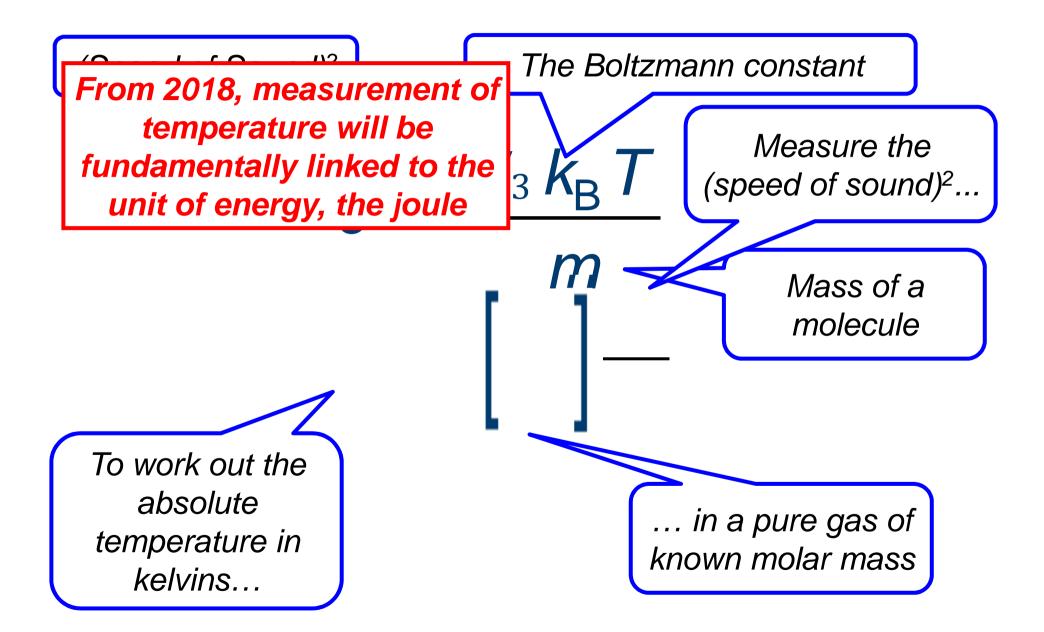




## The International System of Units



## An acoustic thermometer



### How to work out an unknown temperature after 2018

