

Plasmonics: An overview and some new trends

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INSTITUCIÓ CATALANA DE
RECERCA I ESTUDIS AVANÇATS



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Plasmonics: An overview and some new trends

Introduction to plasmons

Graphene plasmons

Quantum-mechanical description

Classical description

Complete optical absorption

Quantum optics with graphene plasmons

Sensing with graphene plasmons

Plasmons in other atomically thin materials

The scales of light

Things Natural



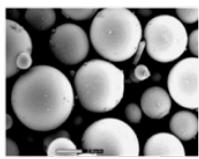
Dust mite
200 μm



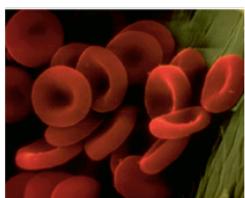
Ant
~ 5 mm



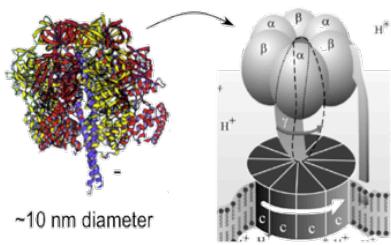
Human hair
~ 60-120 μm wide



Fly ash
~ 10-20 μm



Red blood cells
(~7-8 μm)

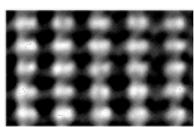


~10 nm diameter

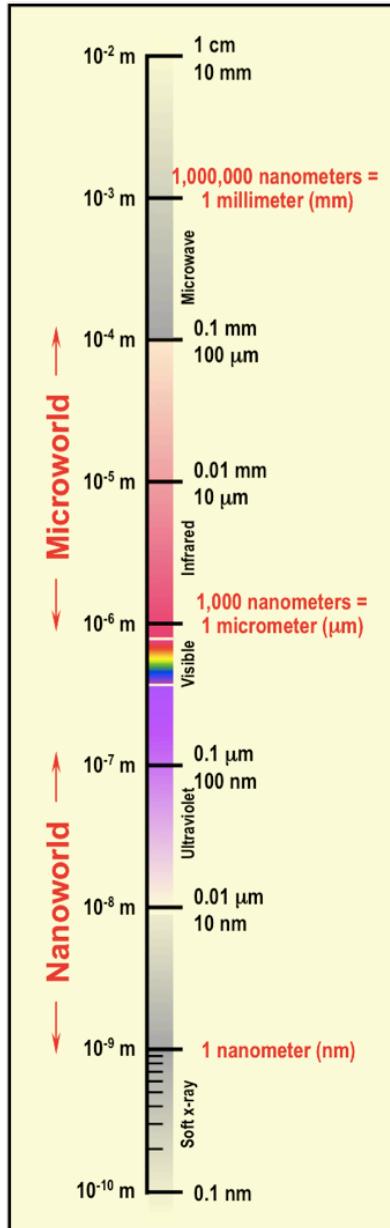
ATP synthase



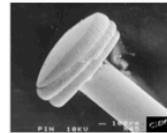
DNA
~2-1/2 nm diameter



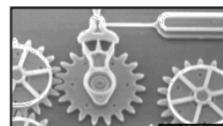
Atoms of silicon
spacing 0.078 nm



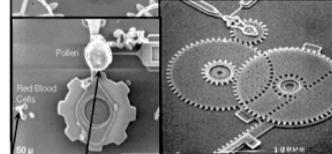
Things Manmade



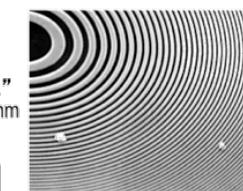
Head of a pin
1-2 mm



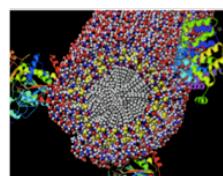
MicroElectroMechanical (MEMS) devices
10 -100 μm wide



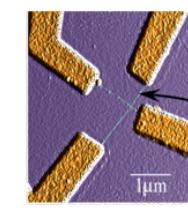
Pollen grain
Red blood cells



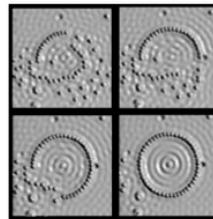
Zone plate x-ray "lens"
Outer ring spacing ~35 nm



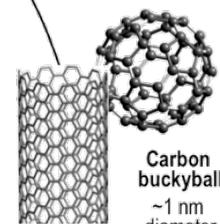
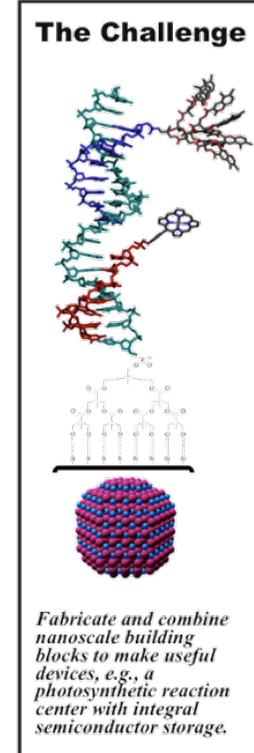
Self-assembled,
Nature-inspired structure
Many 10s of nm



Nanotube electrode
1 μm

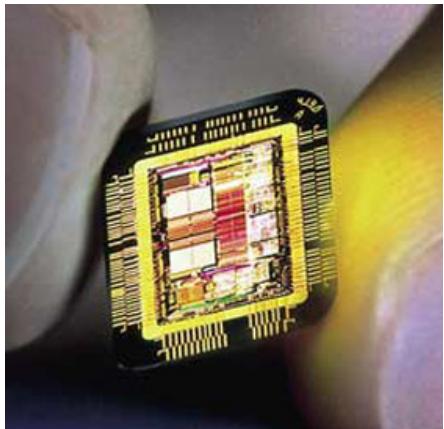


Quantum corral of 48 iron atoms on copper surface
positioned one at a time with an STM tip
Corral diameter 14 nm

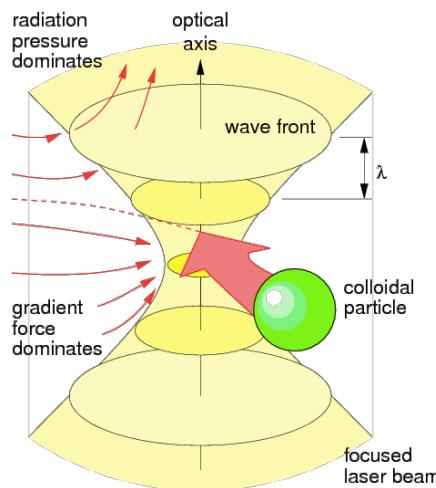


Carbon buckyball
~1 nm diameter

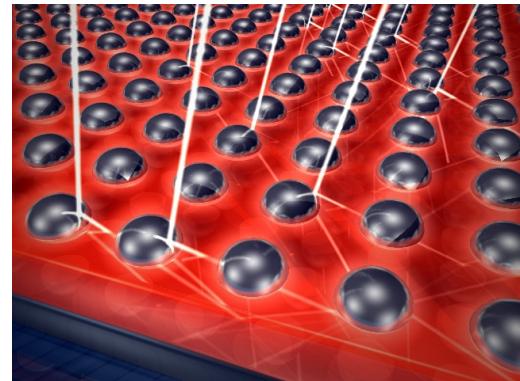
Light in technology



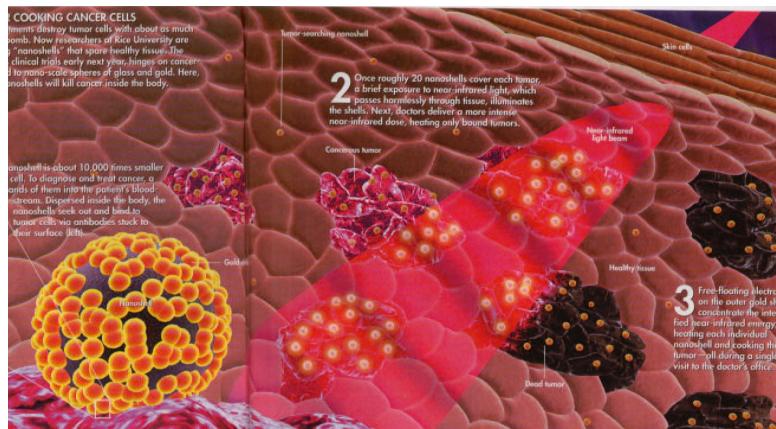
optical lithography



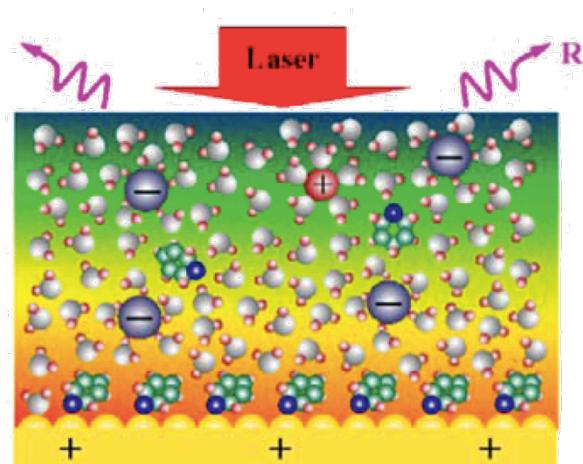
optical trapping



improved photovoltaics

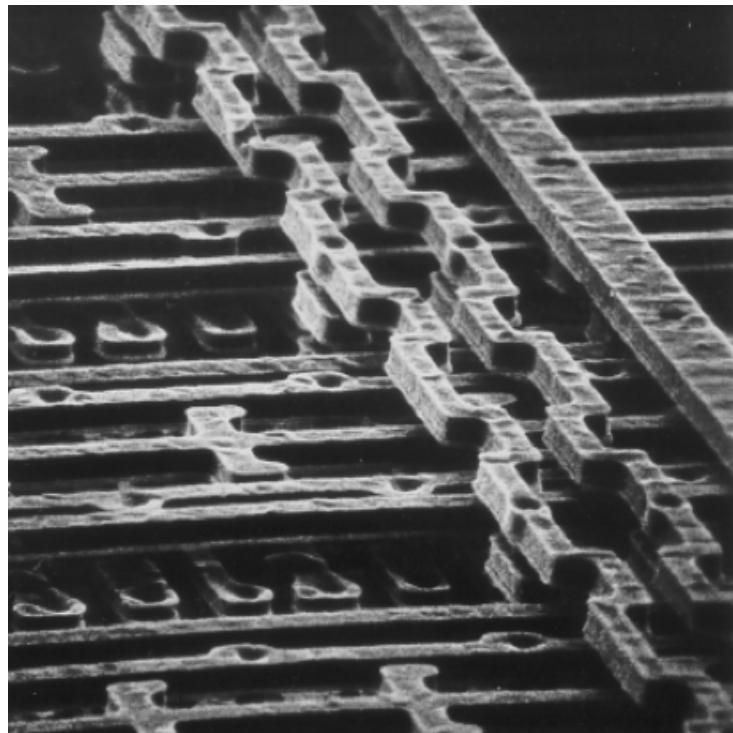
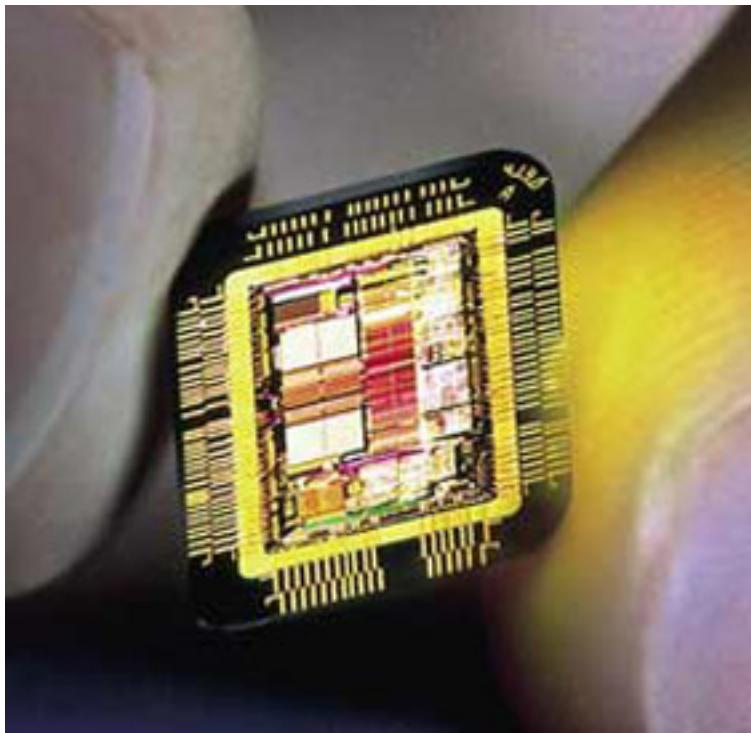


cancer therapy



**single-molecule sensing
photocatalysis**

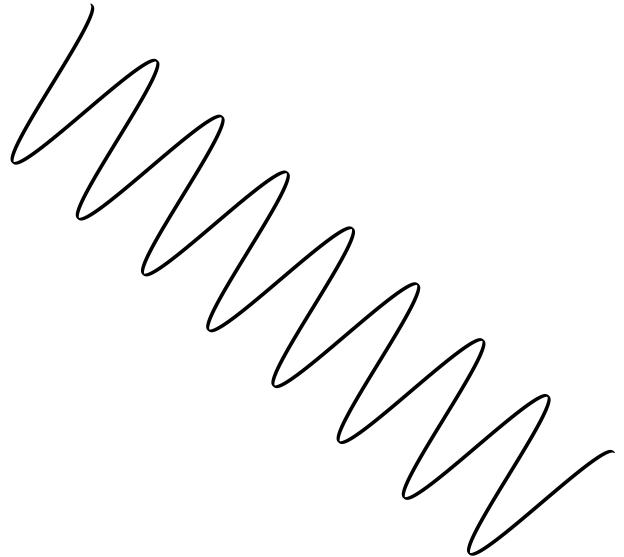
Optical lithography limited by diffraction



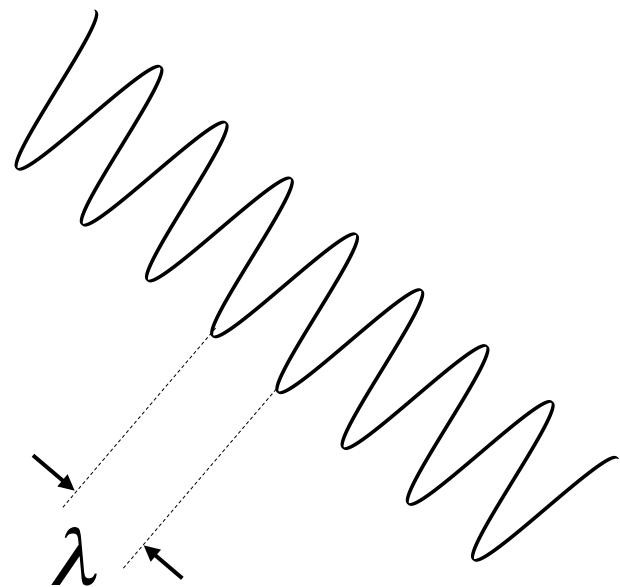
32 nm lines

193 nm ArF excimer laser in water (refractive index 1.44)

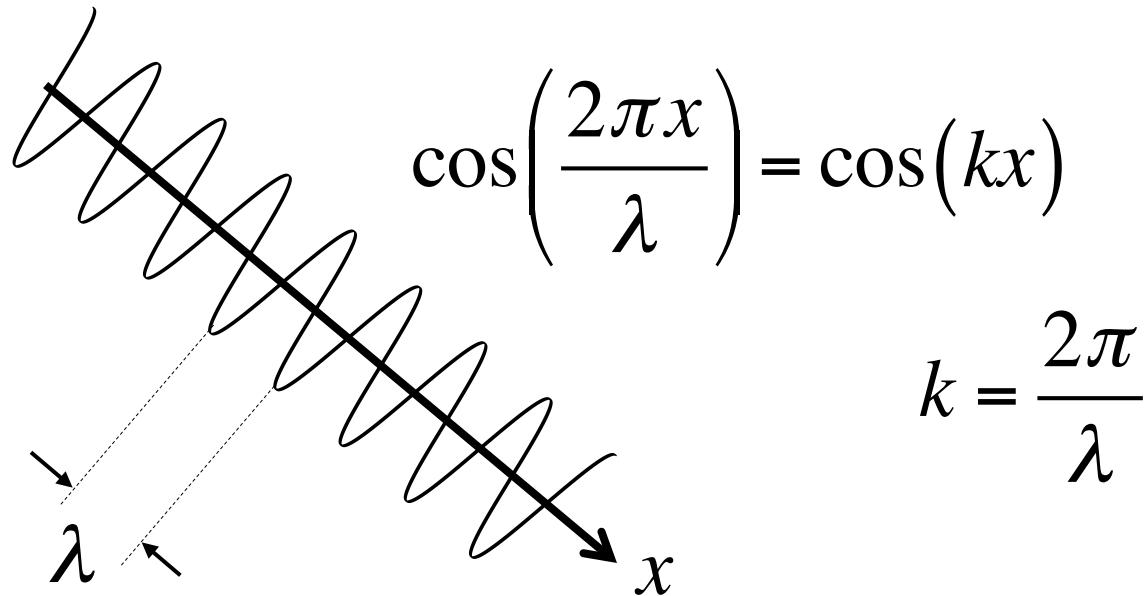
The diffraction limit



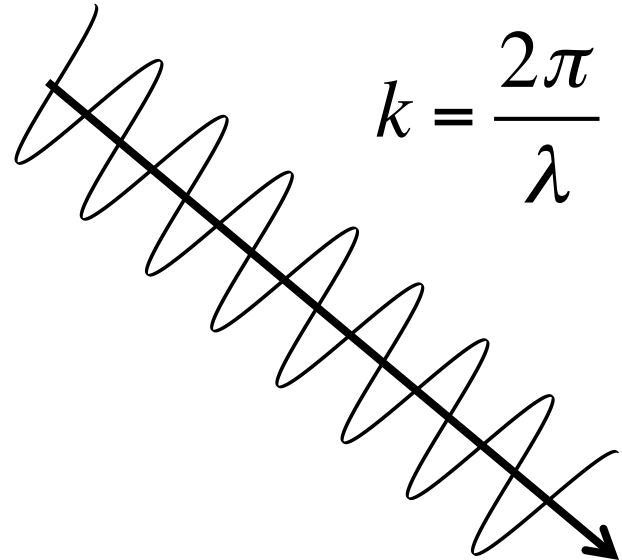
The diffraction limit



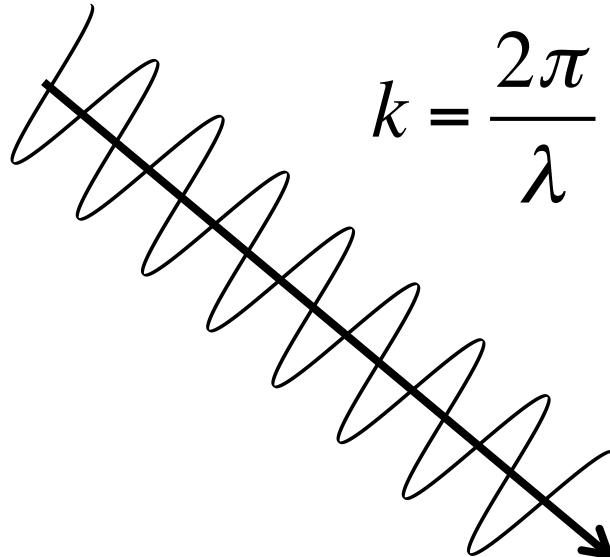
The diffraction limit



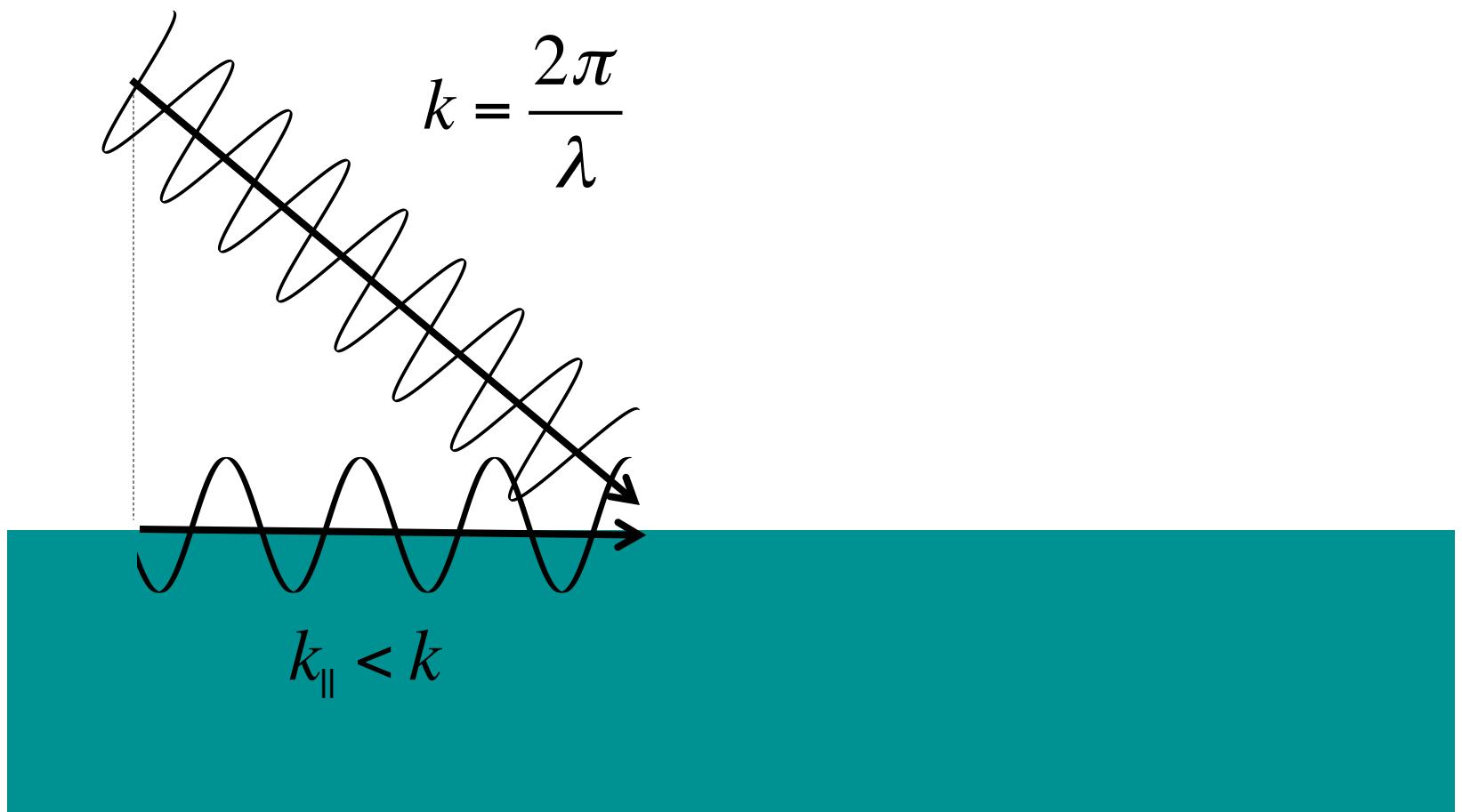
The diffraction limit



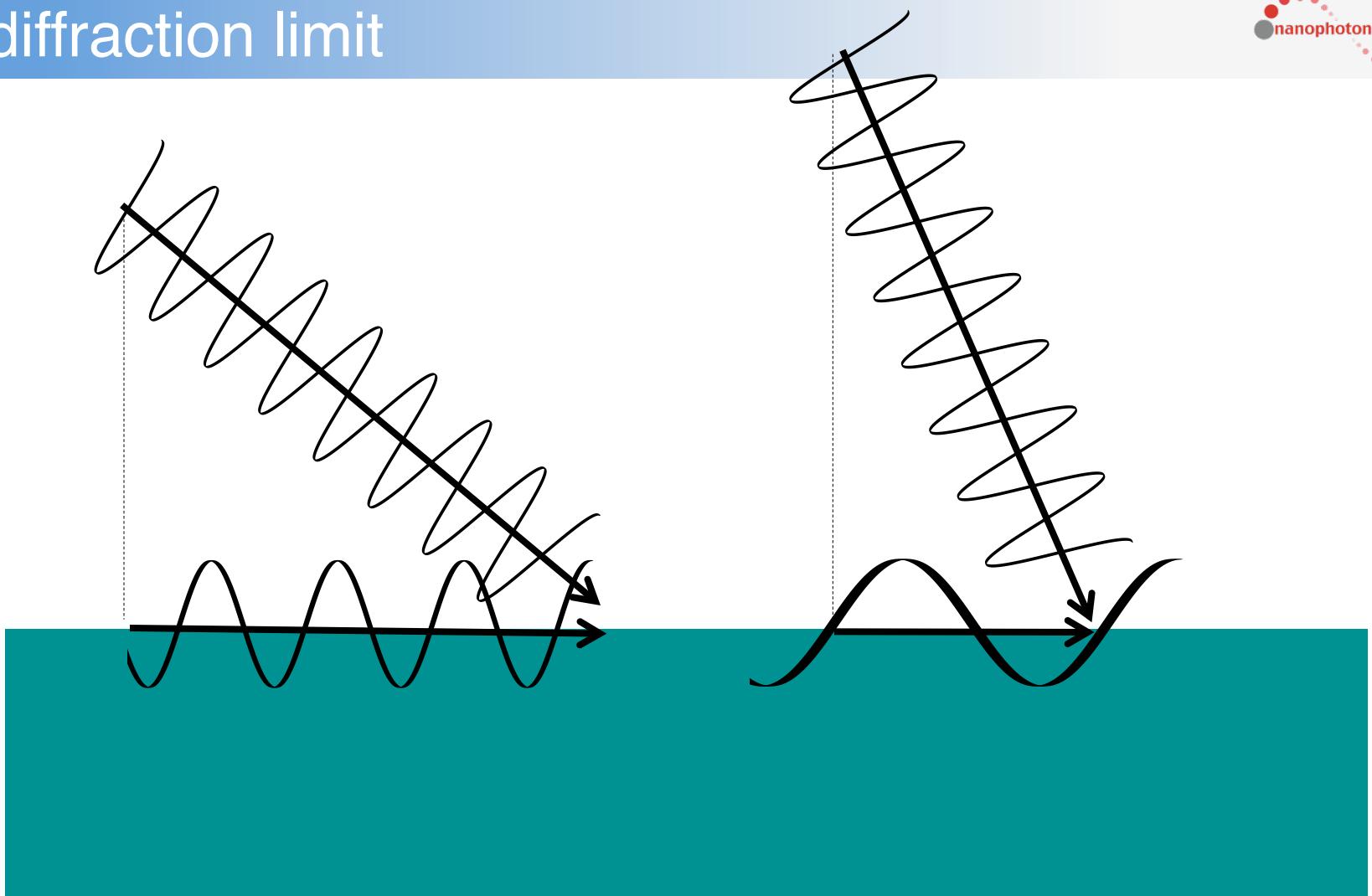
The diffraction limit



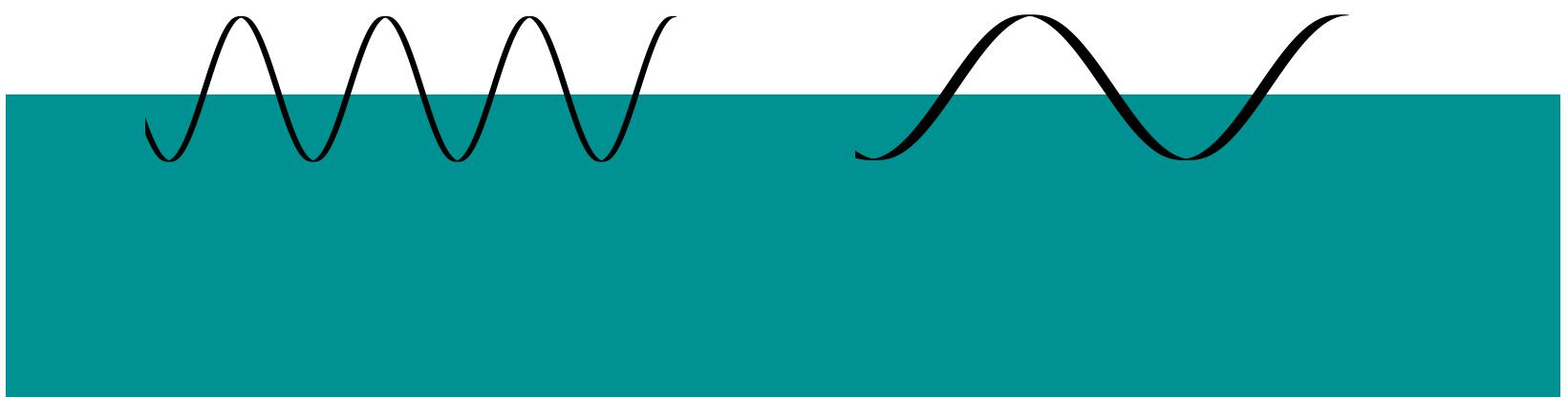
The diffraction limit



The diffraction limit



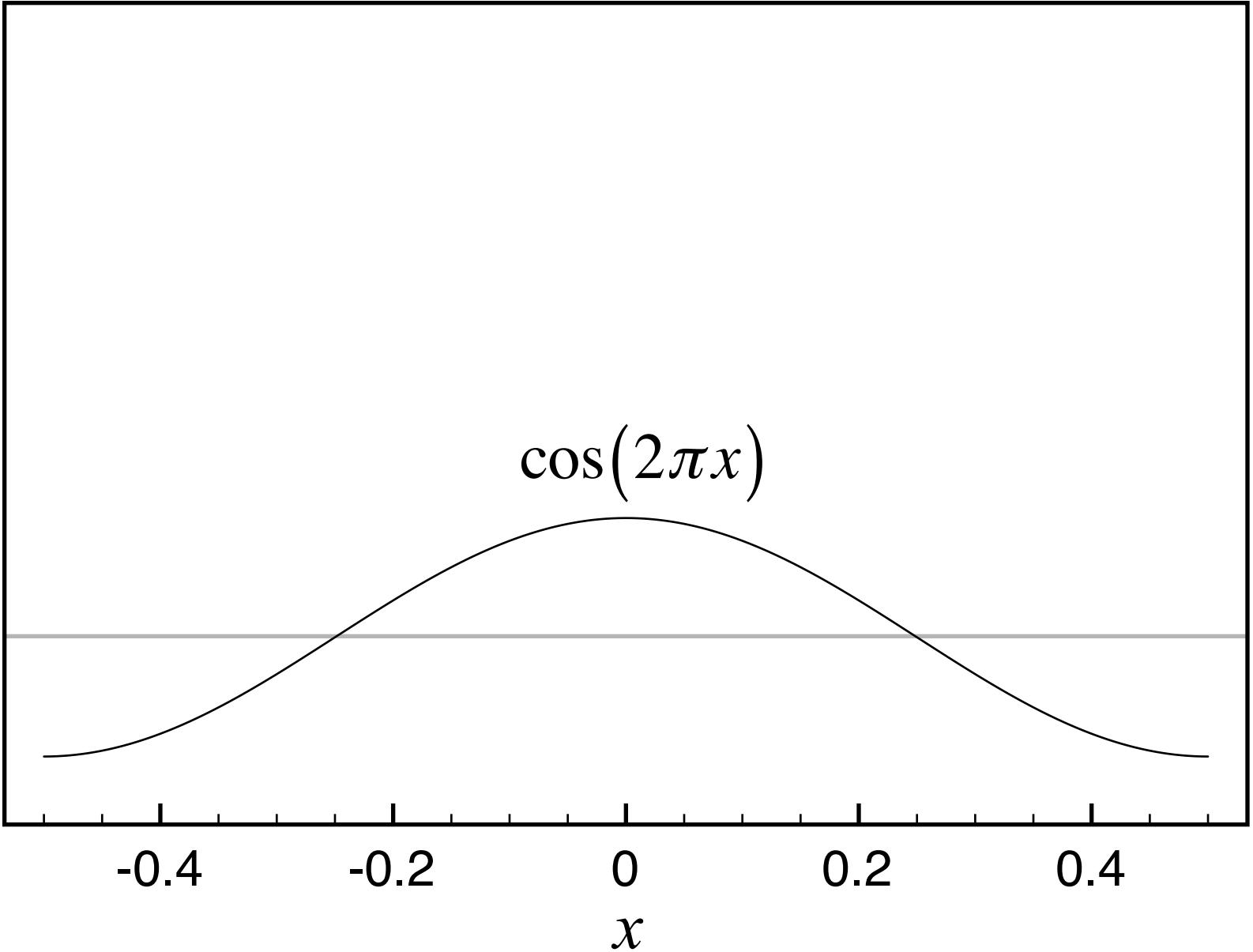
The diffraction limit



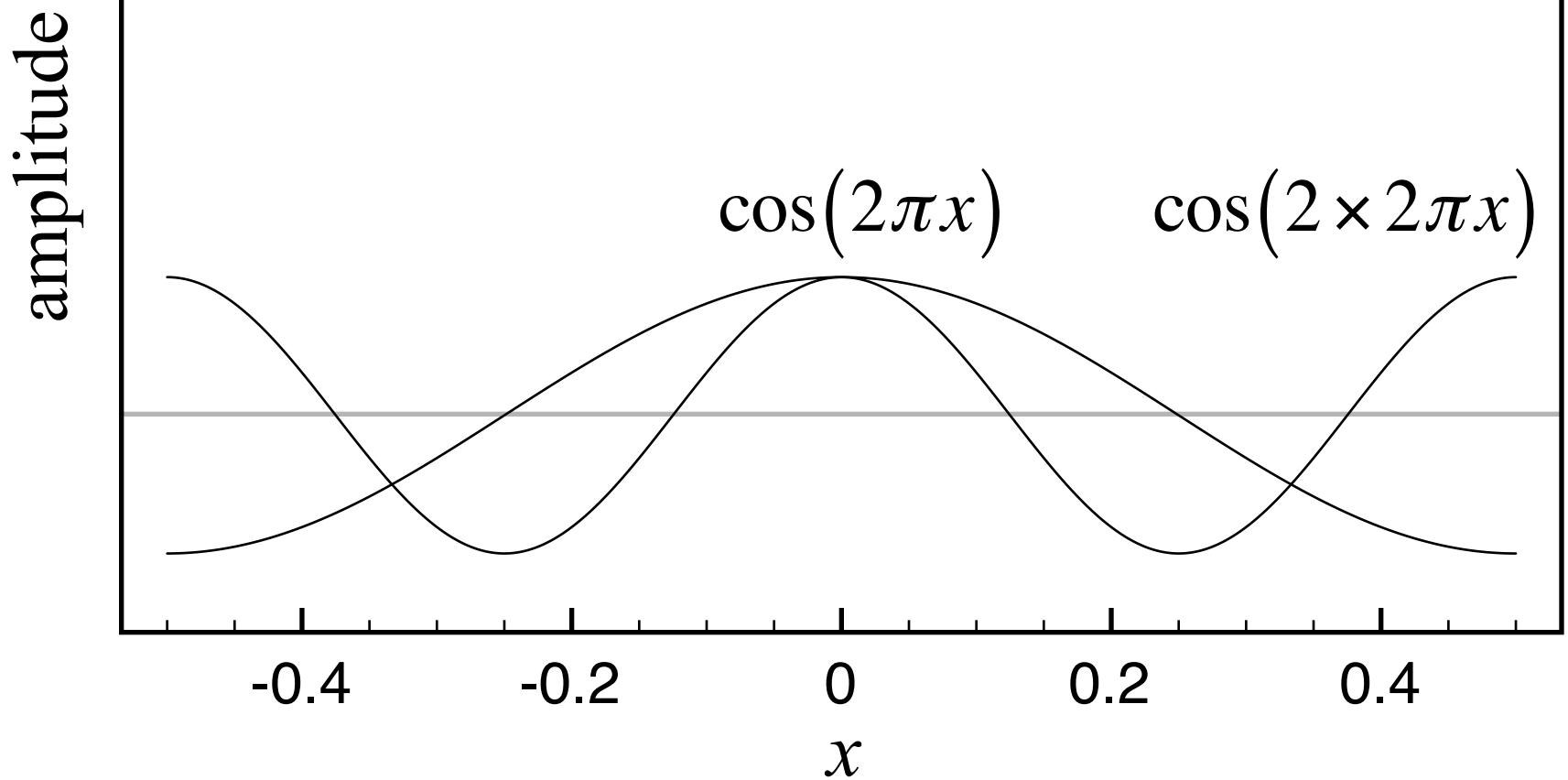
The diffraction limit

amplitude

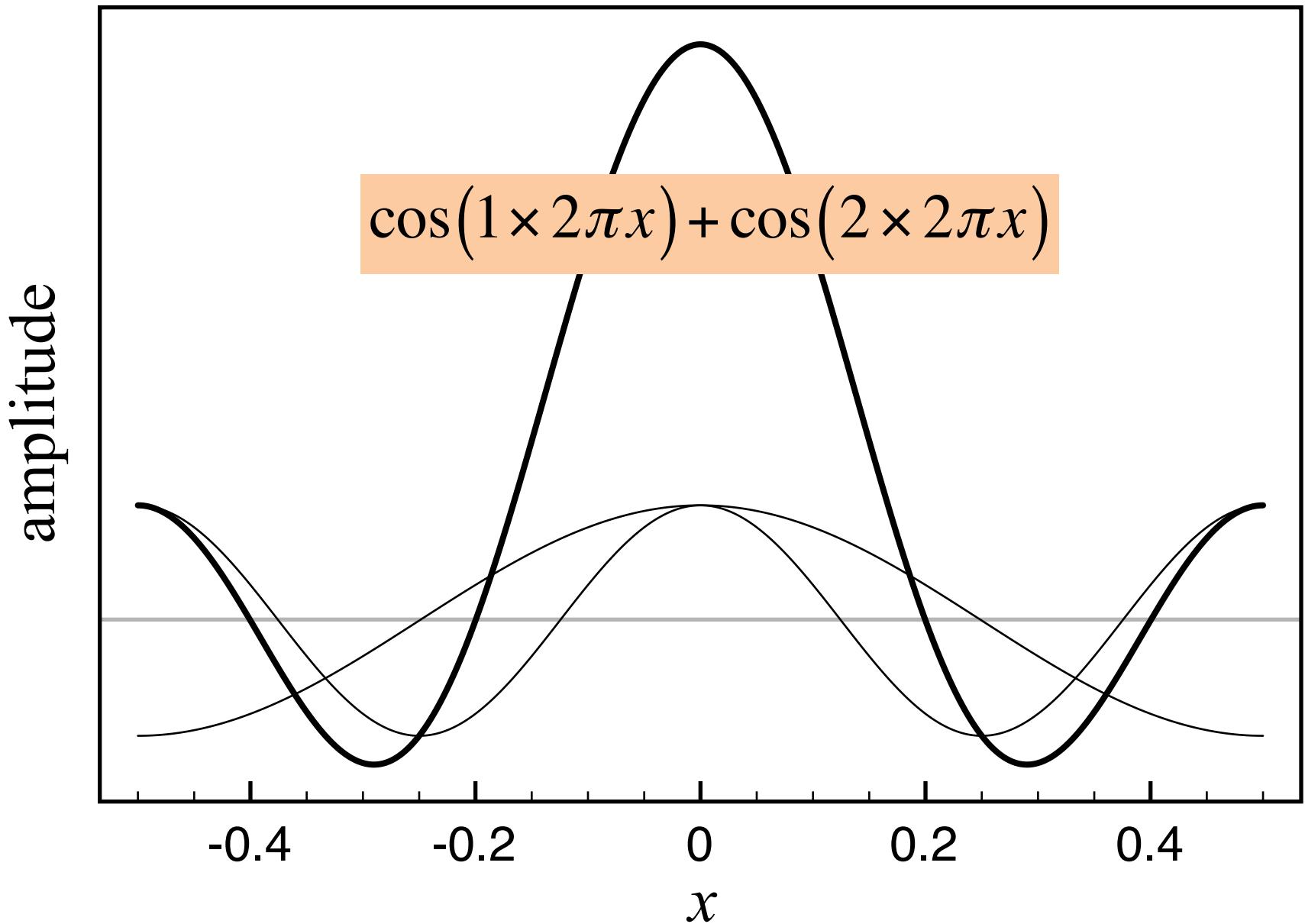
$$\cos(2\pi x)$$



The diffraction limit



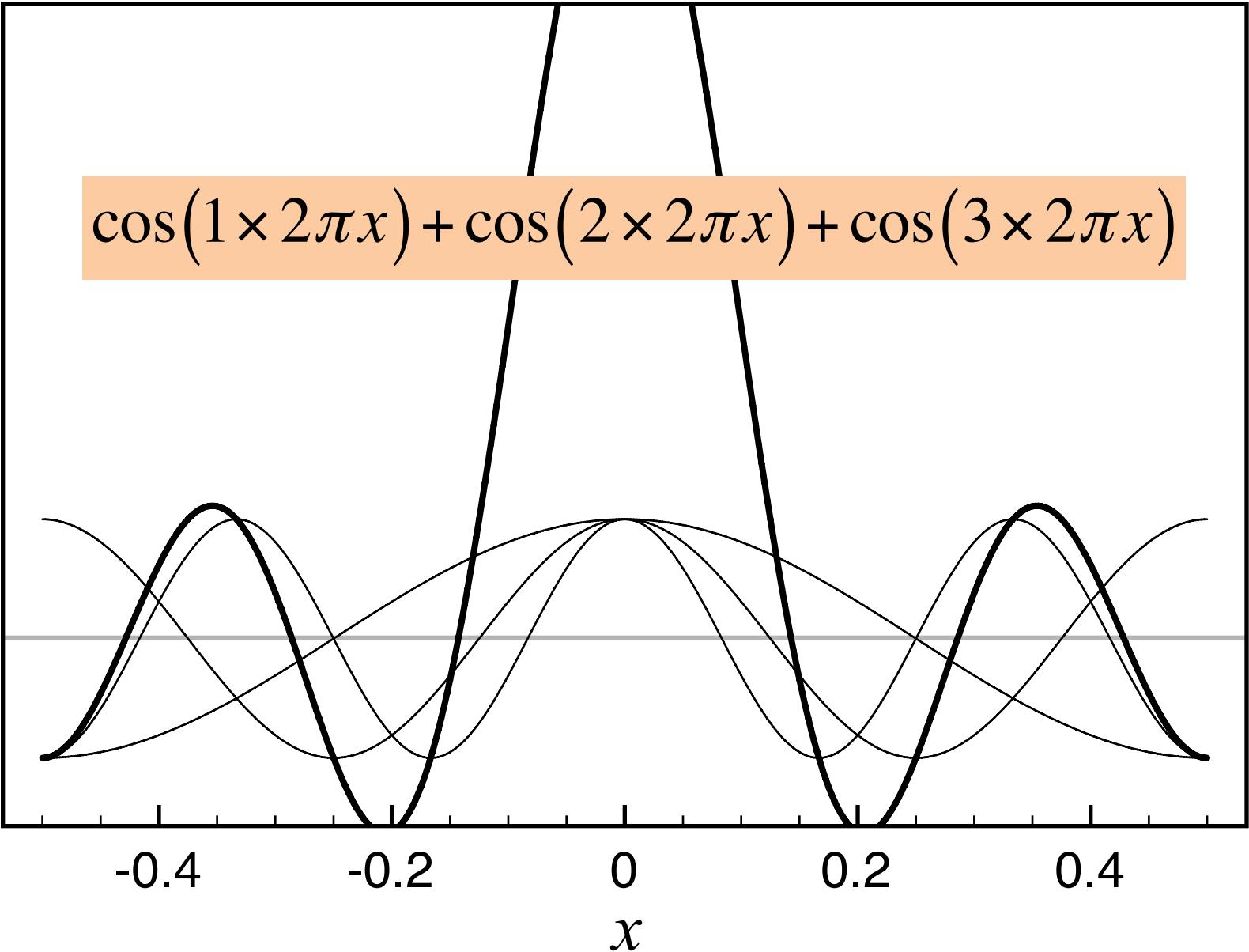
The diffraction limit



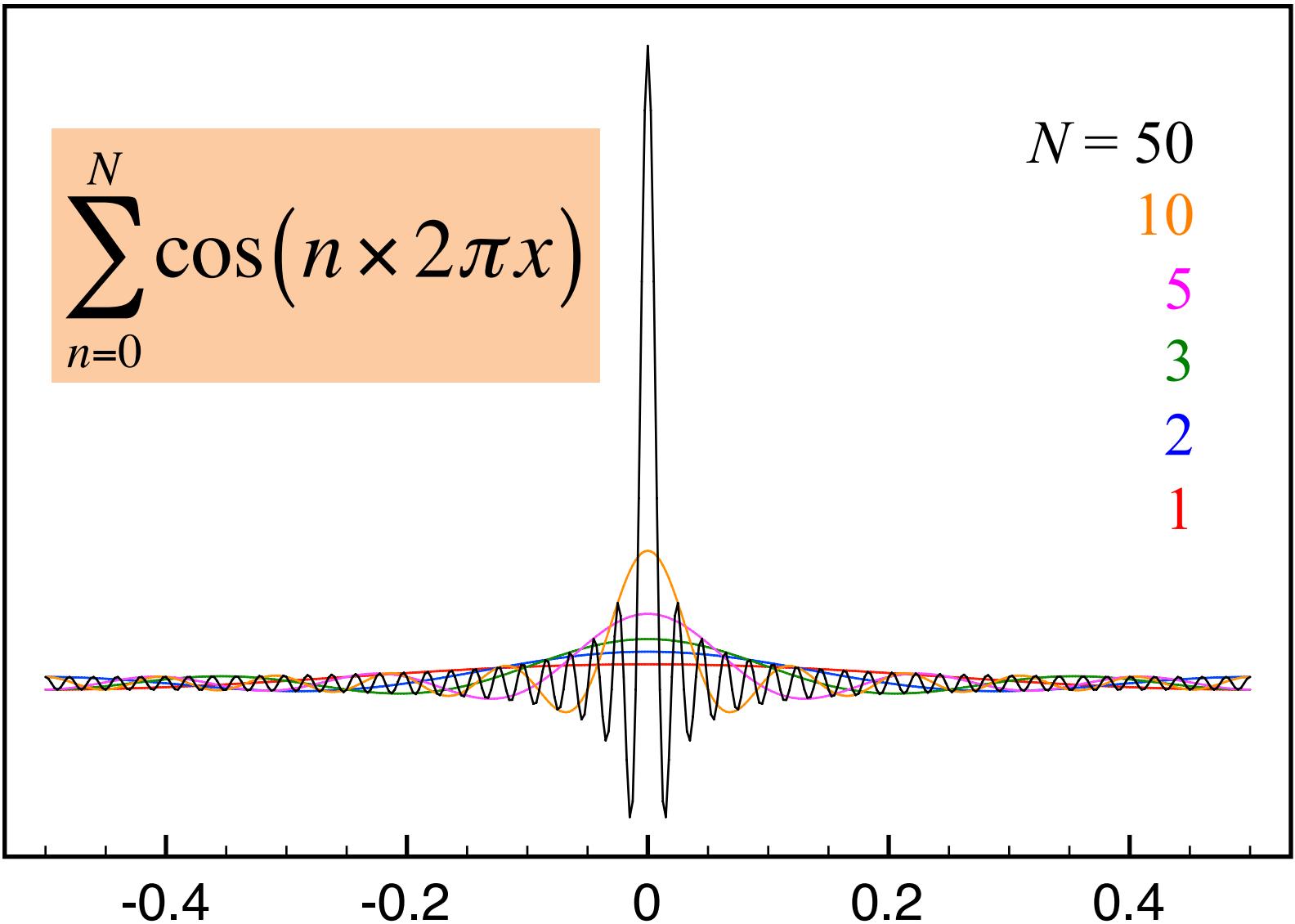
The diffraction limit

amplitude

$$\cos(1 \times 2\pi x) + \cos(2 \times 2\pi x) + \cos(3 \times 2\pi x)$$



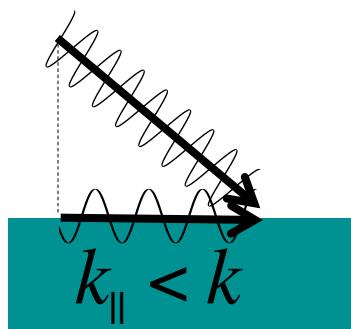
The diffraction limit



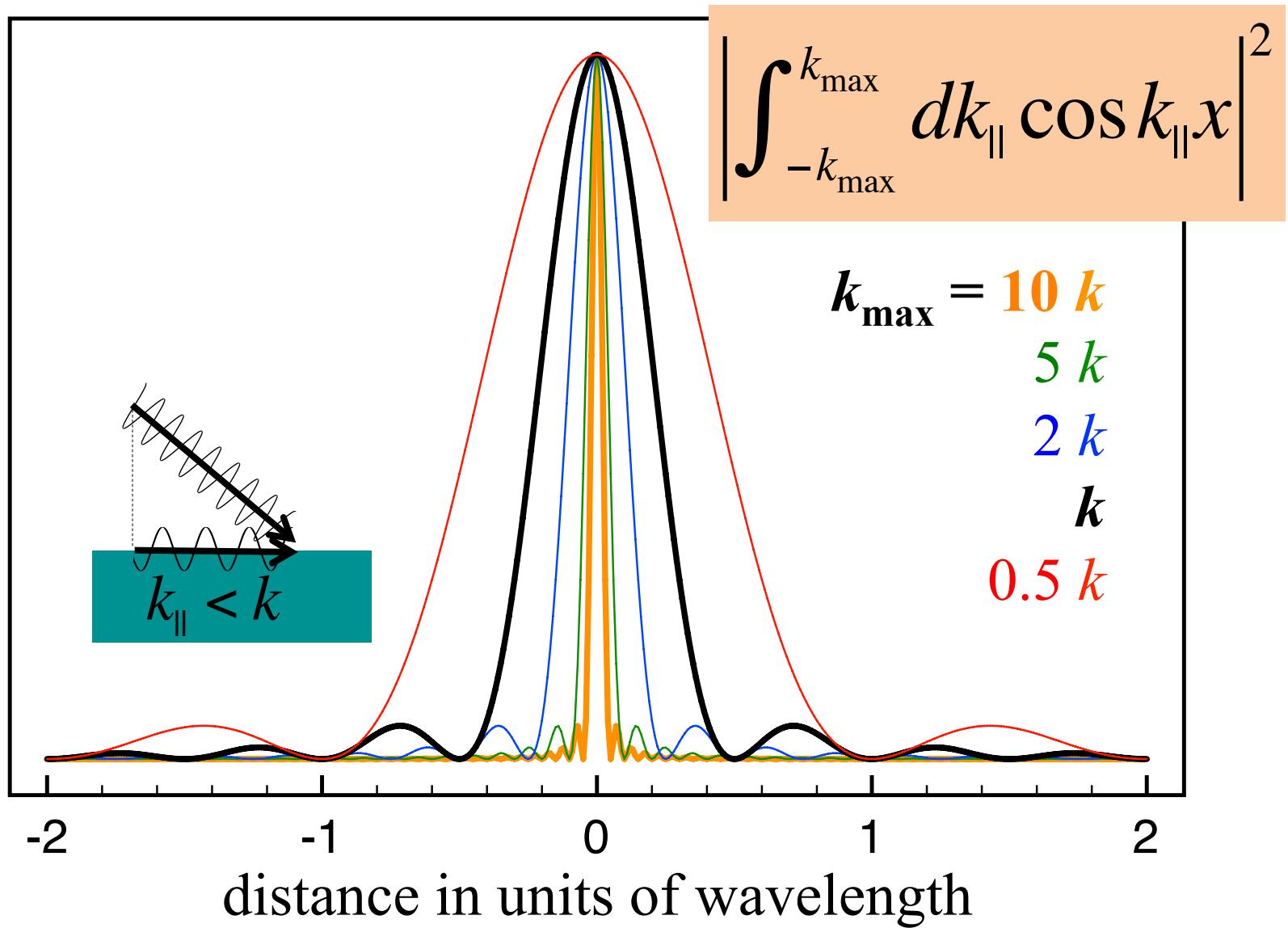
The diffraction limit

$$\sum_{n=0}^N \cos(n \times 2\pi x)$$

$$\int_{-k_{\max}}^{k_{\max}} dk_{||} \cos k_{||} x$$

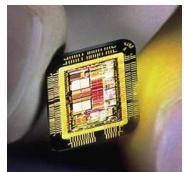


The diffraction limit

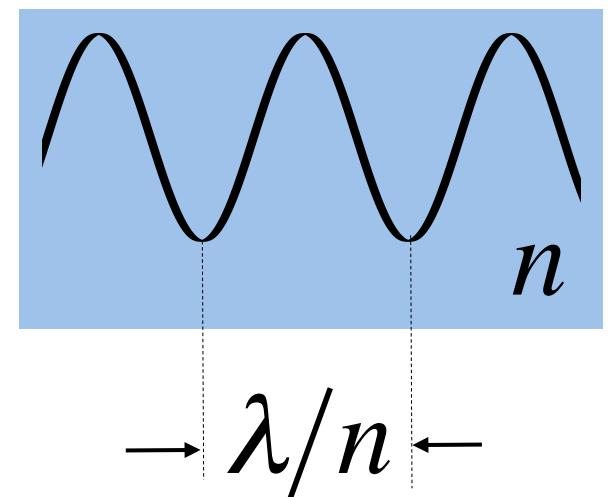
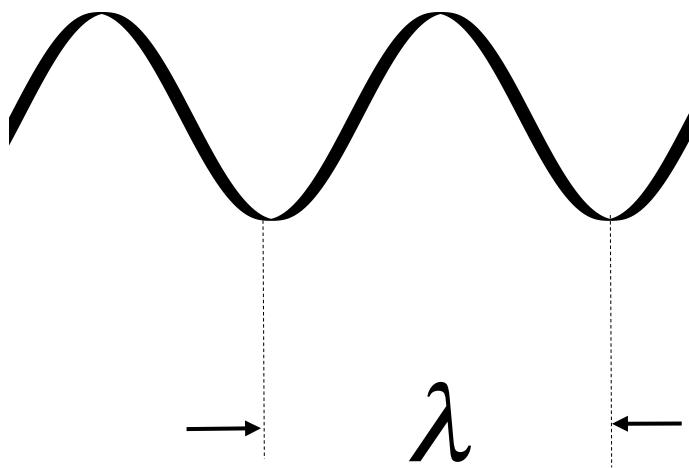


How to beat the diffraction limit

Dielectric materials



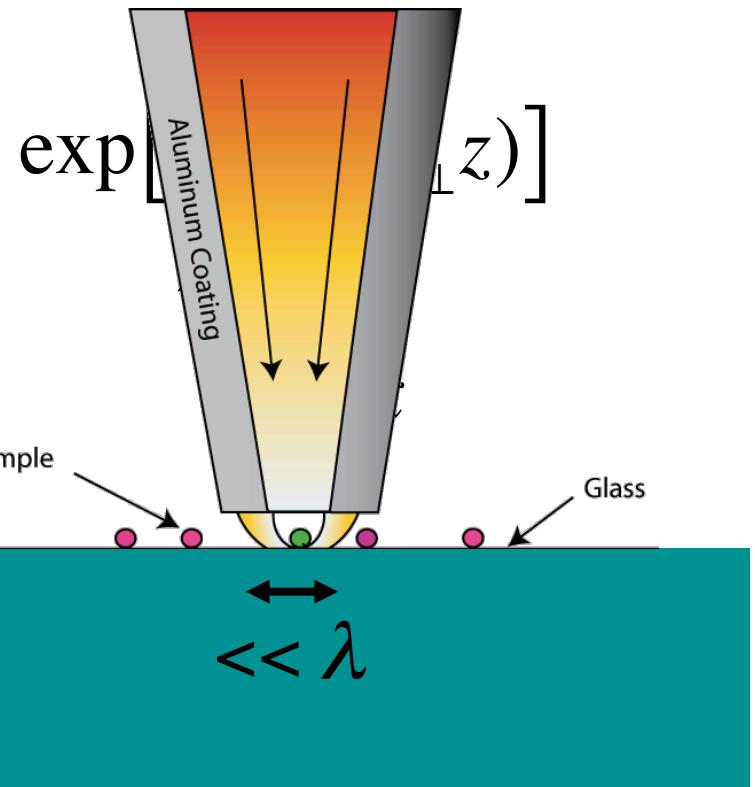
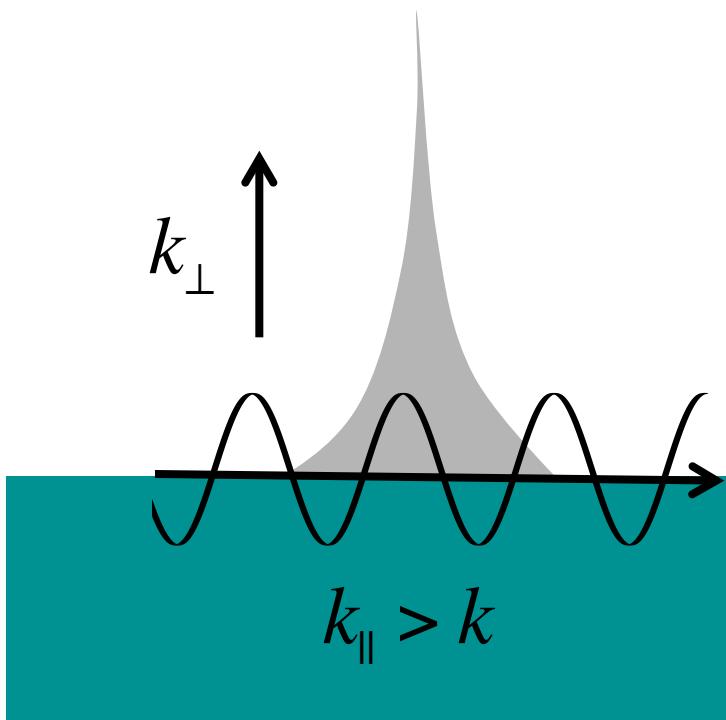
32 nm lines
193 nm ArF excimer laser in **water** (refractive index **$n=1.44$**)



Limited by n ☹

How to beat the diffraction limit

Evanescence waves

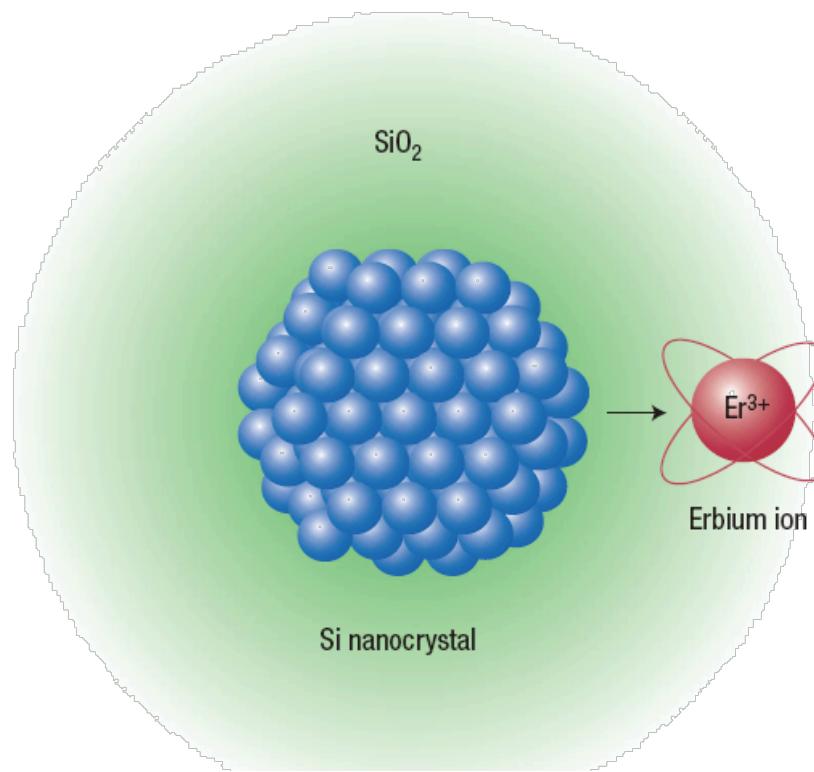


$$k_{\parallel}^2 + k_{\perp}^2 = k^2 \quad \rightarrow \quad k_{\perp} \text{ is imaginary}$$

How to beat the diffraction limit

Hybridize light and electronic excitations

- single or few electrons in atoms
- many electrons in metal nanostructures: **plasmons**



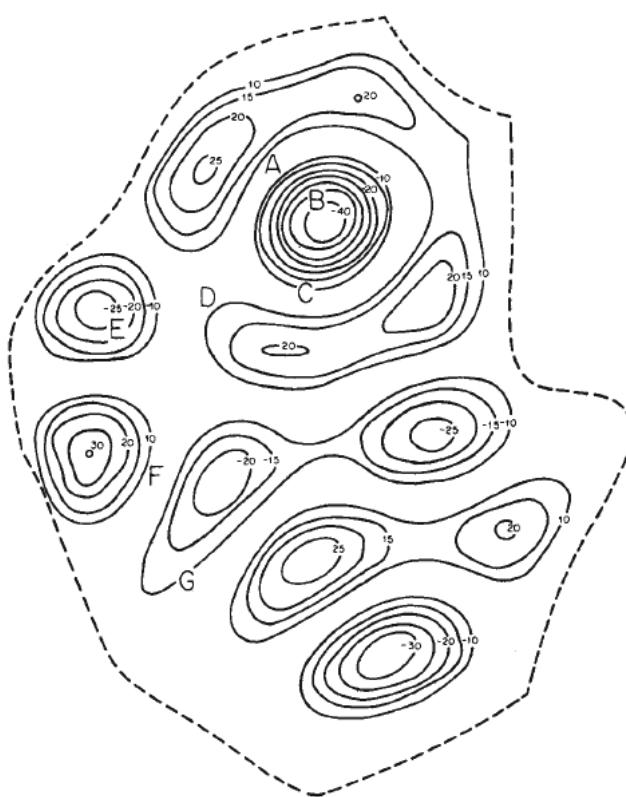
Introduction to plasmons

Surface plasmons are surface waves ...

Propagating surface waves



Propagating surface waves



Flores *et al.*, Nature (1987)

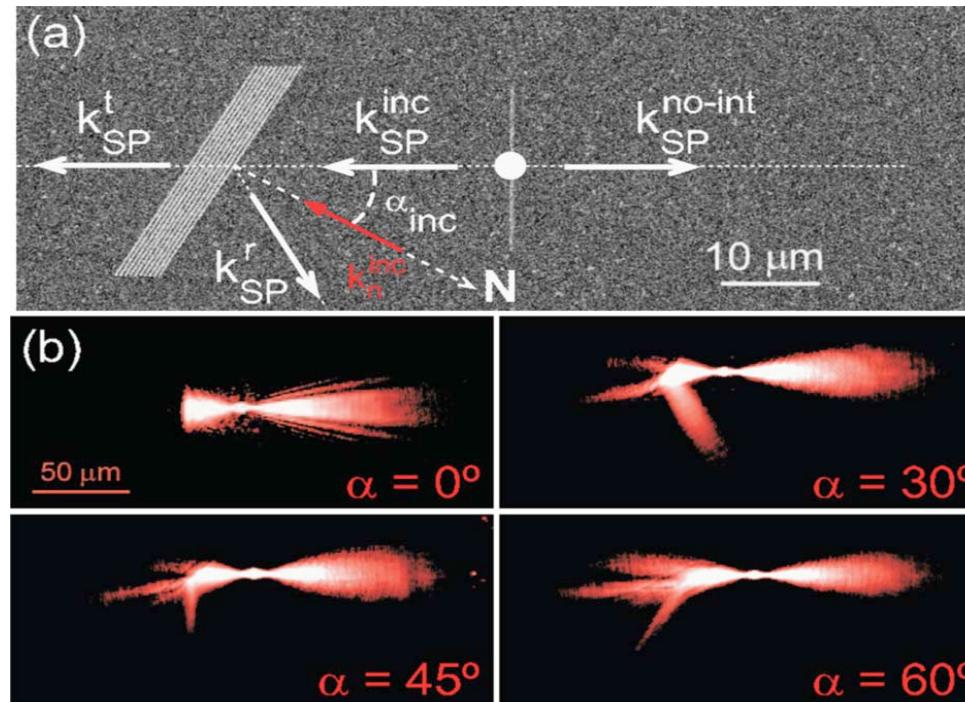
Level of damage in the 1985 earthquake in Mexico city

Introduction to plasmons

Surface plasmons are surface waves
involving collective electron motion
and propagating on metal surfaces ...

Interference and diffraction of surface plasmons

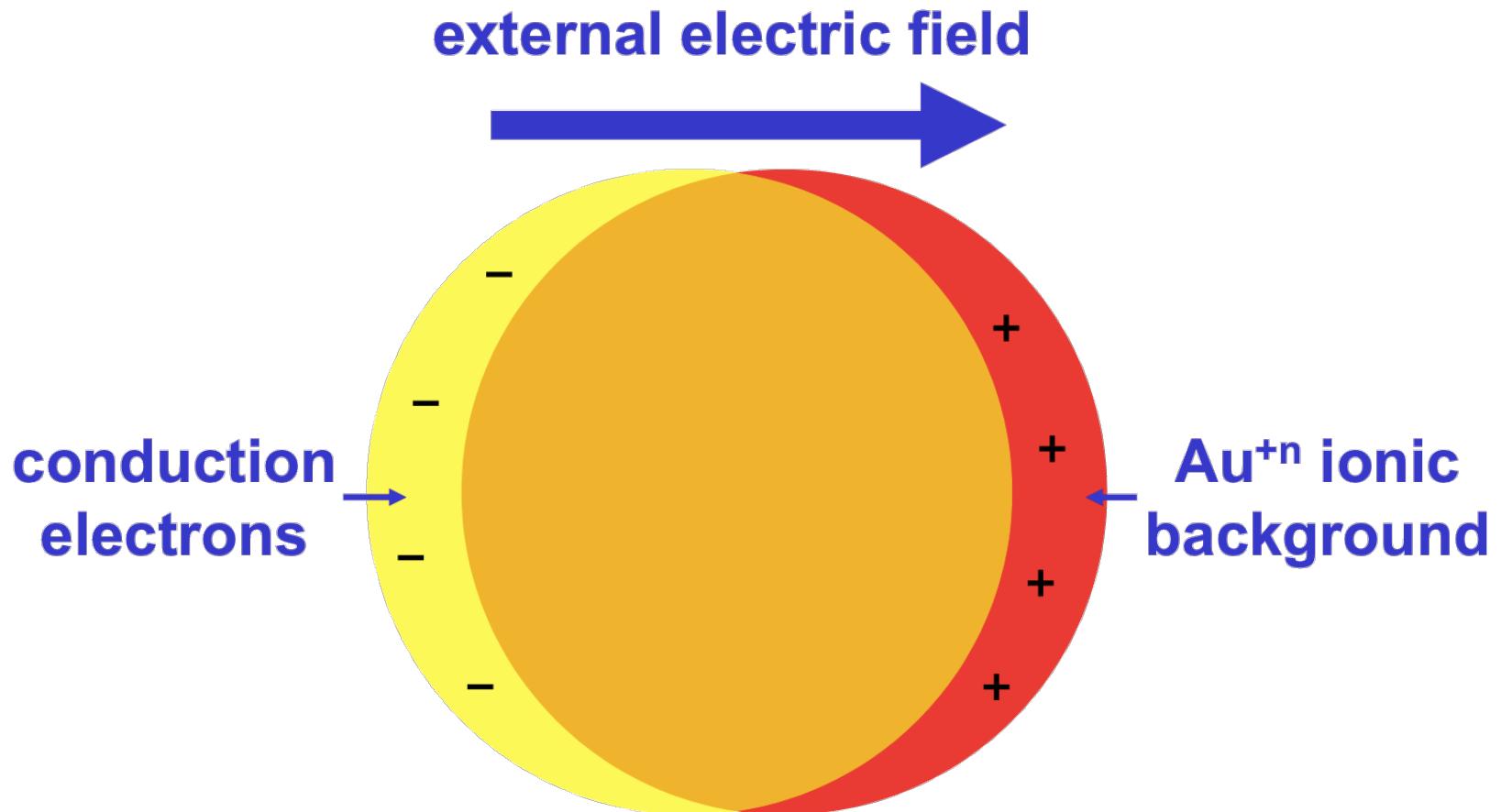
Plasmon Bragg mirrors



Introduction to plasmons

Surface plasmons are surface waves involving collective electron motion and propagating on metal surfaces or localized in metal (nano)structures (e.g., nanoparticles), where they couple efficiently to light ...

Localized plasmons



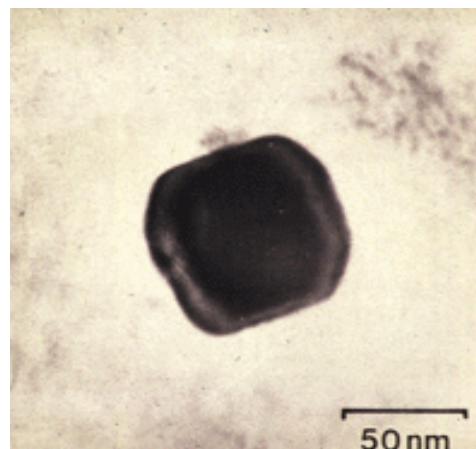
Plasmons in metallic nanoparticles

**Romans played empirically with nanoparticle plasmons:
the Licurgo cup dating from the IV century**

In reflection



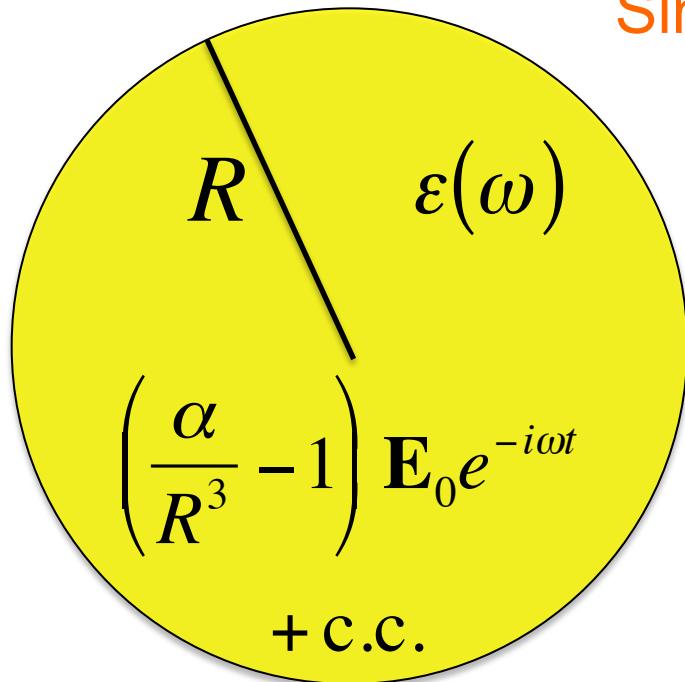
In transmission



An electron microscope image shows 70-nm
Au-Ag nanoparticles inside the glass

Localized plasmons

Simple derivation from Poisson's equation



$$\mathbf{E}^{\text{ext}}(t) = \mathbf{E}_0 e^{-i\omega t} + \mathbf{E}_0^* e^{i\omega t}$$

$$\alpha(\omega) \left[\frac{3\mathbf{r}(\mathbf{E}_0 \cdot \mathbf{r})/r^2 - \mathbf{E}_0}{r^3} \right] e^{-i\omega t} + \text{c.c.}$$

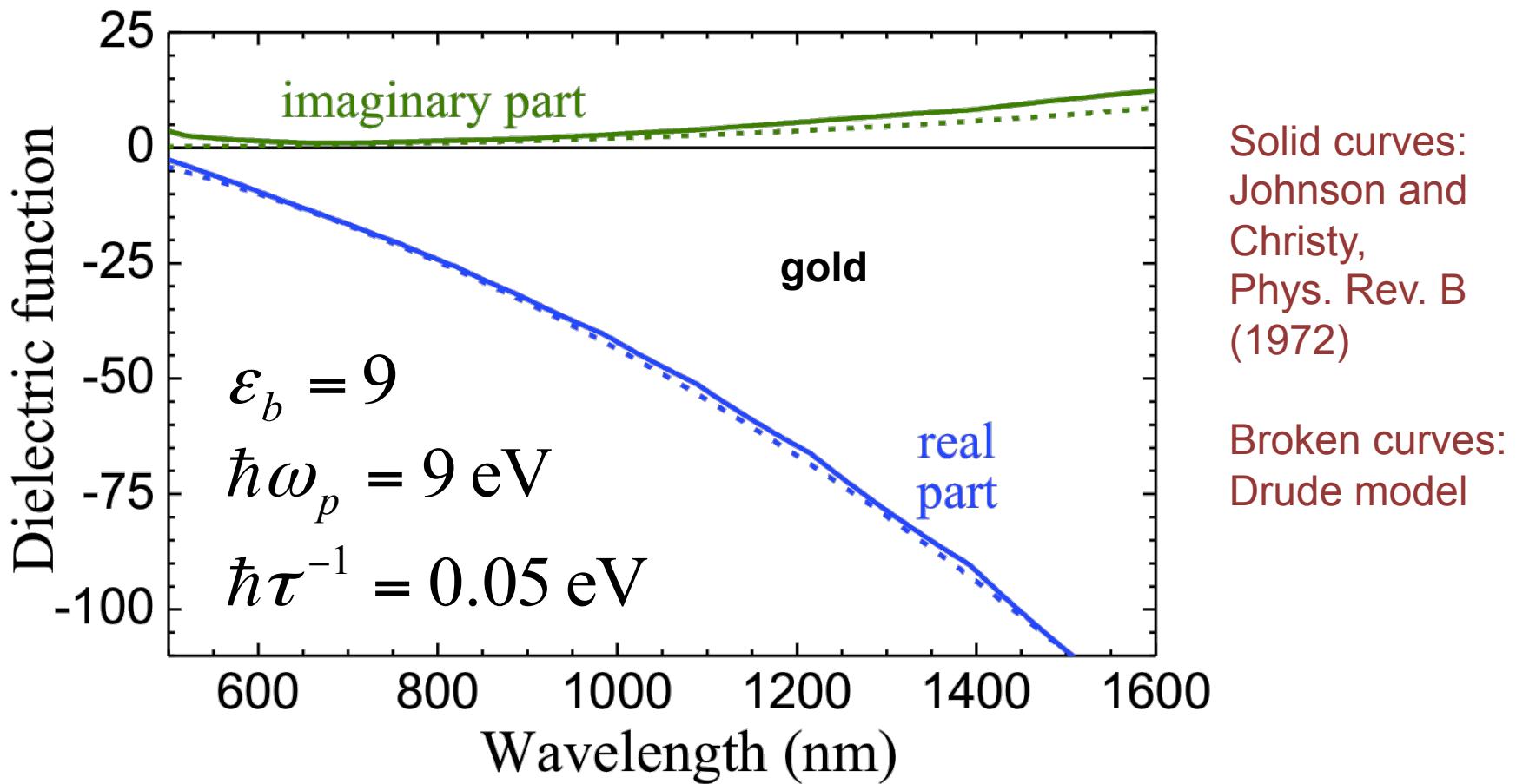
$$\alpha(\omega) = R^3 \frac{\varepsilon - 1}{\varepsilon + 2} \quad \varepsilon = -2$$

$$\varepsilon(\omega) = 1 - \frac{\omega_p^2}{\omega(\omega + i\gamma)}$$

$$\alpha(\omega) = \frac{R^3 \omega_0^2}{\omega_0^2 - \omega(\omega + i\gamma)} \quad \omega_0 = \frac{\omega_p}{\sqrt{3}}$$

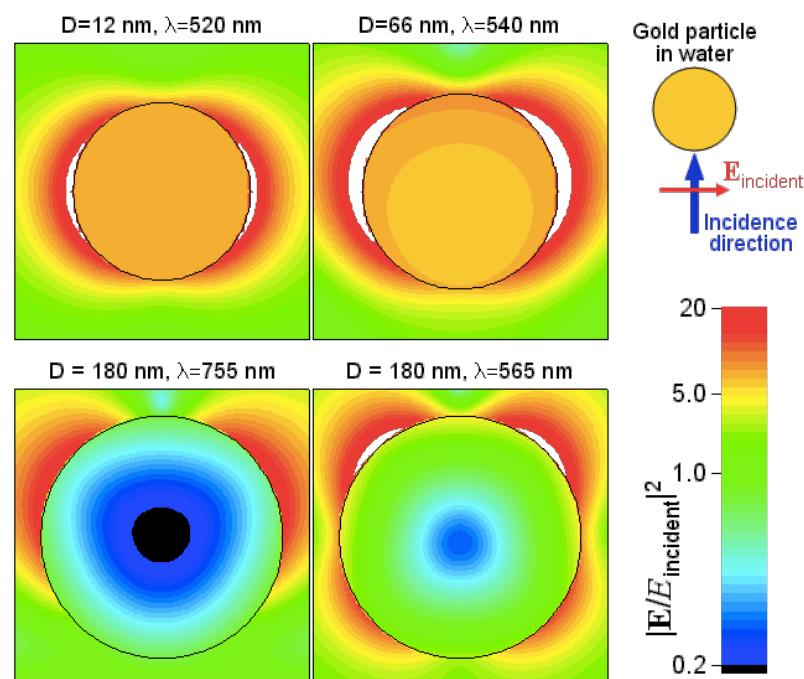
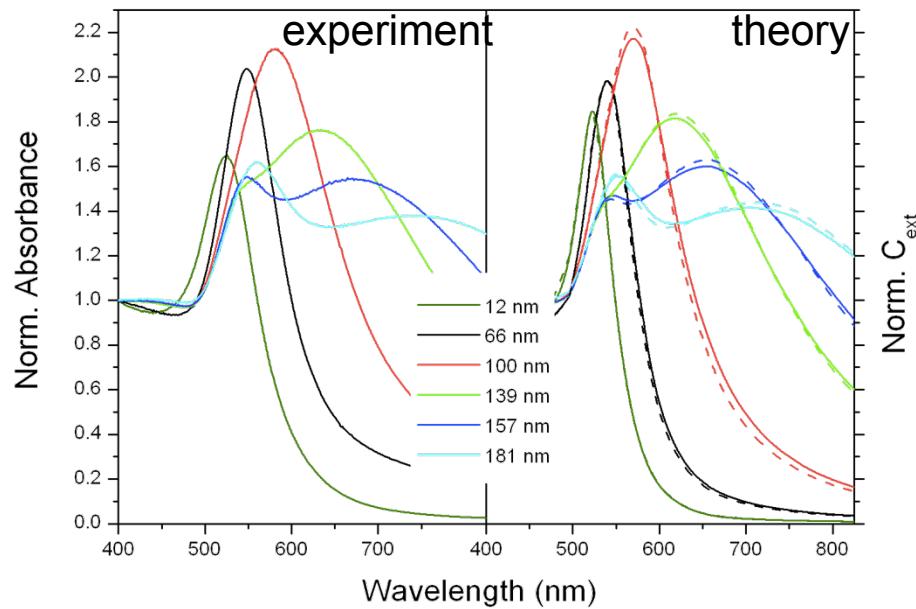
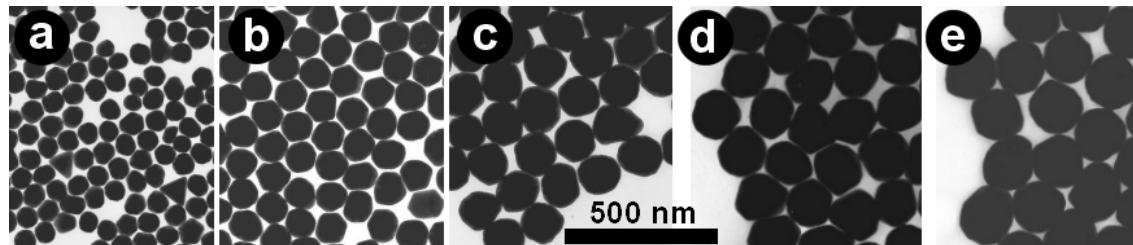
Localized plasmons

$$\varepsilon(\omega) = \varepsilon_b - \frac{\omega_p^2}{\omega(\omega + i\tau^{-1})}$$



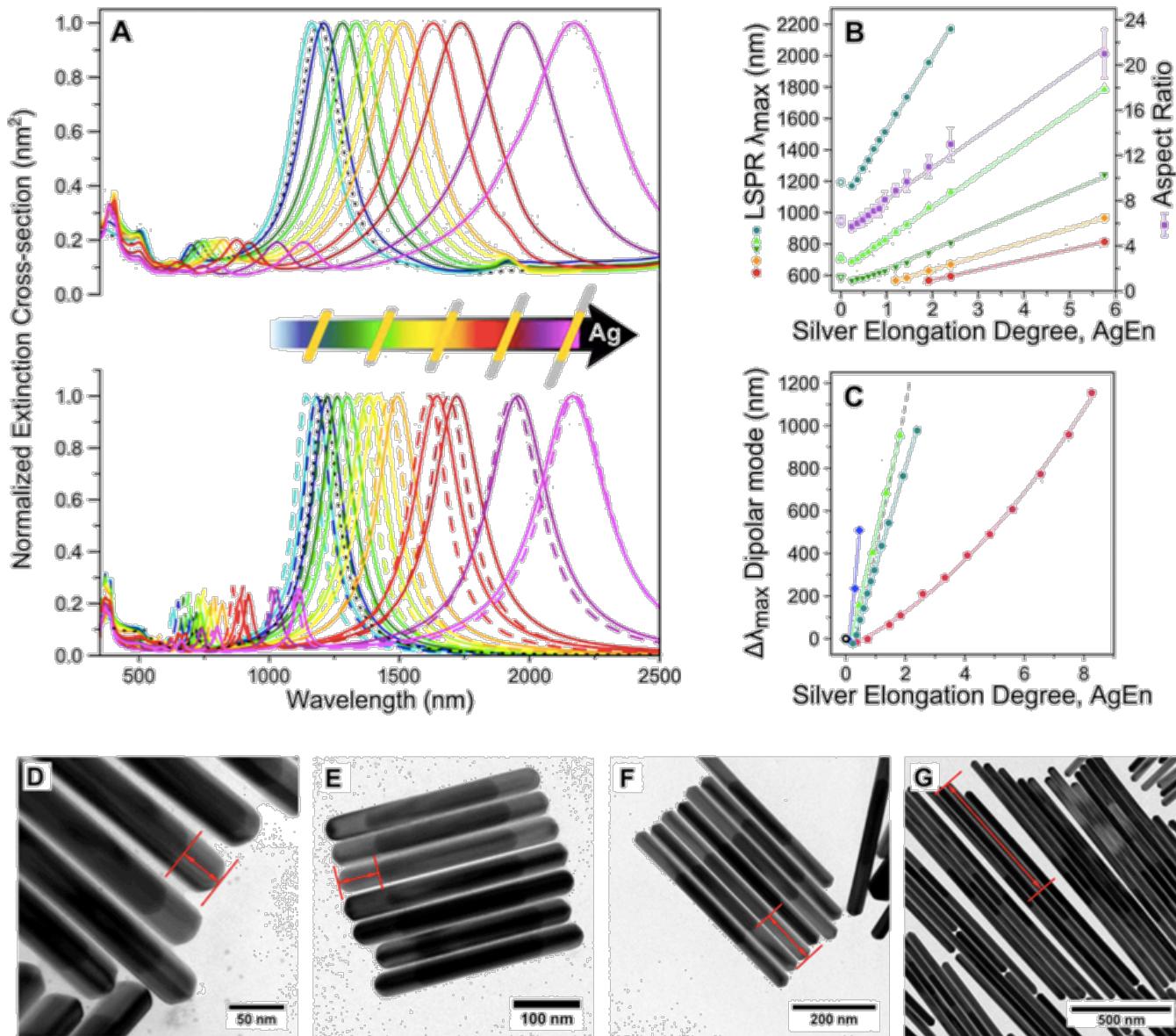
Localized plasmons

Multipolar plasmons and retardation effects

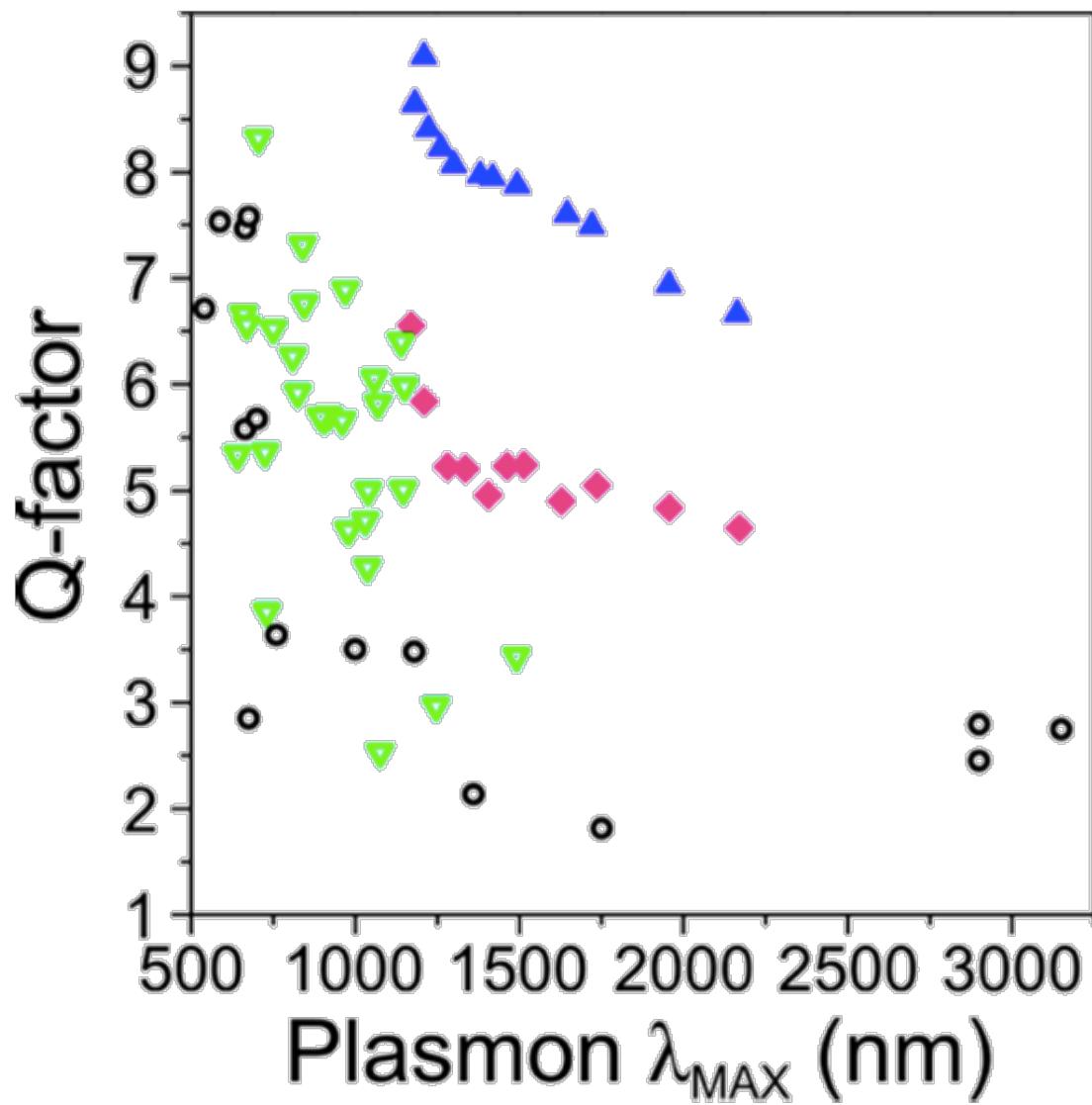


Rodríguez-Fernández *et al.*, Langmuir (2006)

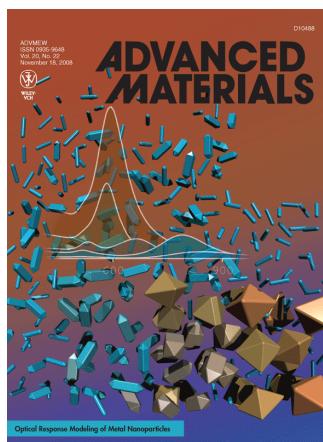
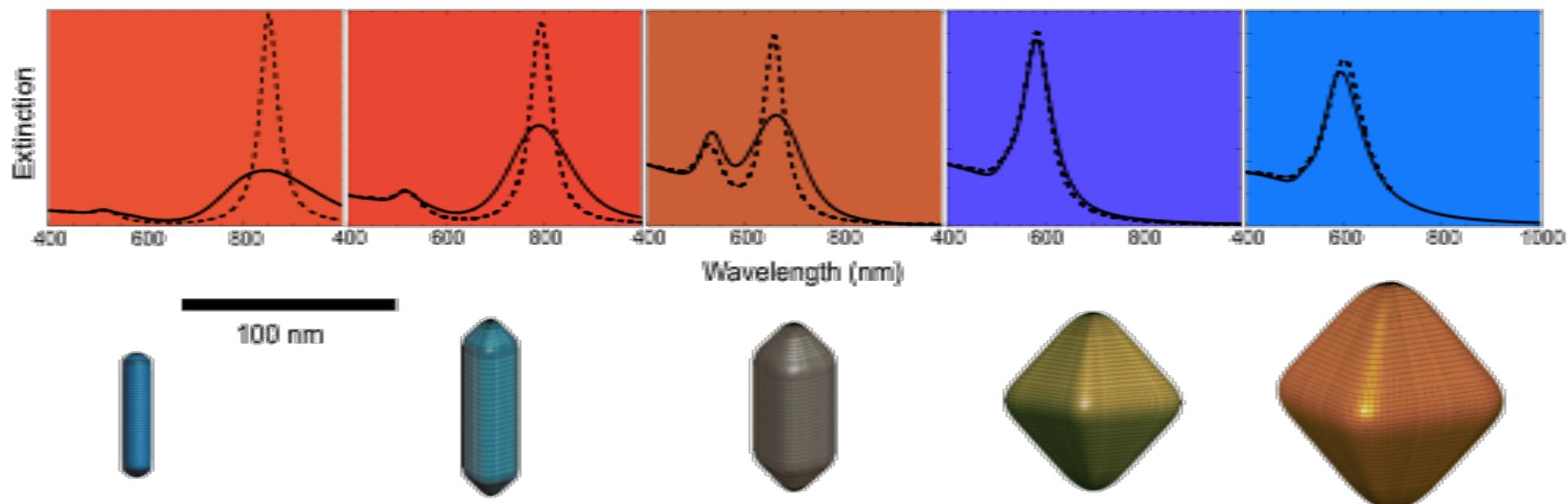
Localized plasmons



Localized plasmons



Localized plasmons



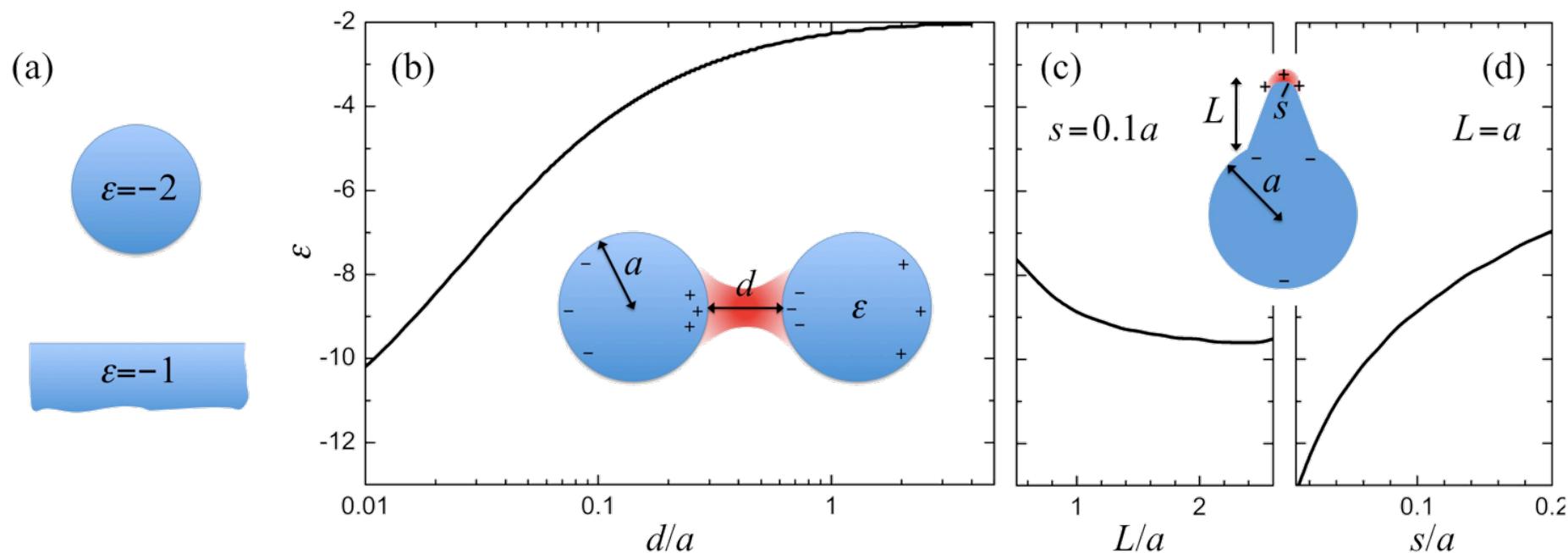
Myroshnychenko *et al.*, Adv. Mater. (2008)

Introduction to plasmons

Surface plasmons are surface waves involving collective electron motion and propagating on metal surfaces or localized in metal (nano)structures (e.g., nanoparticles), where they couple efficiently to light, **they produce strong confinement of the electromagnetic field (size << wavelength) ...**

Why do we need metals?

Plasmons in the long wavelength limit (Poisson equation) are scale-invariant, and therefore, they exist for structures down to a few nm.



Localized excitations require negative permittivity

Why do we need metals?

Maxwell equations for small particles

$$\mathbf{E}(\mathbf{r}, t) = \mathbf{E}(\mathbf{r}, \omega) e^{-i\omega t} + \mathbf{E}^*(\mathbf{r}, \omega) e^{i\omega t}$$

$$\nabla \cdot \epsilon(\mathbf{r}, \omega) \mathbf{E}(\mathbf{r}, \omega) = 0 \quad \mathbf{E}(\mathbf{r}, \omega) = -\nabla \phi(\mathbf{r}, \omega)$$

$$\boxed{\nabla \cdot \epsilon(\mathbf{r}, \omega) \nabla \phi(\mathbf{r}, \omega) = 0}$$

The Poisson equation also describes stationary heat transport:

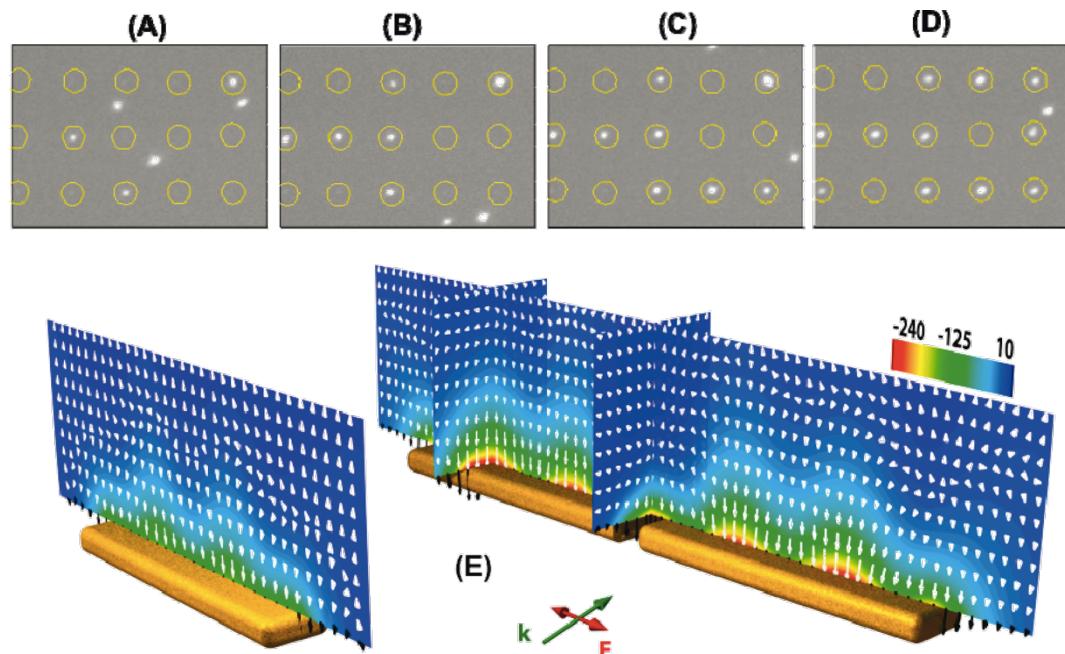
$$\begin{aligned}\epsilon &\rightarrow k, \text{ thermal conductivity} \\ \phi &\rightarrow \text{temperature}\end{aligned}$$

Thermodynamics:

- flow towards lower temperature regions $\rightarrow k>0$
- absence of trapped thermal energy

Applications of plasmon confinement

Optical trapping - nanotweezers

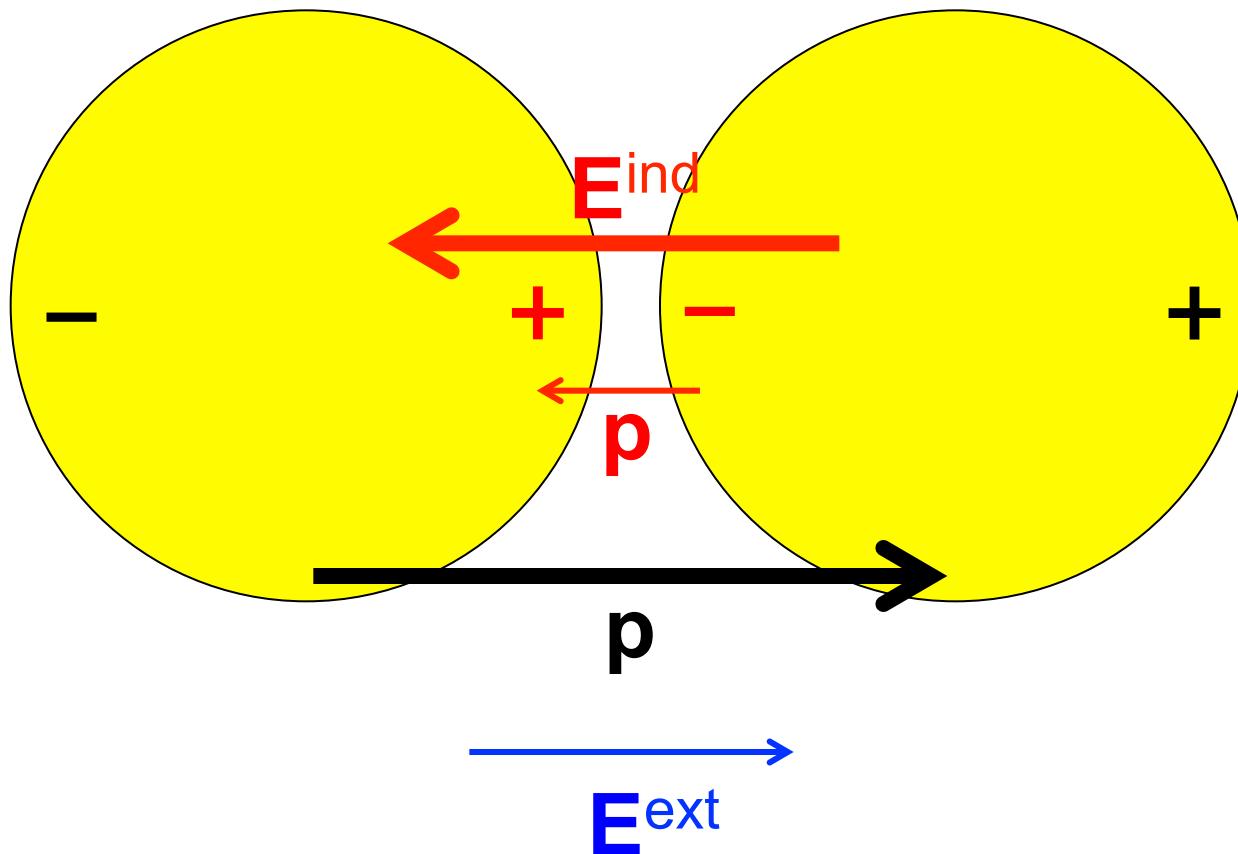


Righini et al. (2009)

Introduction to plasmons

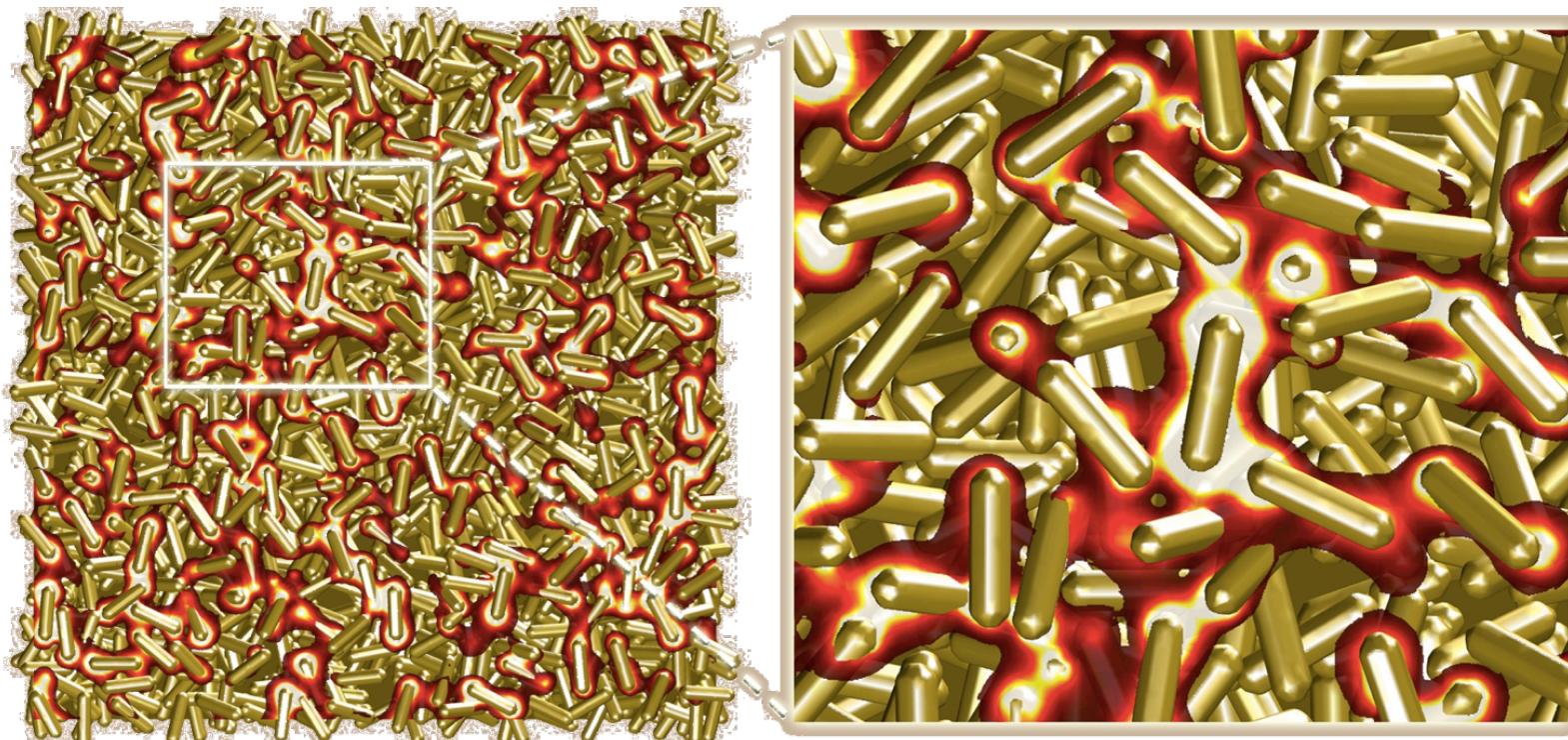
Surface plasmons are surface waves involving collective electron motion and propagating on metal surfaces or localized in metal (nano)structures (e.g., nanoparticles), where they couple efficiently to light, they produce strong confinement of the electromagnetic field (size \ll wavelength), and they generate huge enhancement of the optical electric-field intensity.

Field enhancement and confinement

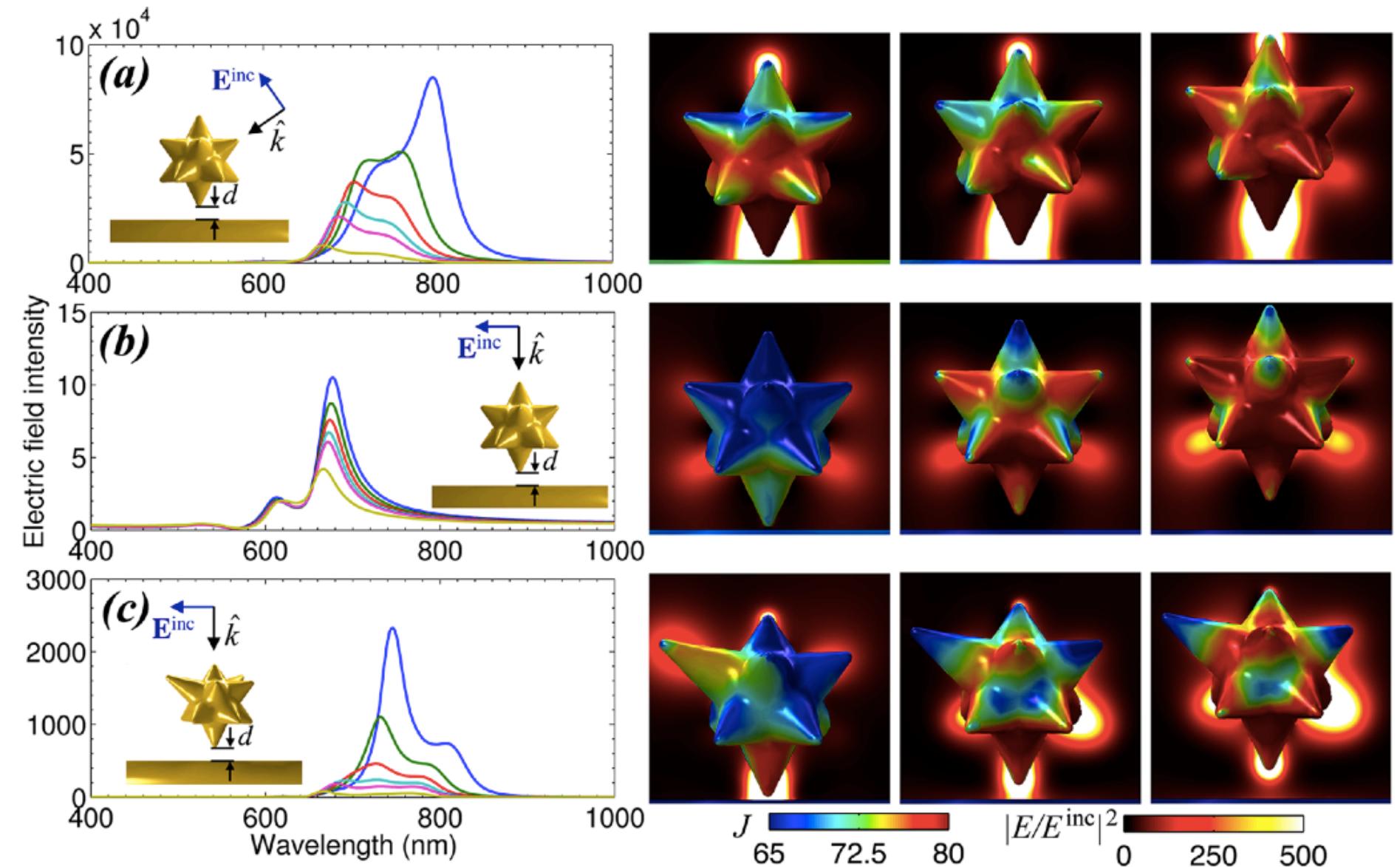


Charge neutrality \rightarrow strong coupling to light through \mathbf{p} , strong enhancement in the gap

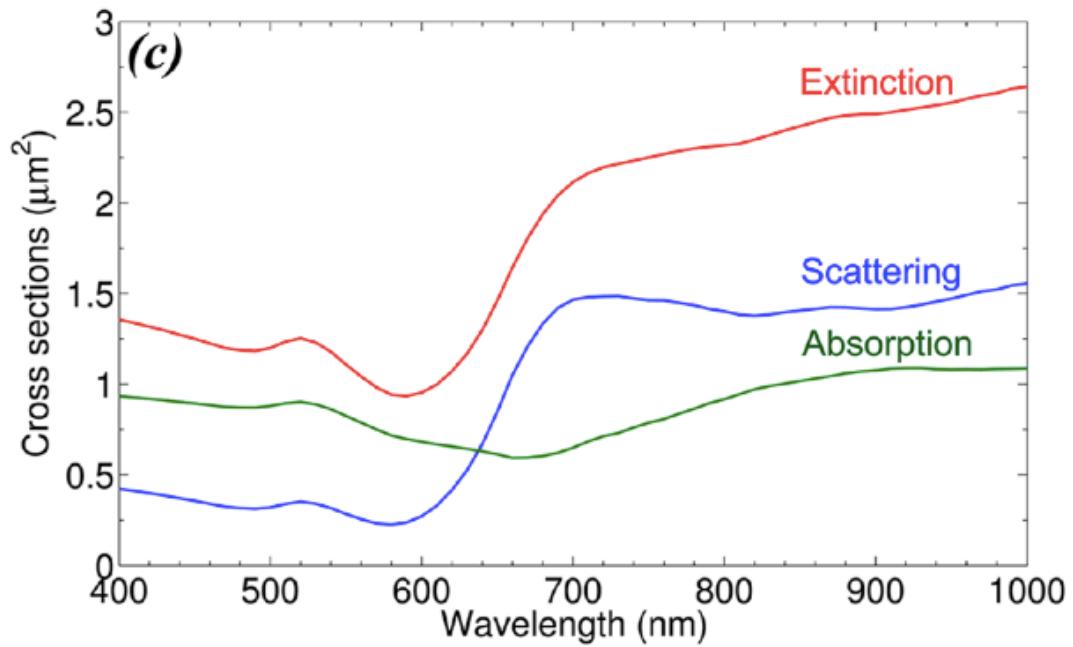
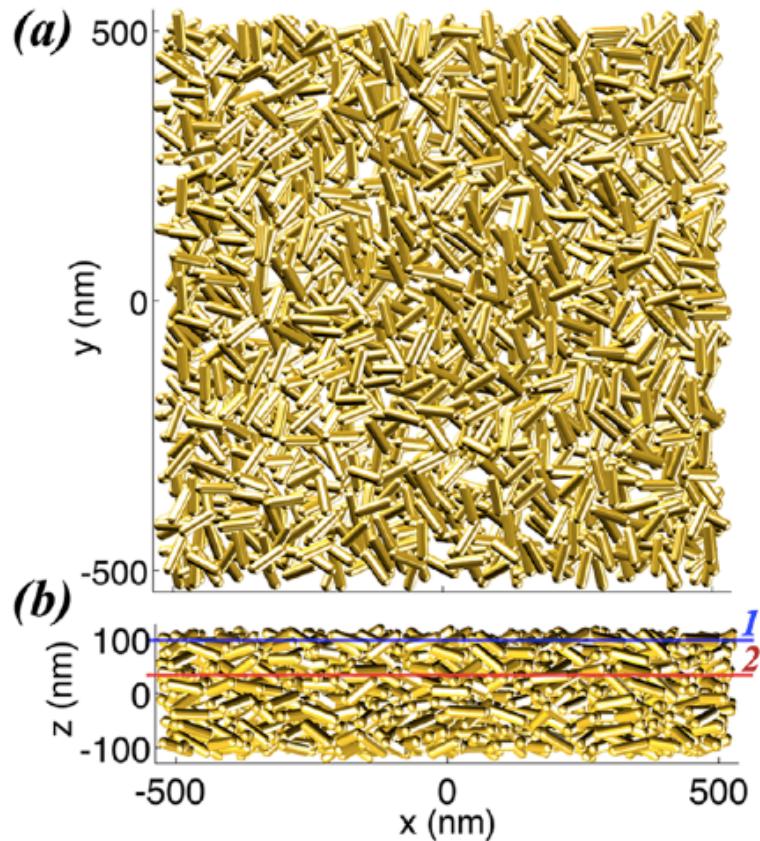
Designing field enhancers



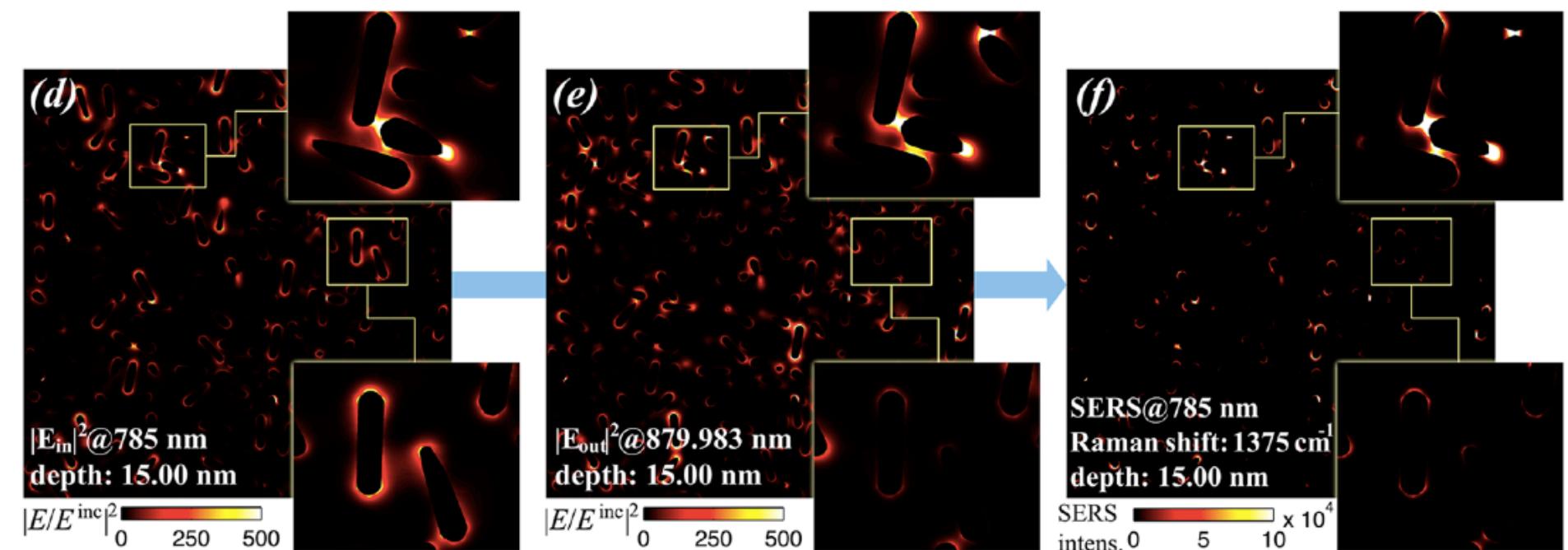
Designing field enhancers



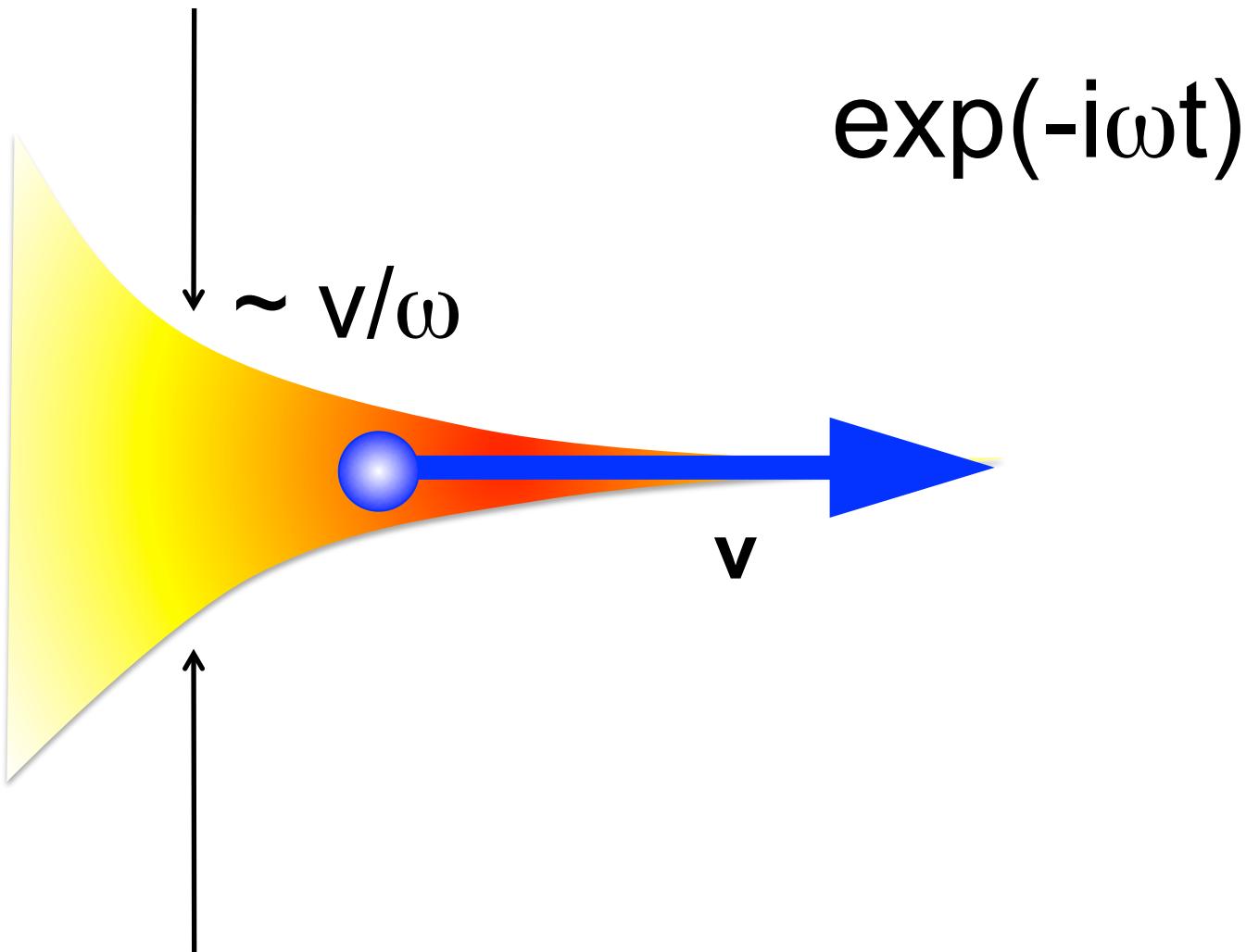
Designing field enhancers



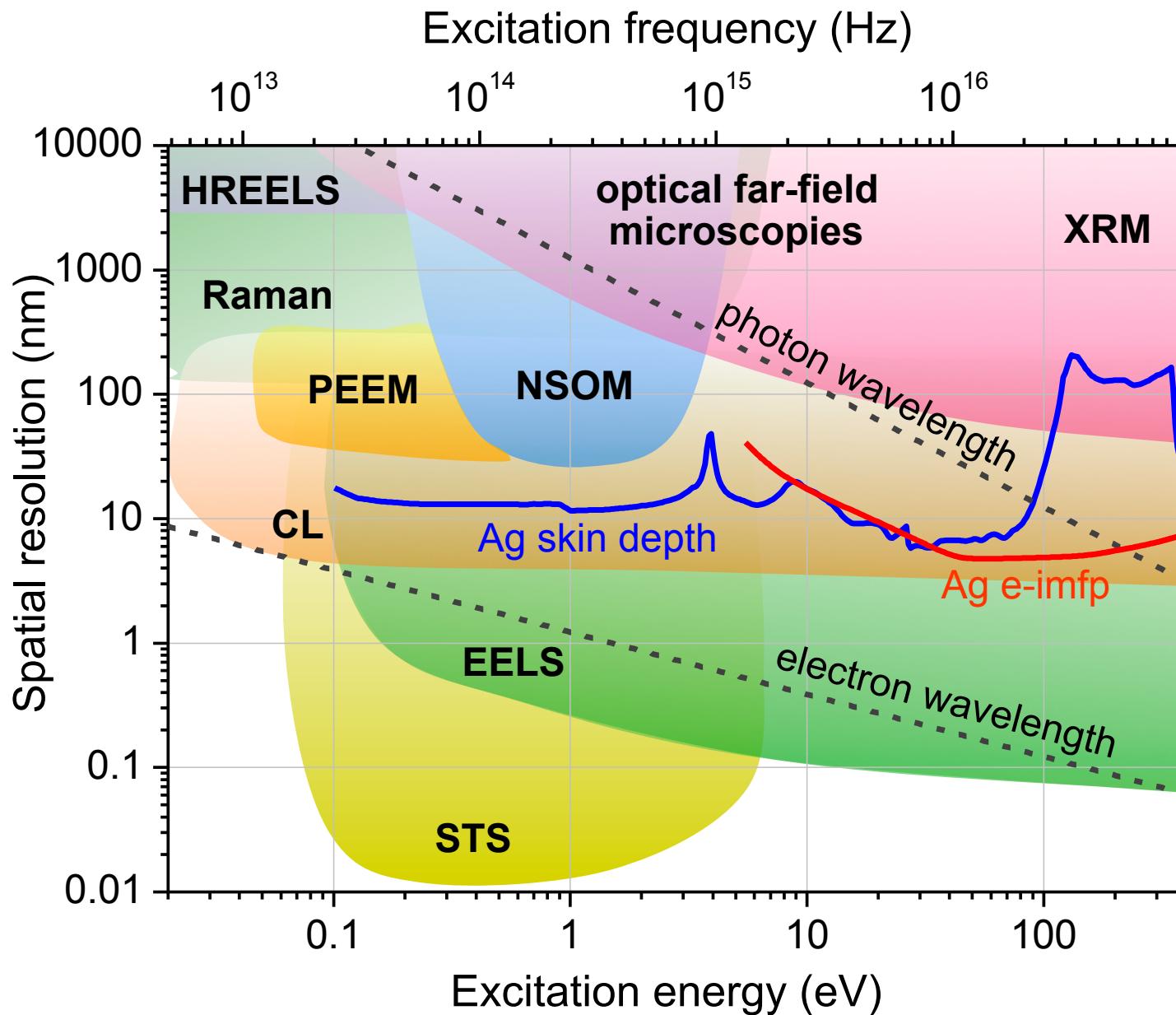
Designing field enhancers



Probing plasmons with electron beams

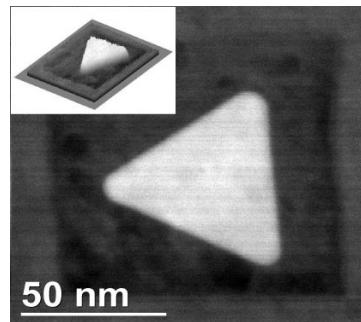


Probing plasmons with electron beams

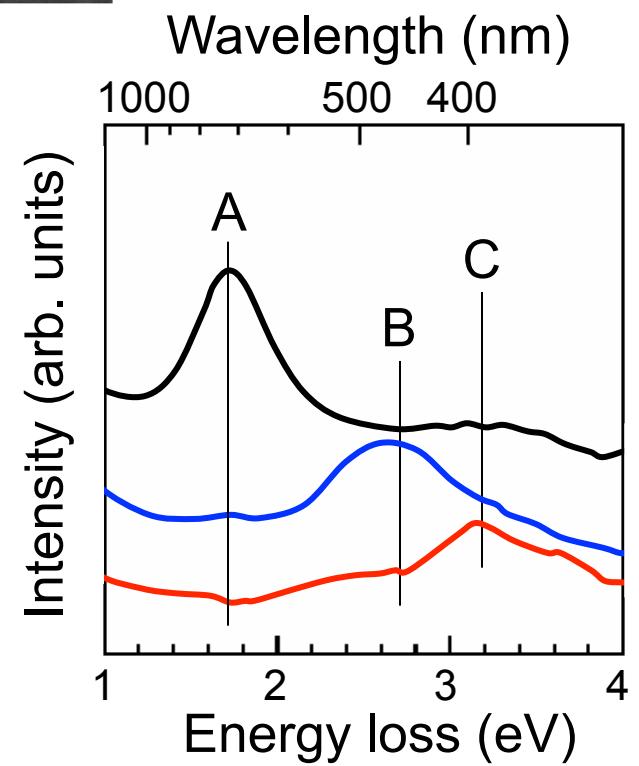
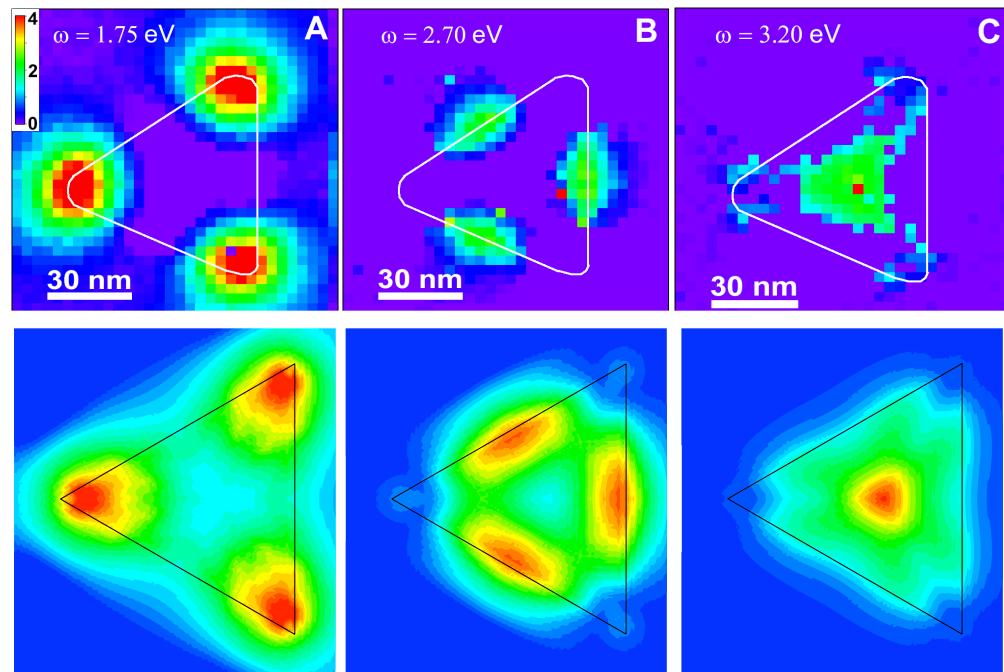


Probing plasmons with electron beams

Ag nanotriangle on mica



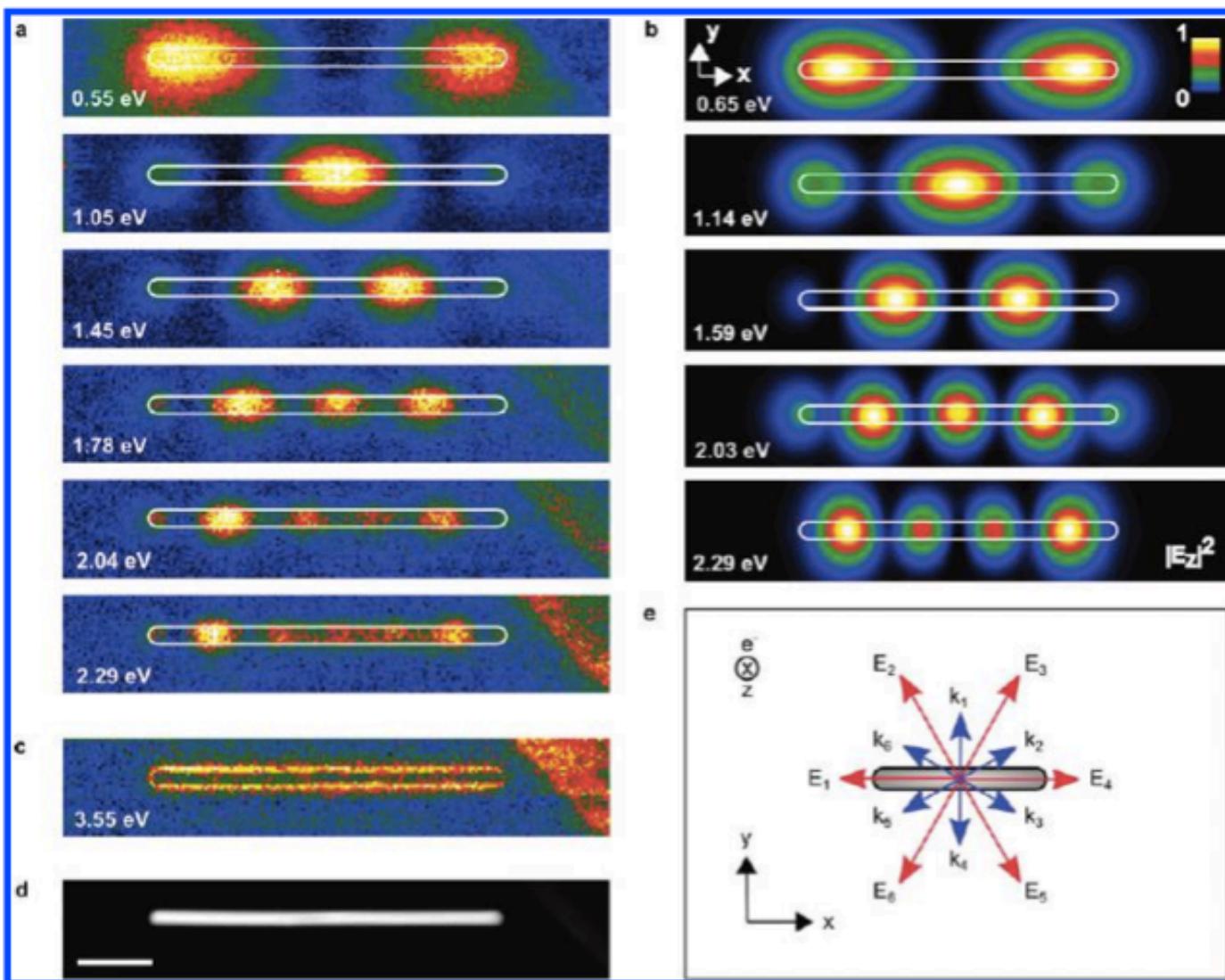
EXPERIMENT: EELS MAPS



THEORY

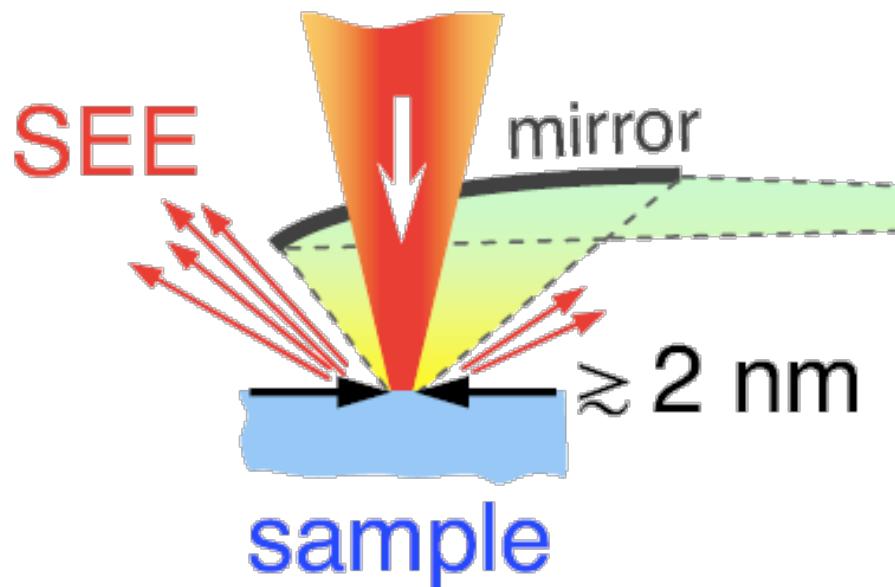
Nelayah *et al.*, Nature Physics (2007)

Probing plasmons with electron beams

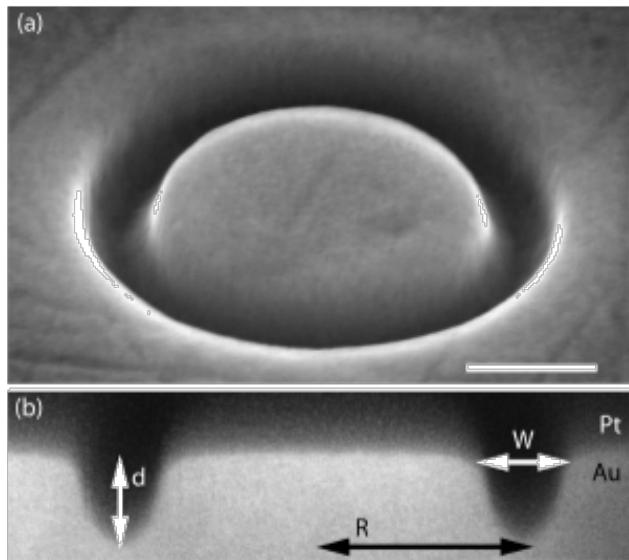


Probing plasmons with electron beams

1-50 keV
electron
beam



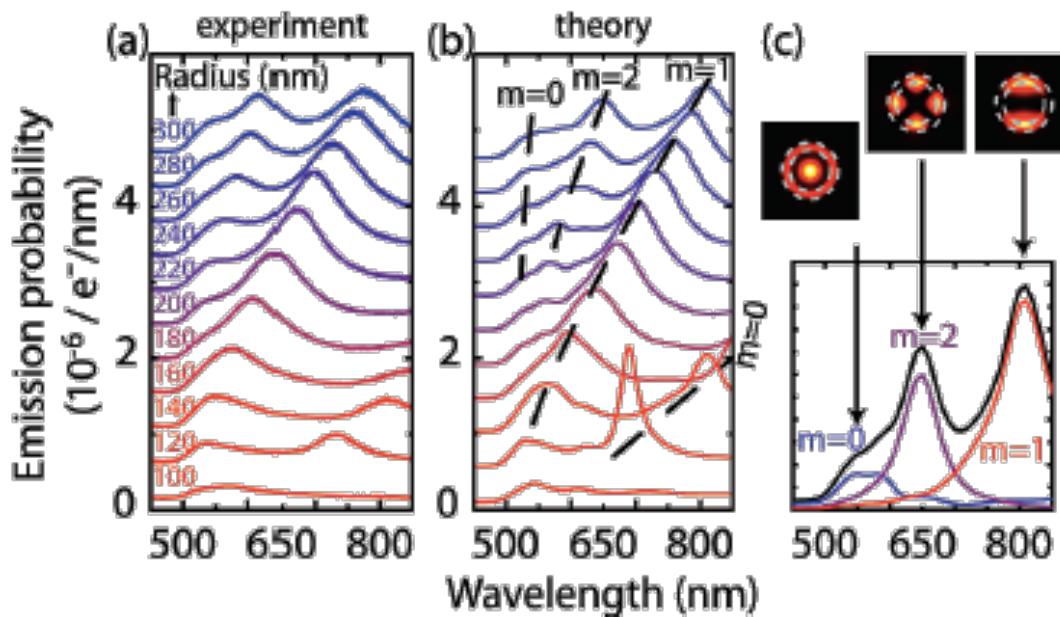
Probing plasmons with electron beams



Modal Decomposition of Surface–Plasmon Whispering Gallery Resonators

Ernst Jan R. Vesseur,^{*†} F. Javier García de Abajo,[‡] and Albert Polman[†]

NANO
LETTERS
2009
Vol. 9, No. 9
3147-3150



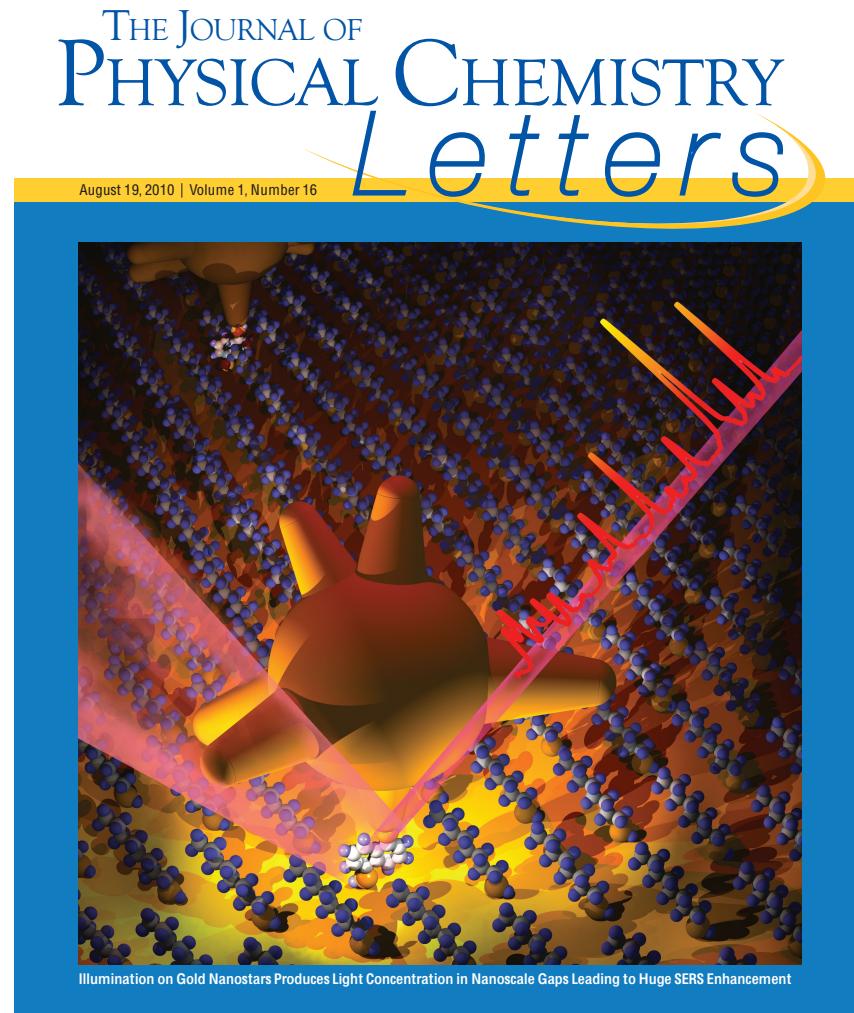
Why are surface plasmons interesting?

- ✓ ▪ Light concentration: plasmon size << wavelength
- ✓ ▪ Field enhancement: induced field >> external field

Applications of optical electric-field enhancement



Controlled 10^{10} SERS enhancement $\rightarrow 10^5$ intensity enhancement



ACS Publications
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Álvarez-Puebla et al.
JACS (2009), JPCL (2010)

Plasmon facts

Plasmons are the quanta of conduction-electron collective oscillations in metals

$$\epsilon(\omega) = 1 - \frac{\omega_p^2}{\omega^2}$$

Plasmons are observed when $\epsilon < 0$ (metallic behavior)

- Aluminum and other materials at UV frequencies
- 0D and 1D carbon structures at UV frequencies
- Noble metals (Ag, Cu, Au) at visible-NIR frequencies 
- 2D carbon structures (graphene) at IR frequencies
- Alkali-halides at THz frequencies
- The ionosphere at (AM) radio frequencies

- Pure conduction-electron oscillations in deep-subwavelength structures
- Hybridization with photons for larger sizes

Applications

- Medical applications – imaging
- Medical applications – drug delivery
- Medical applications – bio-molecule ultrasensitive sensing
- Medical applications – thermal cell-apoptosis
- Optical signal processing
- Metamaterials (extensive light manipulation at subwavelength scales)
- Optical manipulation
- Enhanced radiative transfer
- Signal amplification (spacer)
- More metamaterials ($\mu \neq 1$ at high frequency, negative refraction, ...)
- Solar cells
- ...

Why are surface plasmons interesting?

- ✓ ▪ Light concentration: plasmon size << wavelength
- ✓ ▪ Field enhancement: induced field >> external field
- ✗ ▪ Fast tunability: electrical doping

Plasmonics: An overview and some new trends

Introduction to plasmons

Graphene plasmons

Quantum-mechanical description

Classical description

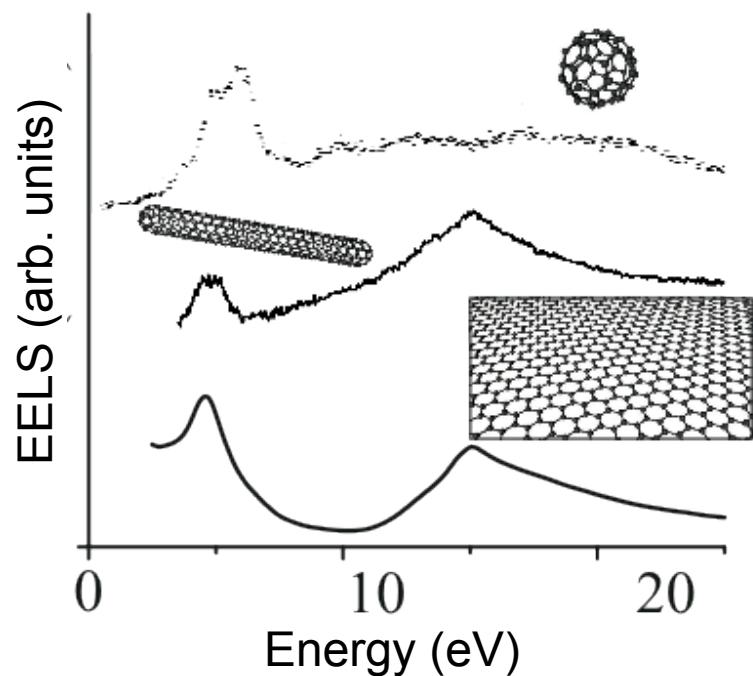
Complete optical absorption

Quantum optics with graphene plasmons

Sensing with graphene plasmons

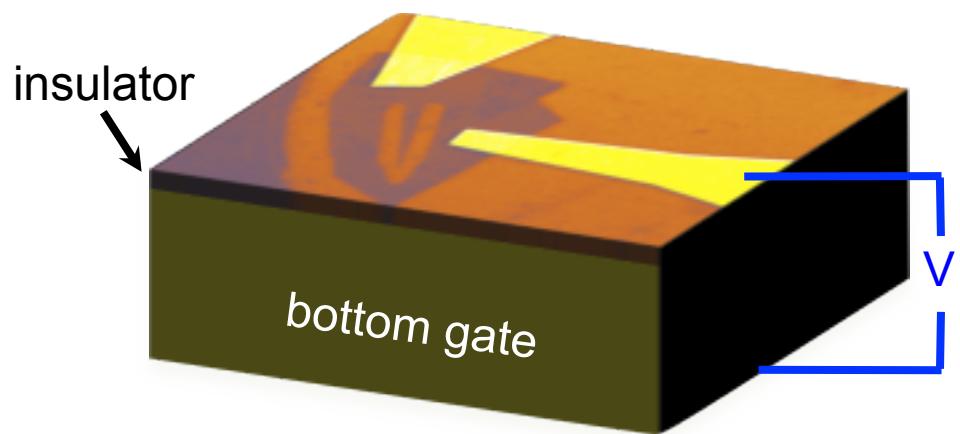
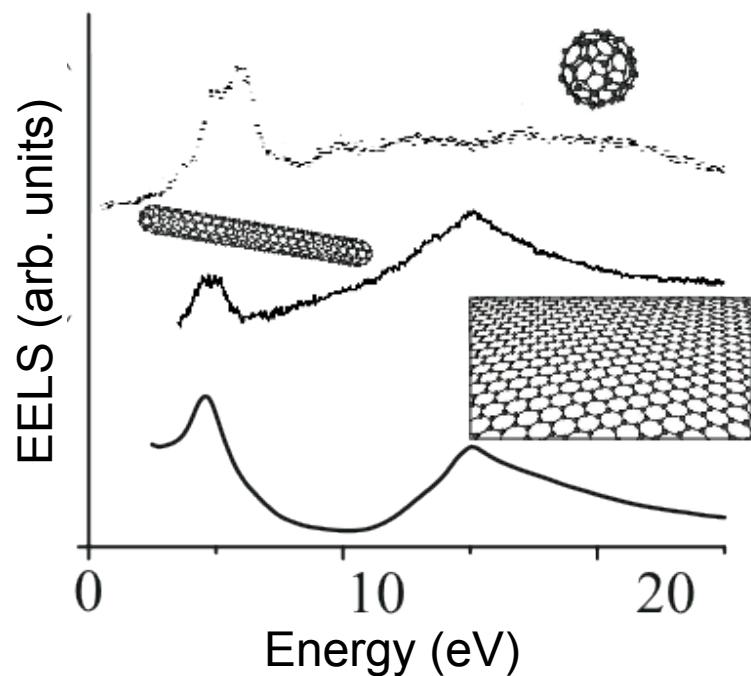
Plasmons in other atomically thin materials

Graphene plasmons

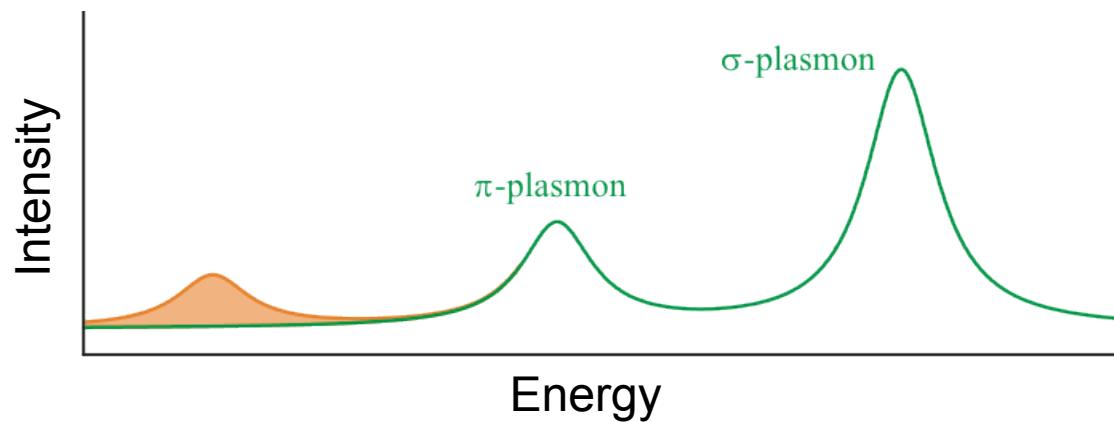
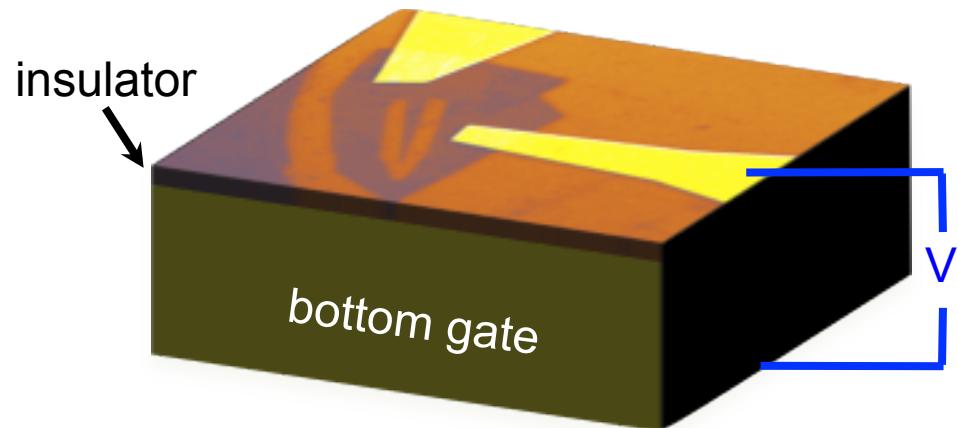
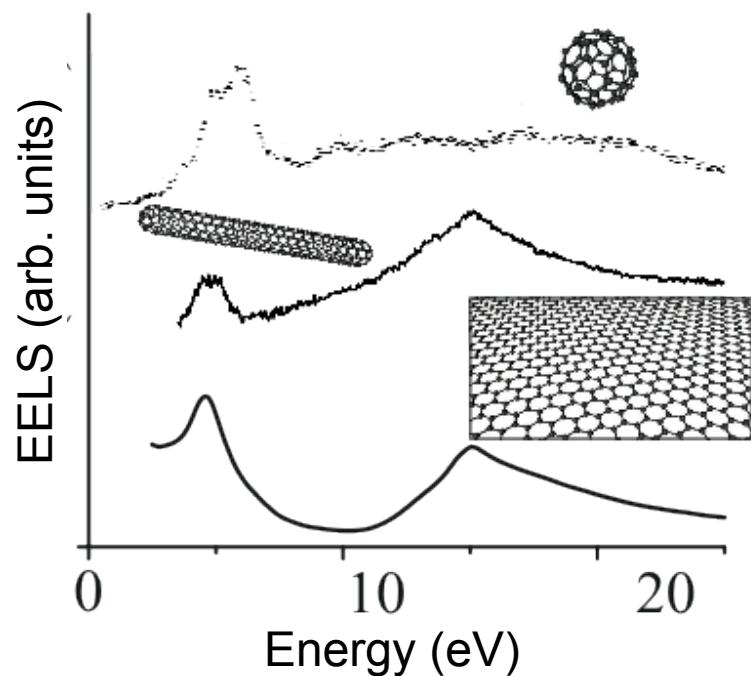


Keller and Coplan, Chem. Phys. Lett. (1992)
Stéphan, ..., Colliex, Phys. Rev. B (2002)
Zhou, ..., Idrobo, Nat. Nanotech. (2012)

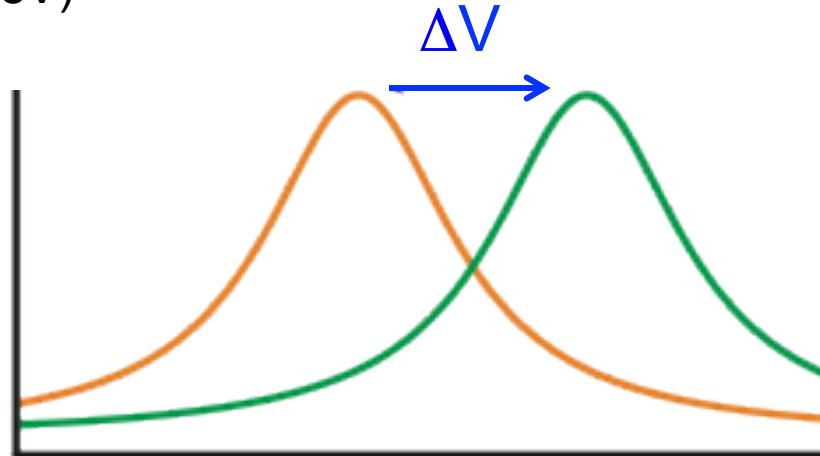
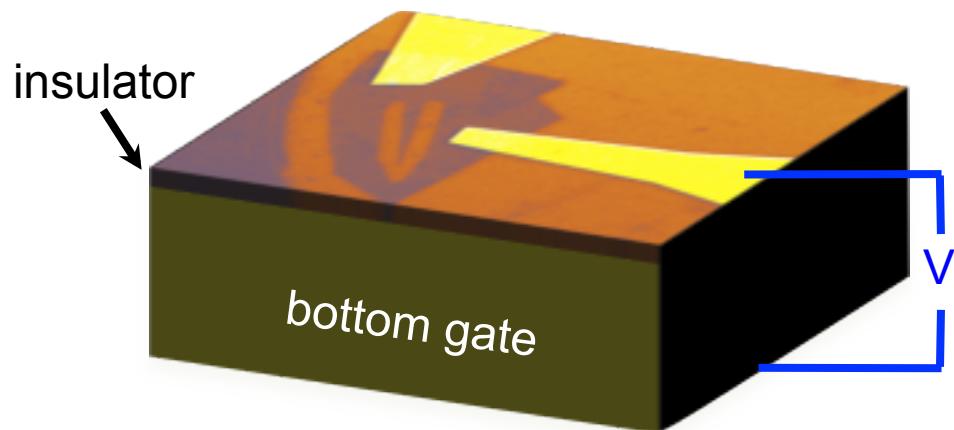
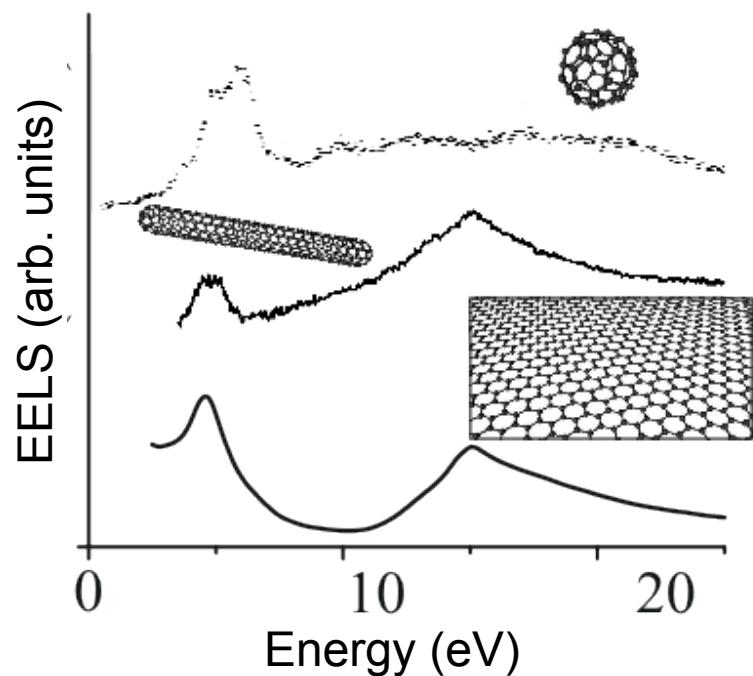
Graphene plasmons



Graphene plasmons

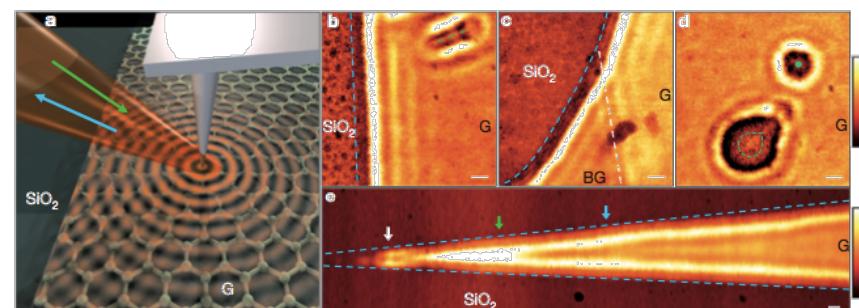
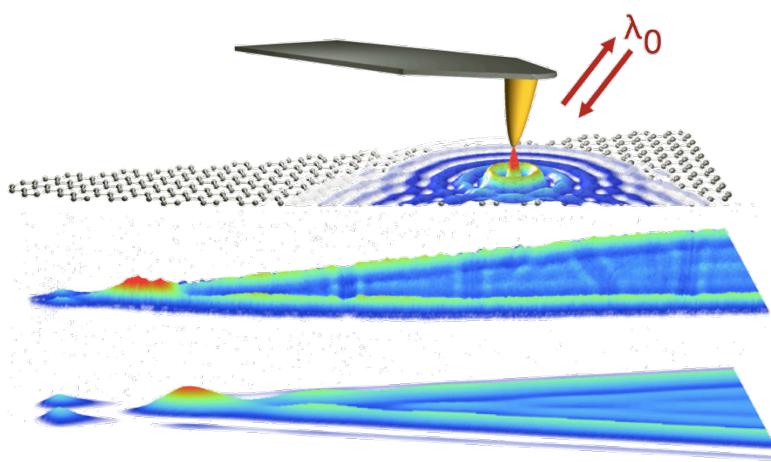


Graphene plasmons



Graphene Plasmonics

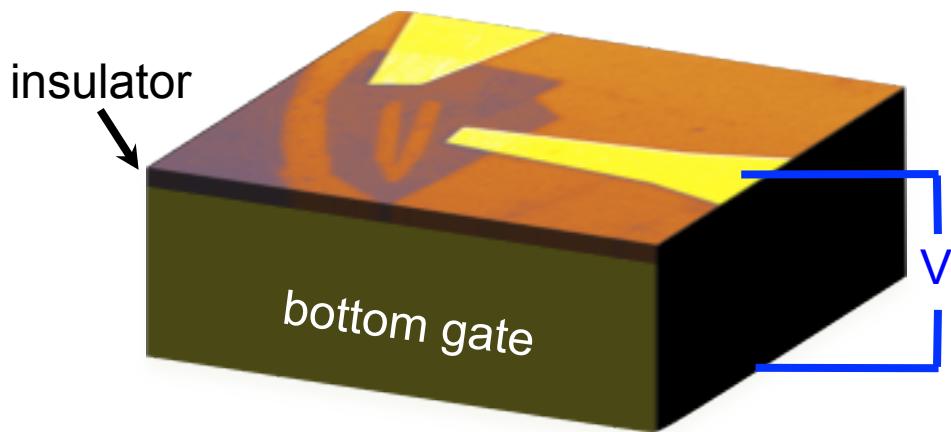
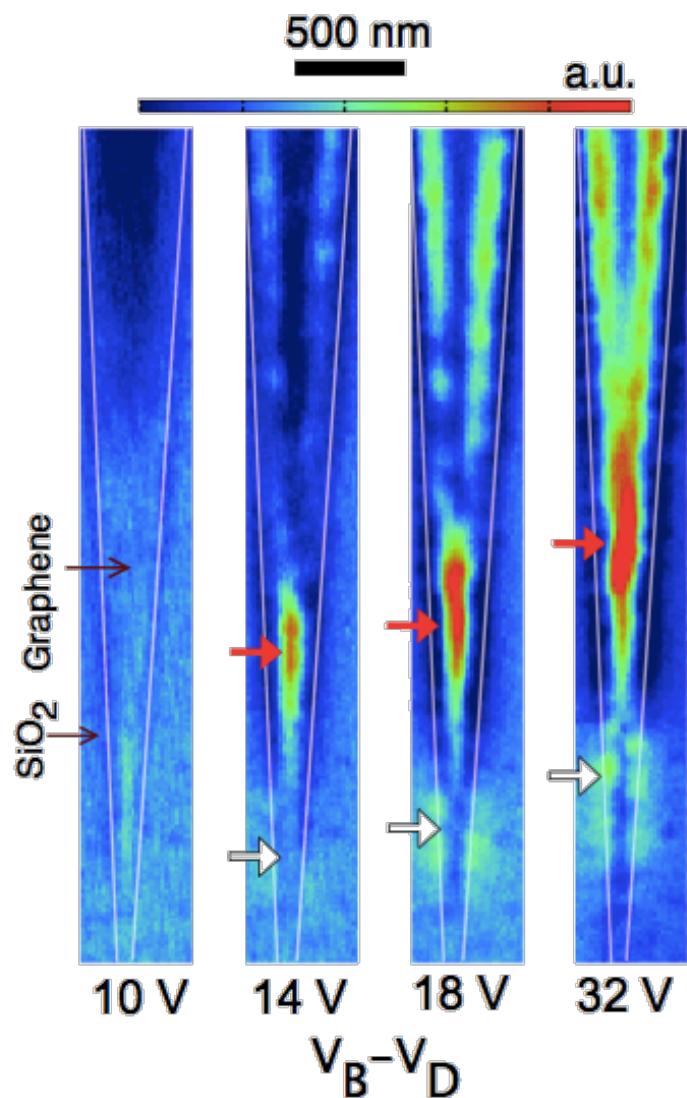
Experimental demonstration of spatial mapping and electrical tunability of graphene plasmons



Chen *et al.*, Nature (2012)

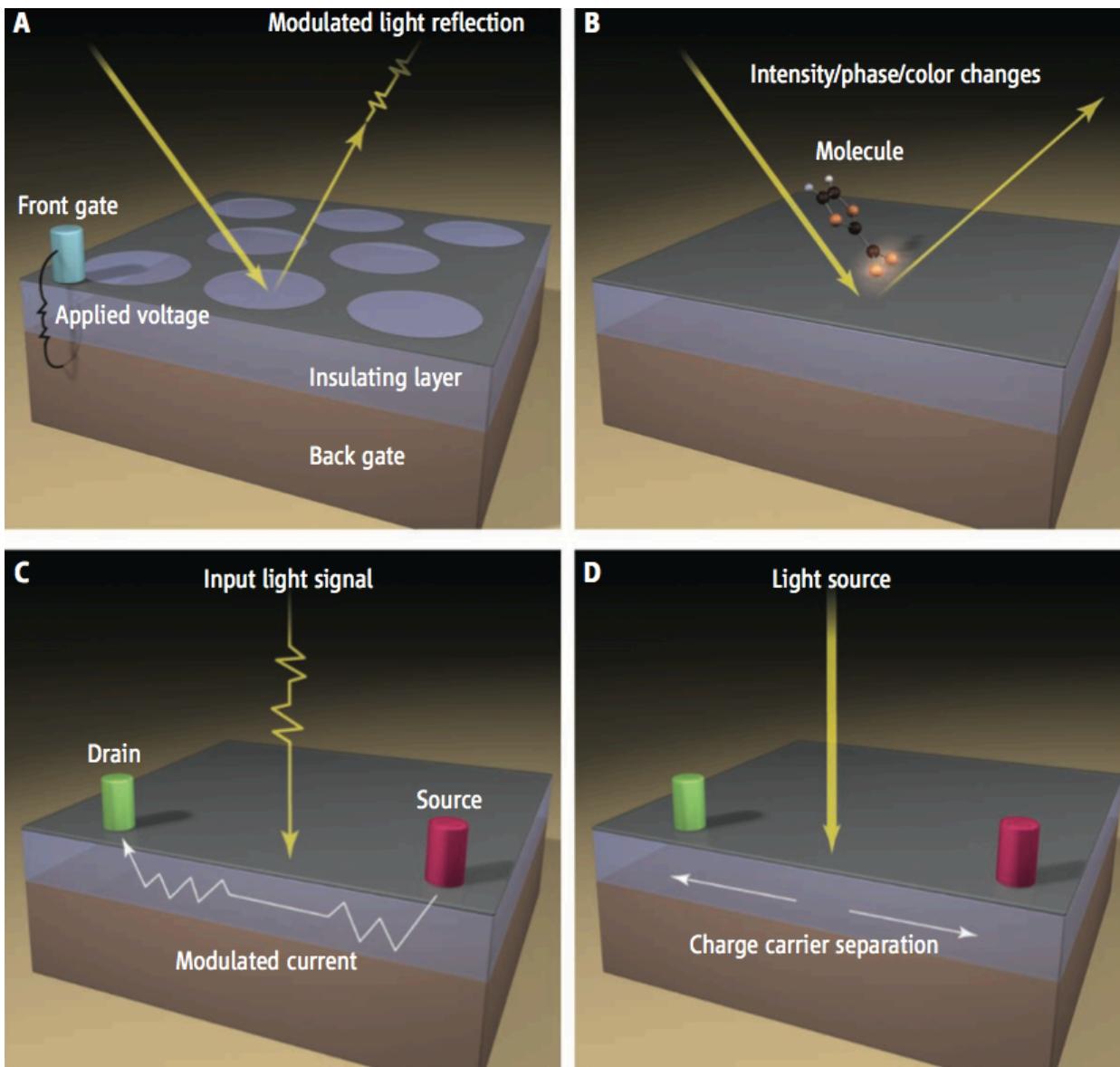
Basov's group Fei *et al.*, Nature (2012)

Experimental mapping of graphene plasmons



Chen *et al.*, Nature (2012)
Fei *et al.*, Nature (2012)

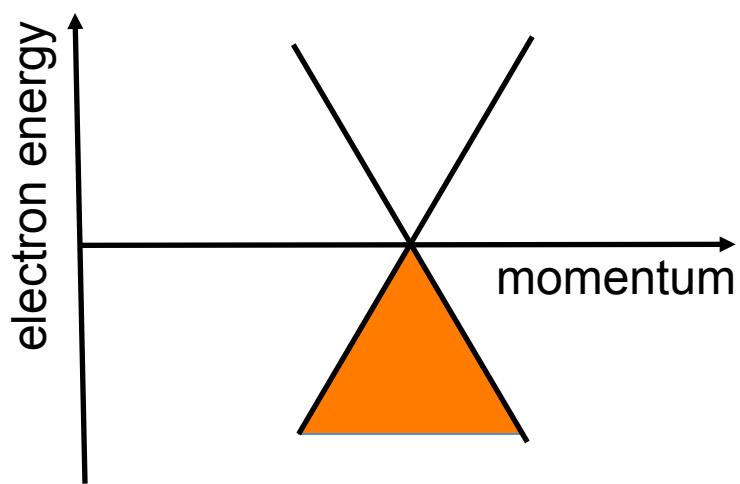
Graphene plasmons perspectives



García de Abajo, Science (2013)

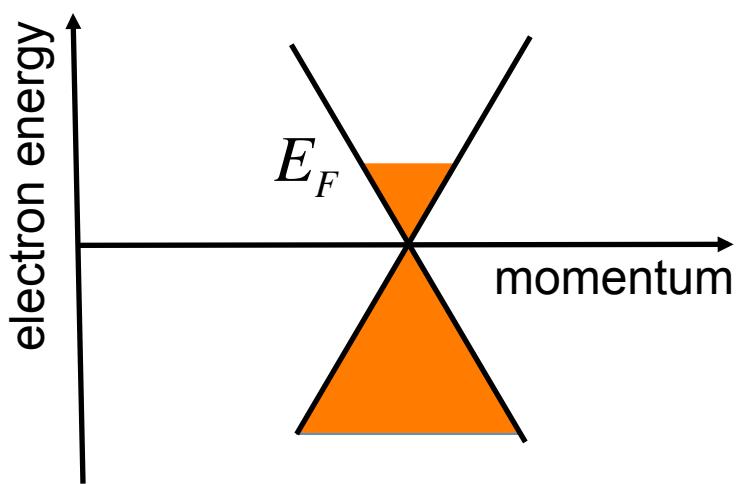
Electrostatic doping of graphene

screening
electron density graphene
 $n = E_{DC} / 4\pi e$ ↑ layer
DC electric field
 E_{DC}



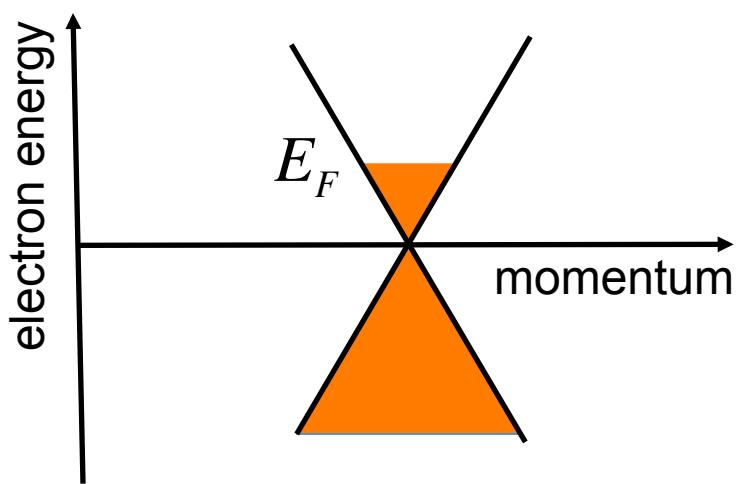
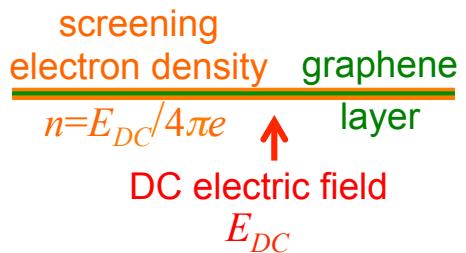
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$$\sigma \approx \frac{e^2 E_F}{\hbar^2 \pi} \frac{i}{\omega + i\tau^{-1}}$$

Electrostatic doping of graphene

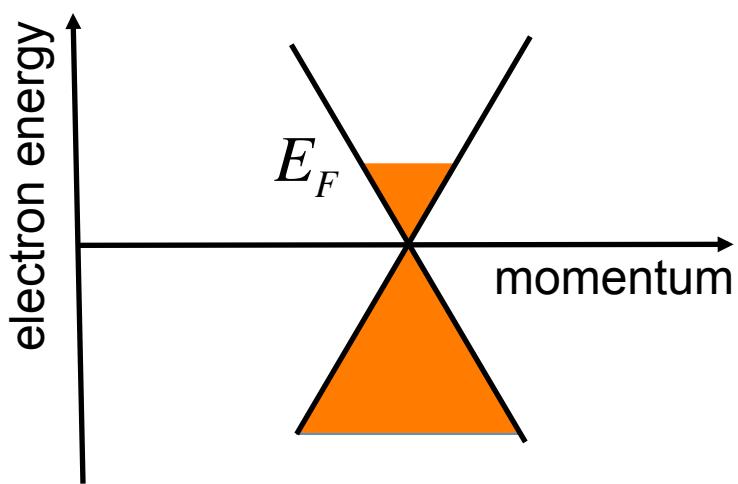


$$\sigma \approx \frac{e^2 E_F}{\hbar^2 \pi} \frac{i}{\omega + i\tau^{-1}}$$

$$\lambda_{sp} = \frac{-2\pi i \sigma}{c} \lambda_0$$

Electrostatic doping of graphene

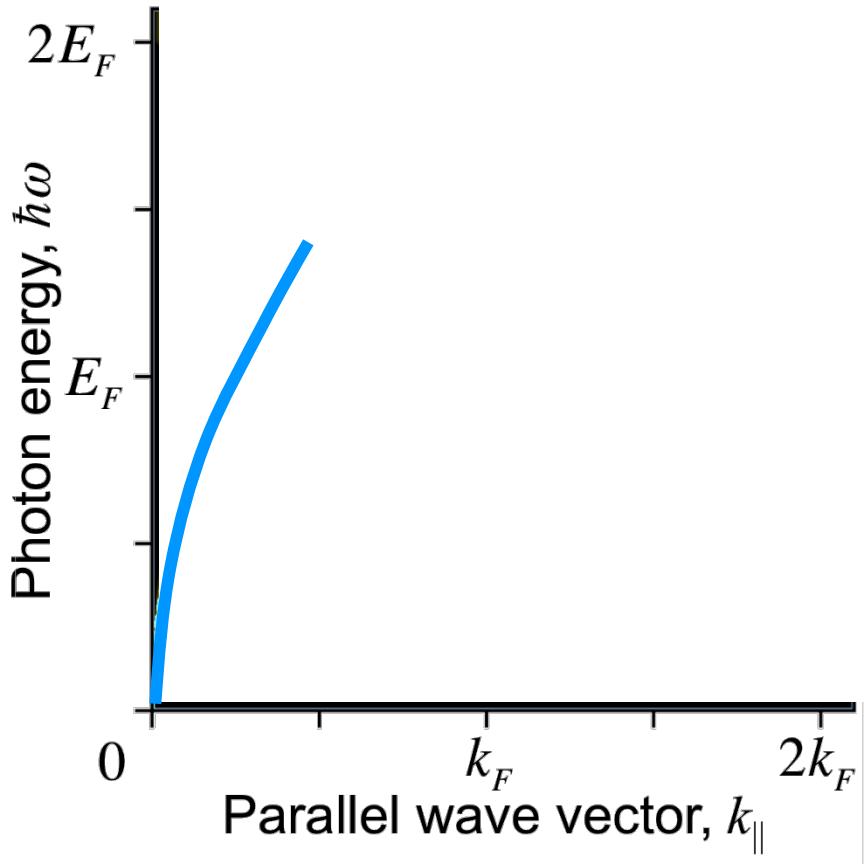
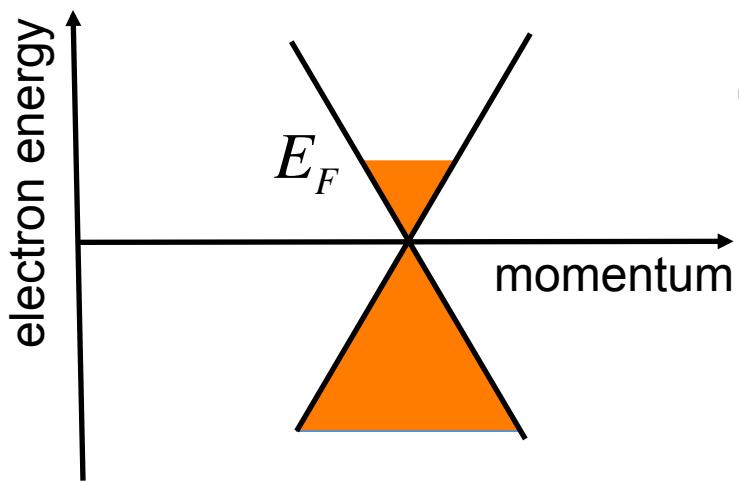
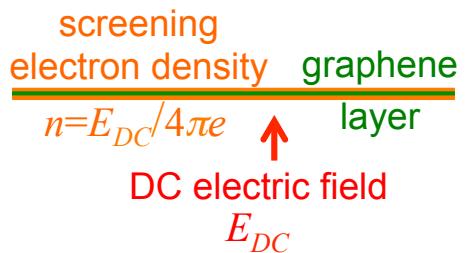
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 E_{DC}



$$\sigma \approx \frac{e^2 E_F}{\hbar^2 \pi} \frac{i}{\omega + i\tau^{-1}}$$

$$\lambda_{sp} = 2\alpha \frac{E_F}{\hbar\omega} \lambda_0$$

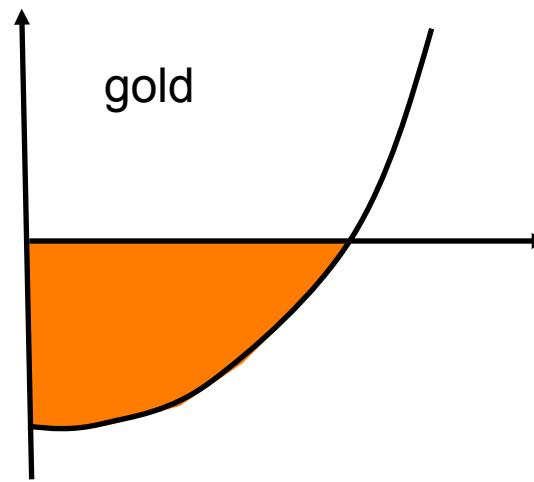
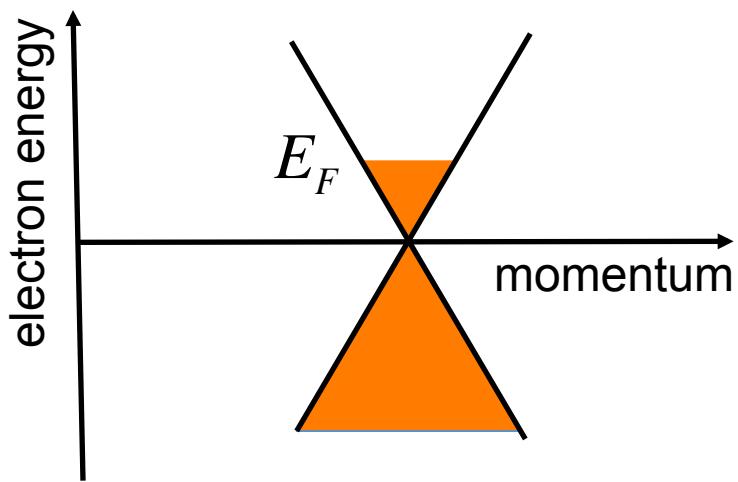
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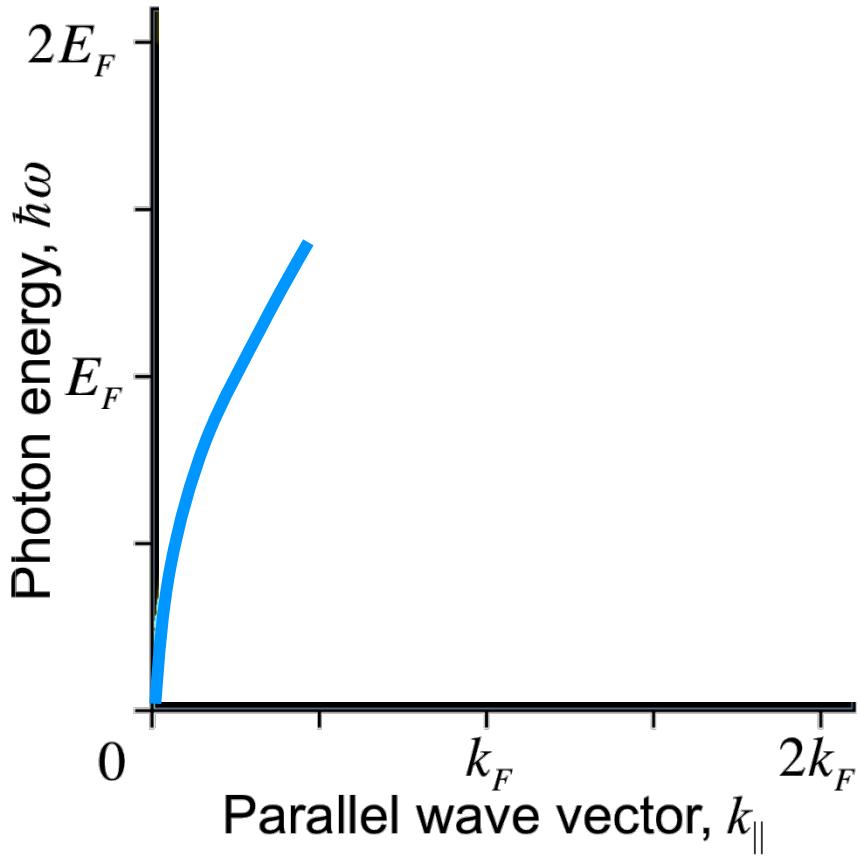
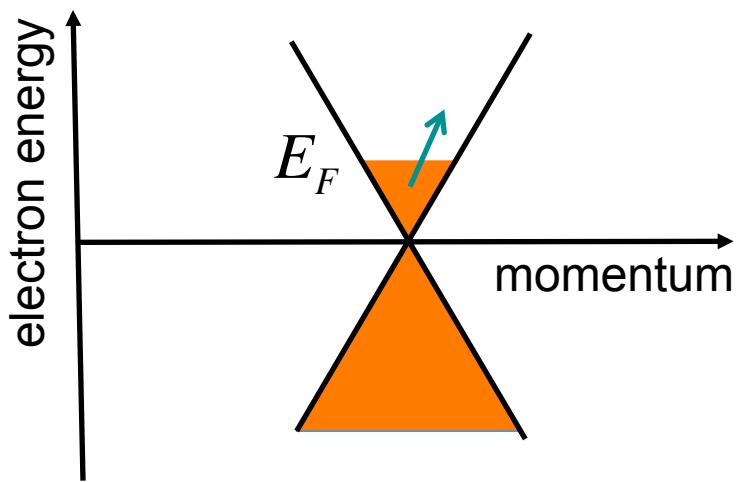
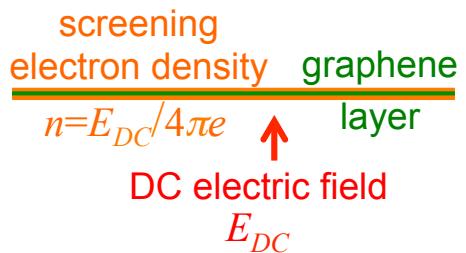
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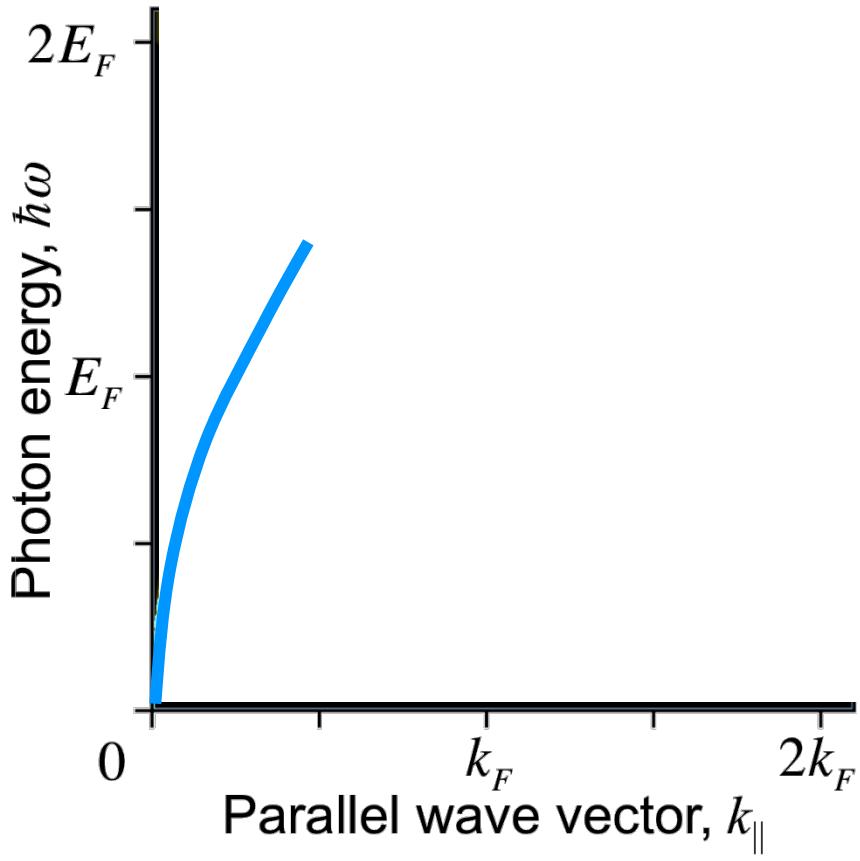
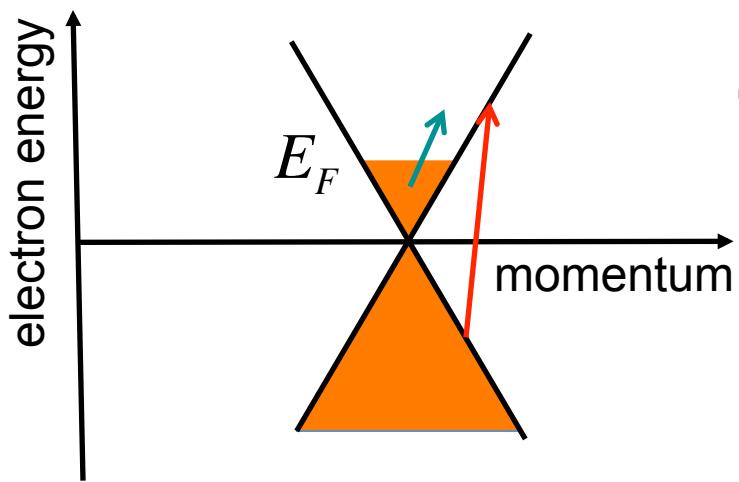
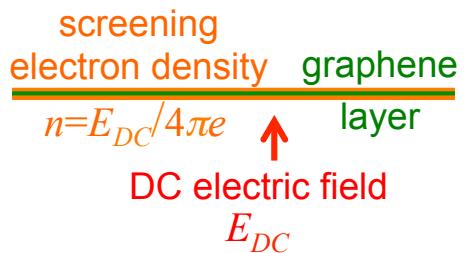


Electrostatic doping of graphene



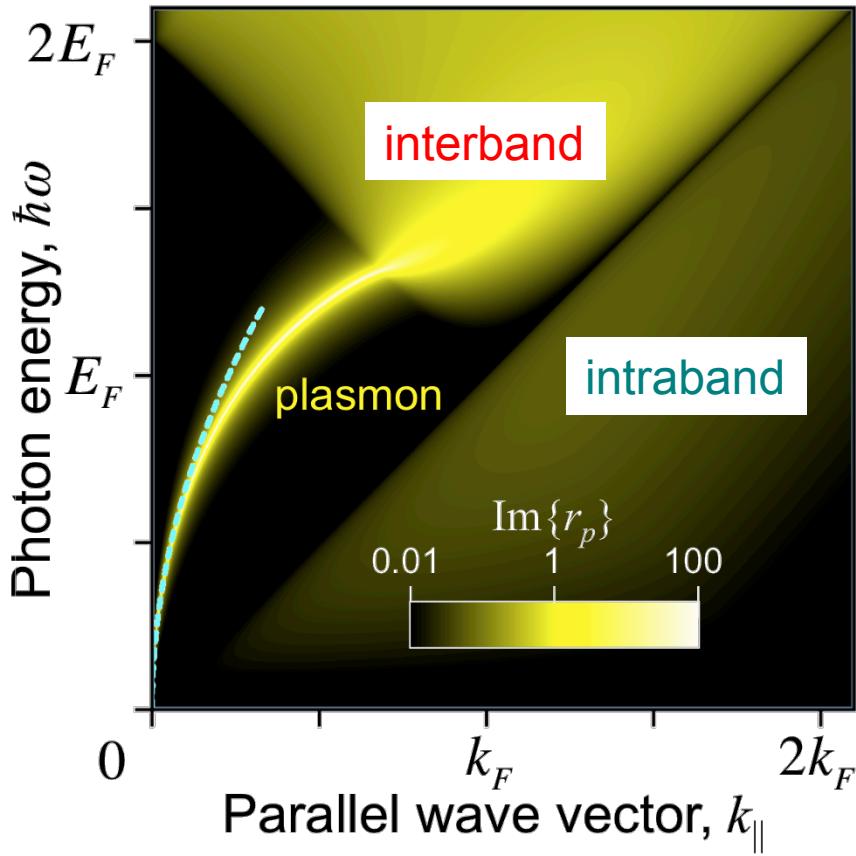
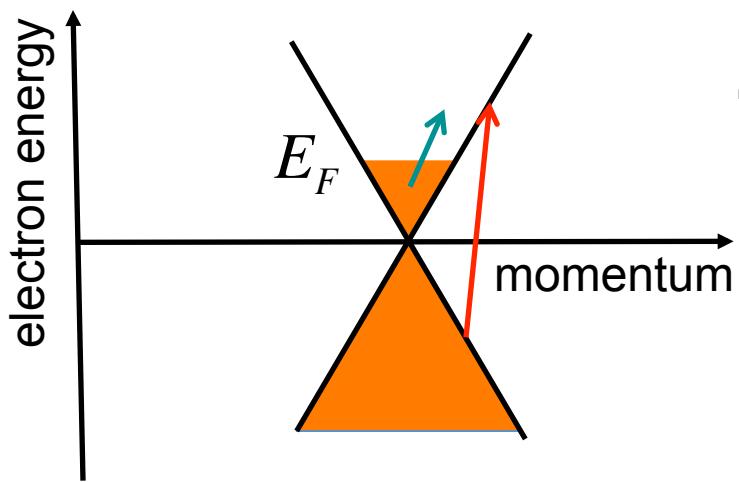
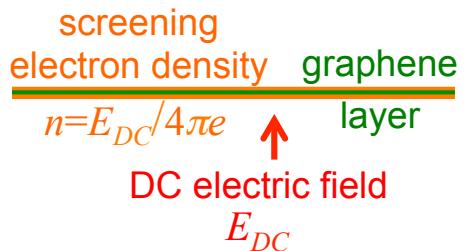
$$\lambda_{sp} = 2\alpha \frac{E_F}{\hbar\omega} \lambda_0$$

Electrostatic doping of graphene



$$\lambda_{sp} = 2\alpha \frac{E_F}{\hbar\omega} \lambda_0$$

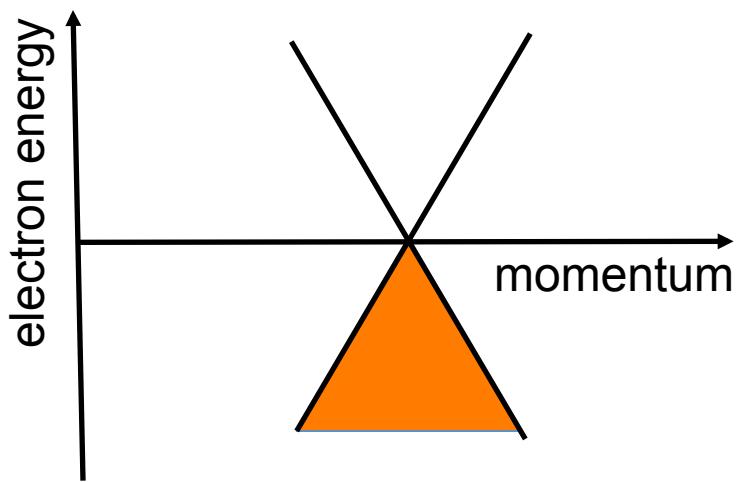
Electrostatic doping of graphene



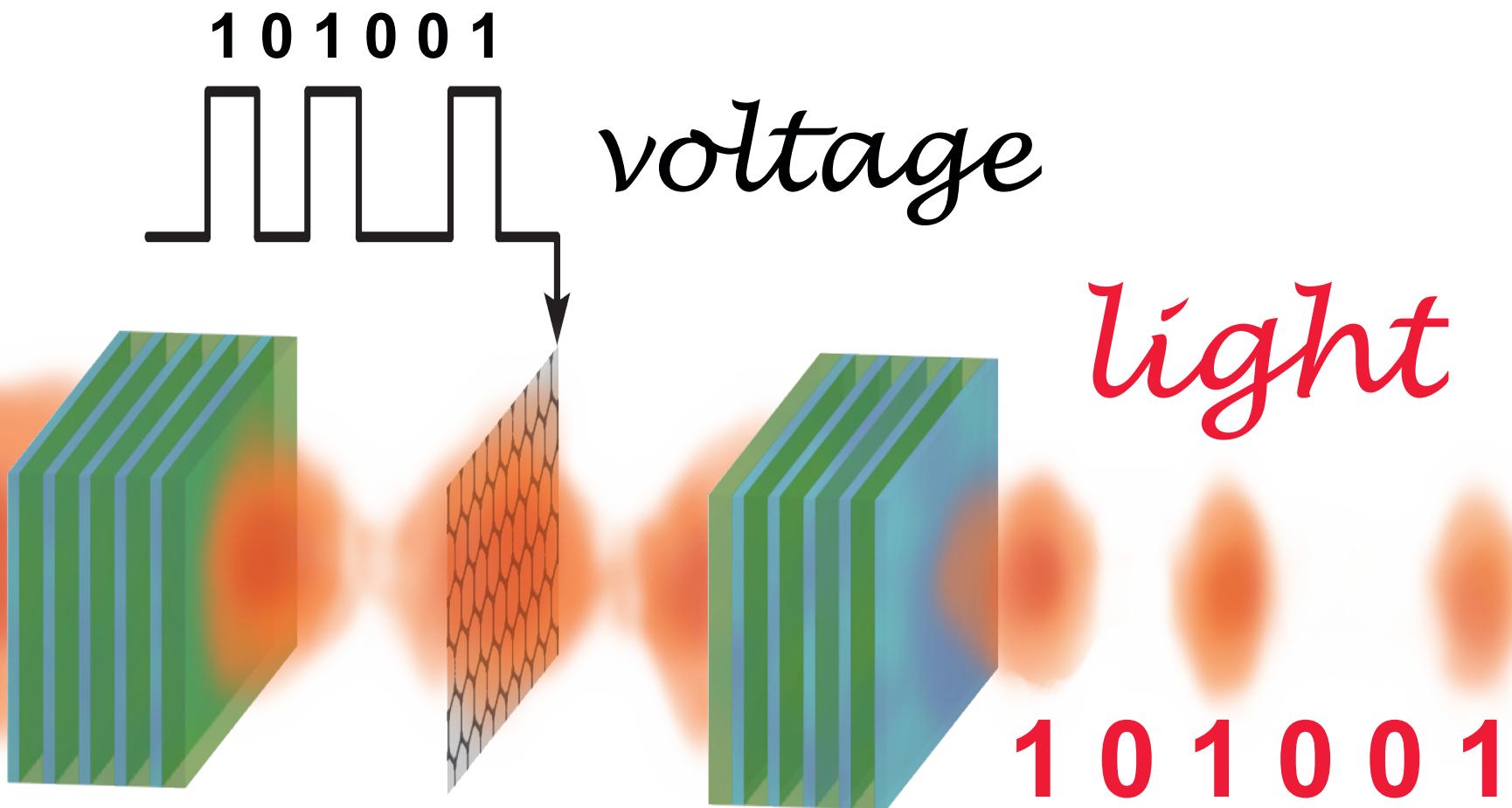
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Electrostatic doping of graphene

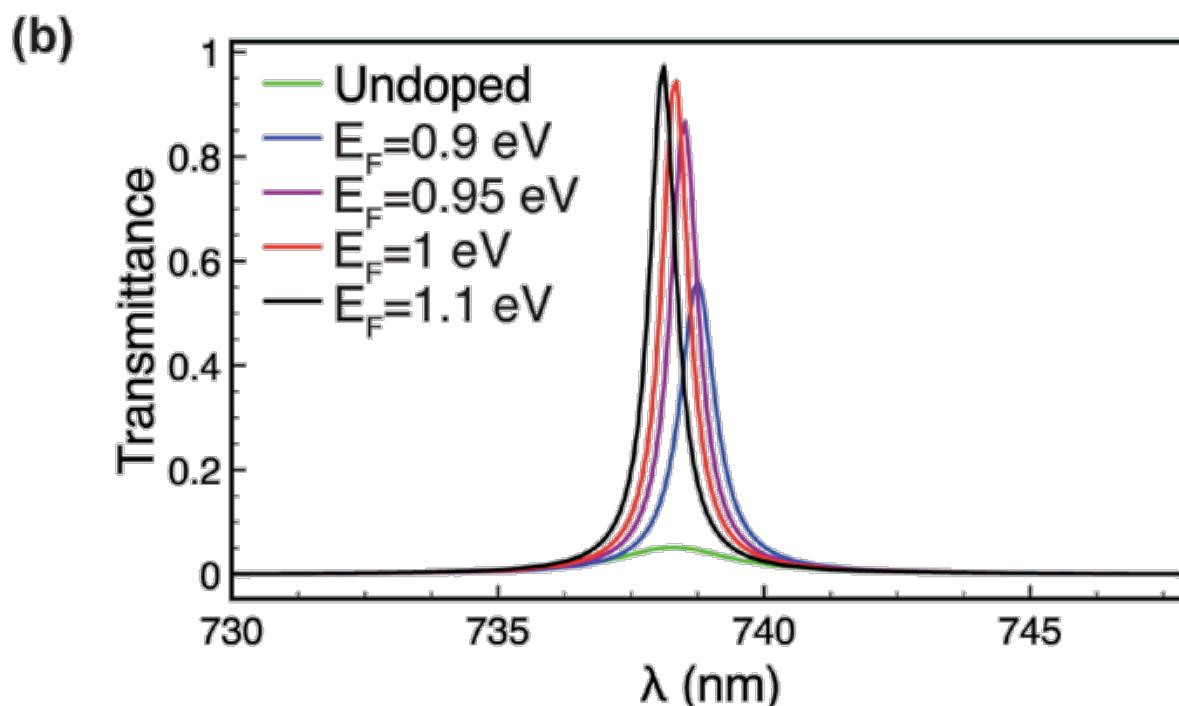
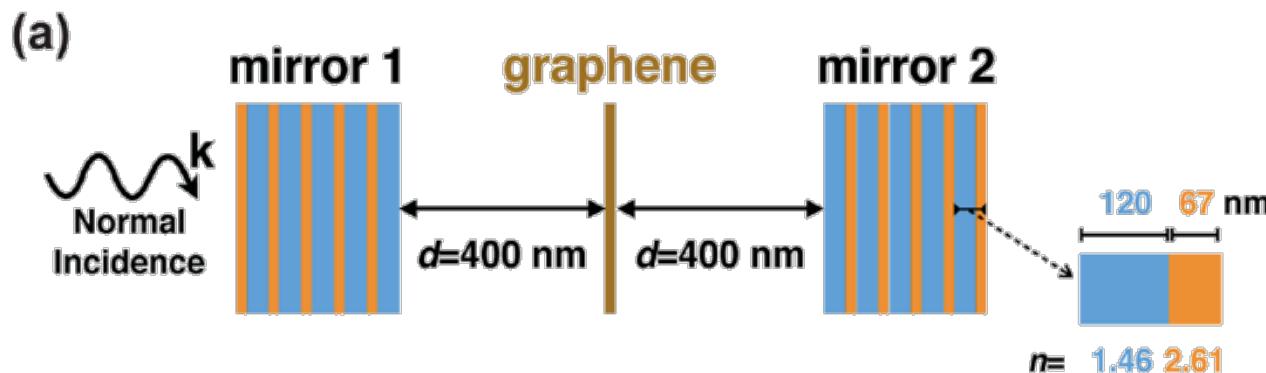
$$\sigma \approx \frac{e^2}{4\hbar} \quad \Rightarrow \quad \text{Absorption} \approx \pi\alpha \approx \frac{\pi}{137}$$



Optical modulation with graphene

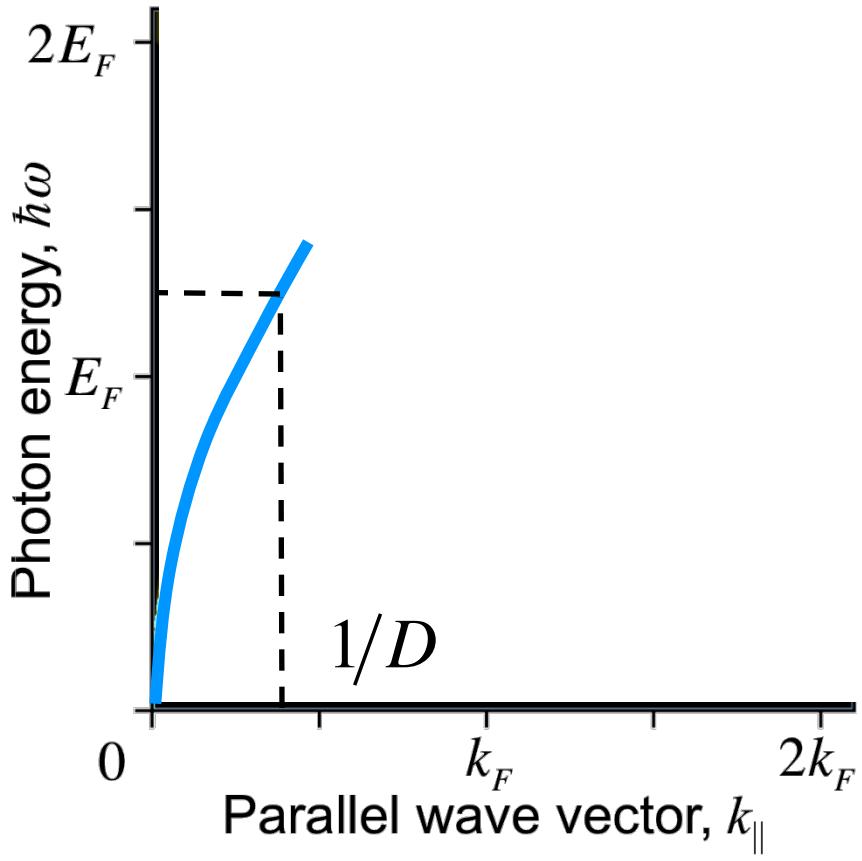
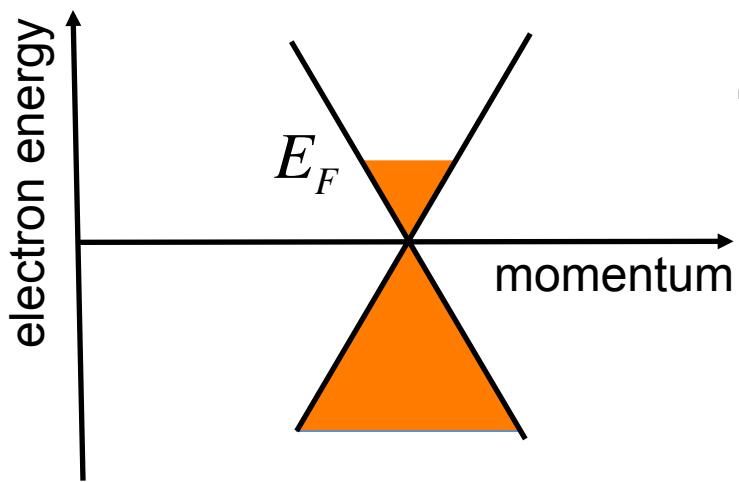


Optical modulation with graphene



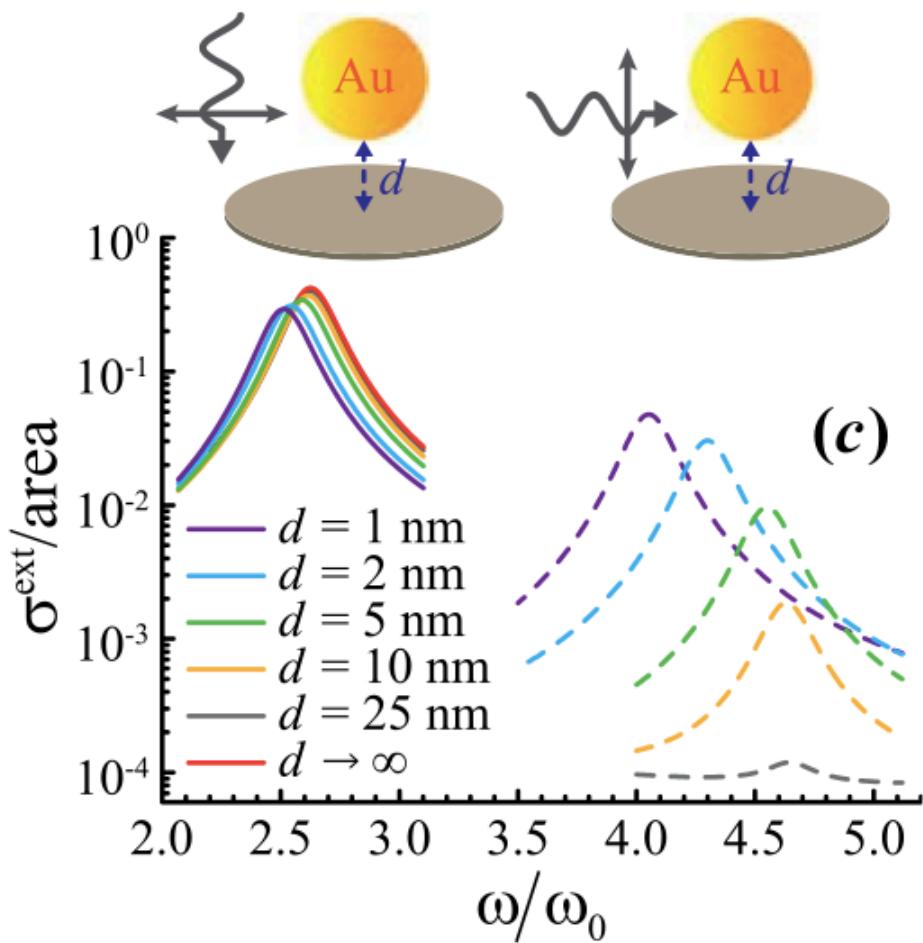
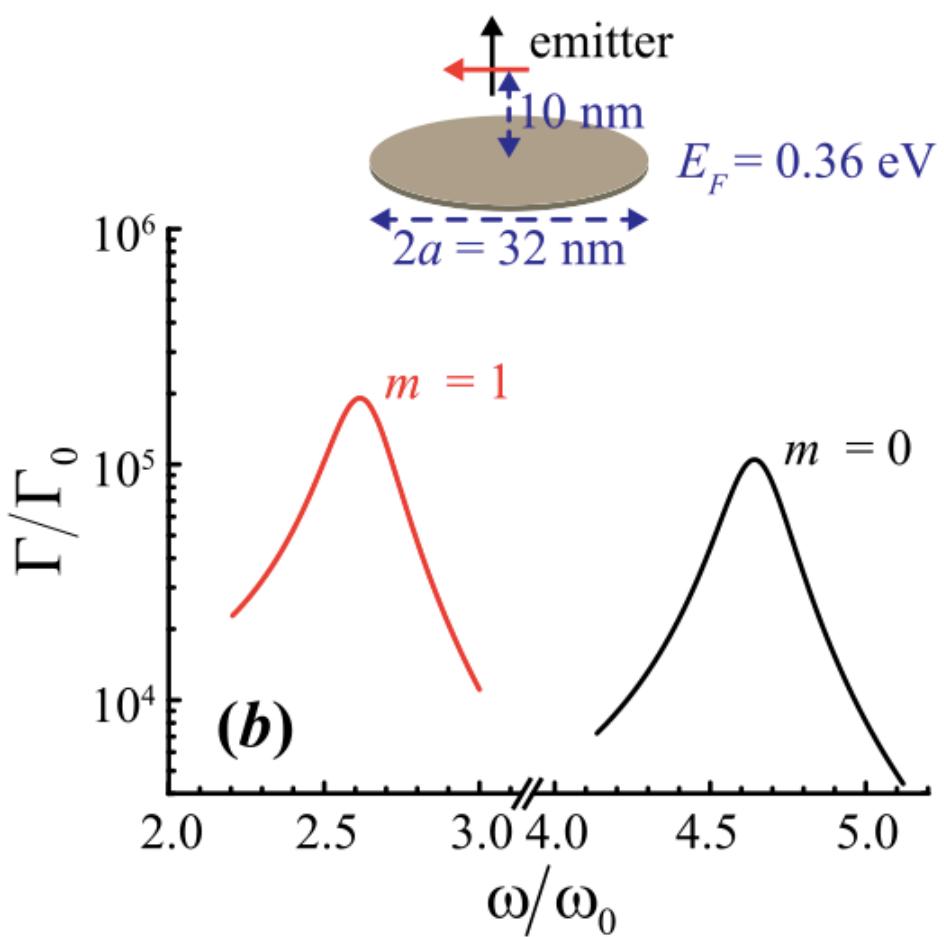
Electrostatic doping of graphene

screening
electron density
 $n = E_{DC}/4\pi e$



$$\lambda_{sp} = 2\alpha \frac{E_F}{\hbar\omega} \lambda_0$$

Plasmons in graphene nanodisks



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Classical description

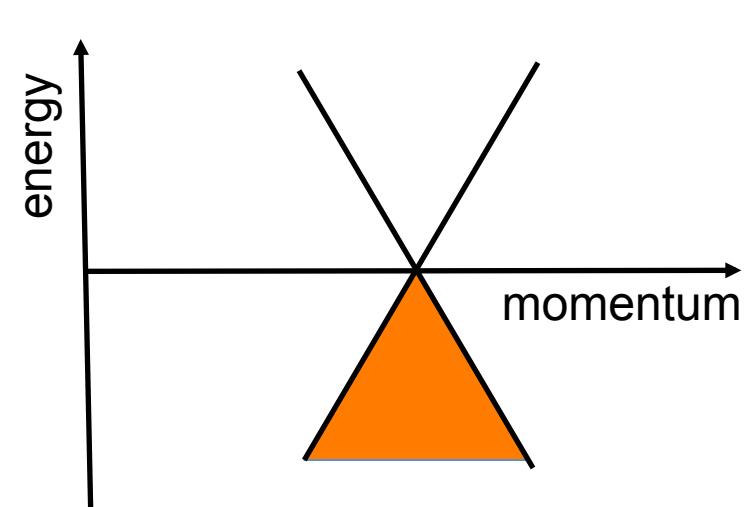
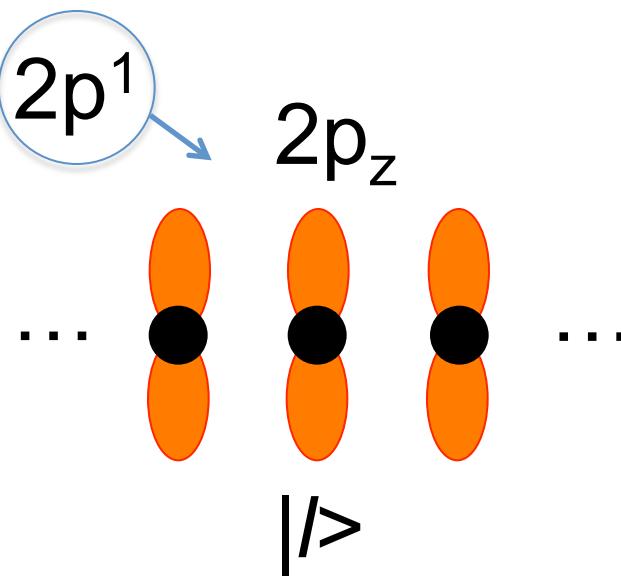
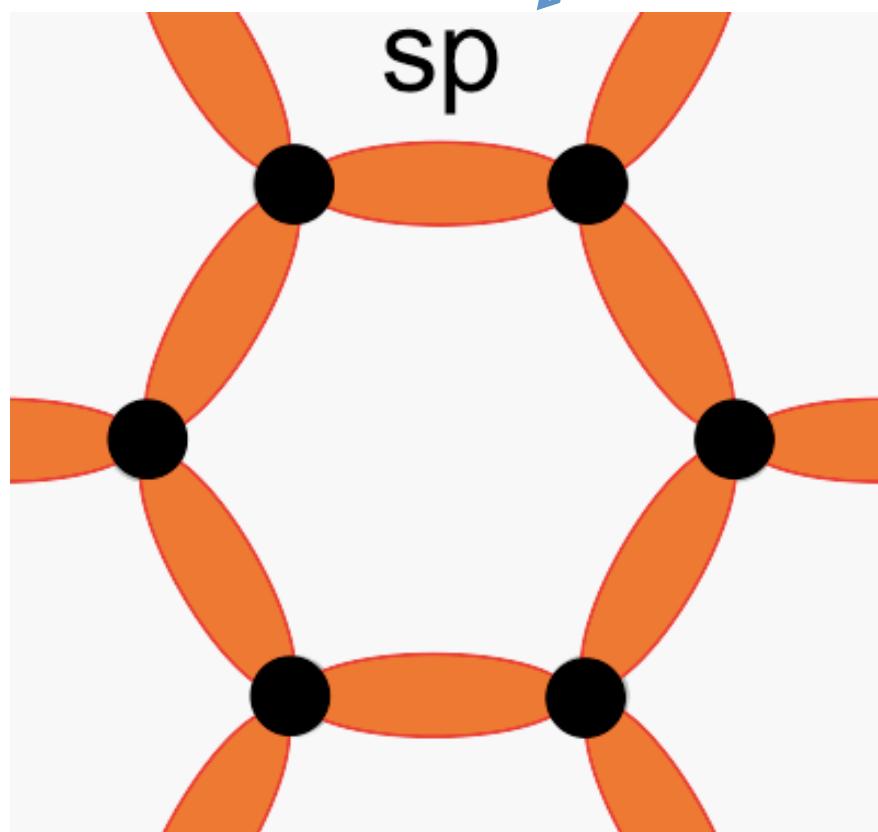
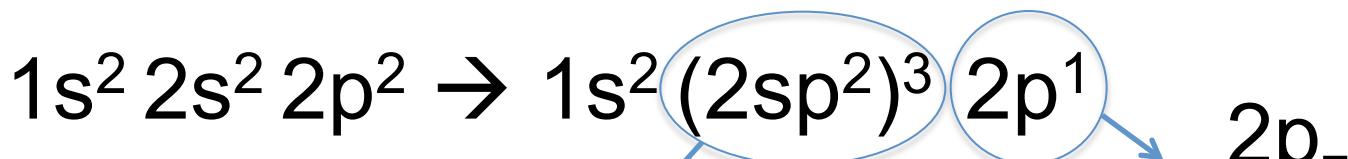
Complete optical absorption

Quantum optics with graphene plasmons

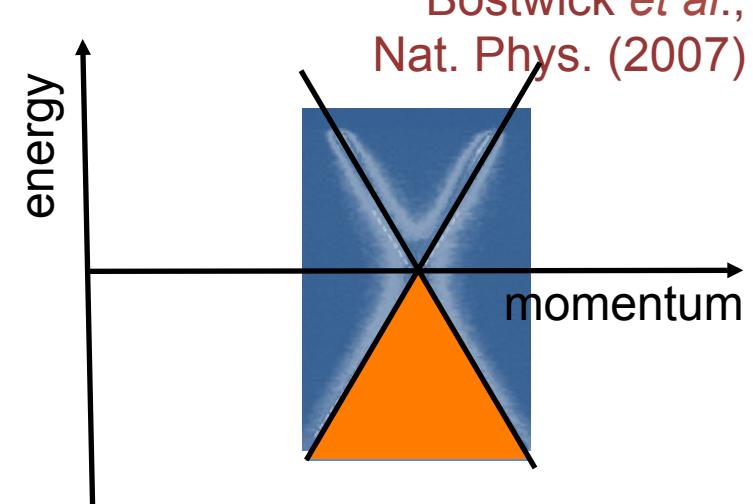
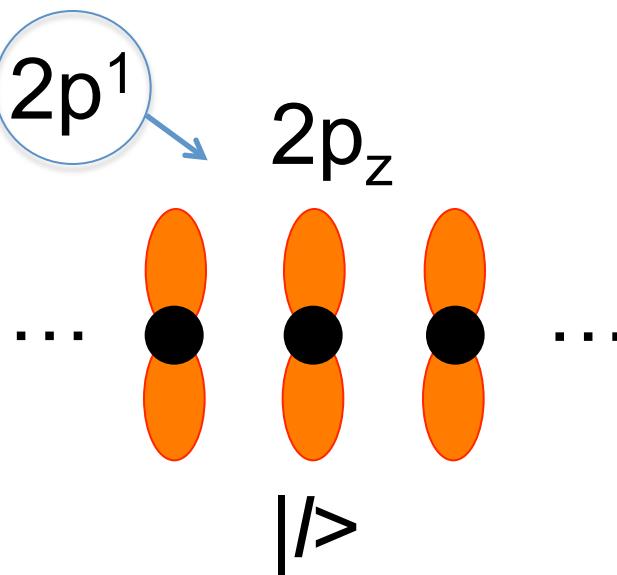
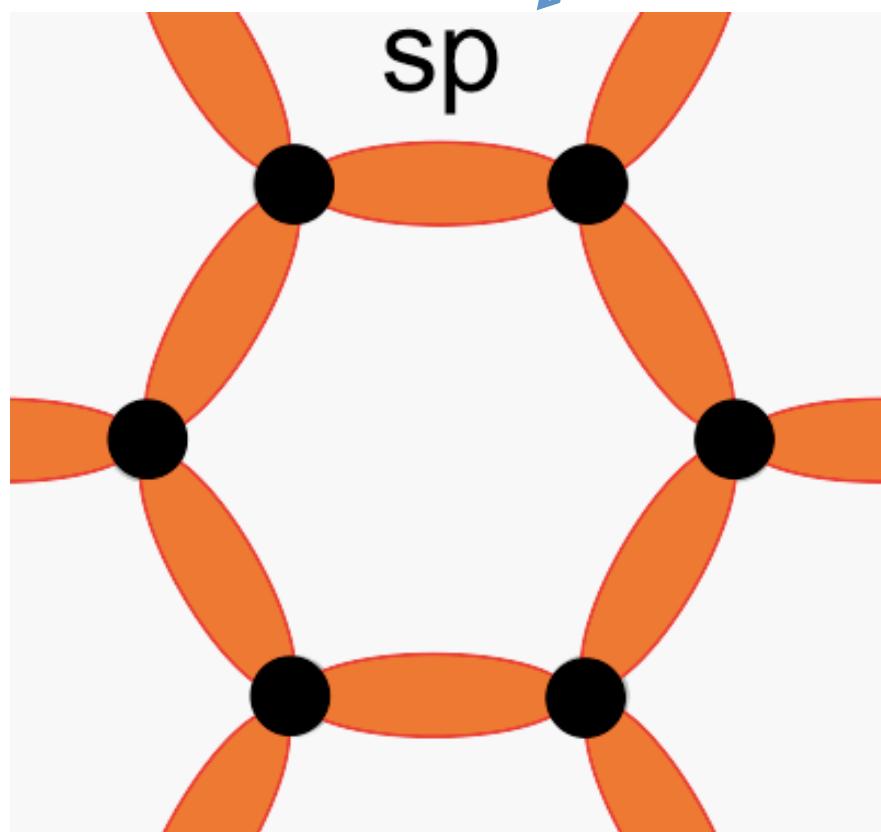
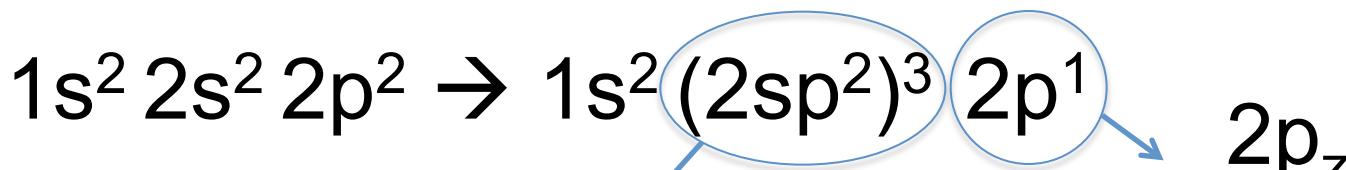
Sensing with graphene plasmons

Plasmons in other atomically thin materials

Quantum description of graphene plasmons

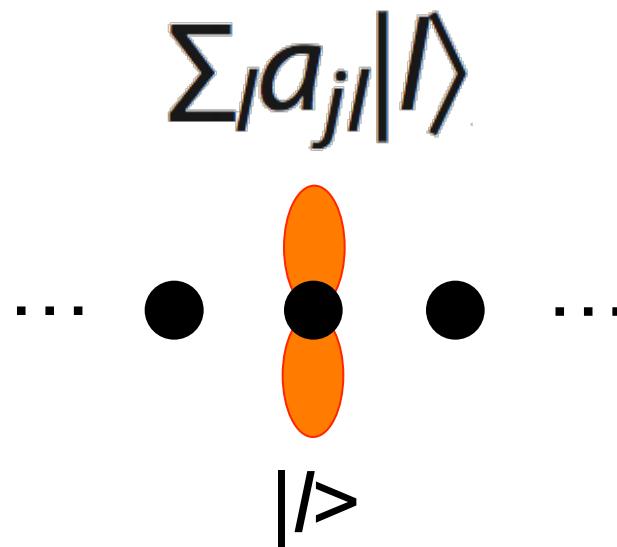


Quantum description of graphene plasmons



Quantum description of graphene plasmons

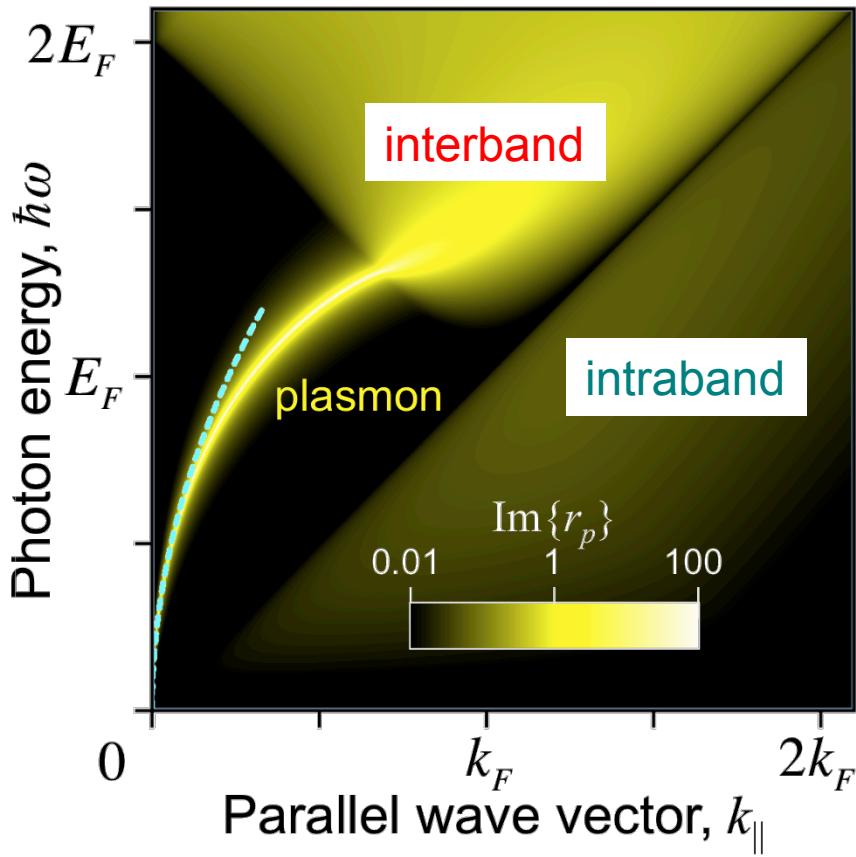
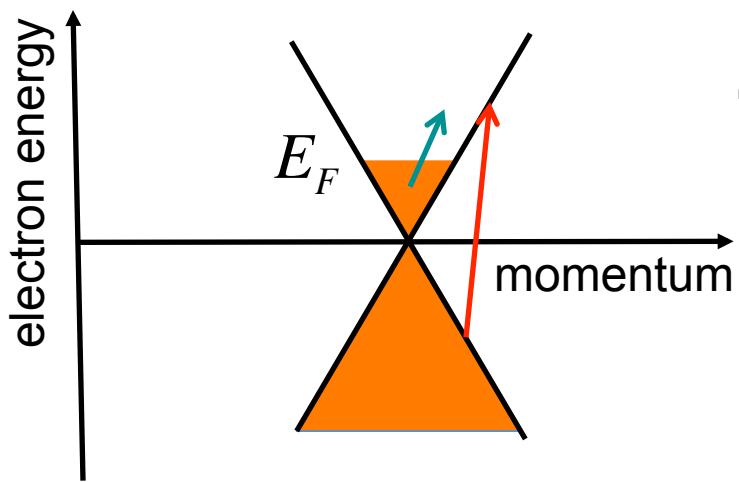
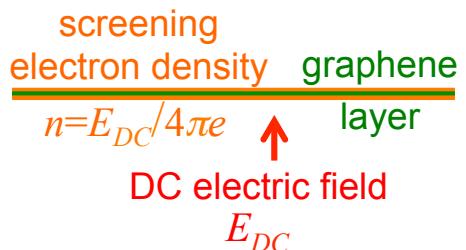
Electron state j
of energy ε_j



RPA response

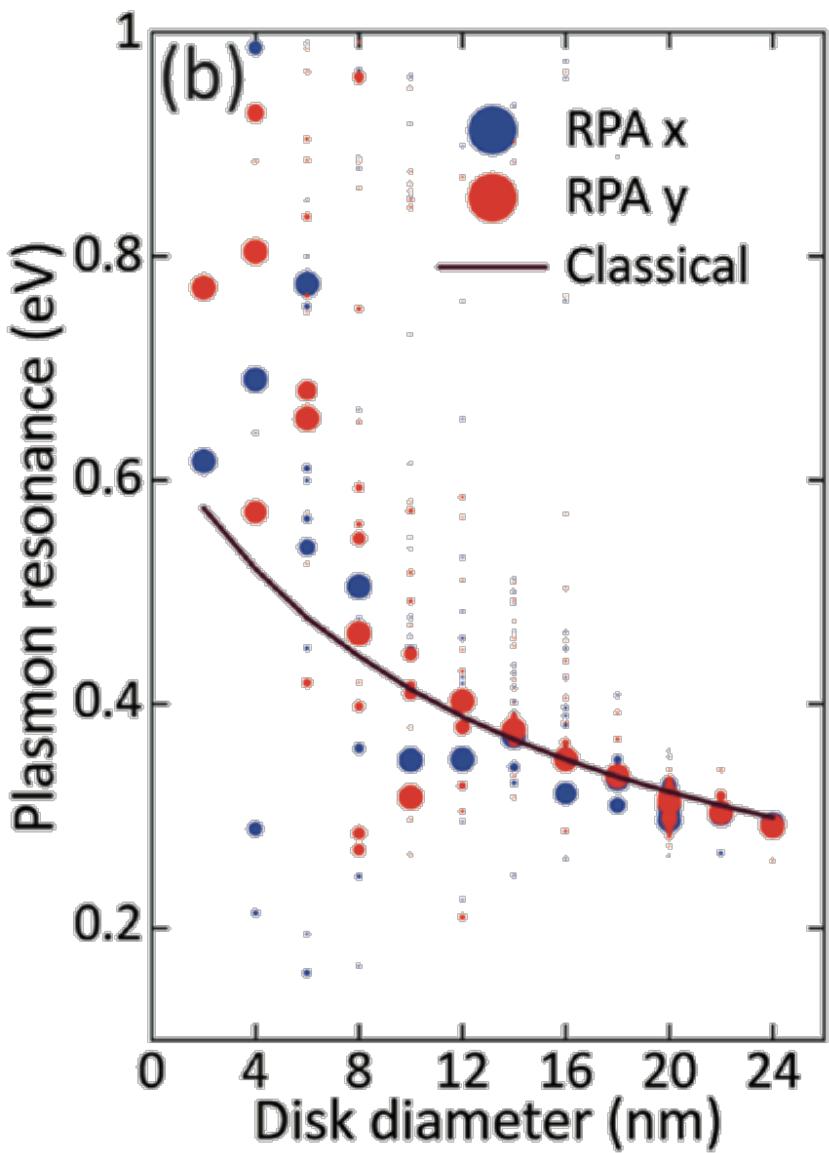
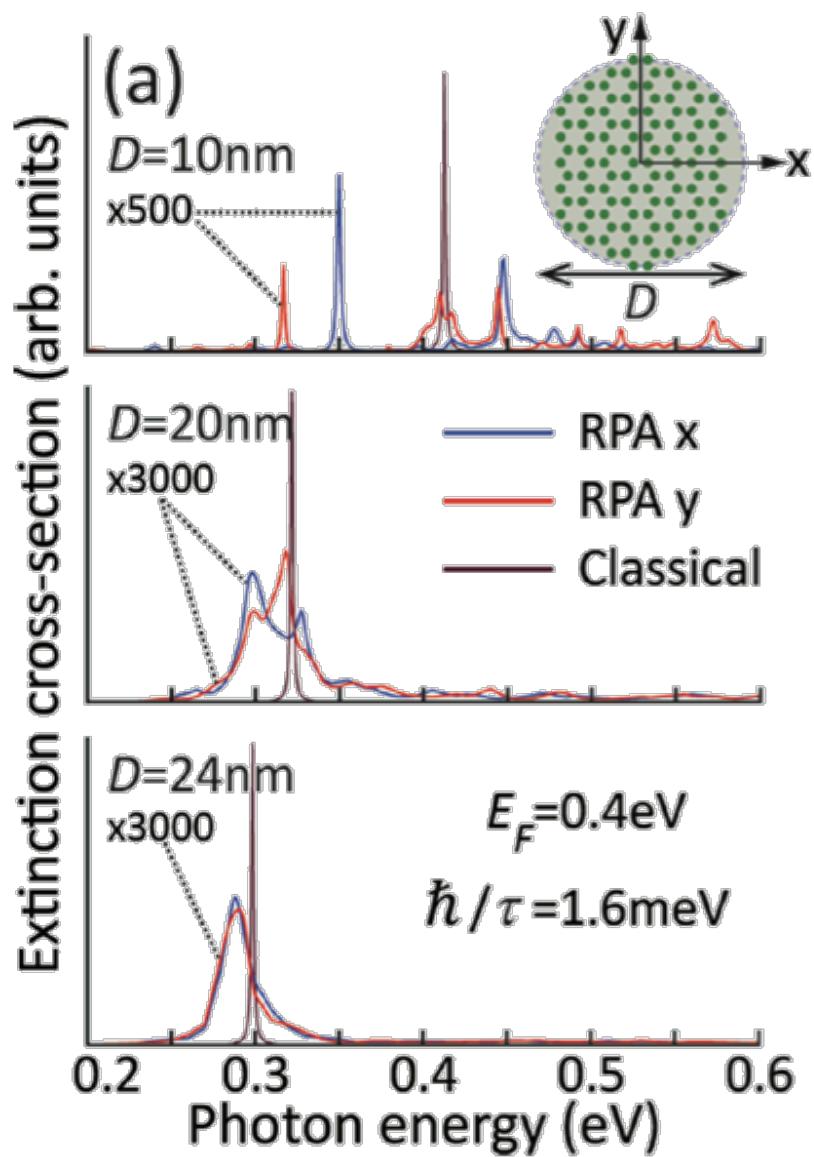
$$\chi_{II'}^0(\omega) = \frac{2e^2}{\hbar} \sum_{jj'} (f_{j'} - f_j) \frac{a_{jI} a_{j'I}^* a_{j'I'}^* a_{j'I''}}{\omega - (\varepsilon_j - \varepsilon_{j'}) + i/2\tau}$$

Electrostatic doping of graphene



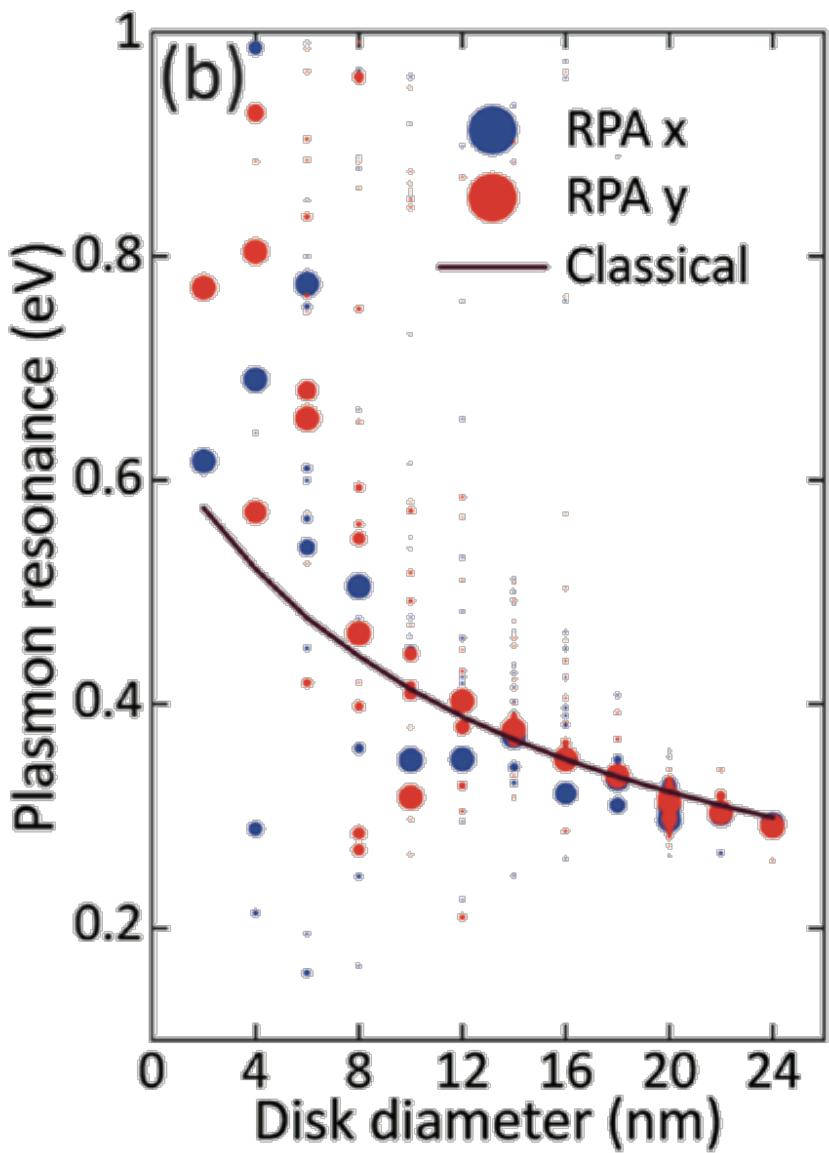
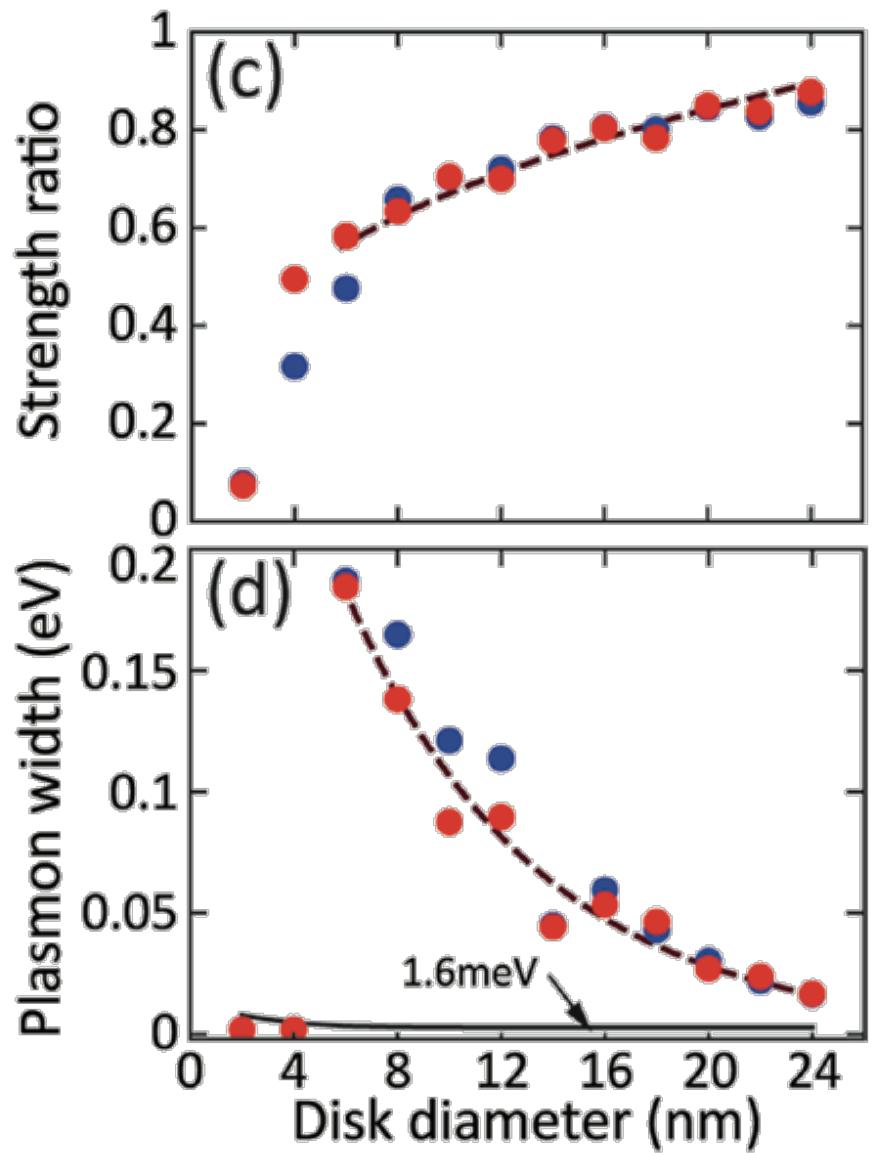
$$\lambda_{sp} = 2\alpha \frac{E_F}{\hbar\omega} \lambda_0$$

Quantum effects in graphene plasmons



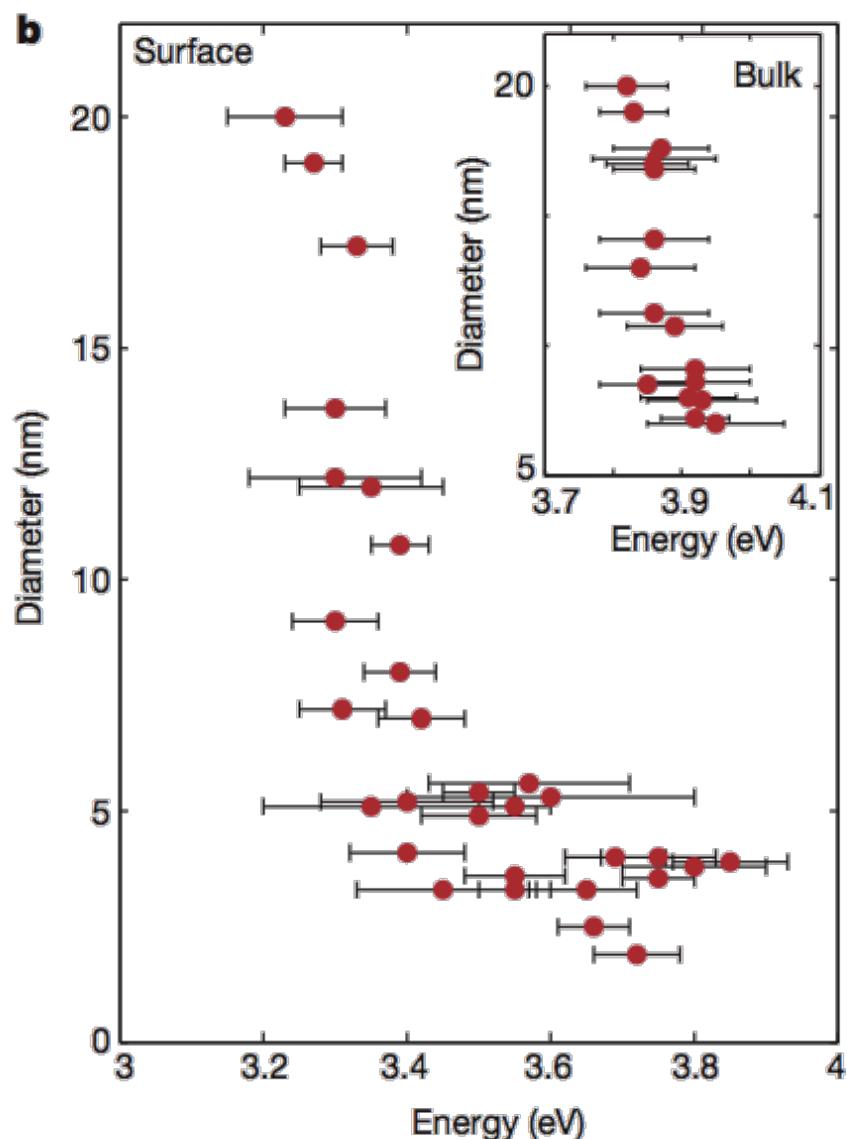
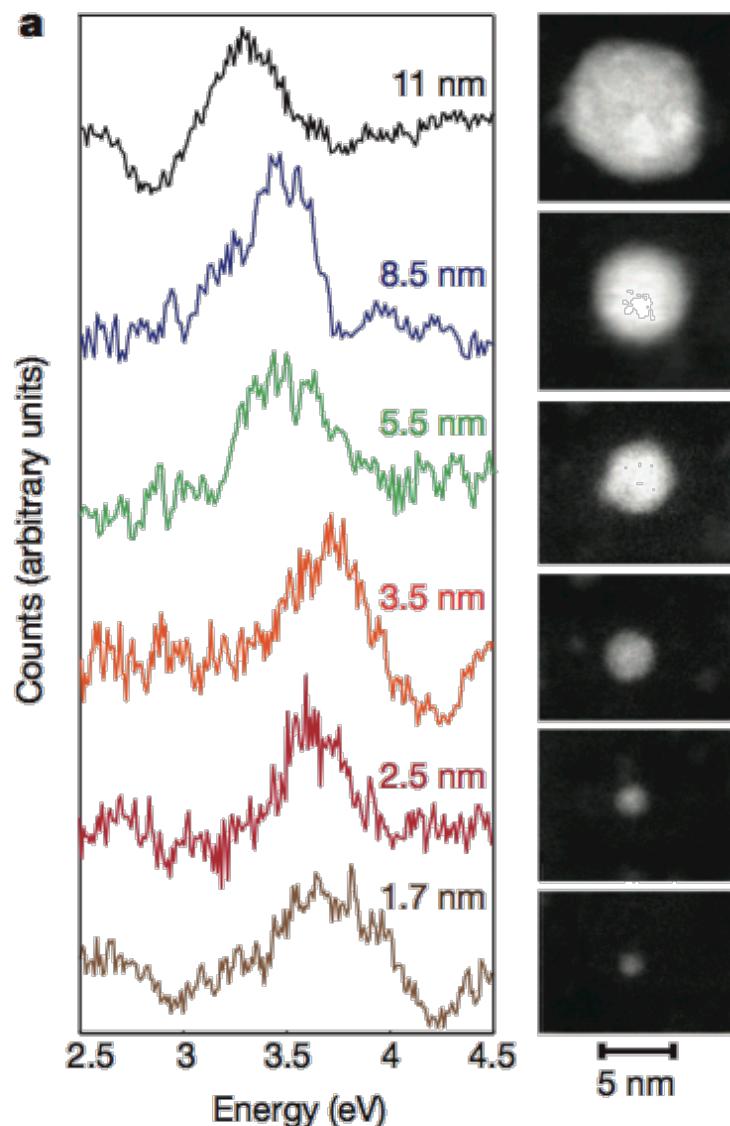
Thongrattanasiri *et al.*, ACS Nano (2012)

Quantum effects in graphene plasmons



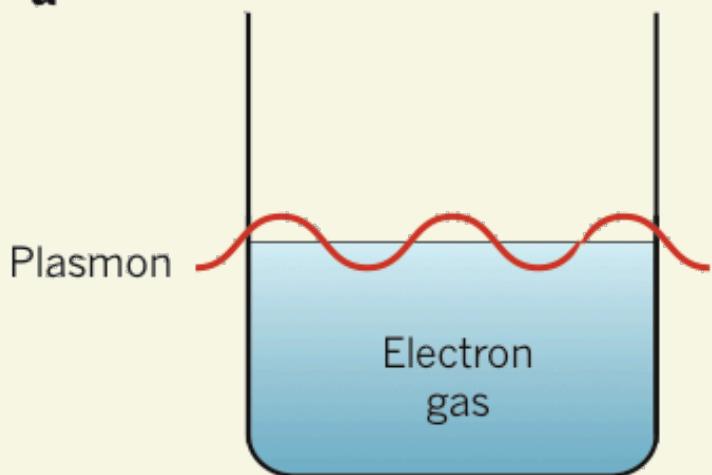
Thongrattanasiri *et al.*, ACS Nano (2012)

Quantum effects in silver nanoplasmons

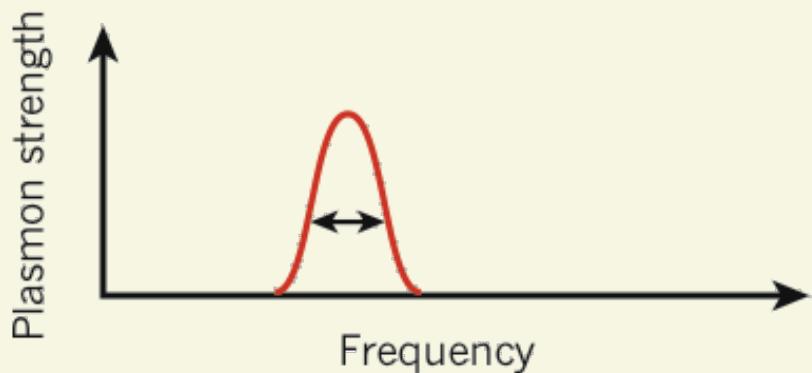
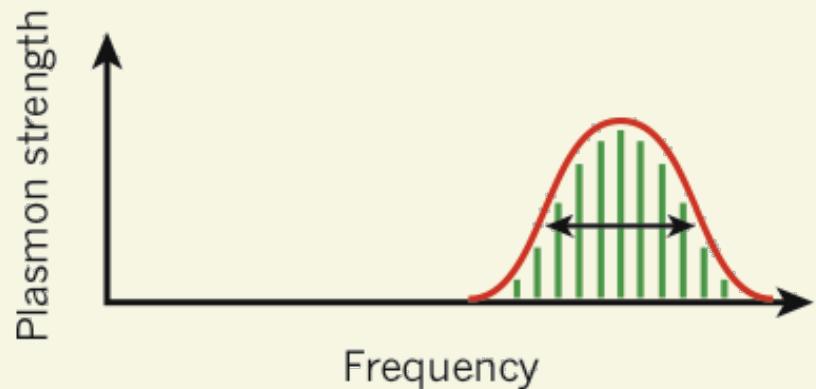
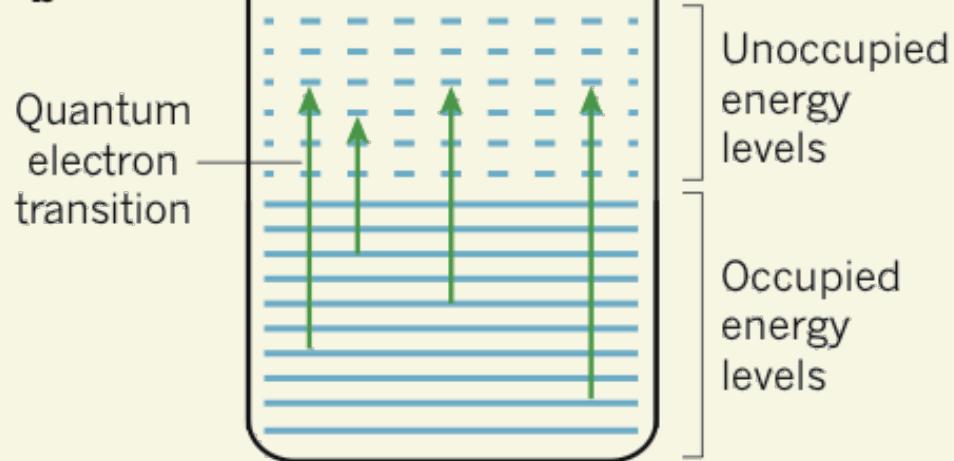


Scholl, Koh, and Dionne, Nature (2012)

Quantum-classical transition

a

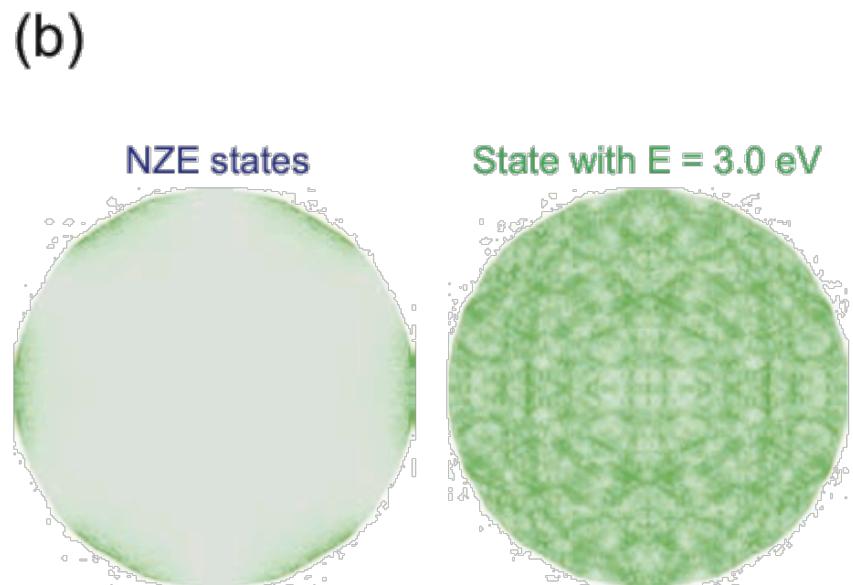
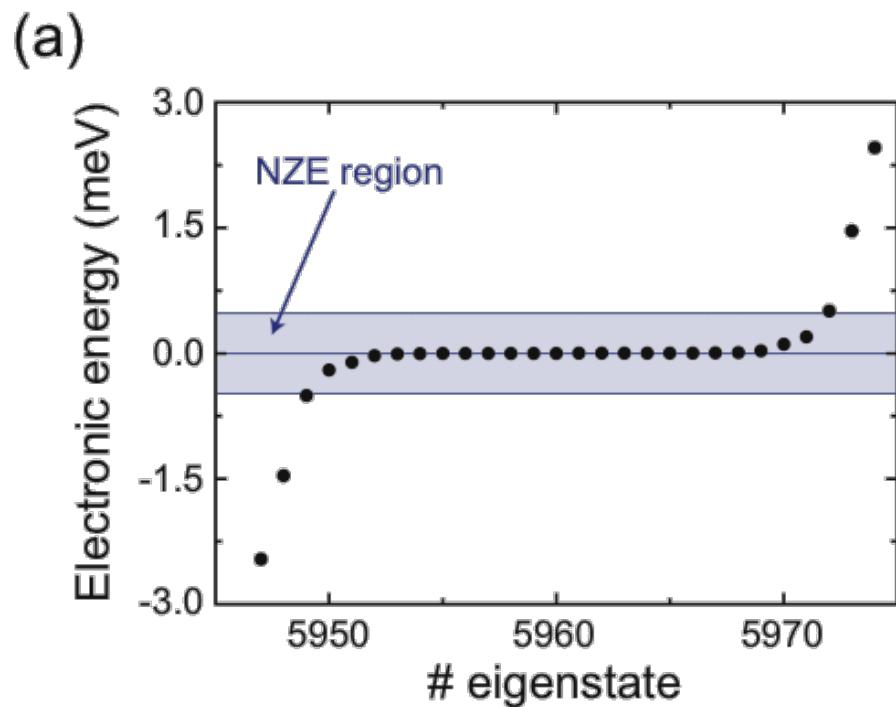
News and Views, Nature 483, 861 (2012)

**b**

Quantum effects in graphene plasmons

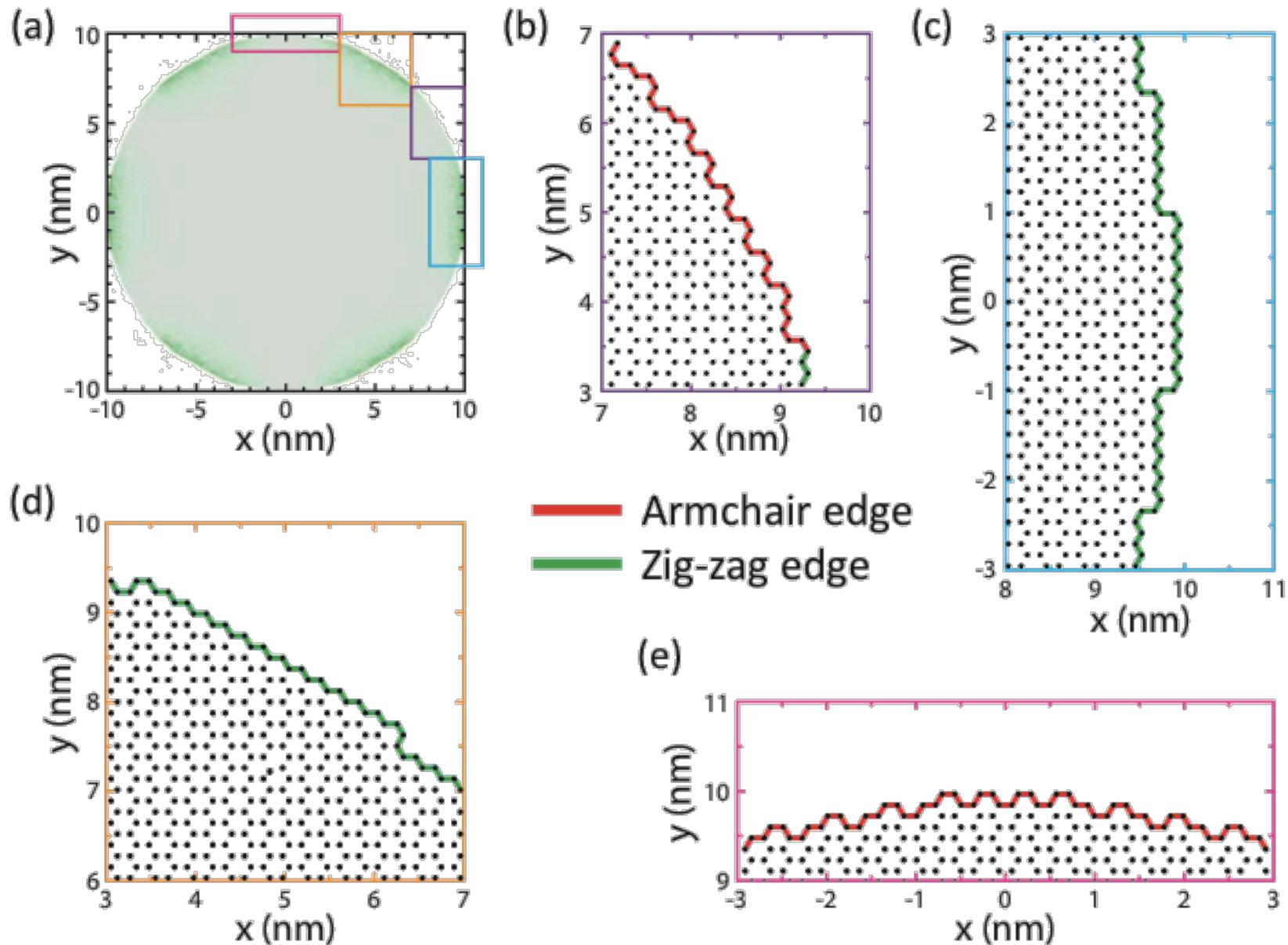
Electron state j
of energy ε_j

$$\sum_I |a_{jI}| I\rangle$$



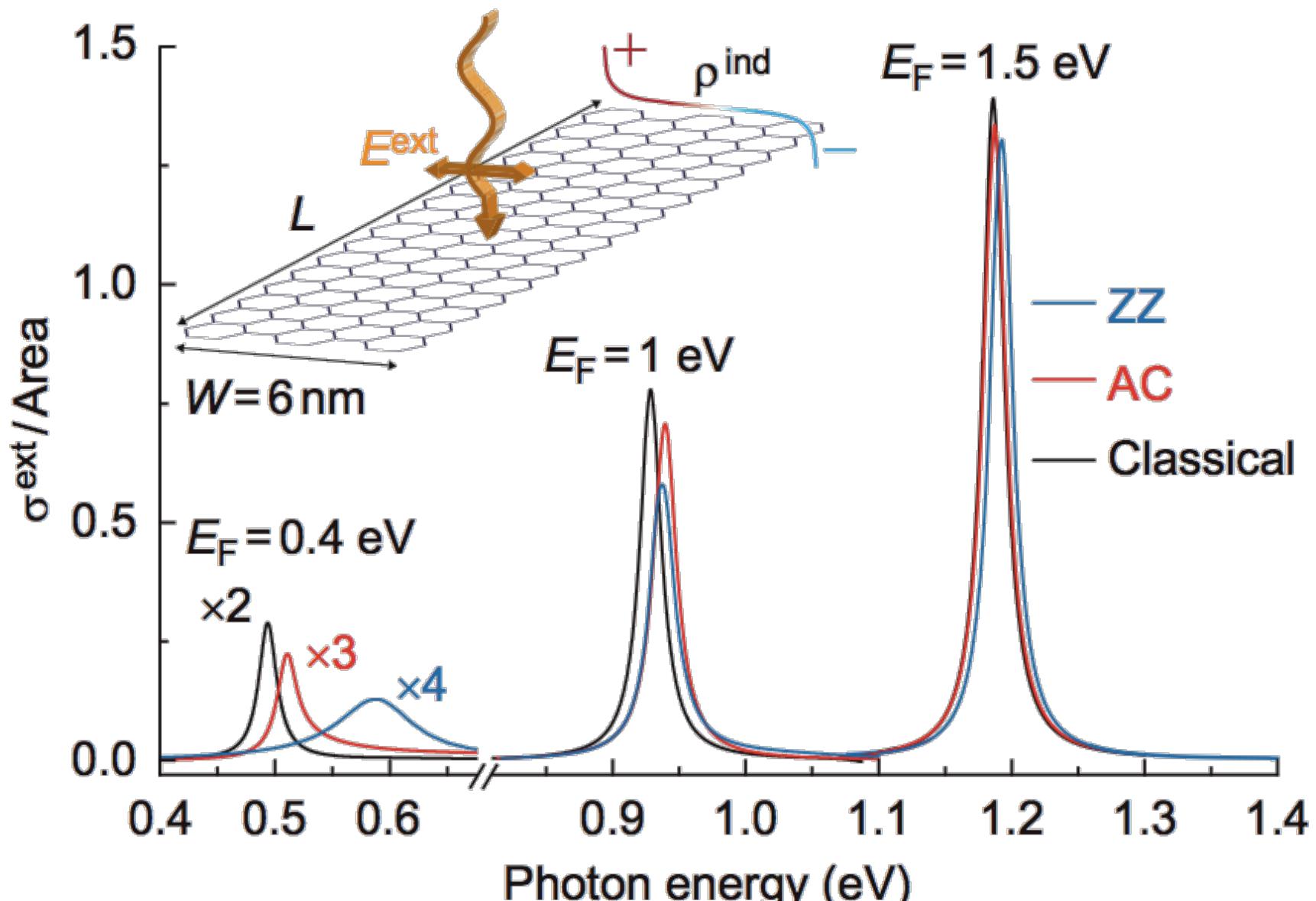
Thongrattanasiri *et al.*, ACS Nano (2012)

Quantum effects in graphene plasmons



Thongrattanasiri *et al.*, ACS Nano (2012)

Quantum description of graphene plasmons



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Electrostatic scaling law

$$\phi(\mathbf{R}, \omega) = \phi^{\text{ext}}(\mathbf{R}, \omega) + \int d\mathbf{R}' \frac{1}{|\mathbf{R} - \mathbf{R}'|} \rho^{\text{ind}}(\mathbf{R}', \omega)$$



Electrostatic scaling law

$$\phi(\mathbf{R}, \omega) = \phi^{\text{ext}}(\mathbf{R}, \omega) + \int d\mathbf{R}' \frac{1}{|\mathbf{R} - \mathbf{R}'|} \left[\frac{1}{i\omega} \nabla' \cdot \mathbf{j}^{\text{ind}}(\mathbf{R}', \omega) \right]$$

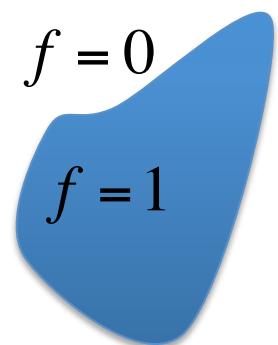


Electrostatic scaling law

$$\phi(\mathbf{R}, \omega) = \phi^{\text{ext}}(\mathbf{R}, \omega) + \int d\mathbf{R}' \frac{1}{|\mathbf{R} - \mathbf{R}'|} \left[\frac{1}{i\omega} \nabla' \cdot f(\mathbf{R}) \sigma(\omega) (-\nabla' \phi(\mathbf{R}', \omega)) \right]$$

$$f = 0$$

$$f = 1$$

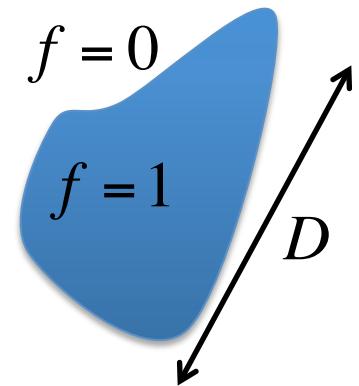


Electrostatic scaling law

$$\phi(\mathbf{R}, \omega) = \phi^{\text{ext}}(\mathbf{R}, \omega) + \eta \int d\mathbf{R}' \frac{1}{|\mathbf{R} - \mathbf{R}'|} \nabla' \cdot f(\mathbf{R}') \nabla' \phi(\mathbf{R}', \omega)$$

$$\eta = \frac{i\sigma(\omega)}{\omega D} = \frac{-\omega_0^2}{\omega(\omega + i\tau^{-1})} \quad \omega_0 = \frac{e}{\hbar} \sqrt{\frac{E_F}{\pi D}}$$

$$\omega_{pl} = \frac{\omega_0}{\sqrt{-\eta}} - i \frac{\tau^{-1}}{2}$$



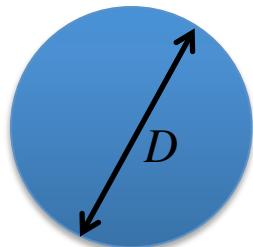
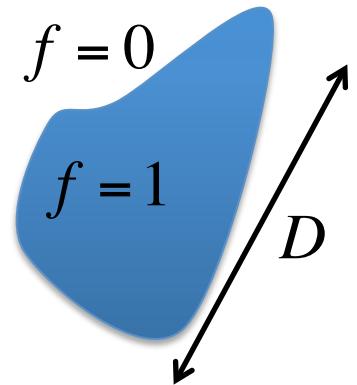
Electrostatic scaling law

$$\phi(\mathbf{R}, \omega) = \phi^{\text{ext}}(\mathbf{R}, \omega) + \eta \int d\mathbf{R}' \frac{1}{|\mathbf{R} - \mathbf{R}'|} \nabla' \cdot f(\mathbf{R}') \nabla' \phi(\mathbf{R}', \omega)$$

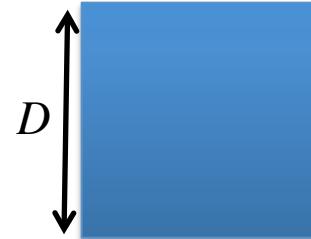
$$\eta = \frac{i\sigma(\omega)}{\omega D} = \frac{-\omega_0^2}{\omega(\omega + i\tau^{-1})}$$

$$\omega_0 = \frac{e}{\hbar} \sqrt{\frac{E_F}{\pi D}}$$

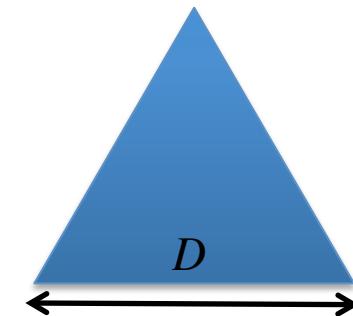
$$\omega_{pl} = \frac{\omega_0}{\sqrt{-\eta}} - i \frac{\tau^{-1}}{2}$$



$$\eta = -0.080$$



$$\eta = -0.053$$



$$\eta = -0.048$$

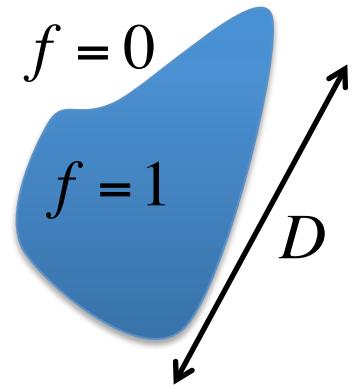
Electrostatic scaling law

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$$\omega_{pl} = \frac{\omega_0}{\sqrt{-\eta}} - i \frac{\tau^{-1}}{2}$$

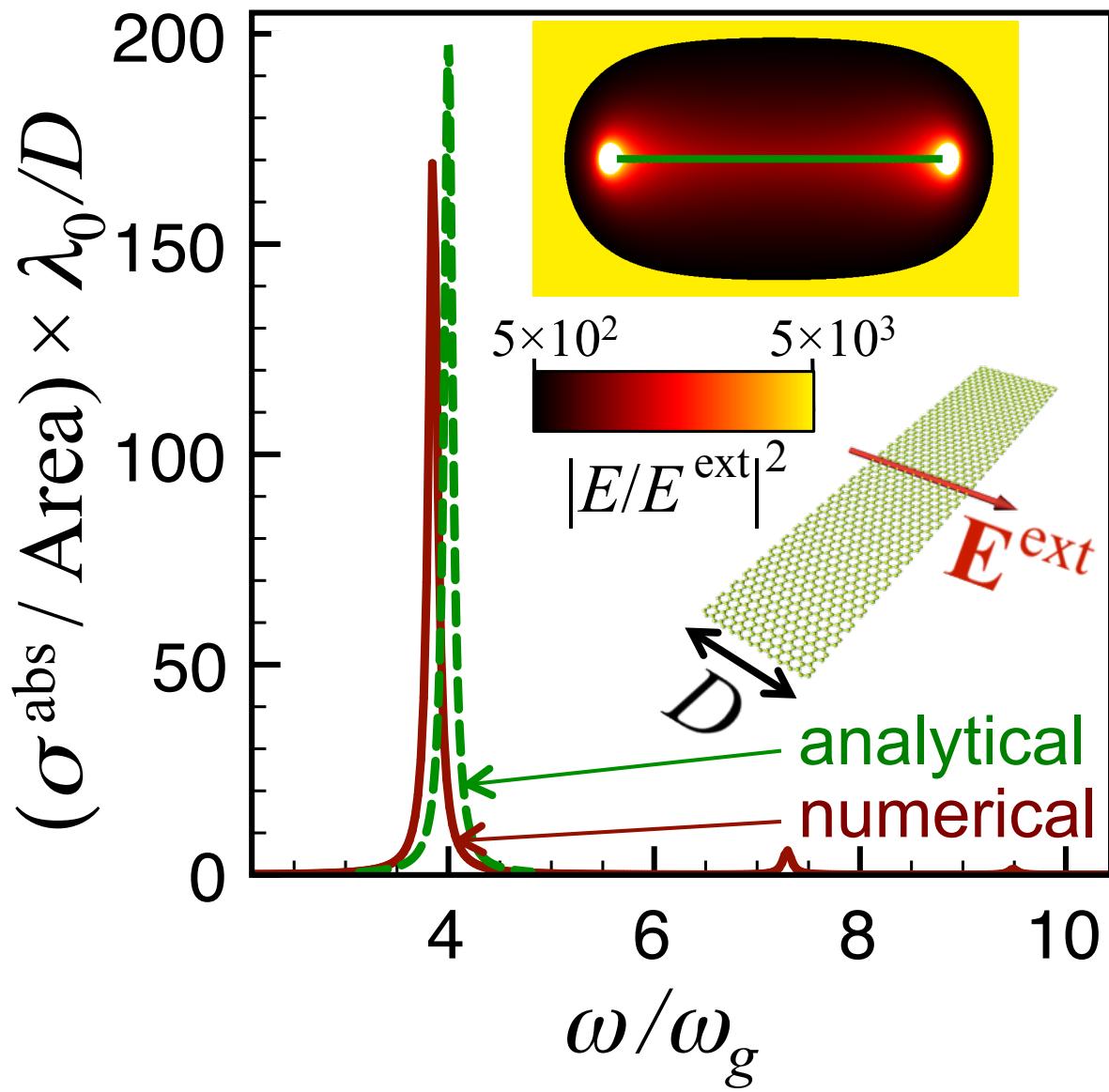


$$\alpha(\omega) = D^3 \sum_j \frac{A_j}{\frac{-2}{\eta_j} - \frac{i\omega D}{\sigma(\omega)}}$$

$$\sum_j A_j = \frac{\text{Area}}{D^2}$$

$$-\sum_j \eta_j A_j = \frac{1}{4\pi} \quad (\text{disk})$$

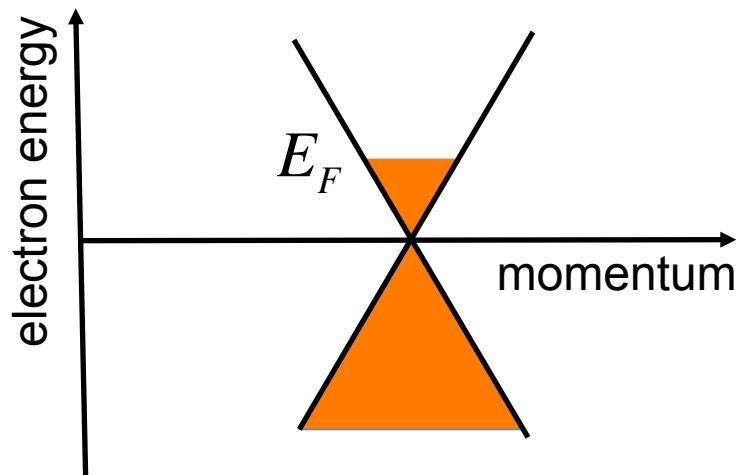
Electrostatic scaling law



$$\frac{\sigma^{\text{abs}}}{\text{Area}} = \frac{8\pi^2 D}{\lambda} \text{Im} \left\{ \frac{\omega_g^2}{16\omega_g^2 - \omega(\omega + i\gamma)} \right\}$$

$$\omega_g = \frac{e}{\hbar} \sqrt{\frac{E_F}{\pi D}}$$

Why graphene enables facile tunability



f-sum rule

$$\int_{\text{plasmon}} \omega d\omega \text{Im}\{\alpha(\omega)\} = \frac{\pi e^2}{2m_e} N_e$$

$$N_e \sim \sqrt{N_{\text{doping}} N_{\text{C atoms}}}$$

Plasmonics: An overview and some new trends

Introduction to plasmons

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Quantum-mechanical description

Classical description

Complete optical absorption

Quantum optics with graphene plasmons

Sensing with graphene plasmons

Plasmons in other atomically thin materials

Short historical overview of perfect absorption

Partially disordered silver films

- O. Hunderi and H. P. Myers, J. Phys. F: Metal Phys. 3, 683 (1973)

Diffraction in gratings, double-period metal gratings, and metamaterials

- M. C. Hutley and D. Maystre, Optics Communications 19, 431 (1976)
- D. Maystre and R. Petit, Optics Communications 17, 196 (1976)
- W.-C. Tan, J. R. Sambles, and T. W. Preist, Phys. Rev. B 61, 13177 (1999)
- E. Popov and L. Tsonev, Surface Science Letters 271, L378 (1992)
- N. I. Landy et al., Phys. Rev. Lett. 100, 207402 (2008)
- N. Liu et al., Nano Lett. 10, 2342 (2010)

Doped silicon lamellar grating

- F. Marquier, M. Laroche, R. Carminati, J.-J. Greffet, Journal of Heat Transfer 129, 11 (2007)
- J.-J. Greffet, R. Carminati, K. Joulain, J.-P. Mulet, S. Mainguy, Y. Chen, Nature 416, 61 (2002)

Semiconductor and metal-semiconductor-metal nanostructures

- S. Collin, F. Pardo, R. Teissier, and J.-L. Pelouard, Appl. Phys. Lett. 85, 194 (2004)
- T.V. Teperik, F.J. García de Abajo, V.V. Popov, and M.S. Shur, Appl. Phys. Lett. 90 251910 (2007)

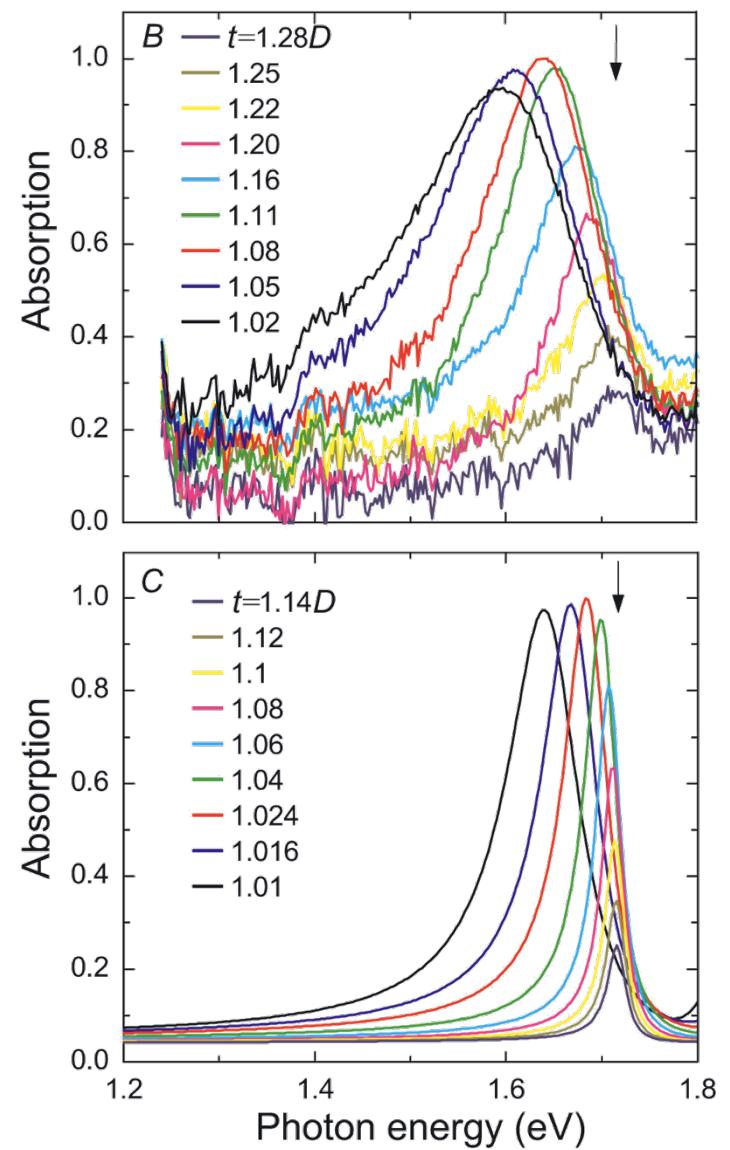
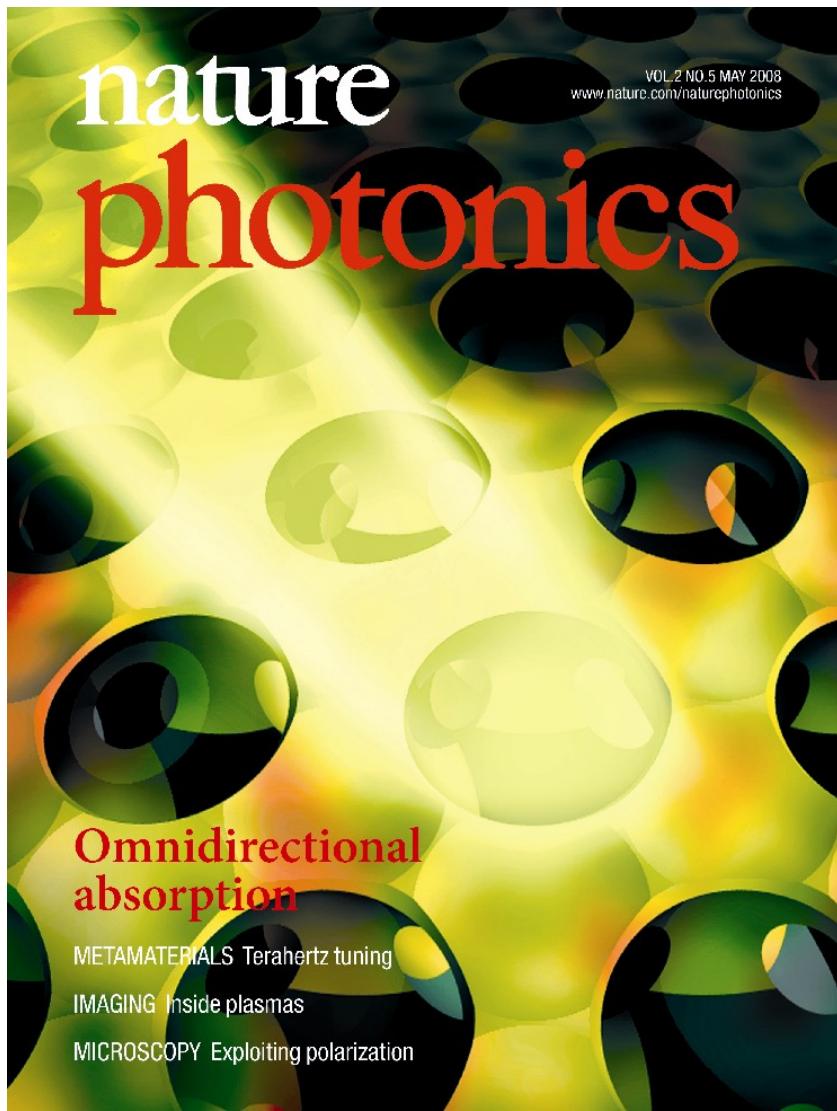
Multiplayer of metallic nanoparticles and nanopores in metal

- T. V. Teperik, V. V. Popov, and F. J. García de Abajo, Phys. Rev. B 71, 085408 (2005)
- T. Teperik, V. Popov, and F. García de Abajo, J. Opt. A: Pure Appl. Opt. 0, 0 (2007)
- S. Kachan, O. Stenzel, and A. Ponyavina, Appl. Phys. B 84, 281 (2006)

Overdense plasma slab (in the microwave frequency range)

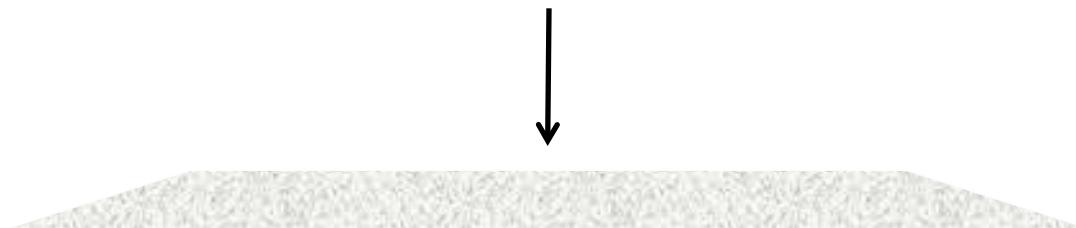
- Y. P. Bliokh, J. Felsteiner, and Y. Z. Slutsker, Phys. Rev. Lett. 95, 165003 (2005)

Nanovoids as perfect absorbers

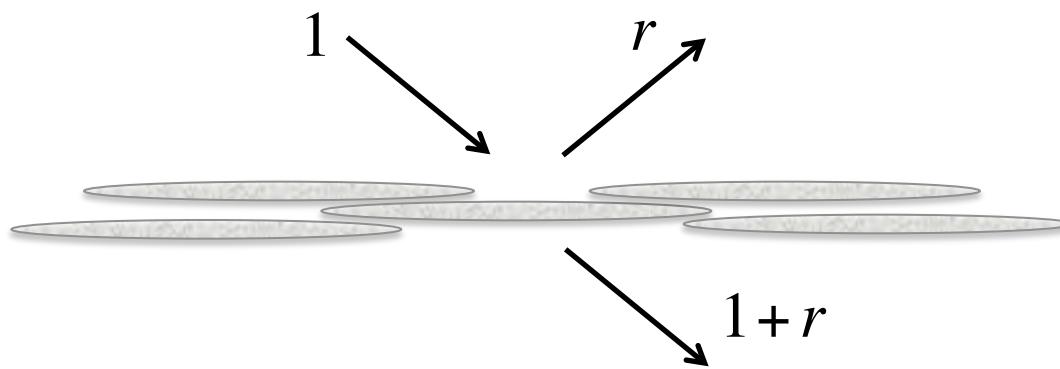


T.V.Teperik *et al.*, *Nature Photon.* (2008)

Light absorption in graphene

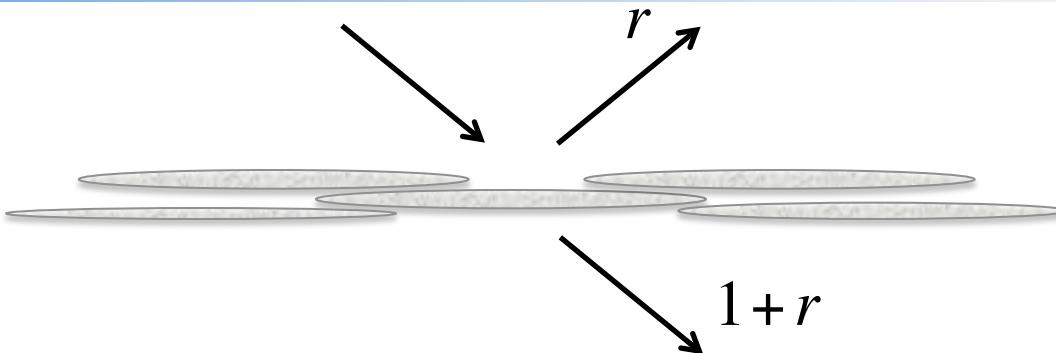


$$\text{Absorption} \approx \pi/137 \approx 2.3\%$$



$$\text{Absorption} = 1 - |r|^2 - |1+r|^2 \rightarrow 50\% \text{ maximum}$$

Maximum absorption in graphene



$$\text{Absorption} = 1 - |r|^2 - |1+r|^2 \quad \rightarrow \quad 50\% \text{ maximum for } r = -1/2$$

$$r = \frac{\pm iS}{\alpha^{-1} - G}$$

$$S = \frac{2\pi\omega}{Ac} (\cos\theta)^{\mp 1}$$

$$G \approx \frac{g}{a^3} + i \left(S - \frac{2\omega^3}{3c^3} \right)$$

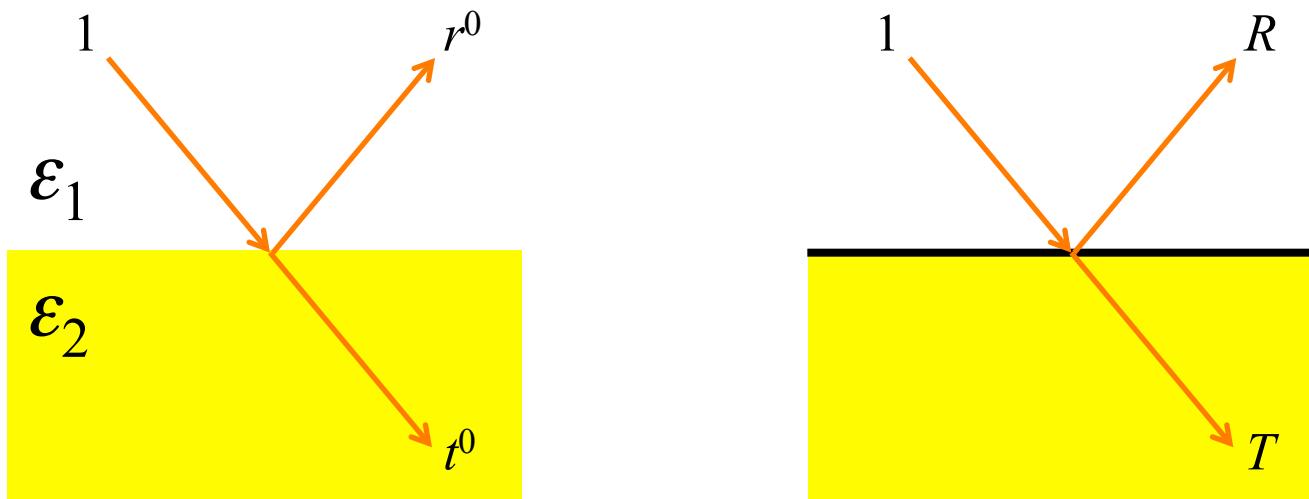
$$\alpha(\omega) = \frac{3c^3}{4\omega^3} \frac{\kappa_r}{\omega_p - \omega - i\kappa/2}$$

$$\omega \approx \omega_p - 3g\kappa_r/4(\omega a/c)^3$$

$$\sigma_{\max}^{\text{ext}} = 2A \times \begin{cases} \cos\theta, & s \text{ polarization}, \\ \cos^{-1}\theta, & p \text{ polarization}. \end{cases}$$

Thongrattanasiri *et al.*, Phys. Rev. Lett. (2012)

Absorption in asymmetric environments

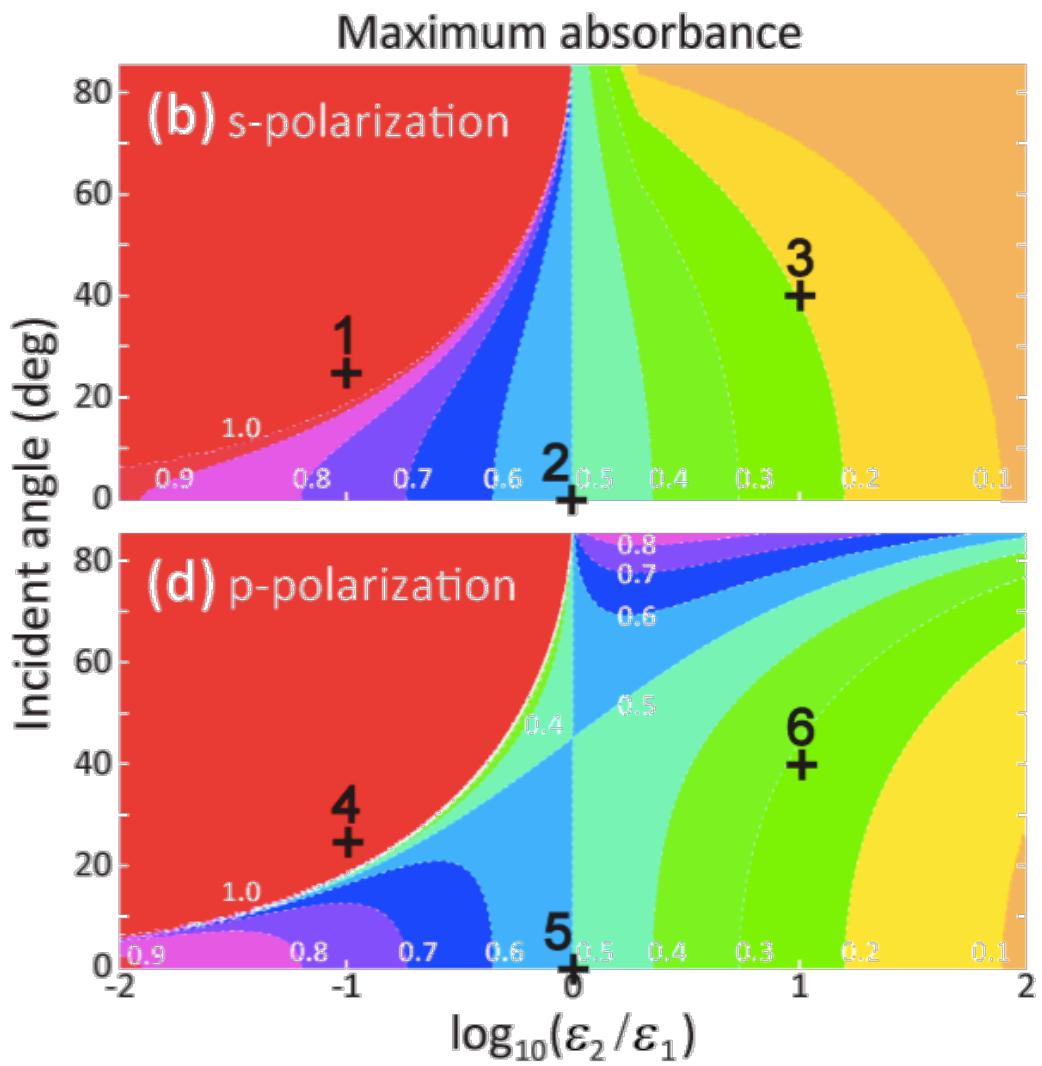


$$\eta = -\frac{r^0 \pm |r^0|^2 \pm \text{Re}\{f\}|t^0|^2}{|1 \pm r^0|^2 + \text{Re}\{f\}|t^0|^2}$$

$$\mathcal{A} = 1 - |r^0 + (1 \pm r^0)\eta|^2 - \text{Re}\{f\}|t^0|^2|1 \pm \eta|^2$$

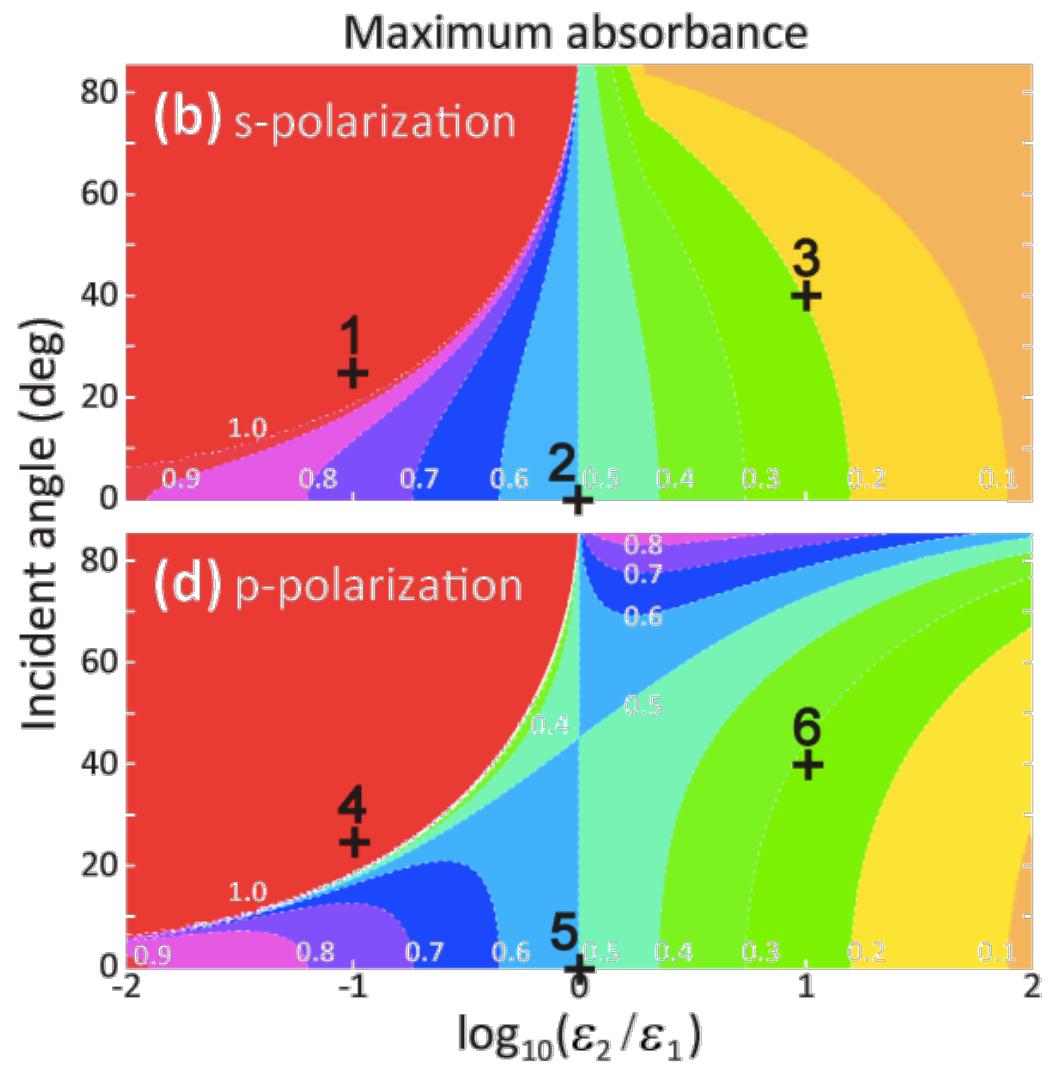
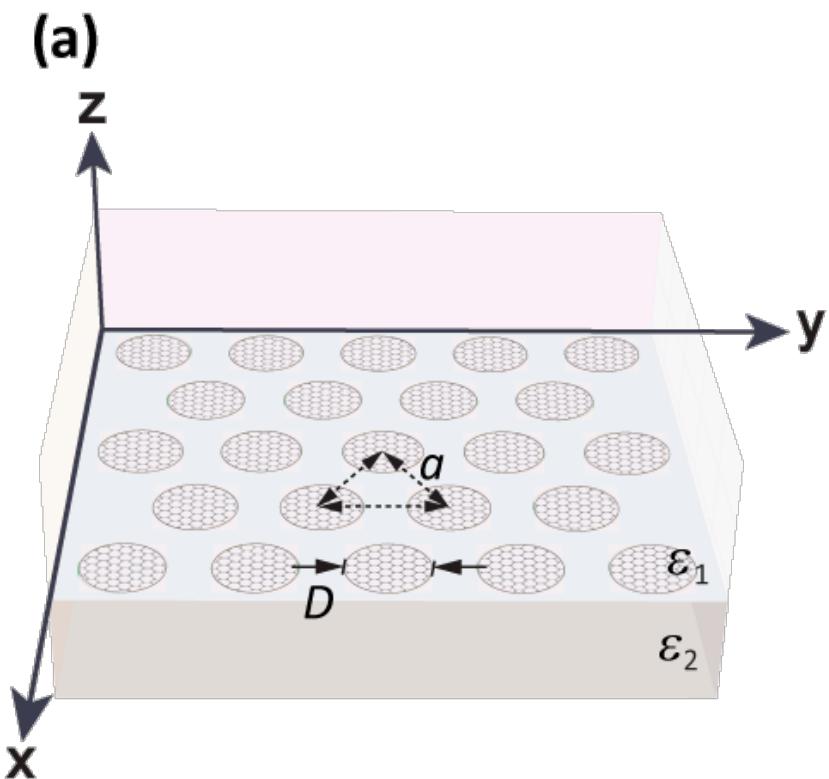
$$f = (\epsilon_2/\epsilon_1 - \sin^2 \theta)^{1/2} / \cos \theta$$

Absorption in asymmetric environments



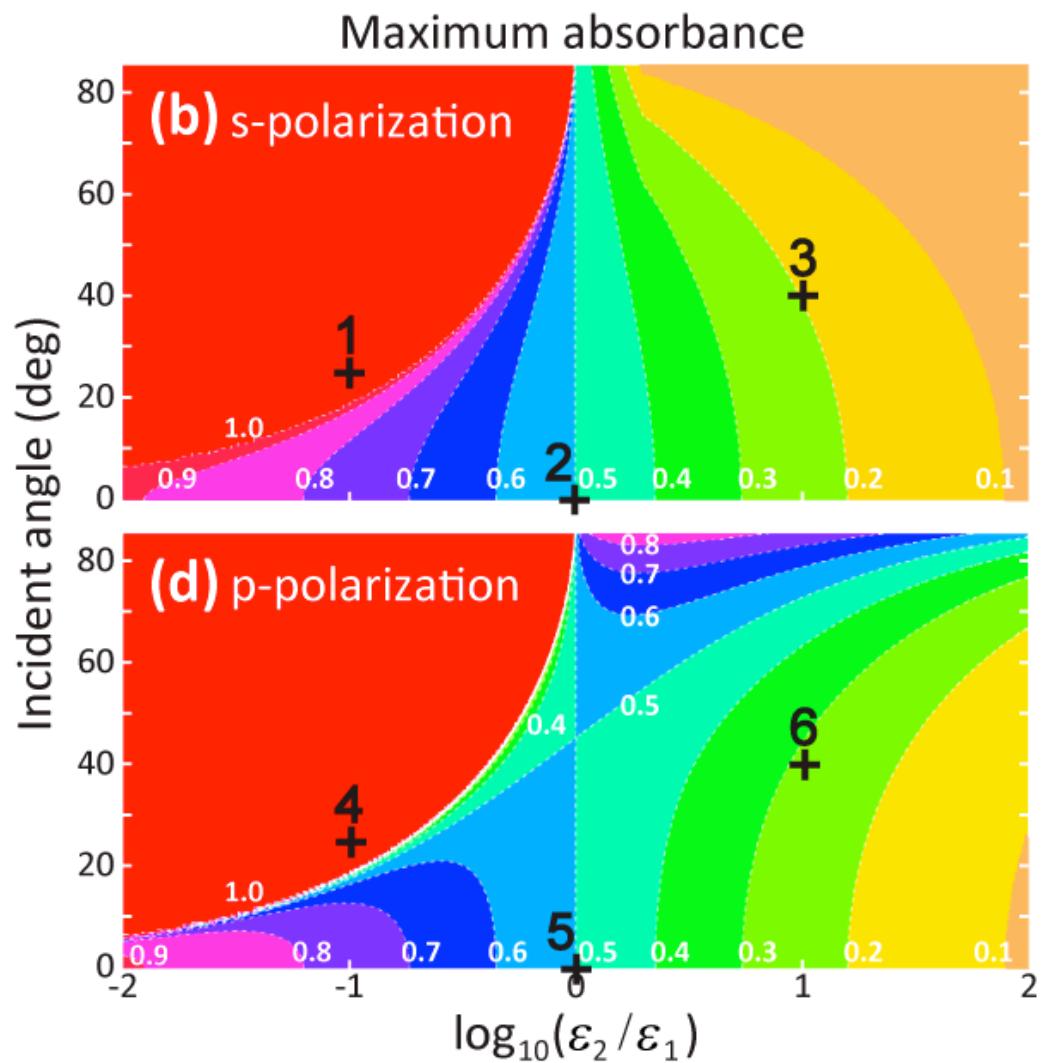
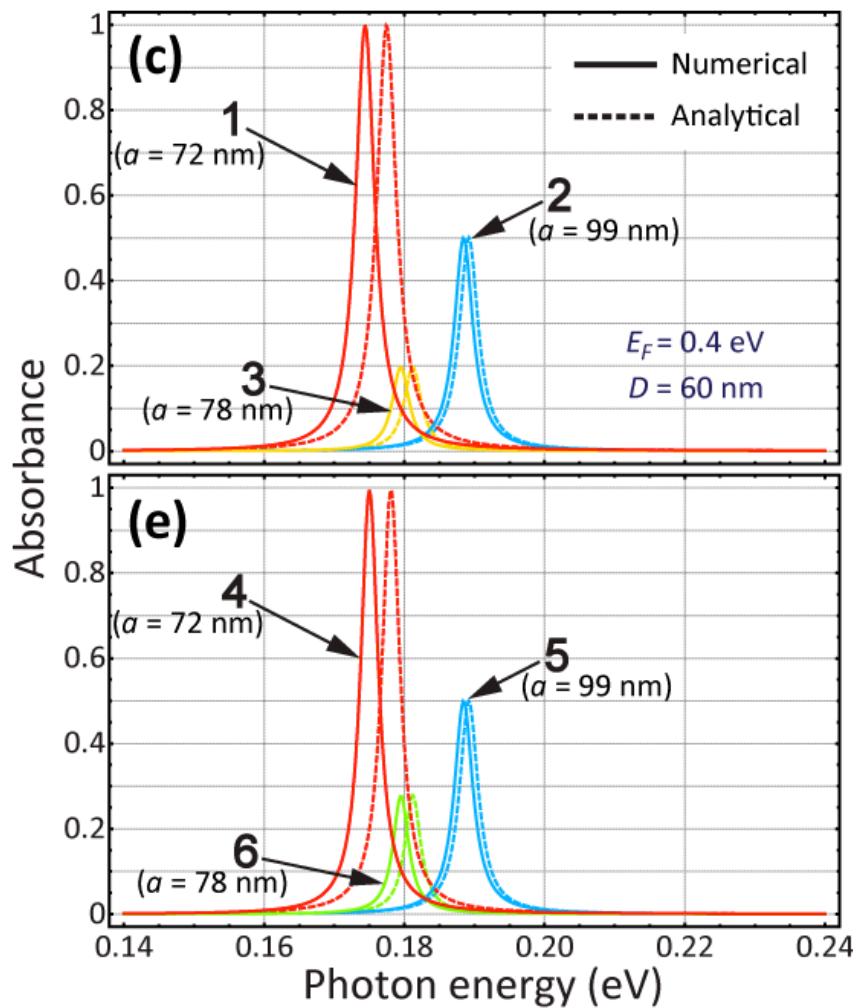
Thongrattanasiri *et al.*, Phys. Rev. Lett. (2012)

Absorption in asymmetric environments



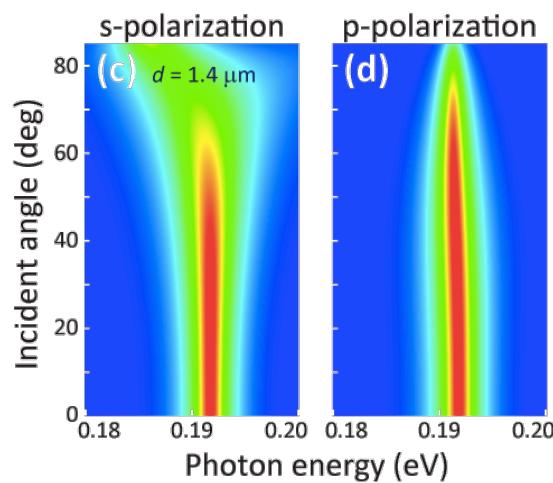
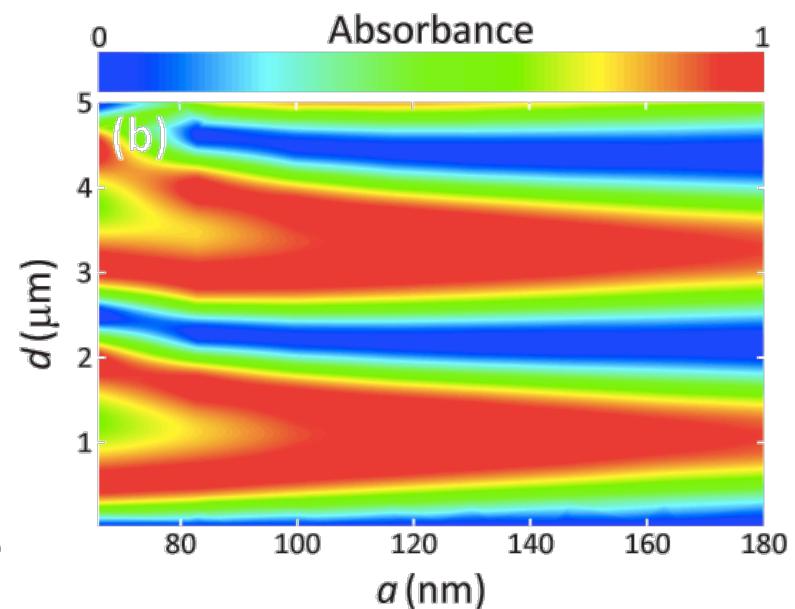
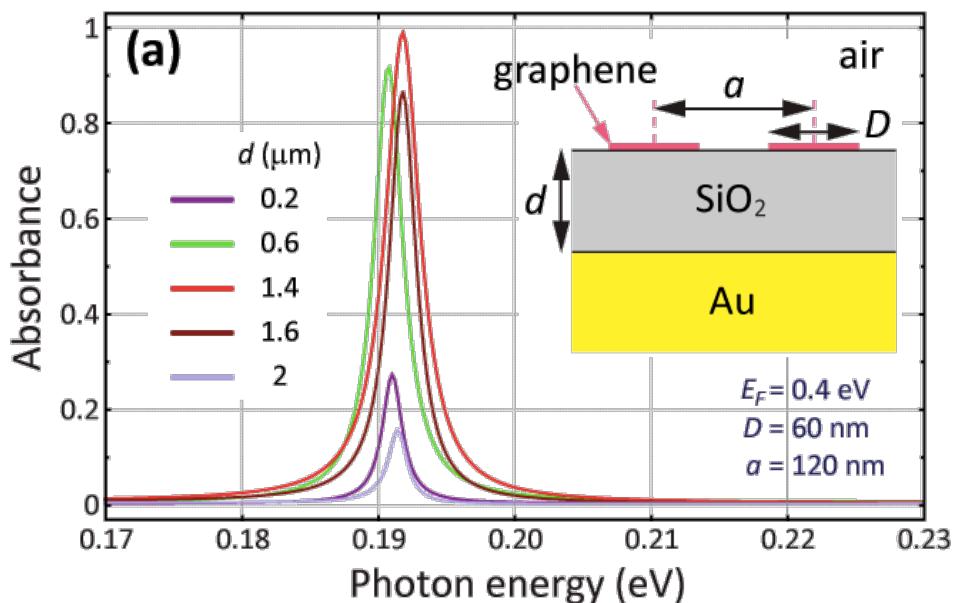
Thongrattanasiri *et al.*, Phys. Rev. Lett. (2012)

Absorption in asymmetric environments

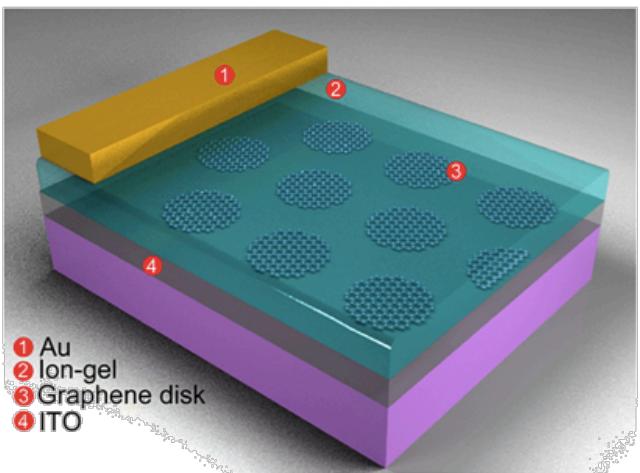


Thongrattanasiri *et al.*, Phys. Rev. Lett. (2012)

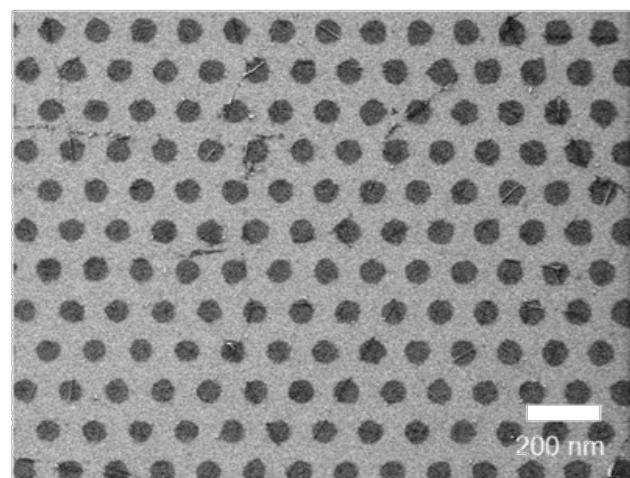
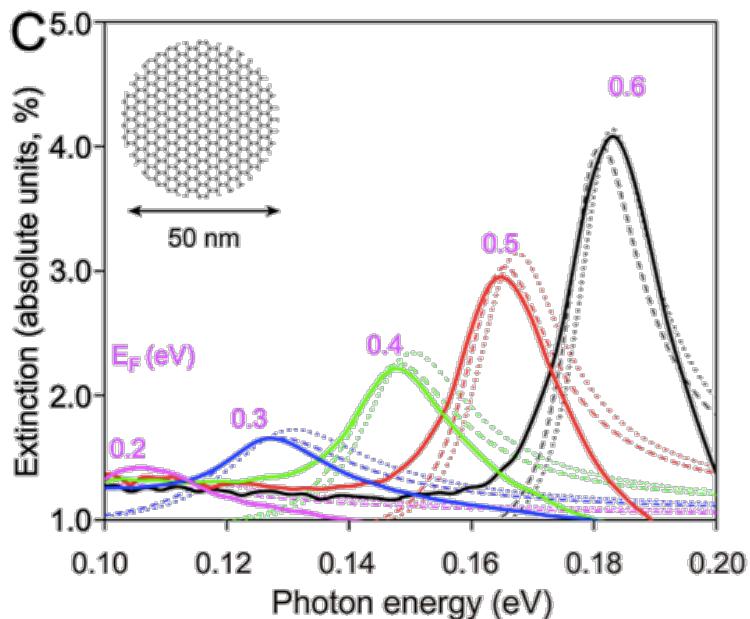
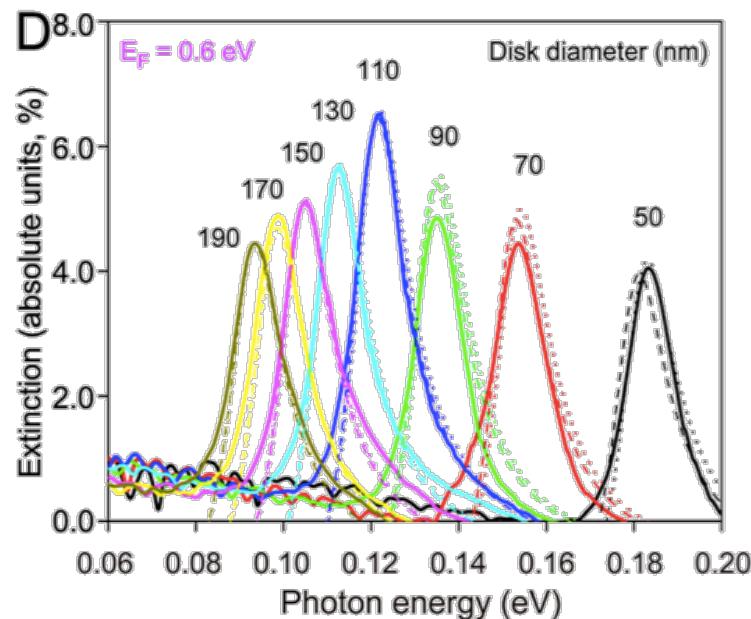
Complete absorption in graphene



Plasmon tuning

A

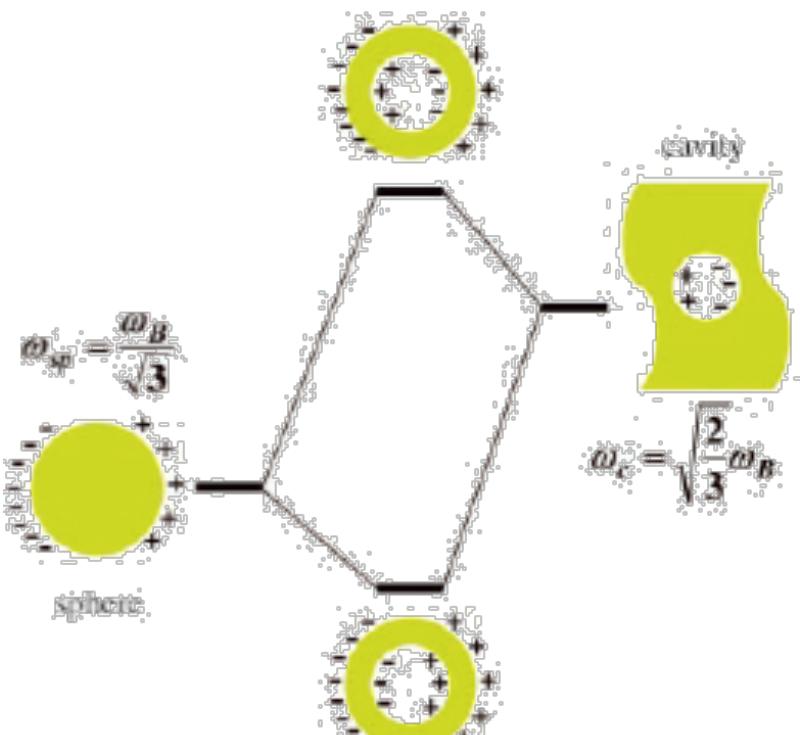
- ① Au
- ② Ion-gel
- ③ Graphene disk
- ④ ITO

B**C****D**

Fang et al., ACS Nano (2013)

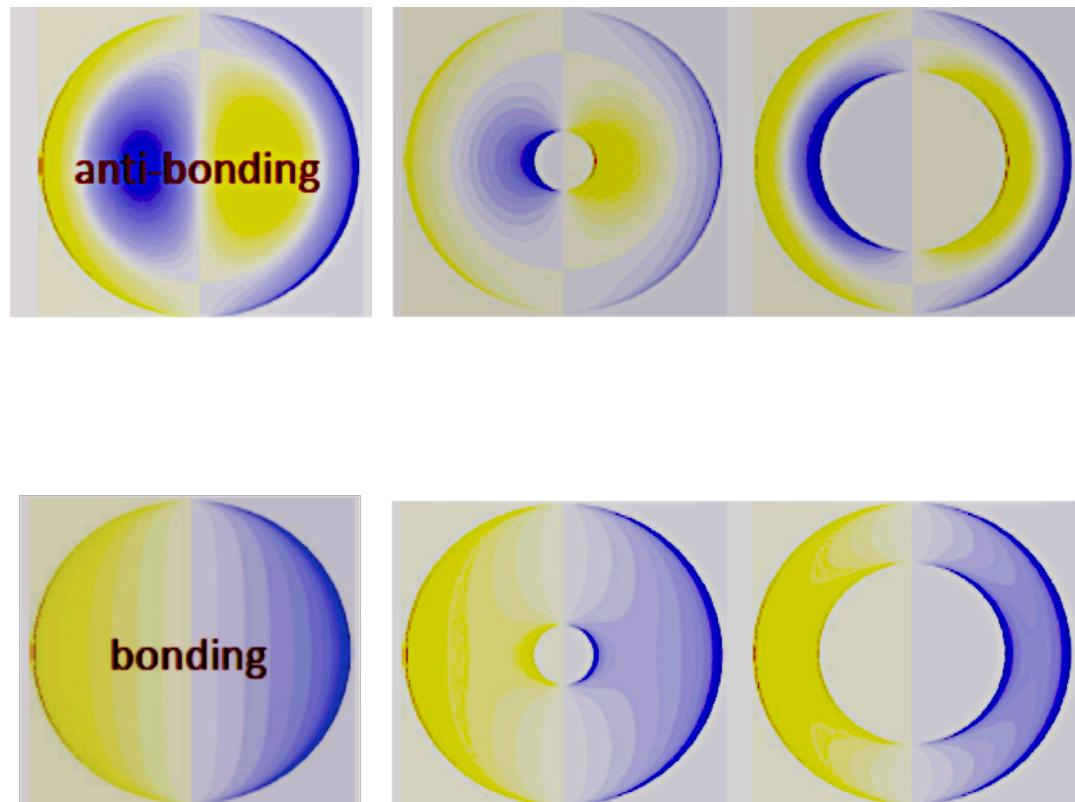
Graphene plasmon hybridization

Anti-bonding mode



Bonding mode

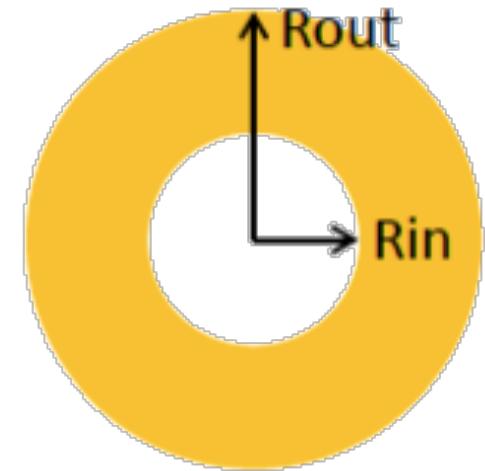
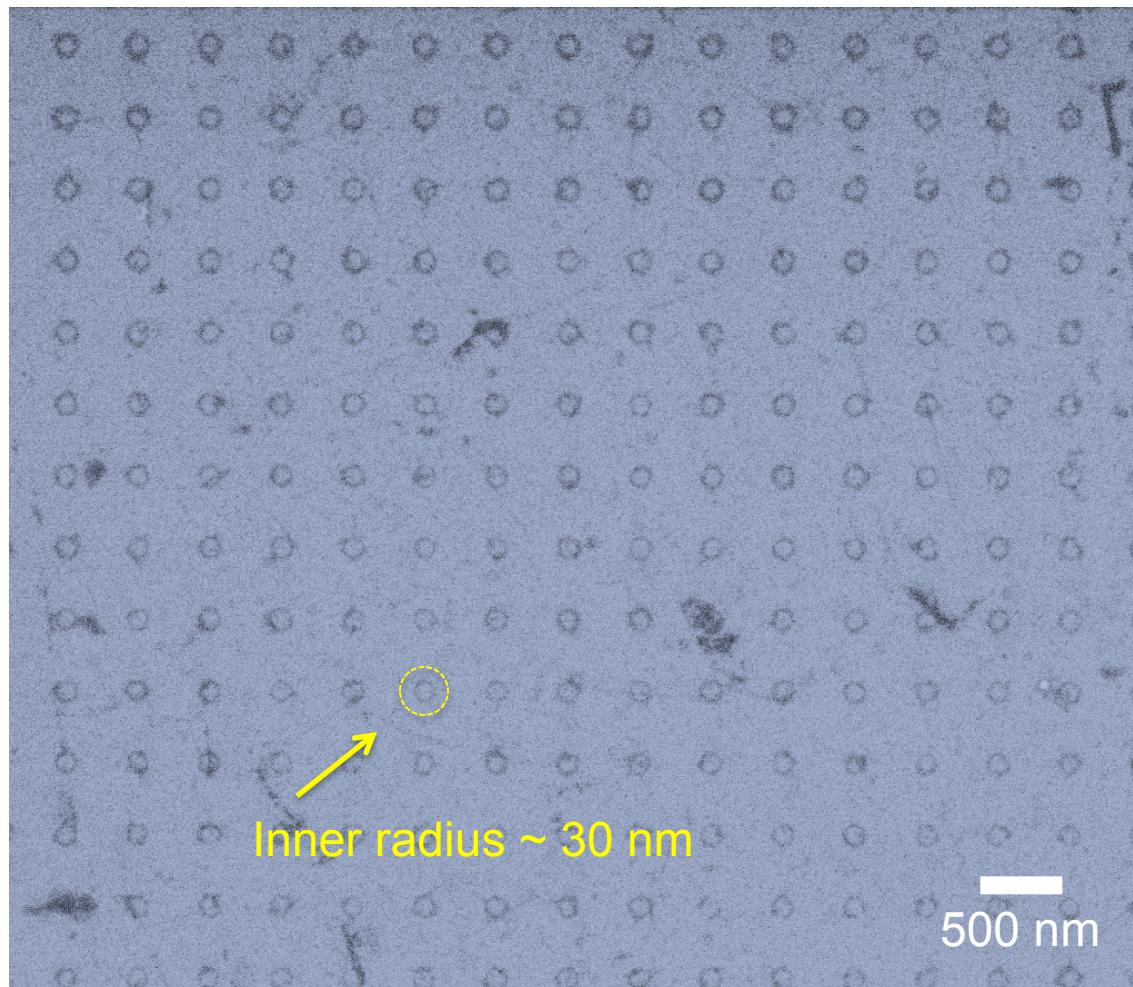
Graphene nanorings



Prodan *et al.*, Science (2003)

Fang, Thongrattanasiri, ..., Ayajan, Nordlander, Halas, JGA, ACS Nano (2013)

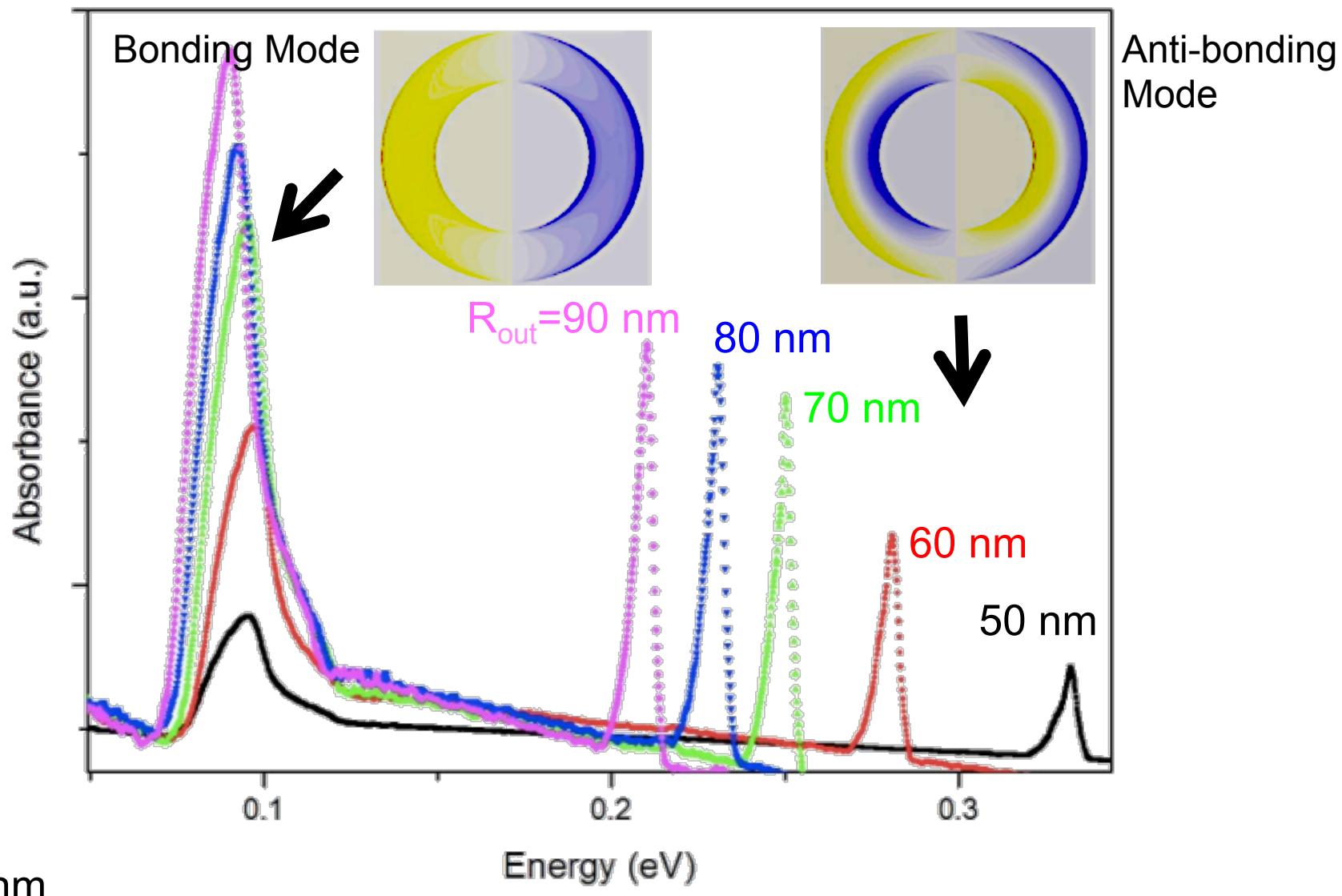
Graphene plasmon hybridization



$$R_{out} = 50 \text{ nm}$$
$$R_{in} = 30 \text{ nm}$$

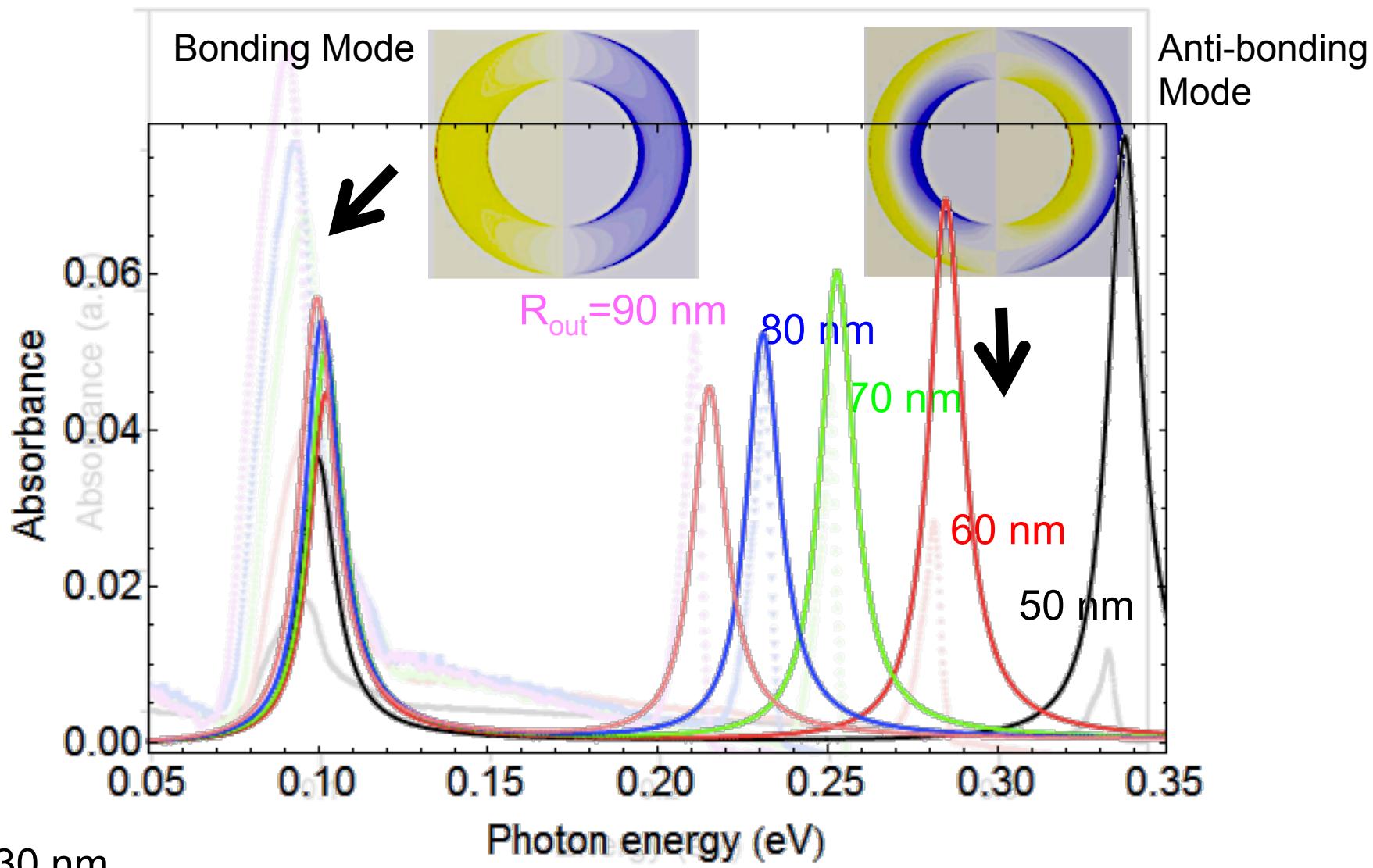
Period=500 nm

Graphene plasmon hybridization



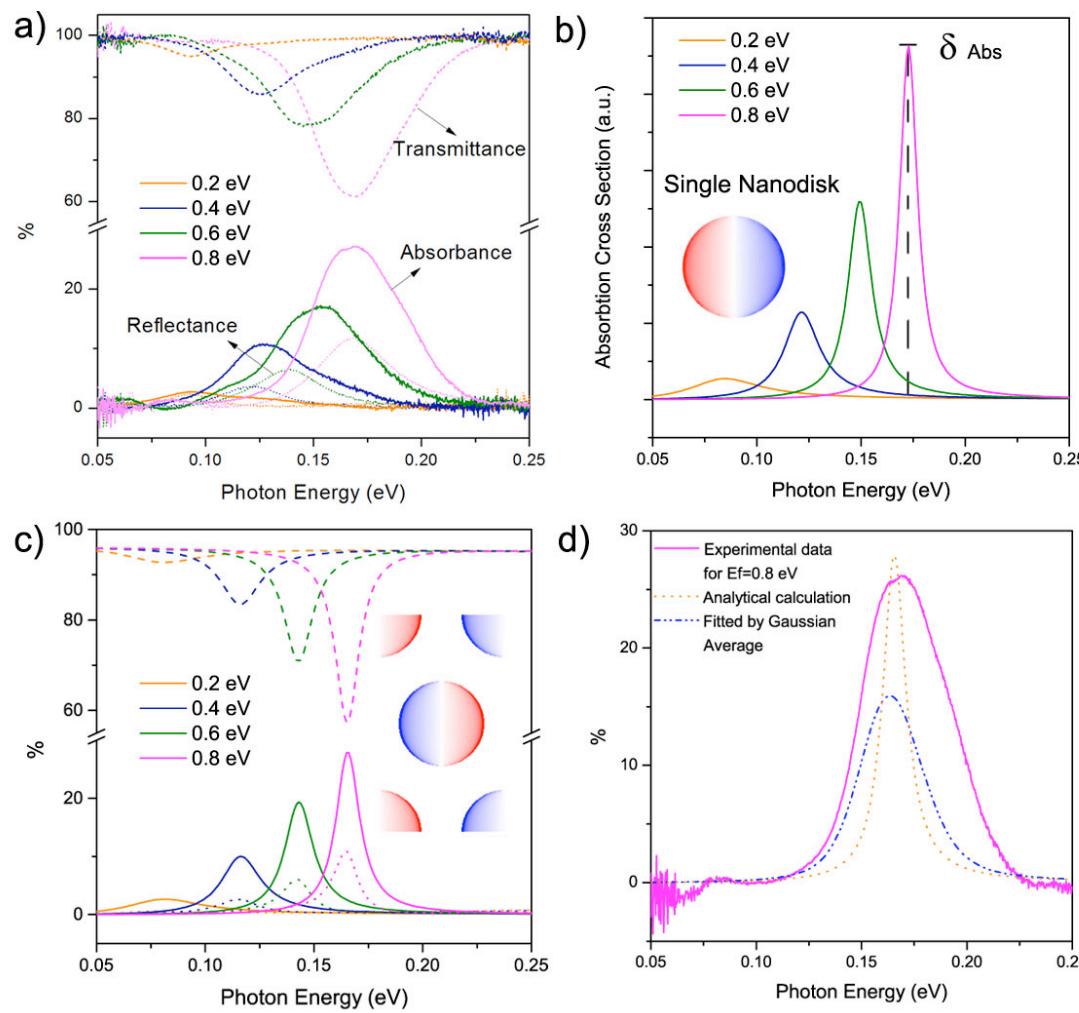
Fang, Thongrattanasiri, ..., Ayajan, Nordlander, Halas, JGA, ACS Nano (2013)

Graphene plasmon hybridization



Fang, Thongrattanasiri, ..., Ayajan, Nordlander, Halas, JGA, ACS Nano (2013)

Towards complete absorption in graphene



Plasmonics: An overview and some new trends

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Complete optical absorption

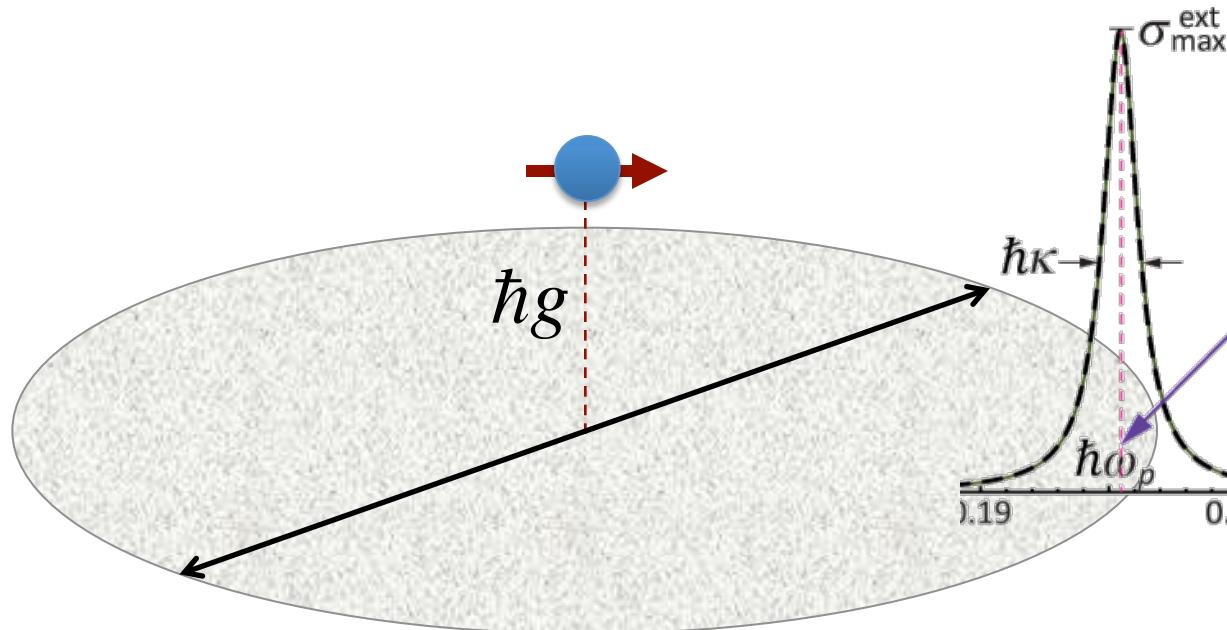
Quantum optics with graphene plasmons

Sensing with graphene plasmons

Plasmons in other atomically thin materials

Quantum optics with graphene plasmons

Vacuum Rabi splitting

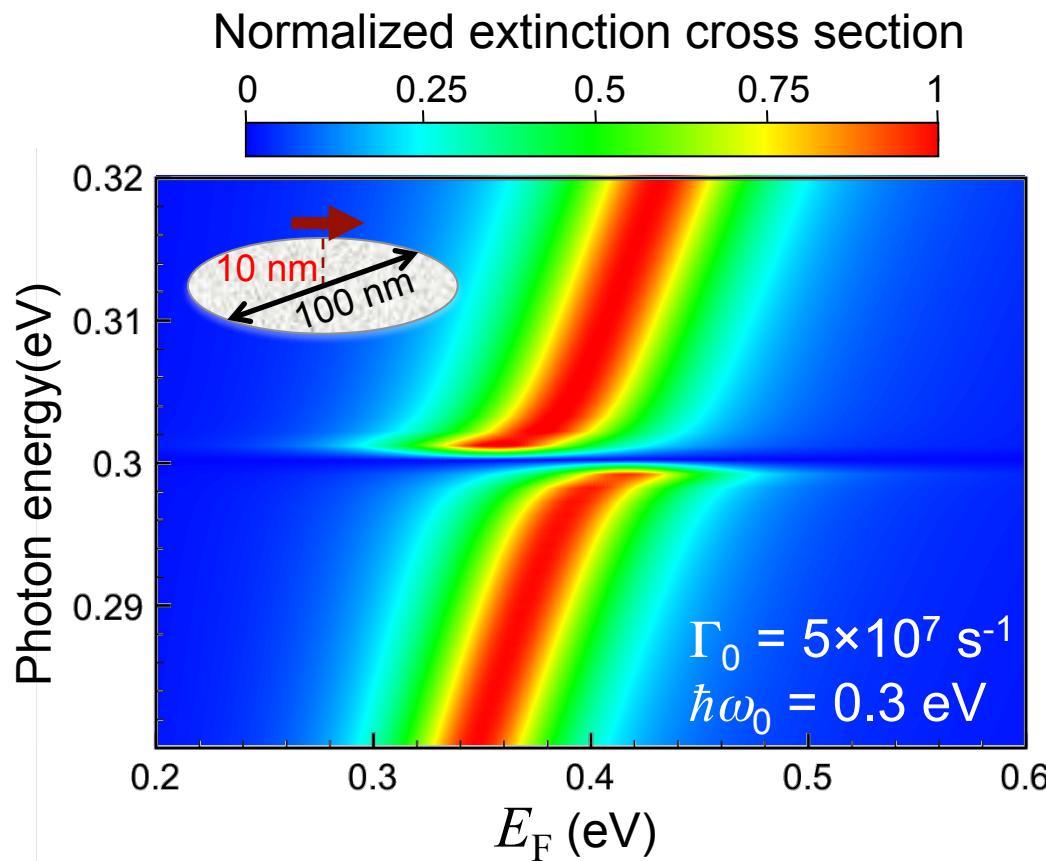


Strong-coupling
regime

$$g \gg K$$

Quantum optics with graphene plasmons

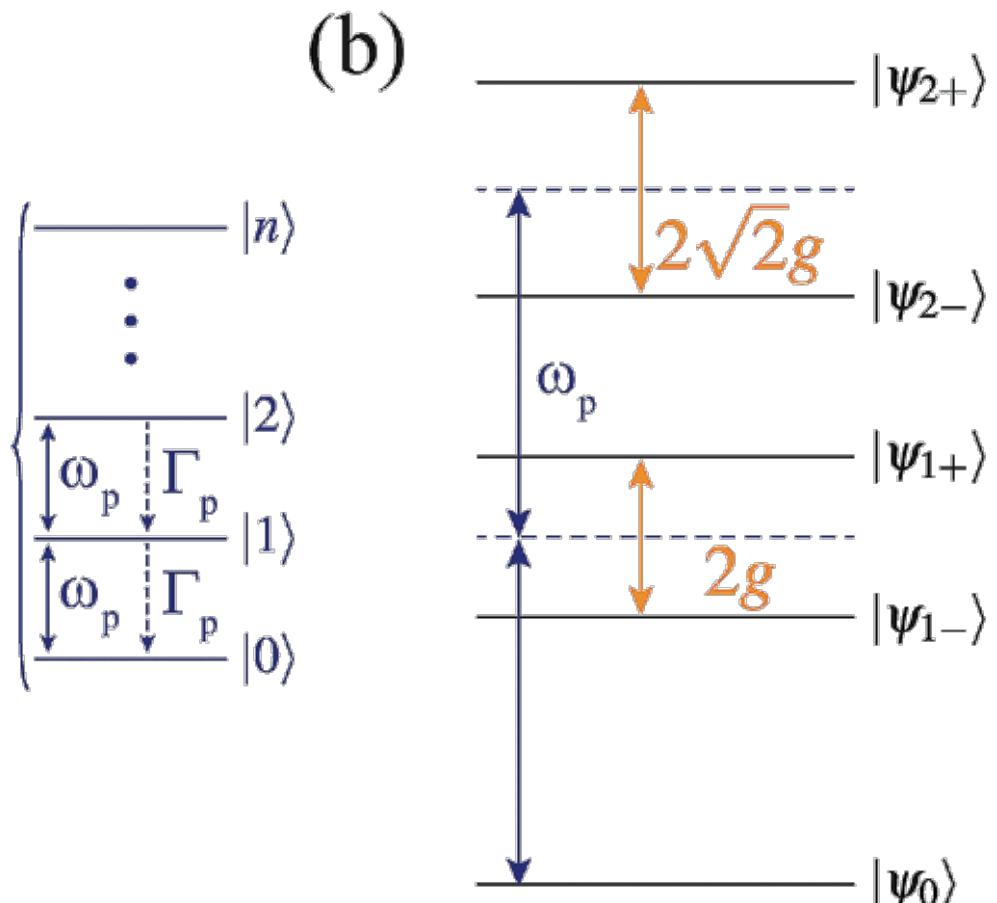
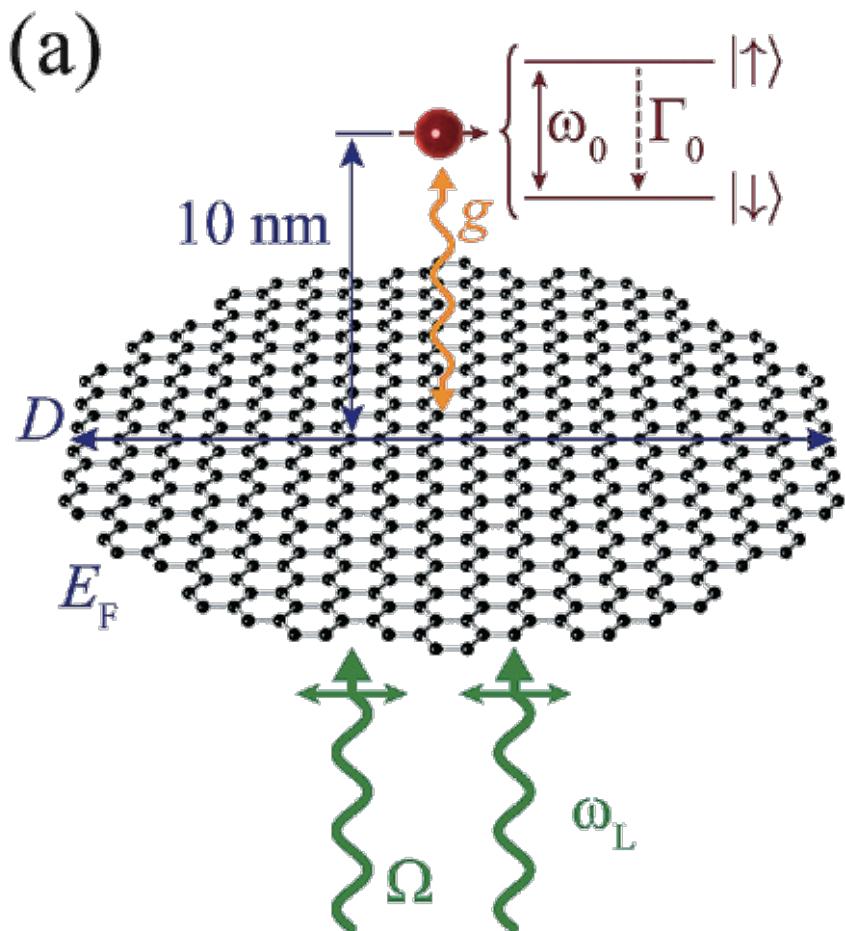
Vacuum Rabi splitting



Koppens, Chang, and García de Abajo, Nano Lett. (2011)

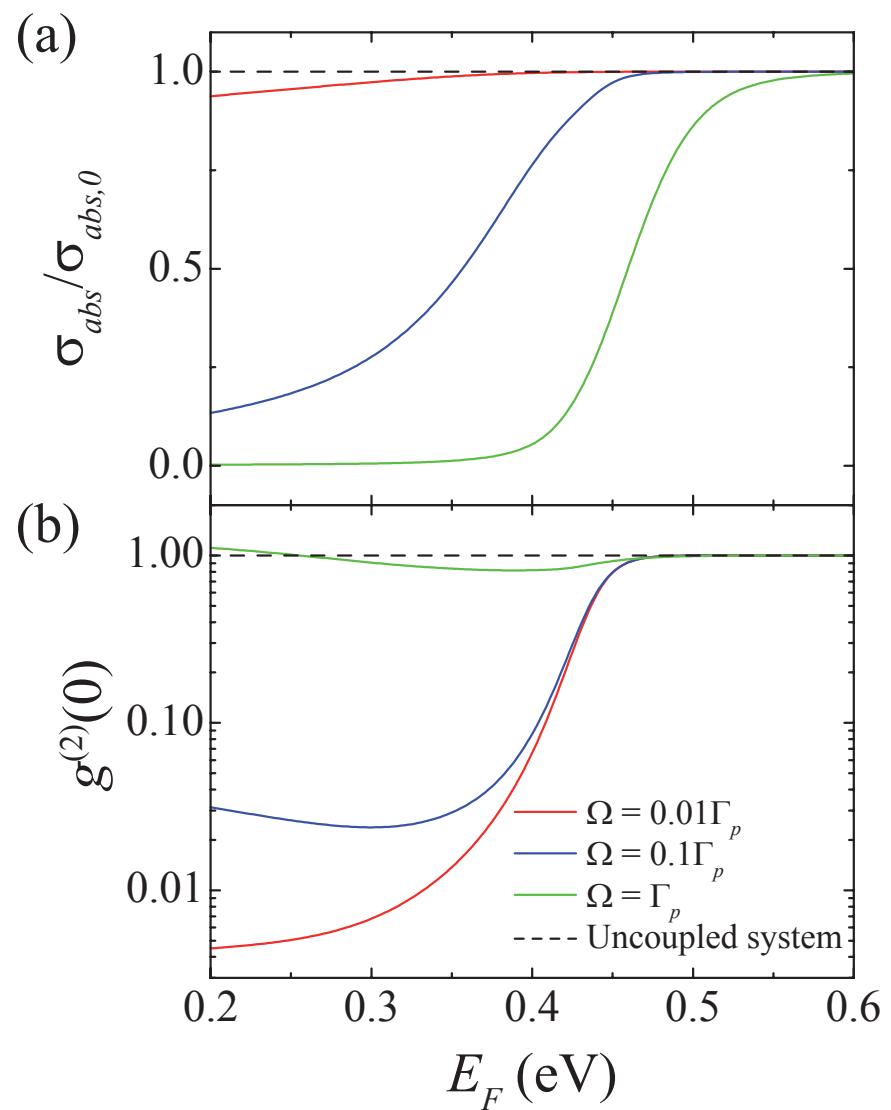
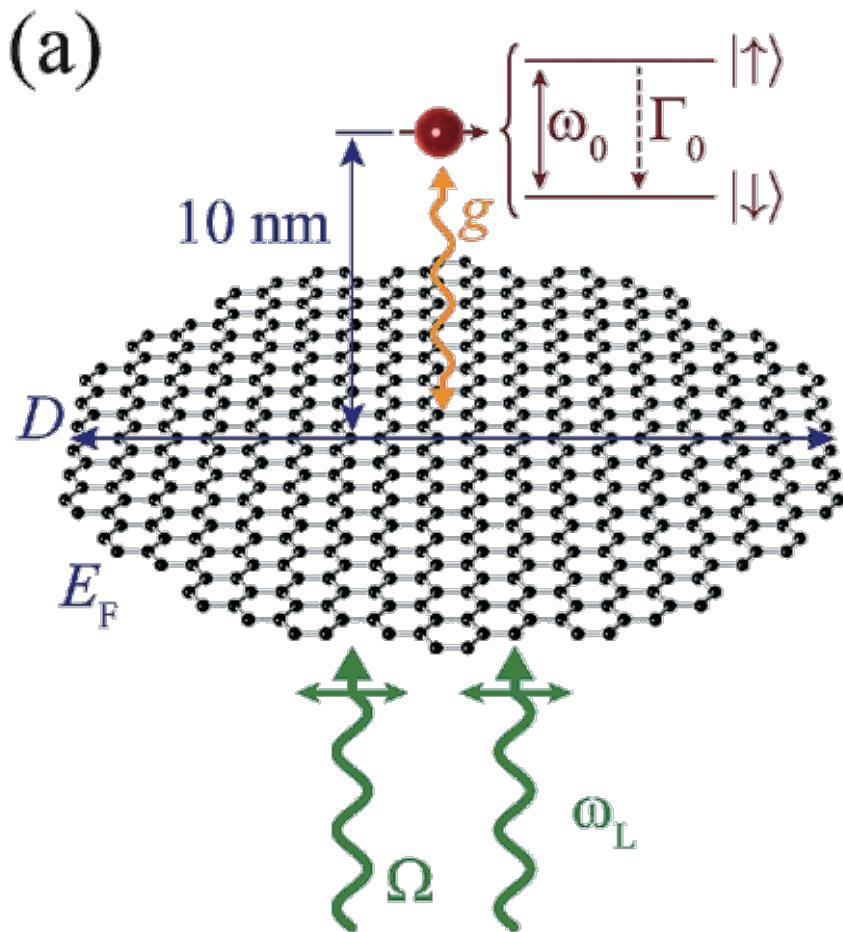
Quantum optics with graphene plasmons

Jaynes-Cummings ladder

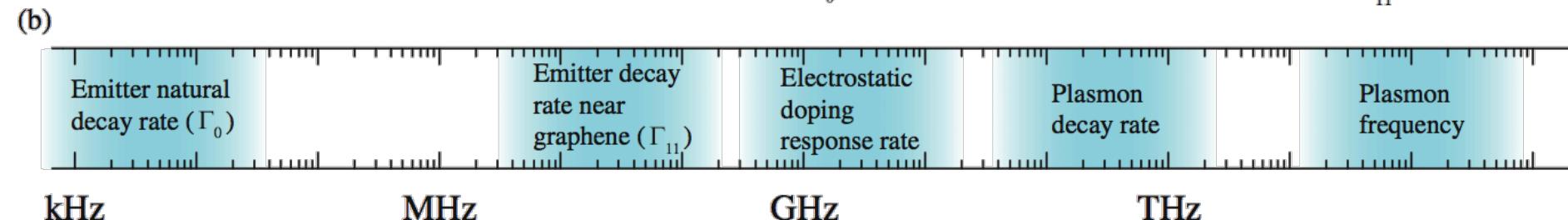
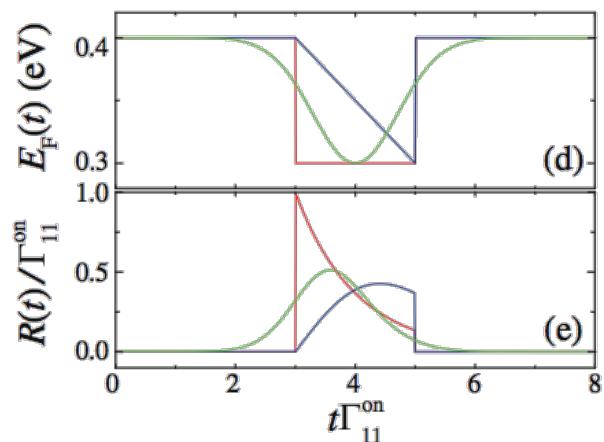
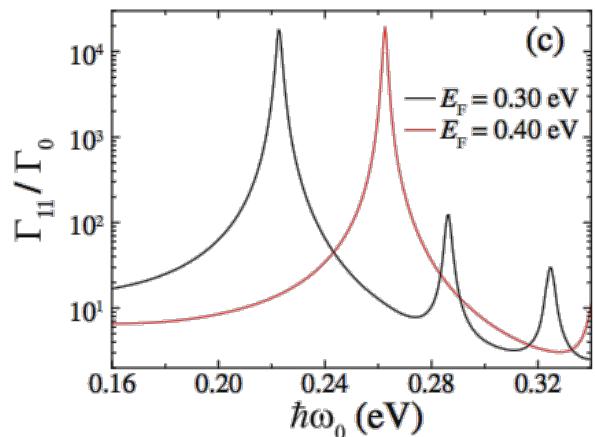
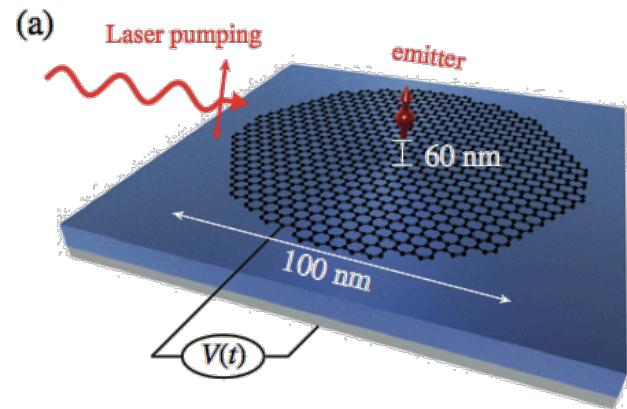


Quantum optics with graphene plasmons

Plasmon blockade



Electrical control of quantum states

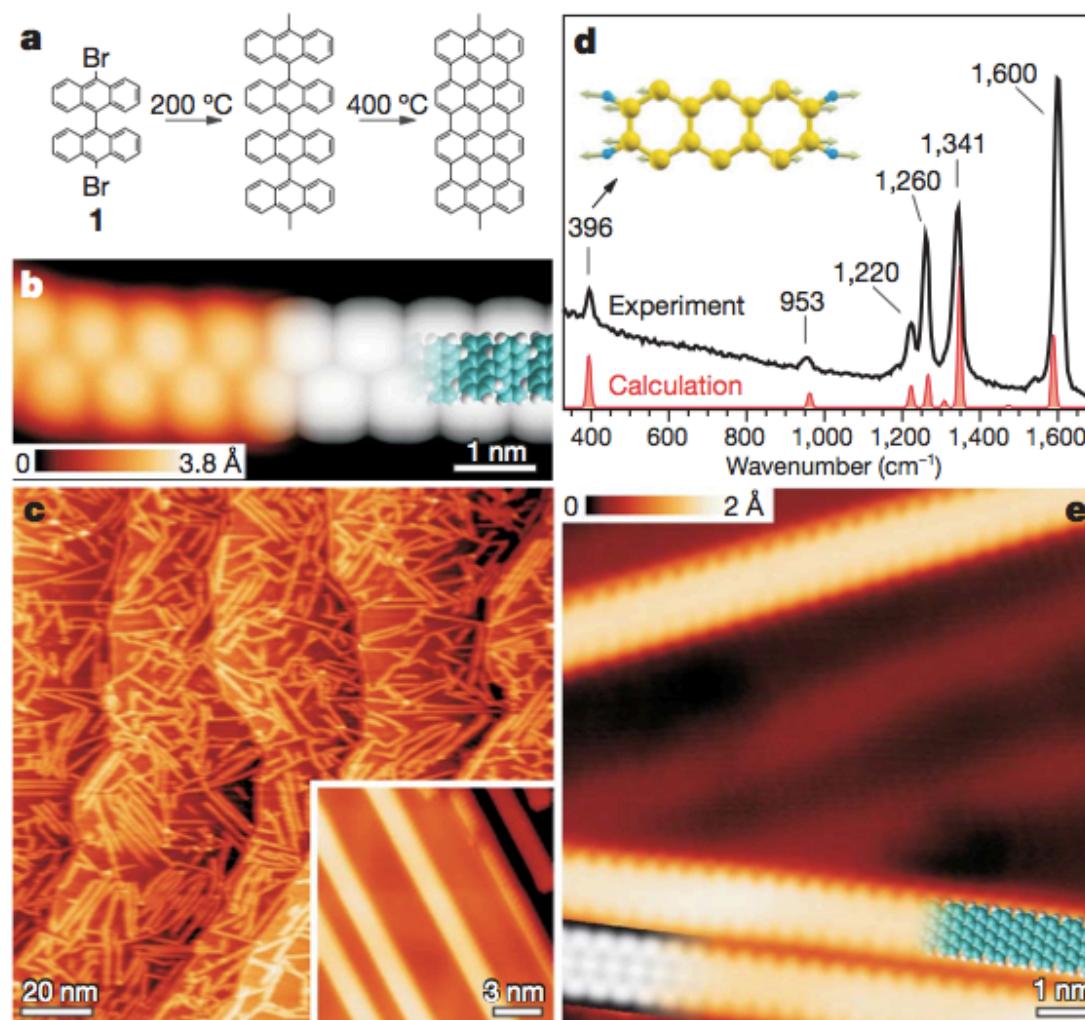


How to move towards the visible-NIR

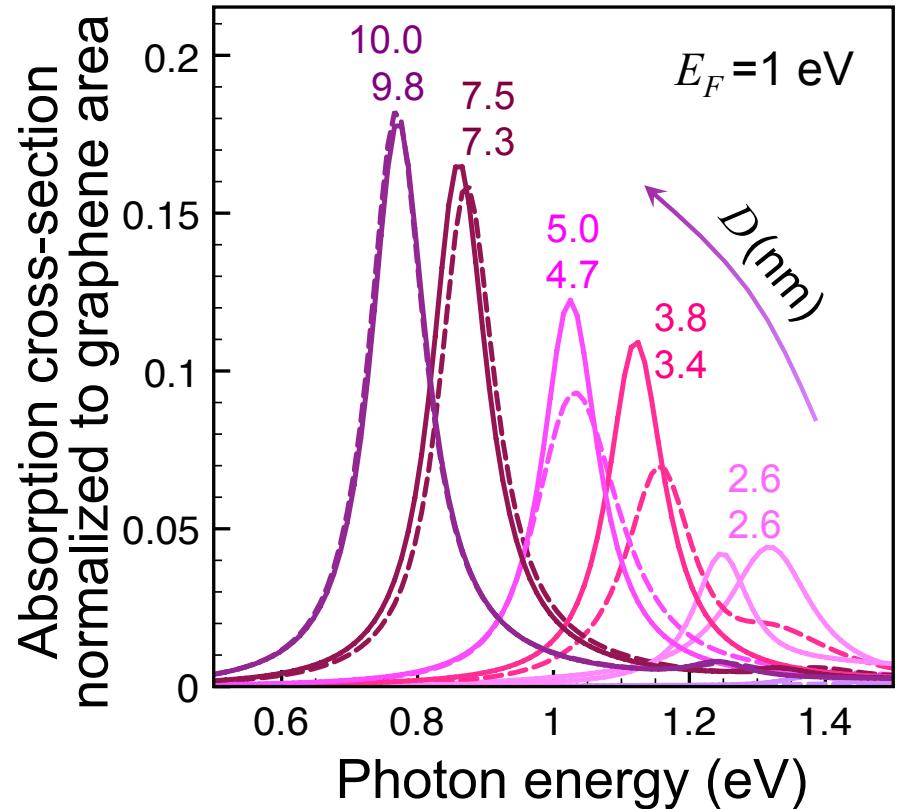
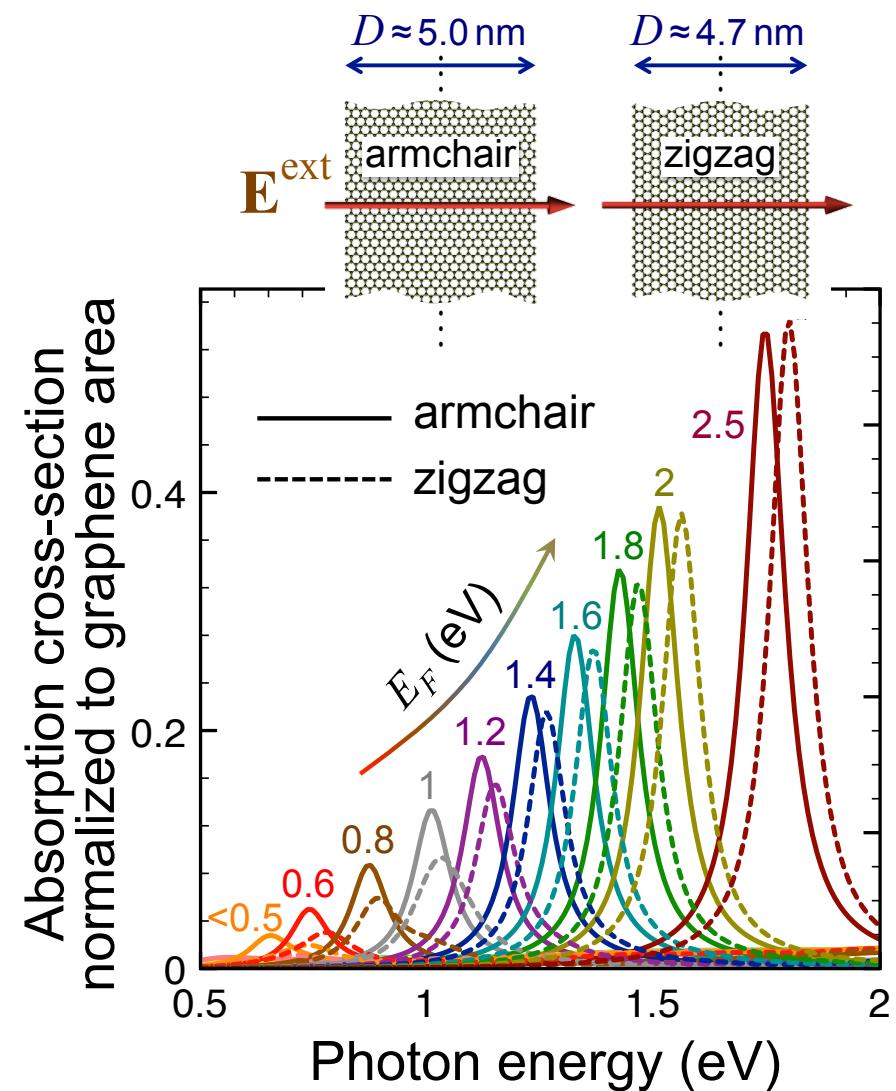
- 1) Increasing doping
- 2) Making smaller structures

$$\omega_{sp} \propto \sqrt{\frac{E_F}{D}}$$

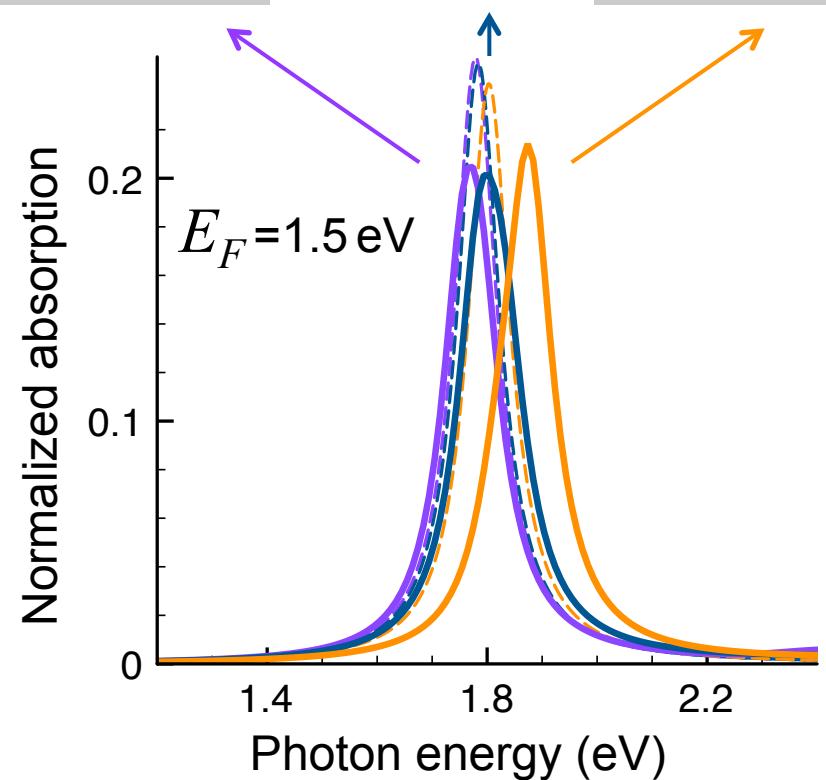
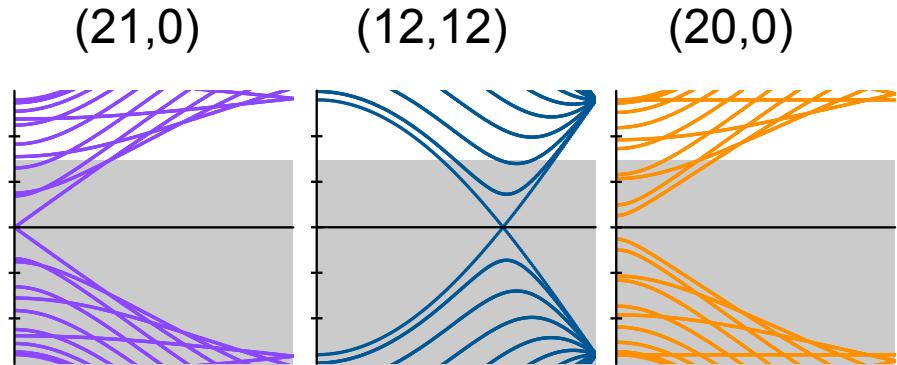
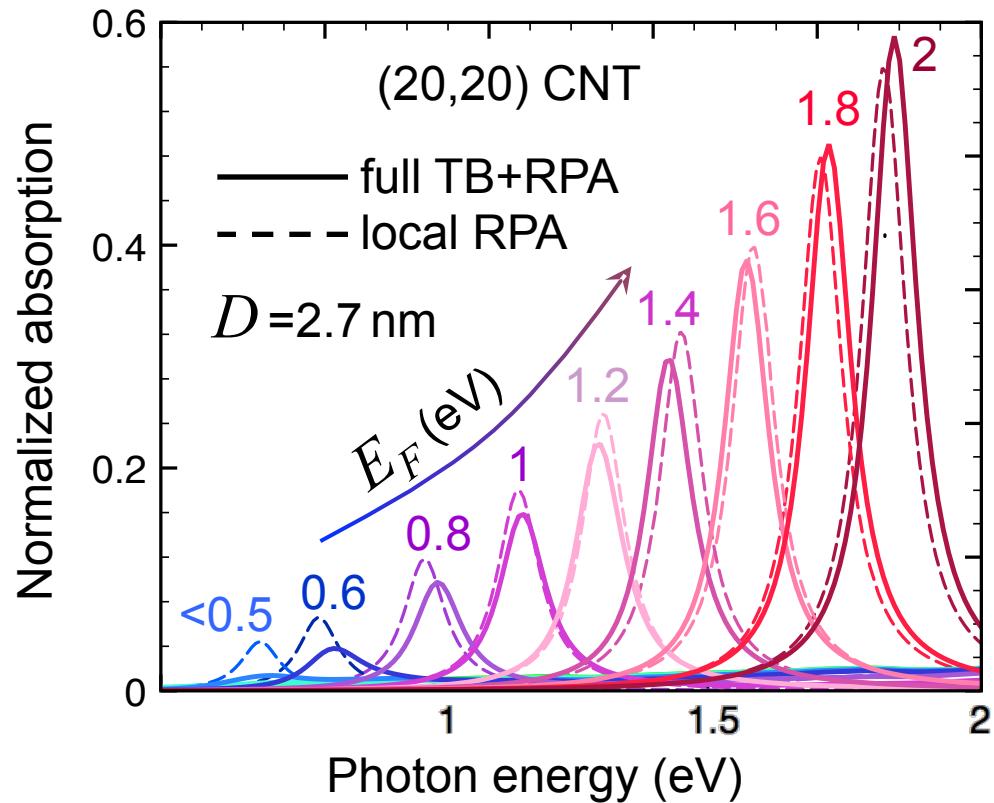
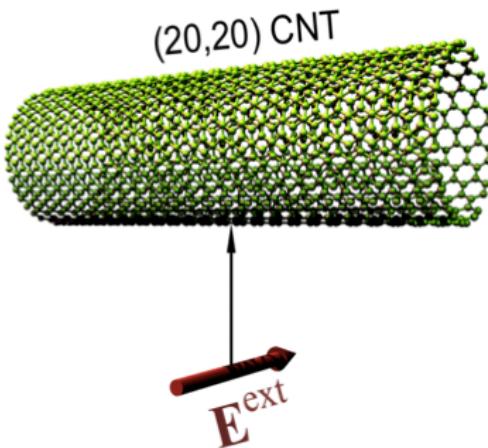
Molecular self-assembly



vis-NIR graphene plasmons

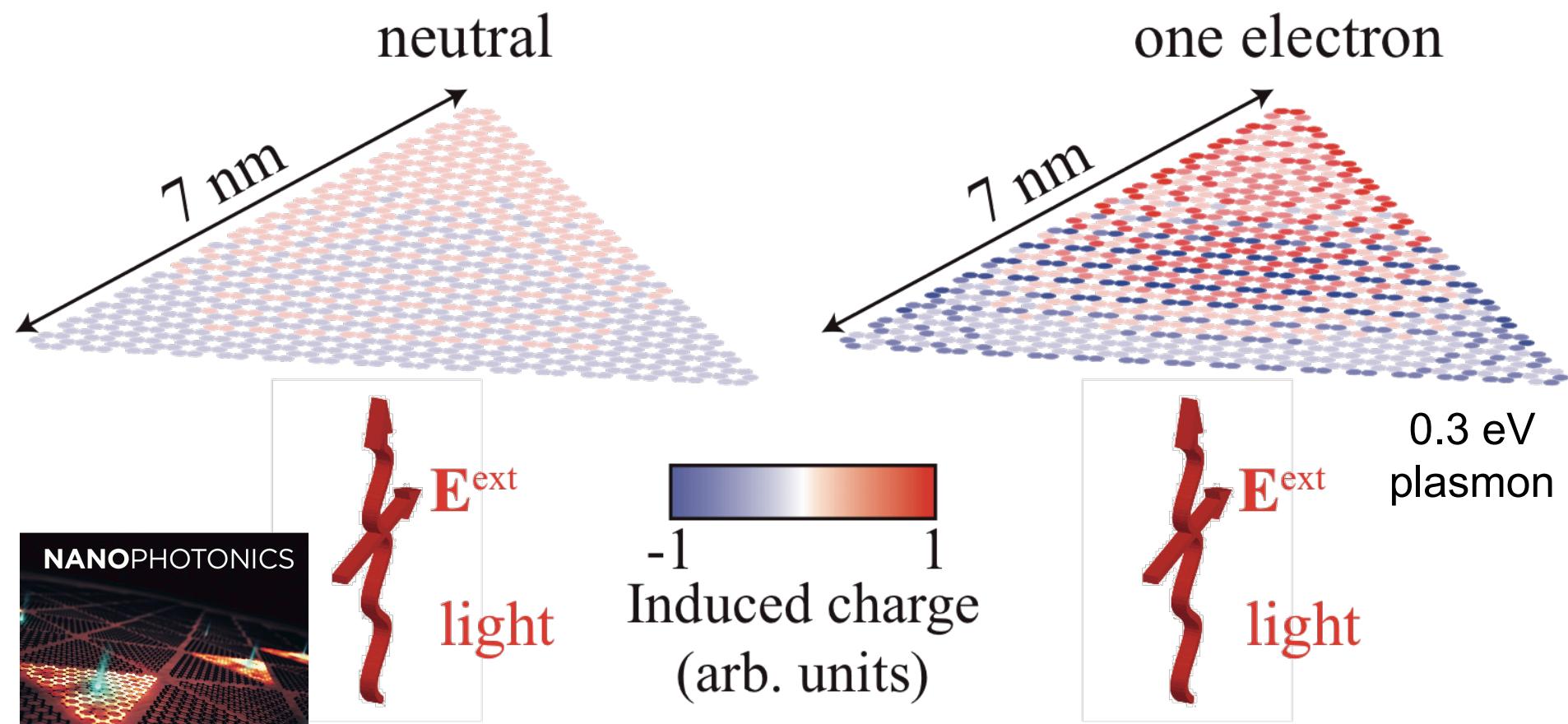


vis-NIR plasmons in CNTs

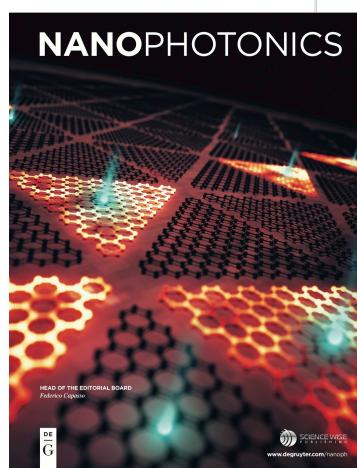


García de Abajo, ACS Photonics (2014)

Single-electron plasmon switching



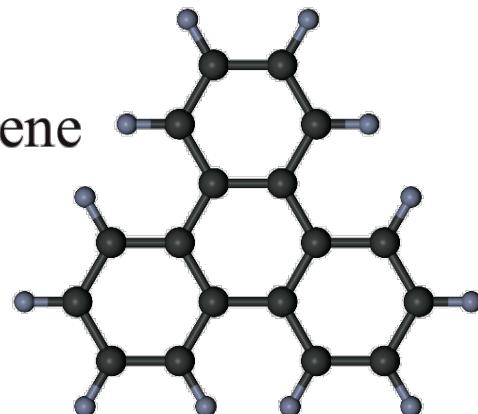
Manjavacas *et al.*, Nanophotonics (2013)



Down to molecules

(a)

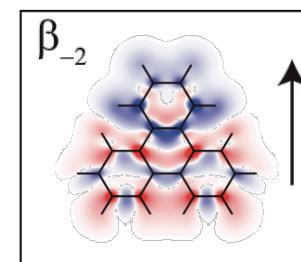
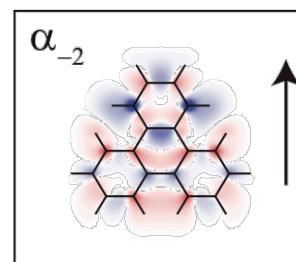
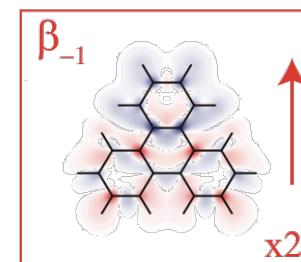
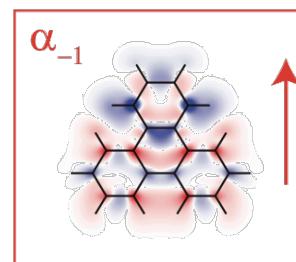
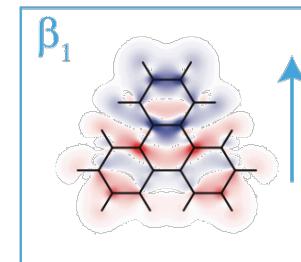
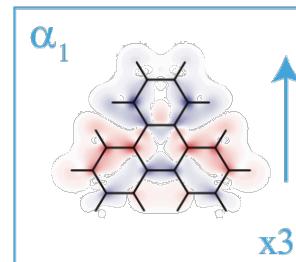
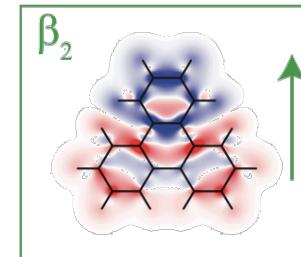
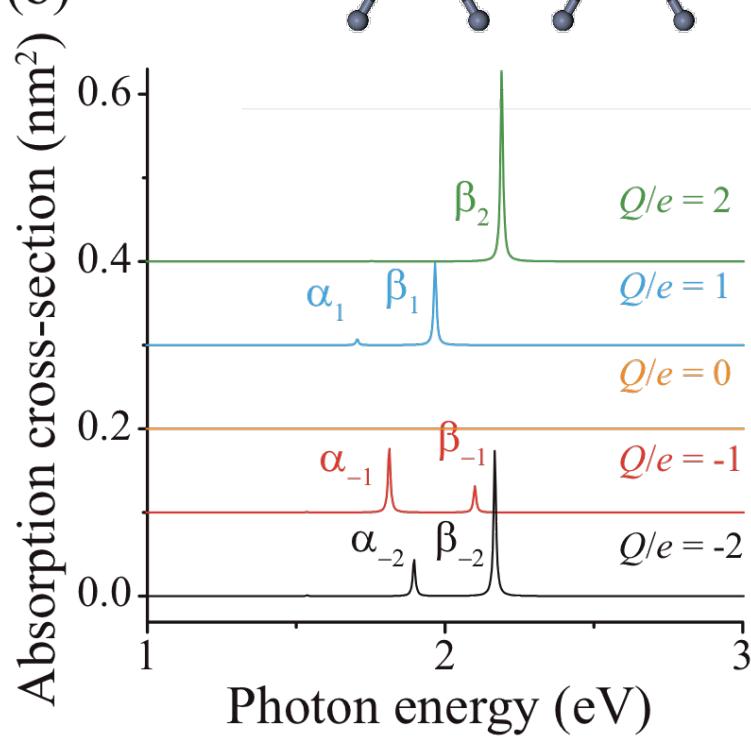
Triphenylene
 $C_{18}H_{12}$



Induced charge
(arb. units)

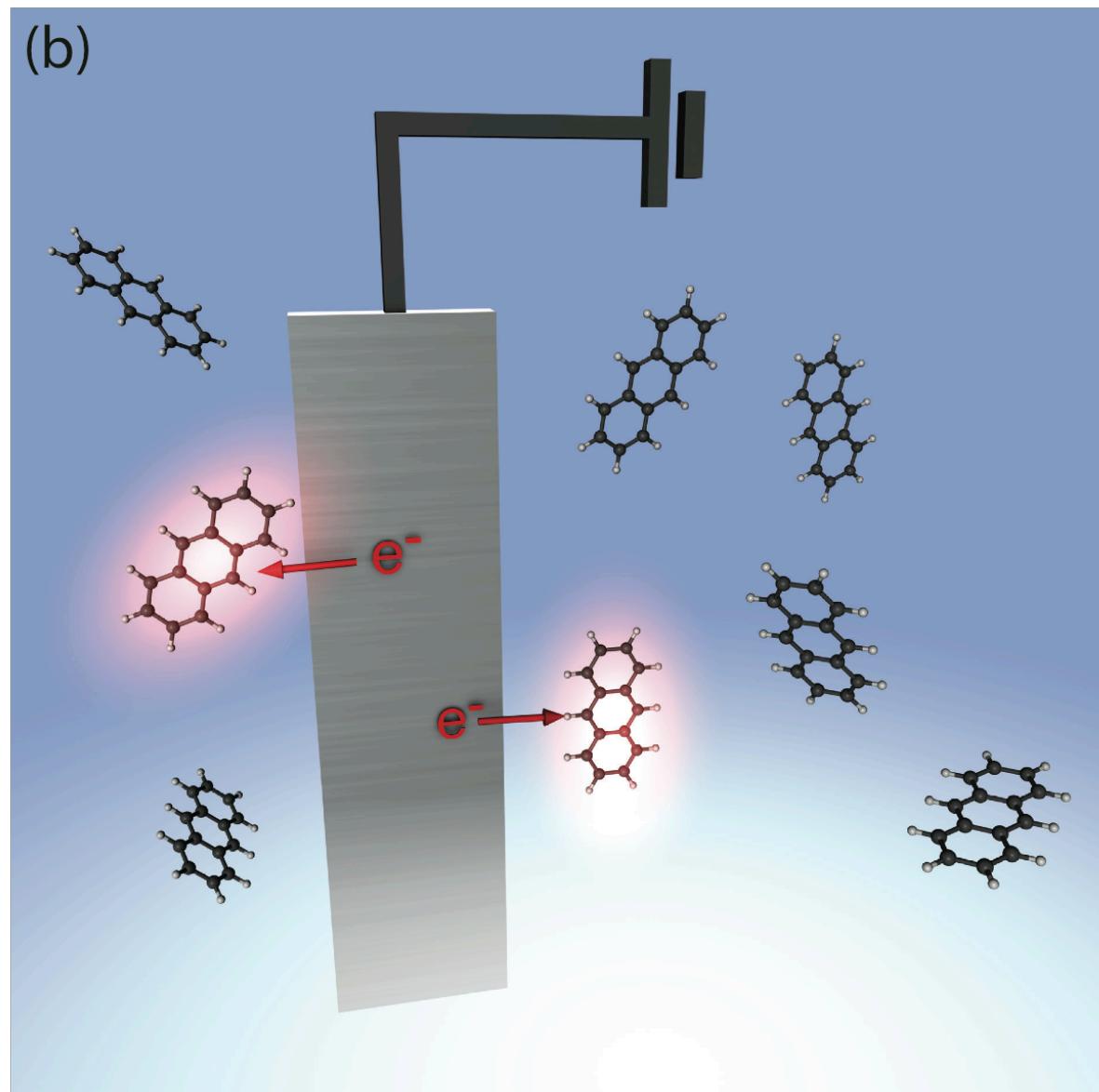
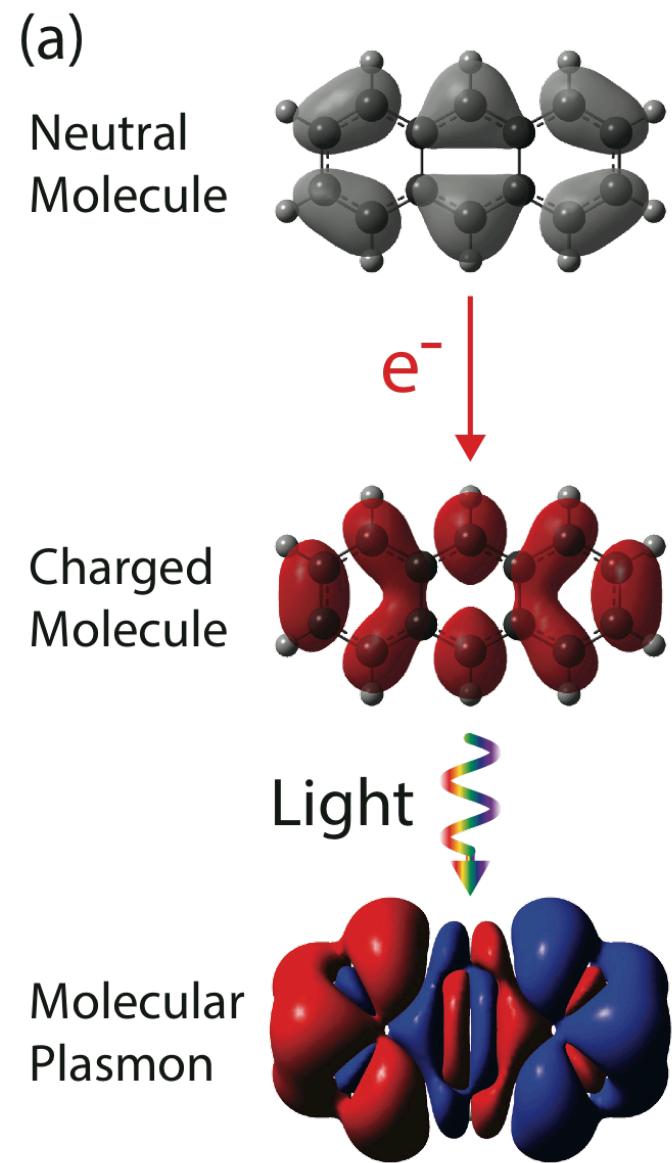


(b)



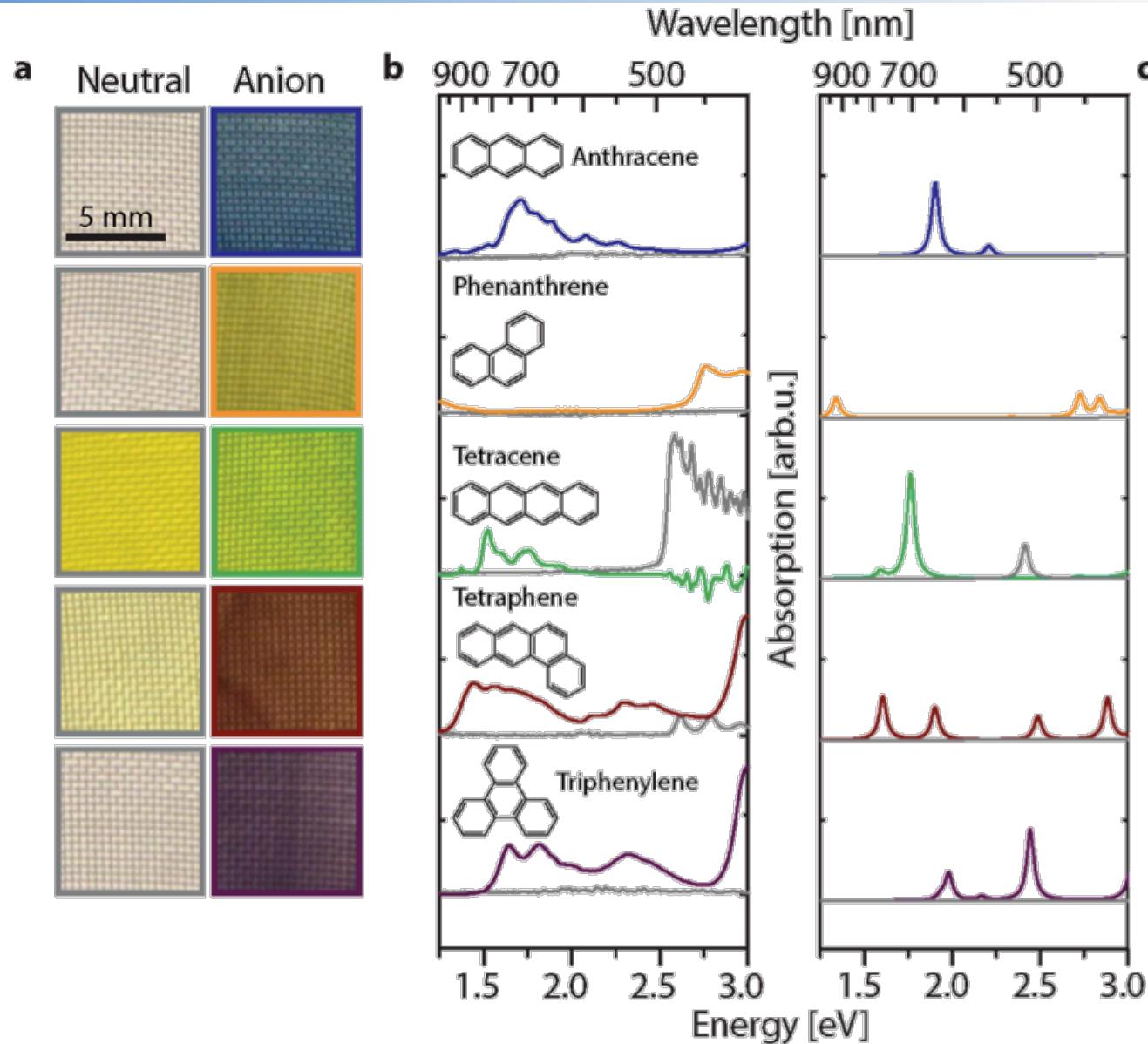
Manjavacas *et al.*, ACS Nano (2013)

Tunable molecular plasmons



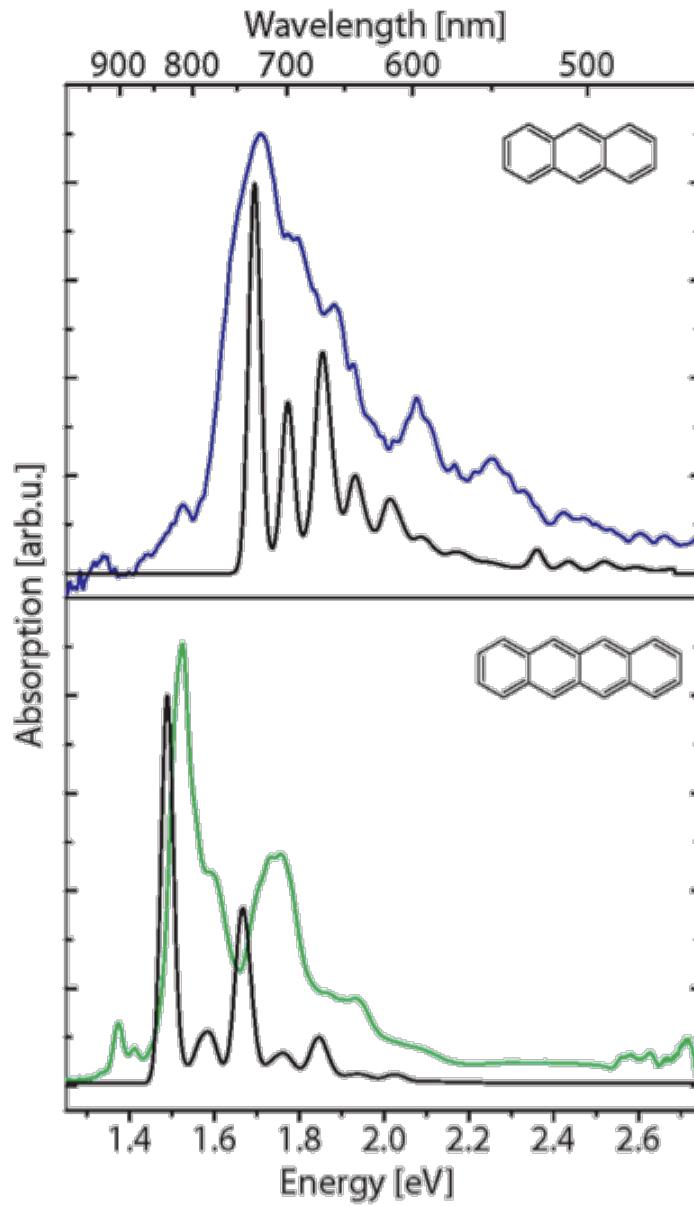
Adam Lauchner *et al.*, in collaboration with Naomi Halas and Peter Nordlander groups

Tunable molecular plasmons



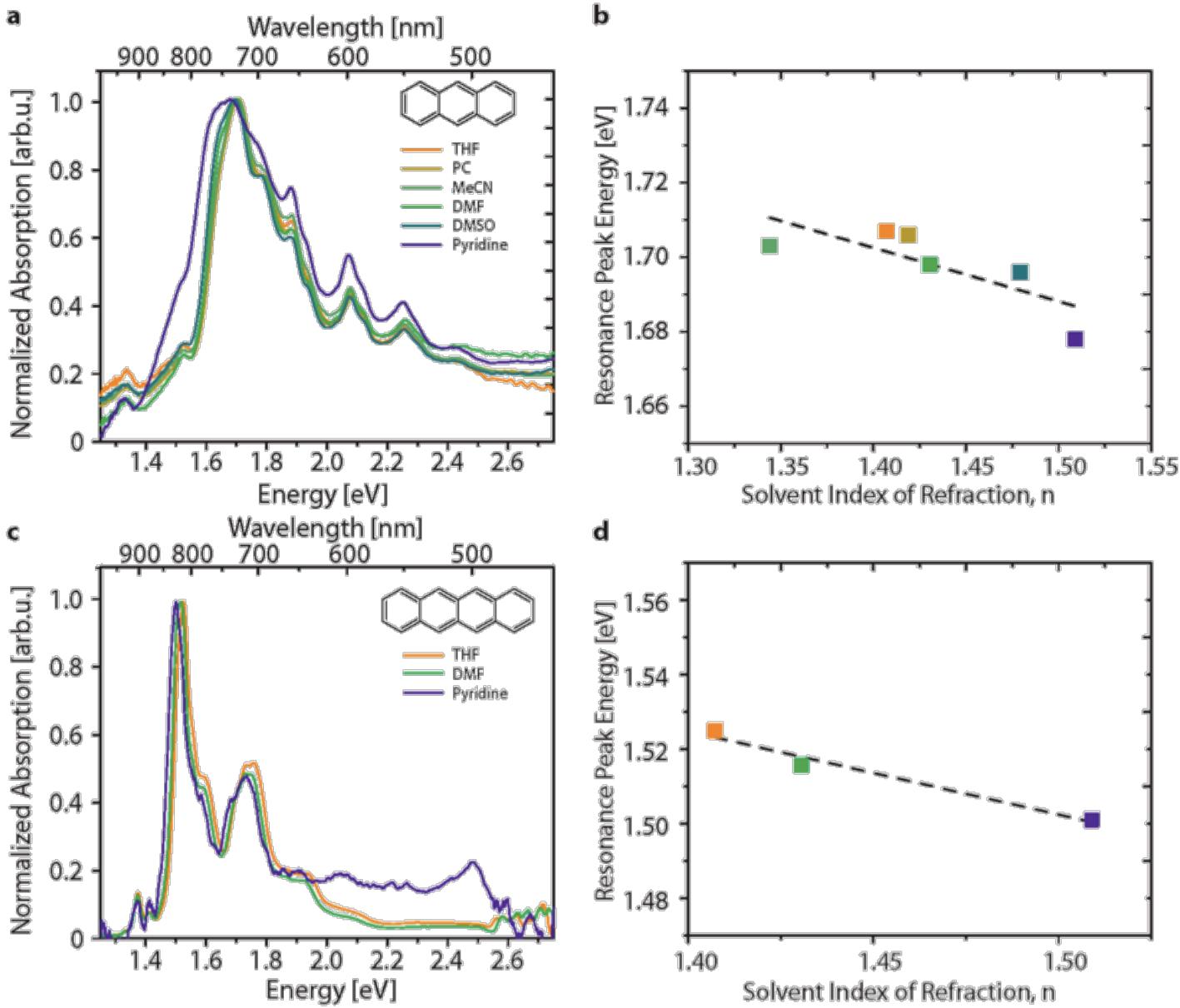
Adam Lauchner *et al.*, in collaboration with Naomi Halas and Peter Nordlander groups

Tunable molecular plasmons



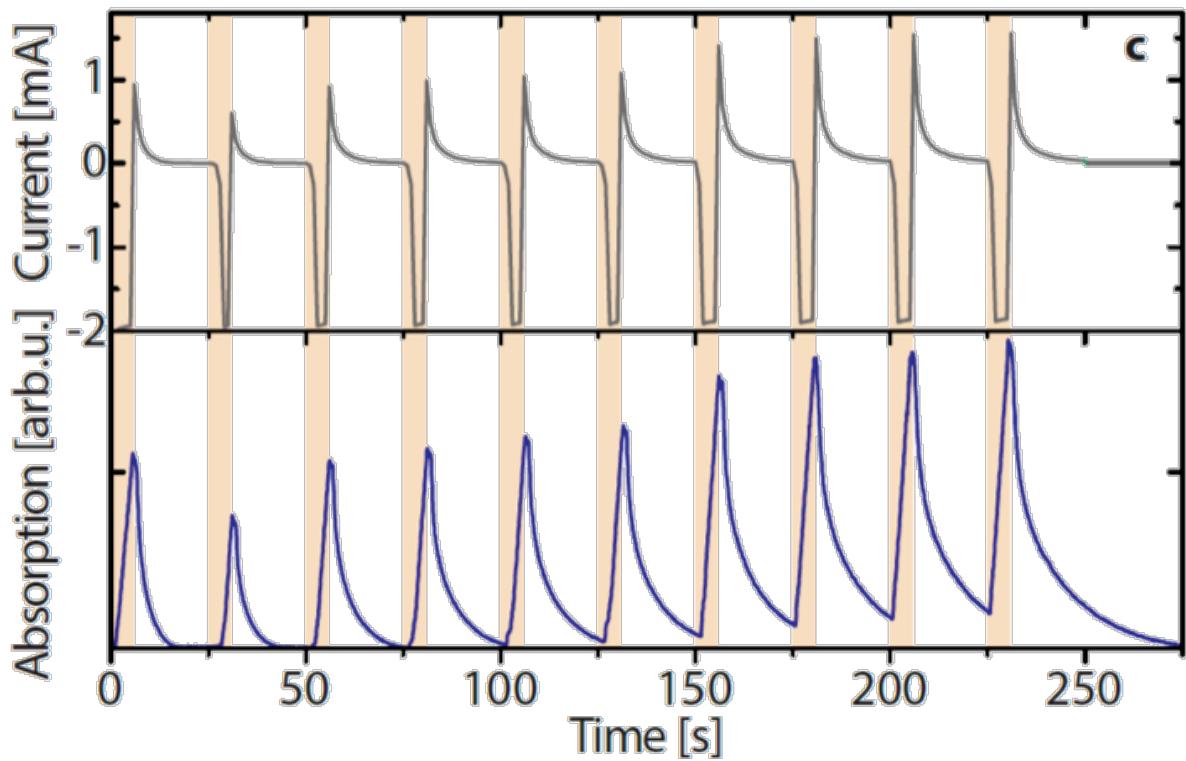
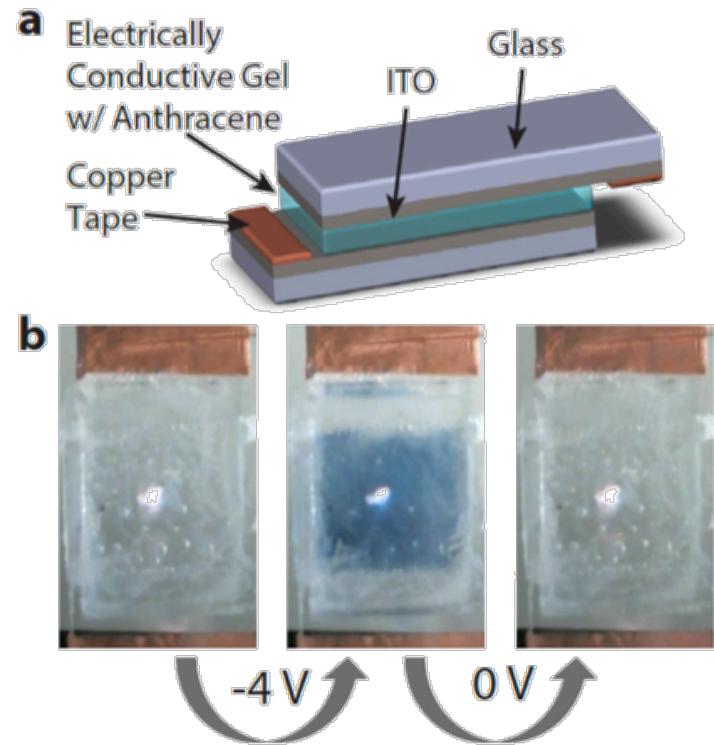
Adam Lauchner *et al.*, in collaboration with Naomi Halas and Peter Nordlander groups

Tunable molecular plasmons



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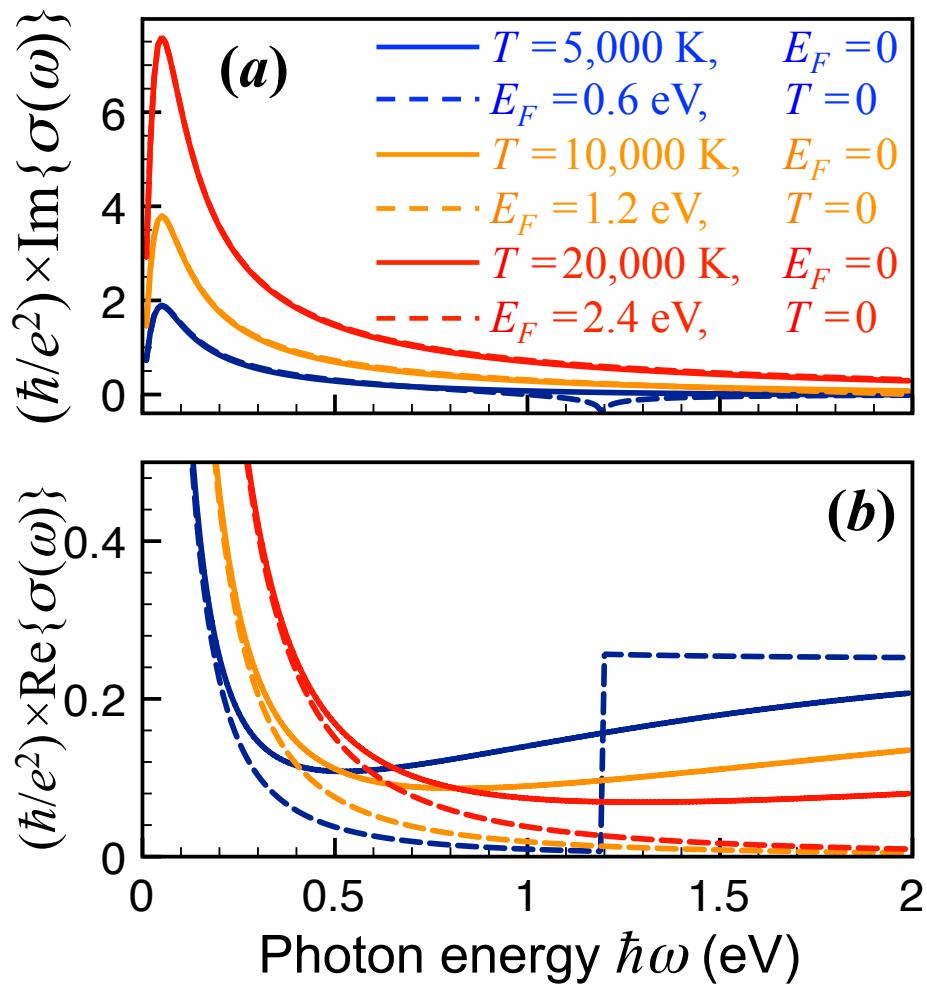
Electrochromic device



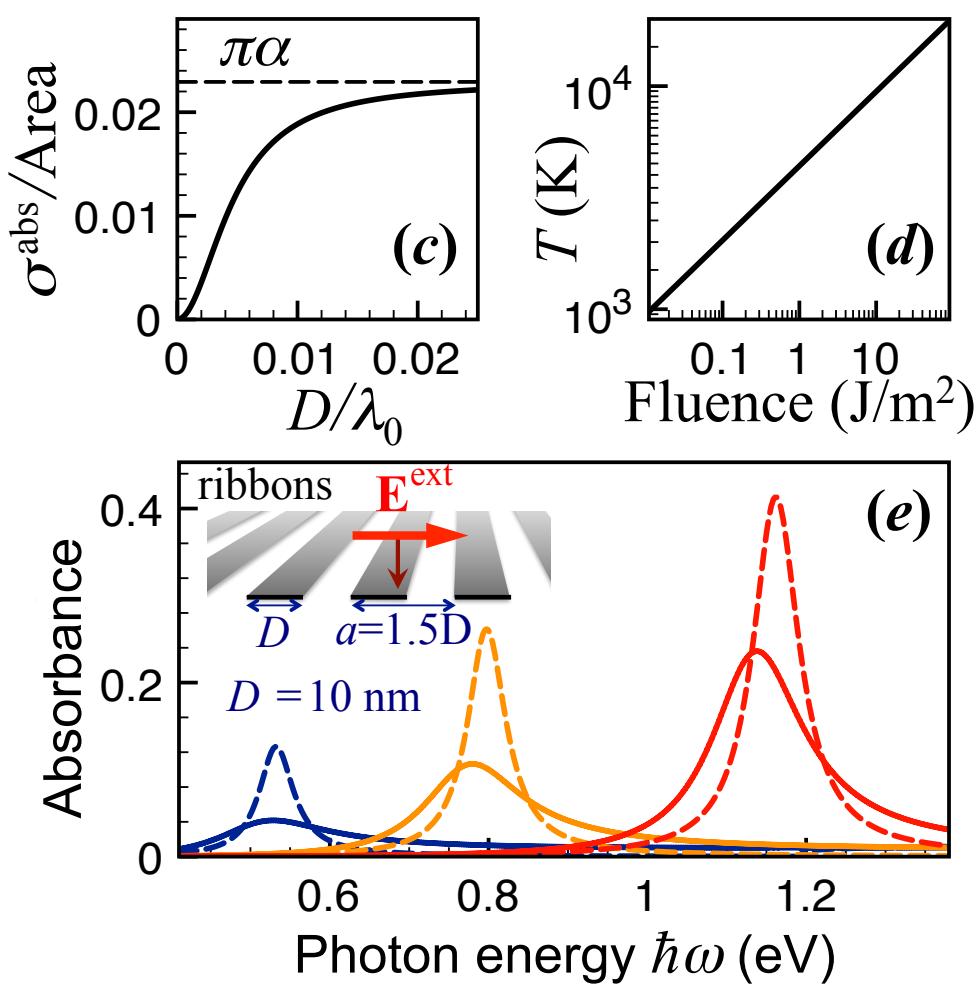
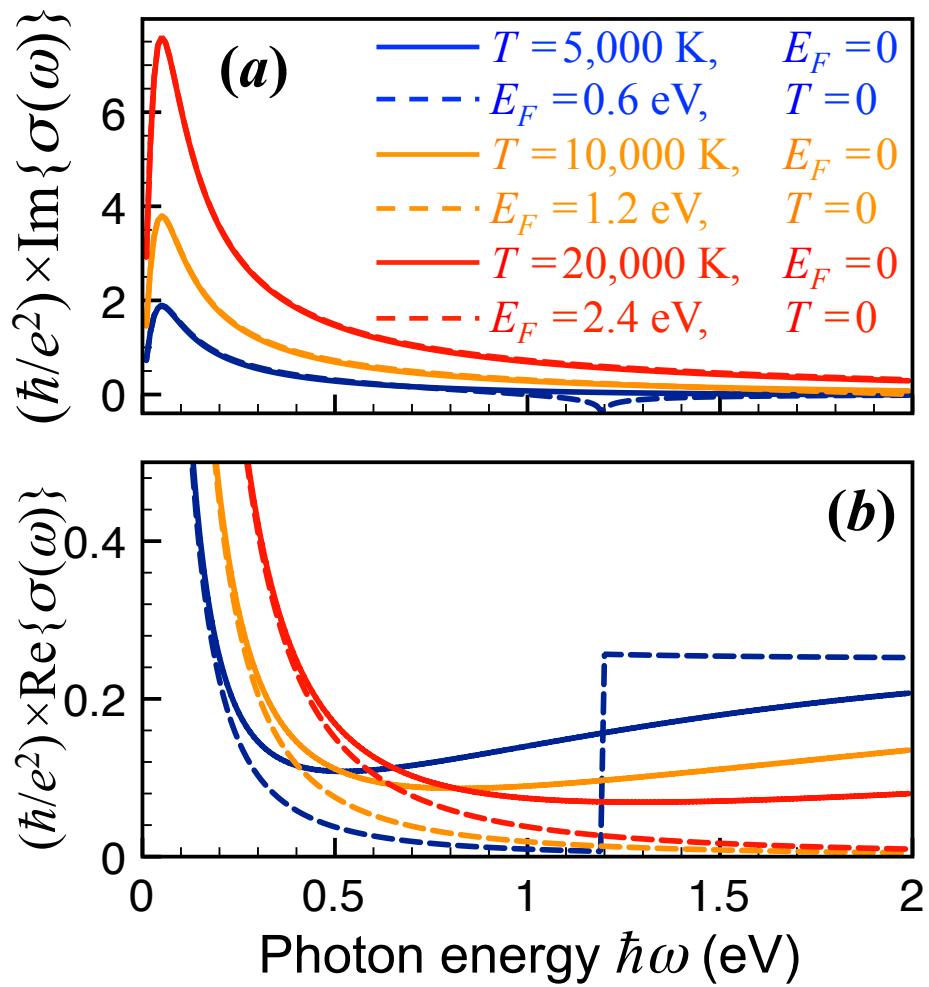
How to move towards the visible-NIR

- 1) Increasing doping
- 2) Making smaller structures
- 3) Exploiting transient phenomena

Transient graphene plasmons



Transient graphene plasmons



Plasmonics: An overview and some new trends

Introduction to plasmons

Graphene plasmons

Quantum-mechanical description

Classical description

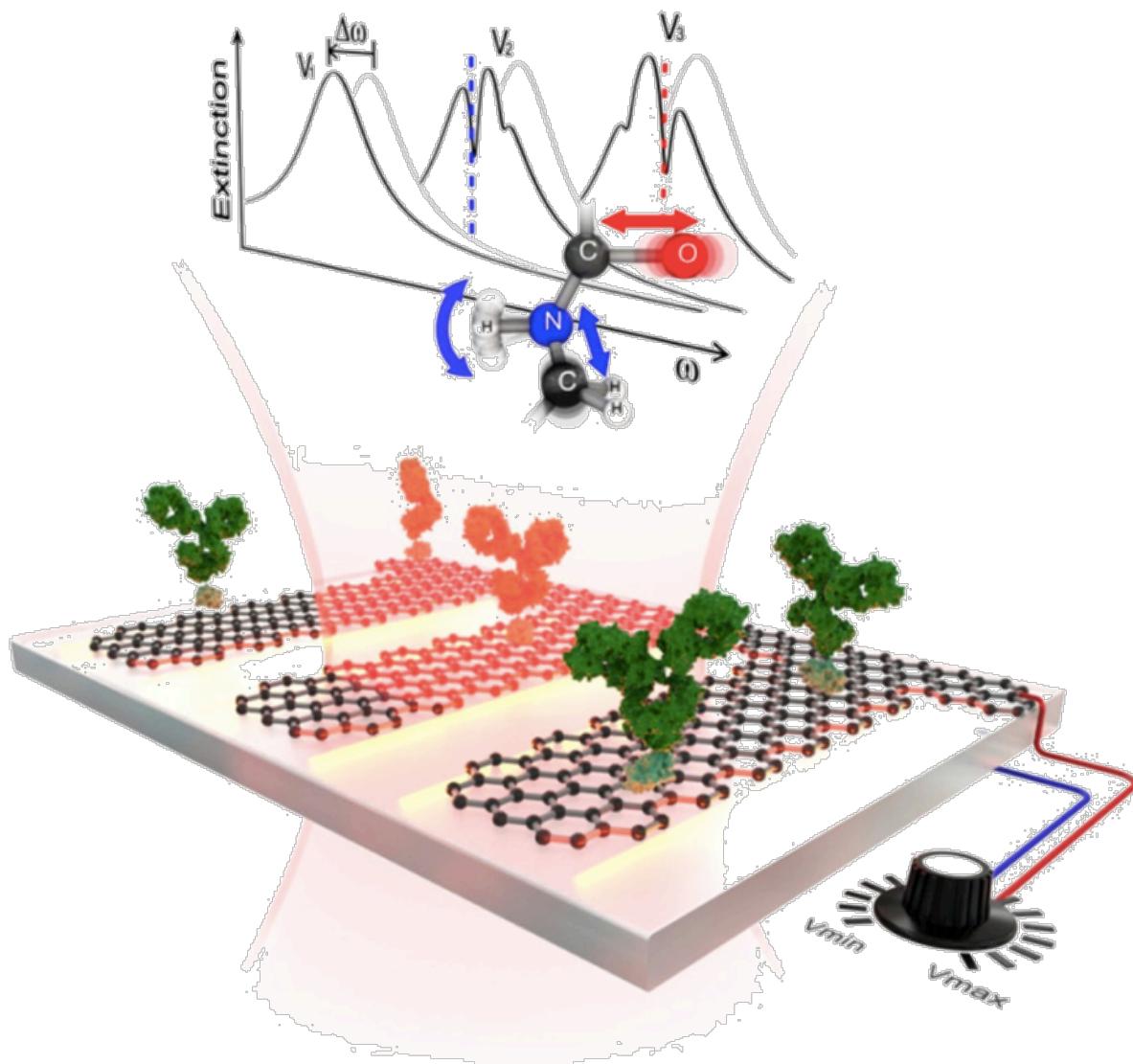
Complete optical absorption

Quantum optics with graphene plasmons

Sensing with graphene plasmons

Plasmons in other atomically thin materials

Mid-IR sensing with graphene plasmons

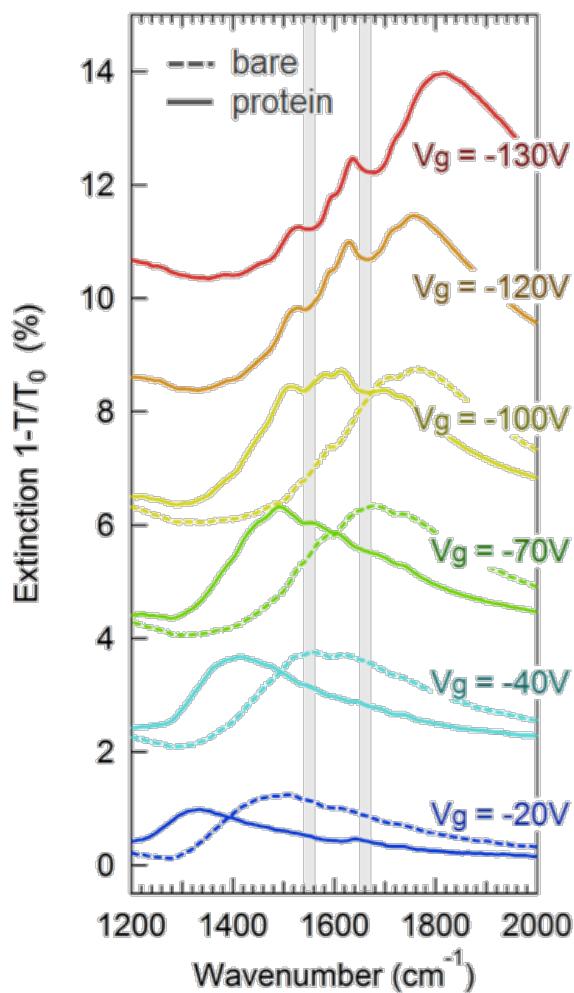


Daniel Rodrigo *et al.*, Science (2015),
in collaboration with Hattice Altug (EPFL) and Valerio Pruneri (ICFO) groups

Mid-IR sensing with graphene plasmons

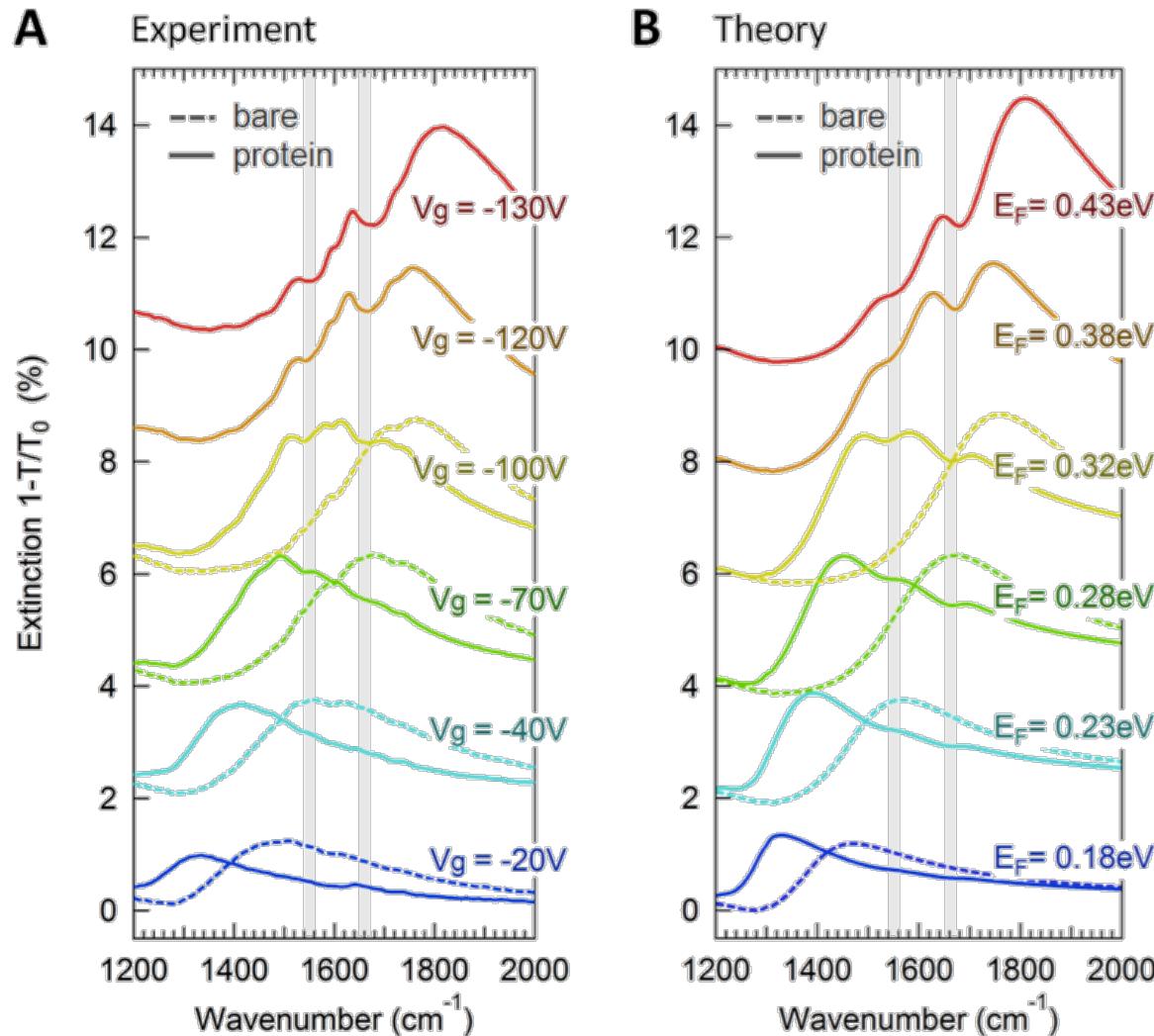
A

Experiment



Daniel Rodrigo *et al.*, Science (2015),
in collaboration with Hattice Altug (EPFL) and Valerio Pruneri (ICFO) groups

Mid-IR sensing with graphene plasmons

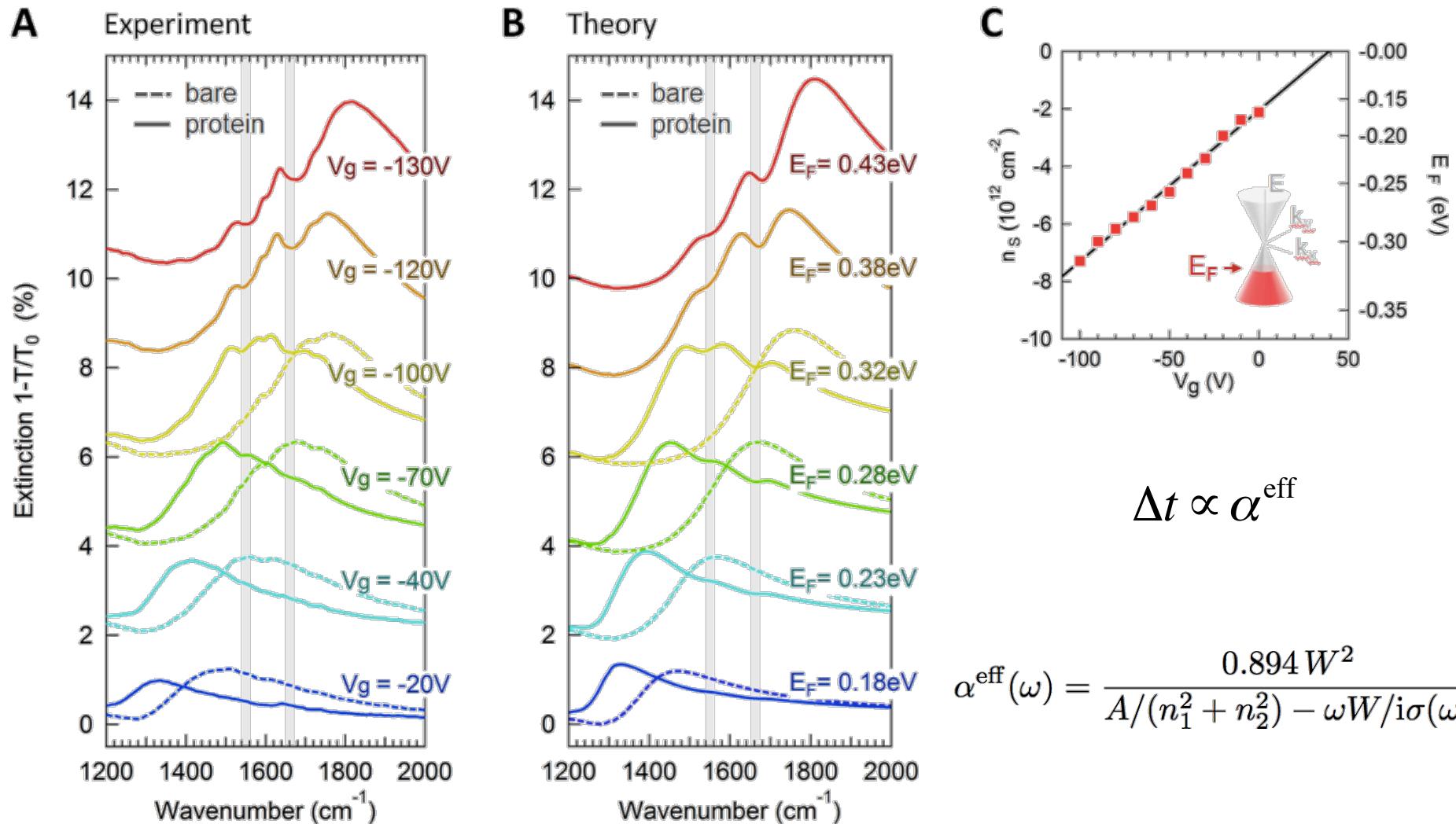


$$\Delta t \propto \alpha^{\text{eff}}$$

$$\alpha^{\text{eff}}(\omega) = \frac{0.894 W^2}{A/(n_1^2 + n_2^2) - \omega W/\text{i}\sigma(\omega)}$$

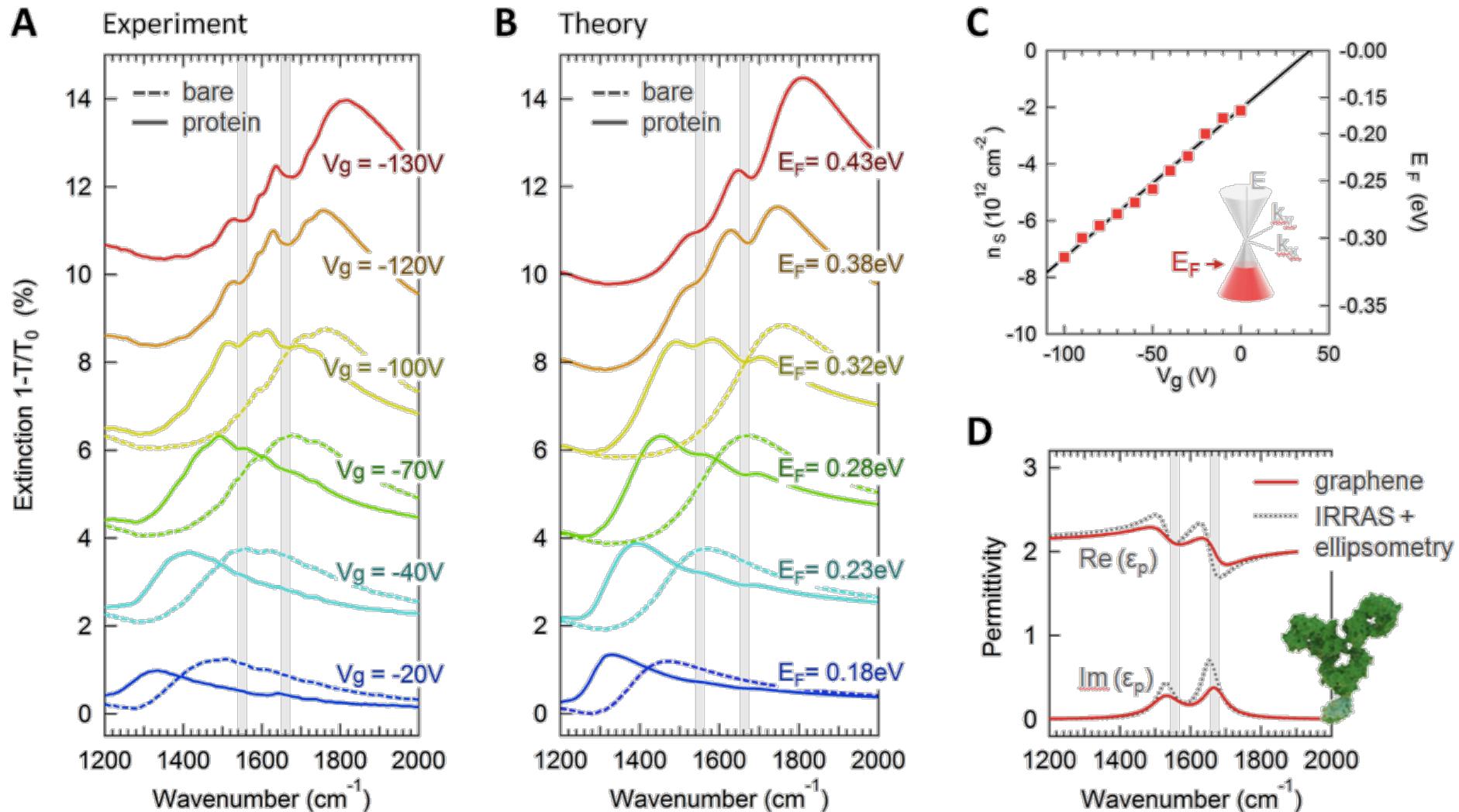
Daniel Rodrigo *et al.*, Science (2015),
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Mid-IR sensing with graphene plasmons



Daniel Rodrigo *et al.*, Science (2015),
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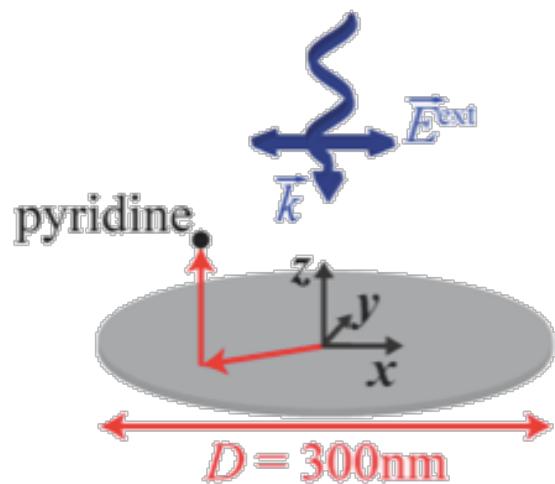
Mid-IR sensing with graphene plasmons



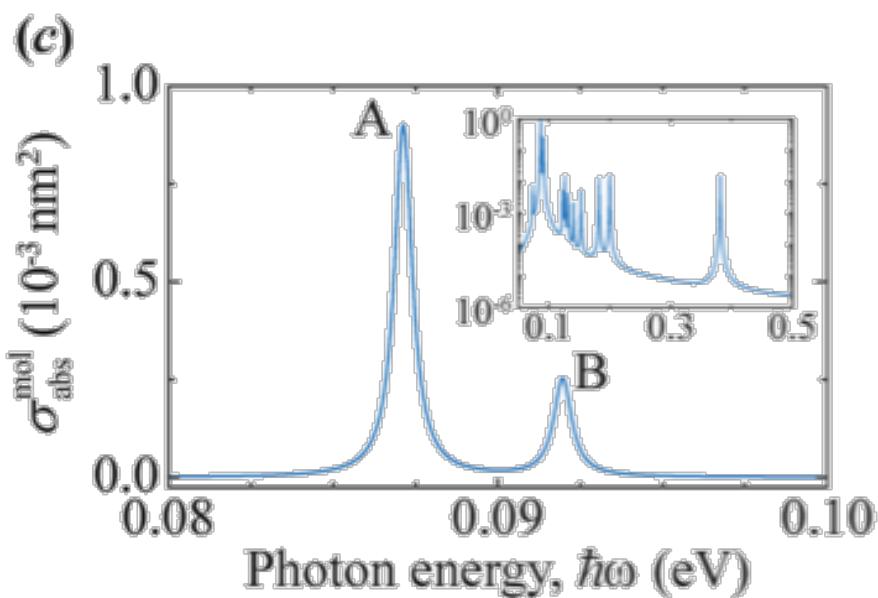
Daniel Rodrigo *et al.*, Science (2015),
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Infrared absorption spectroscopy

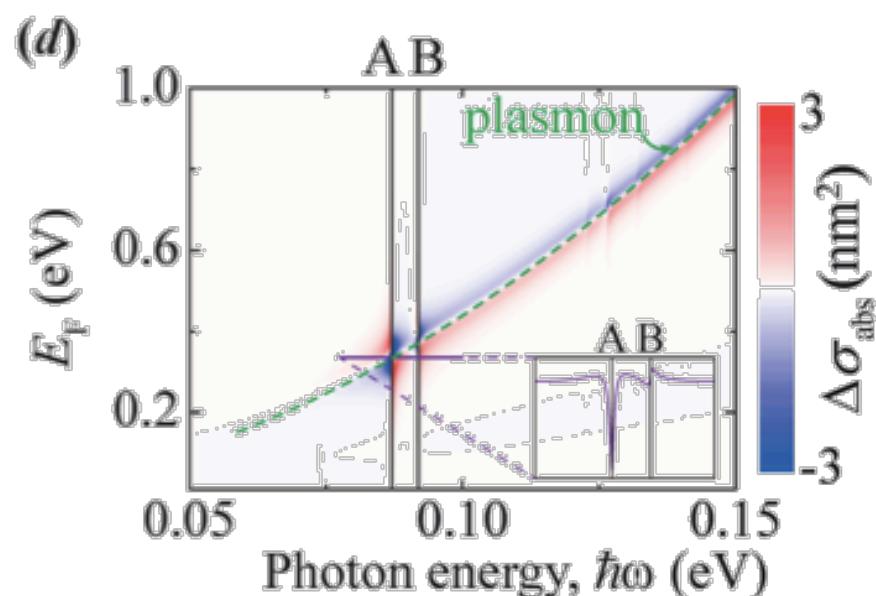
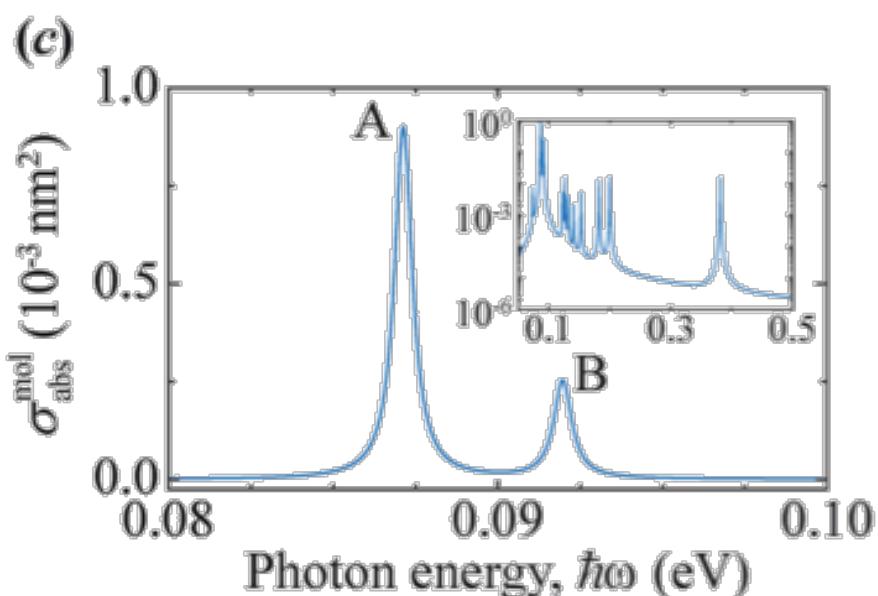
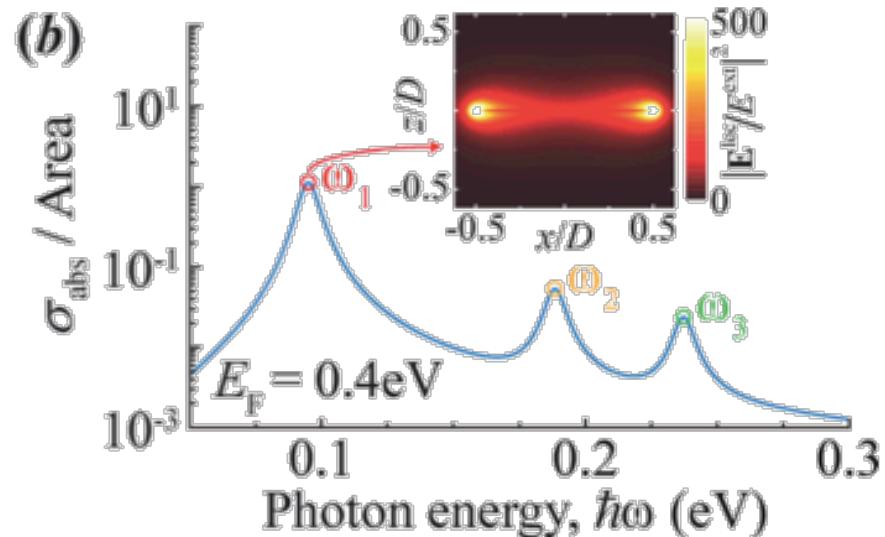
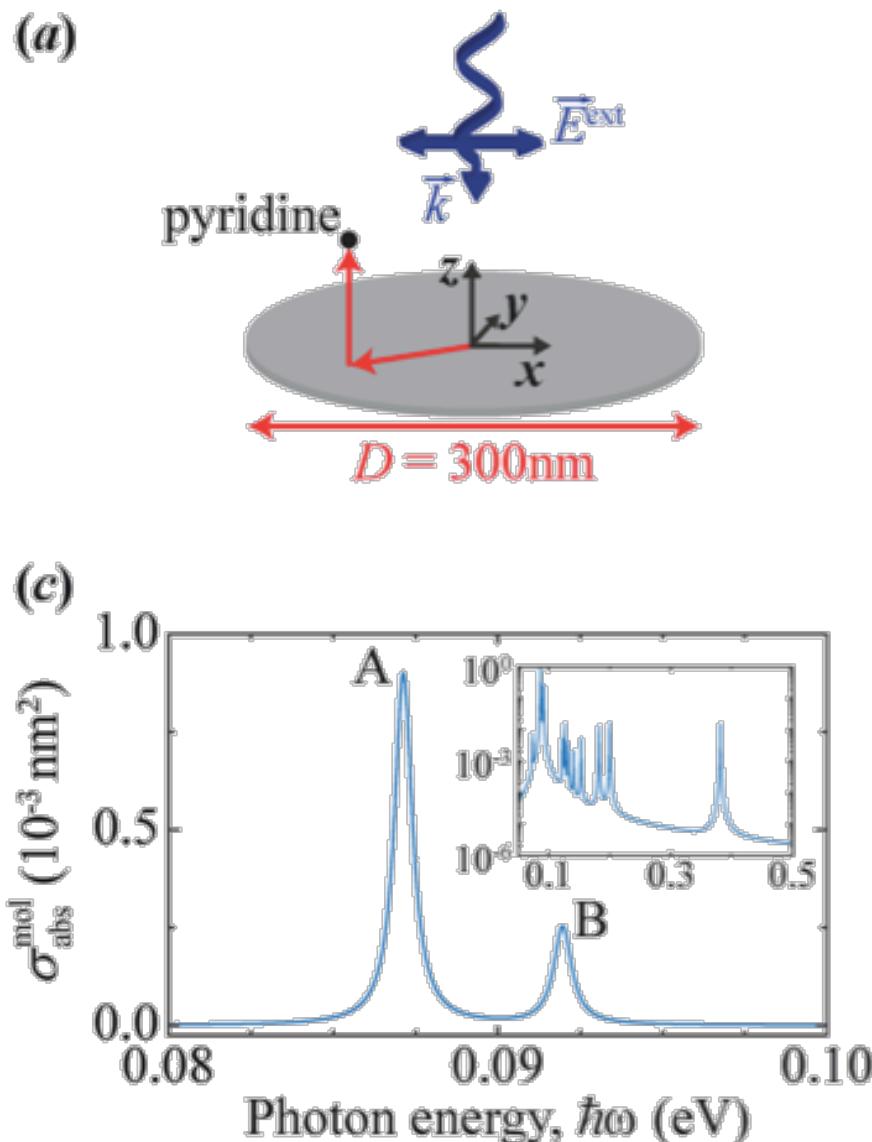
(a)



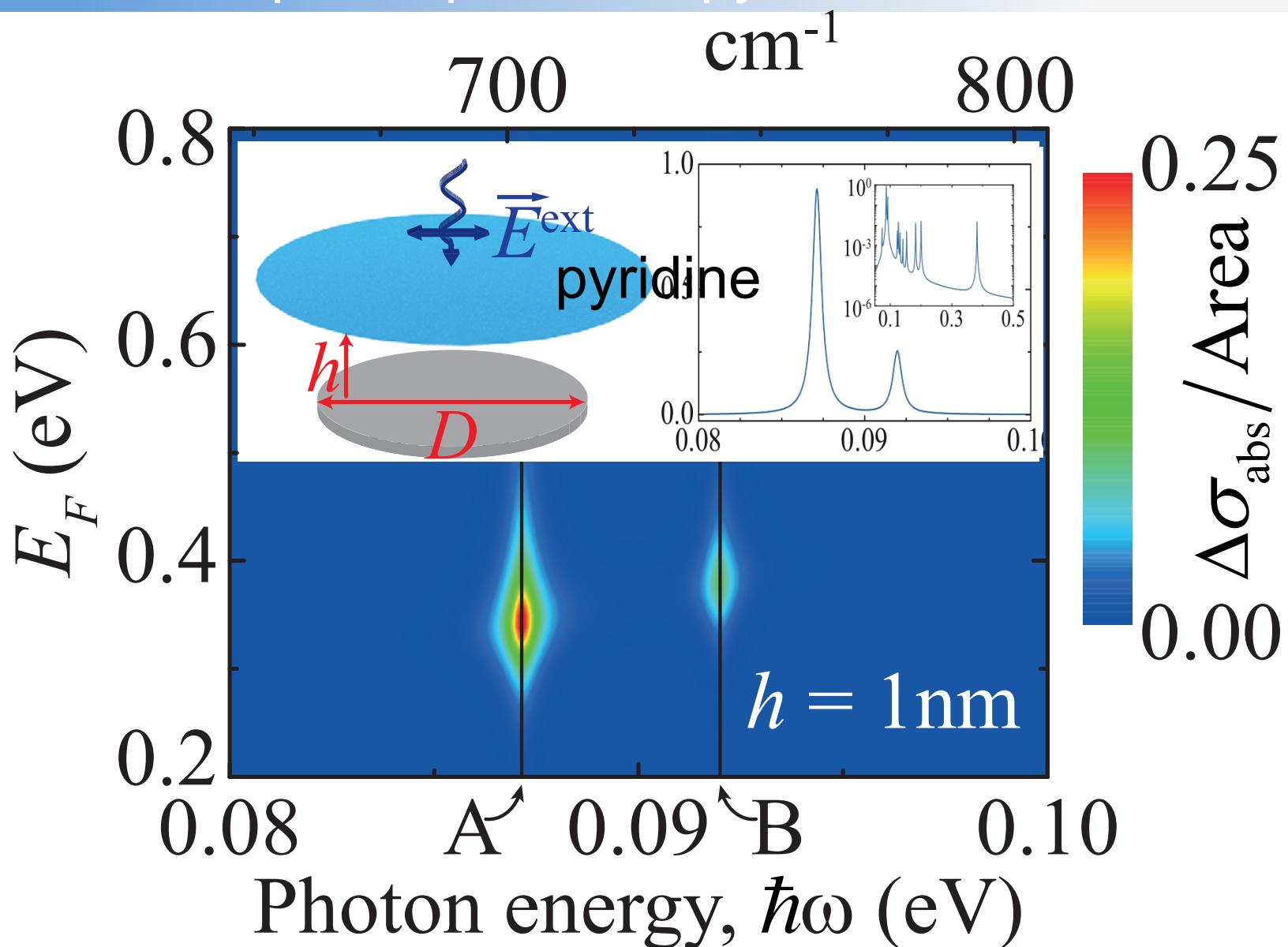
(c)



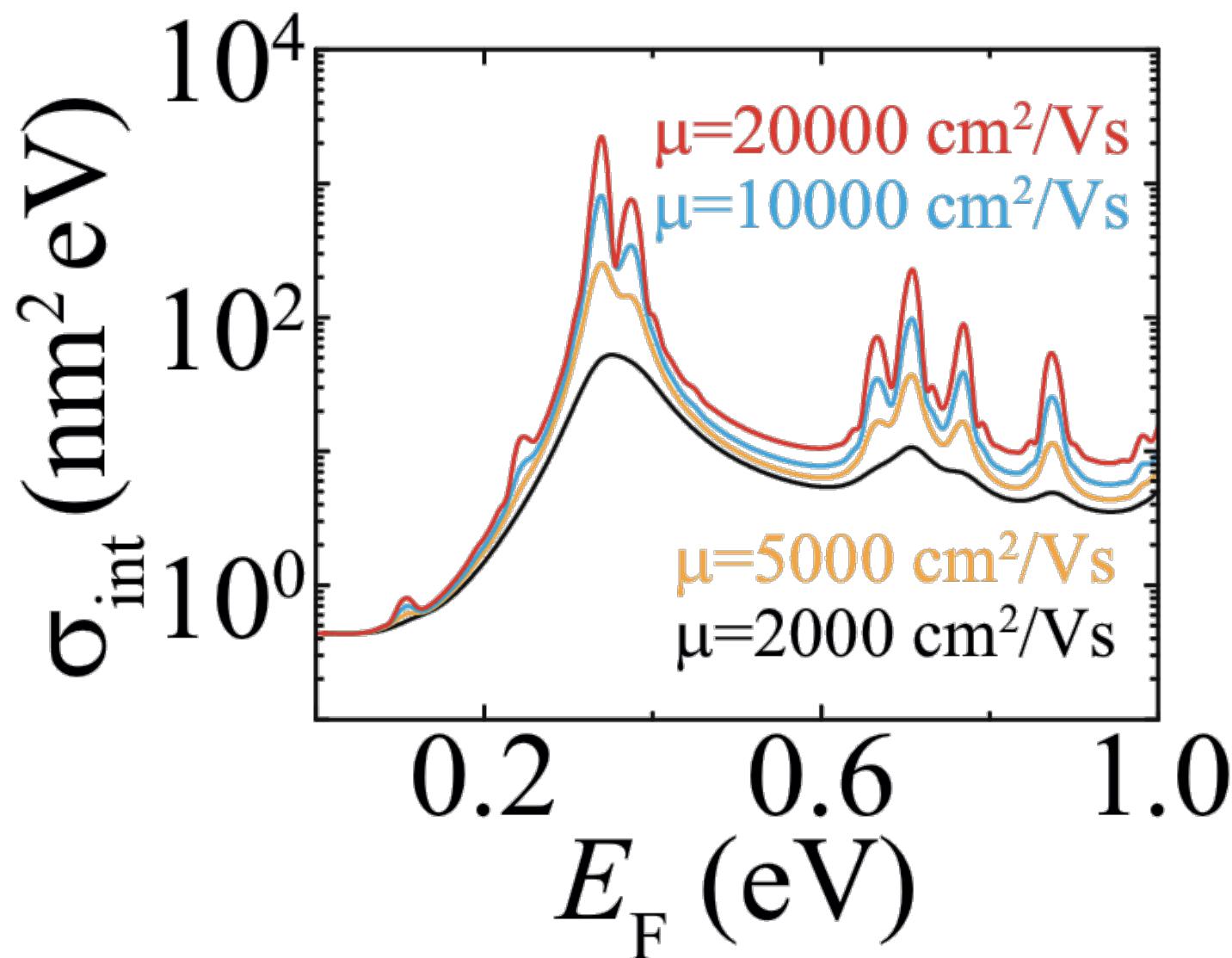
Infrared absorption spectroscopy



Infrared absorption spectroscopy



Infrared absorption spectroscopy



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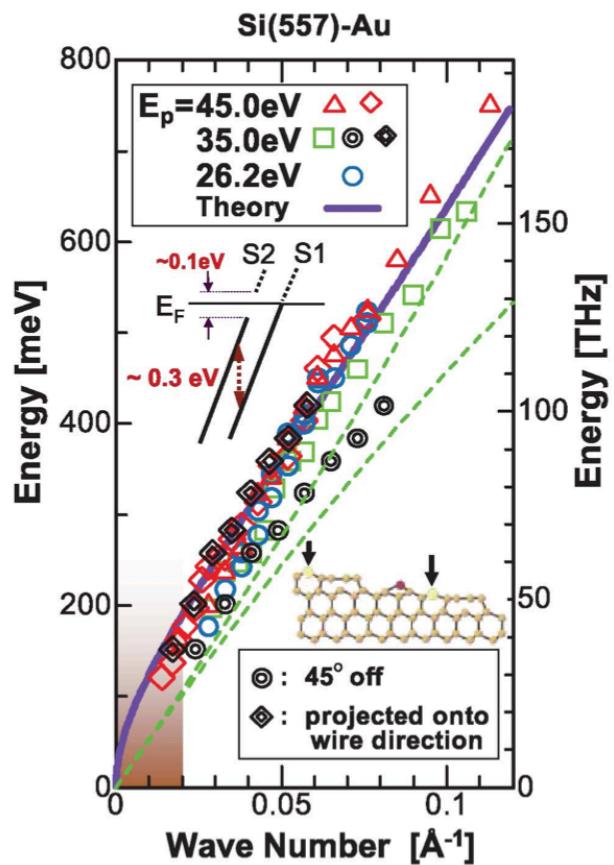
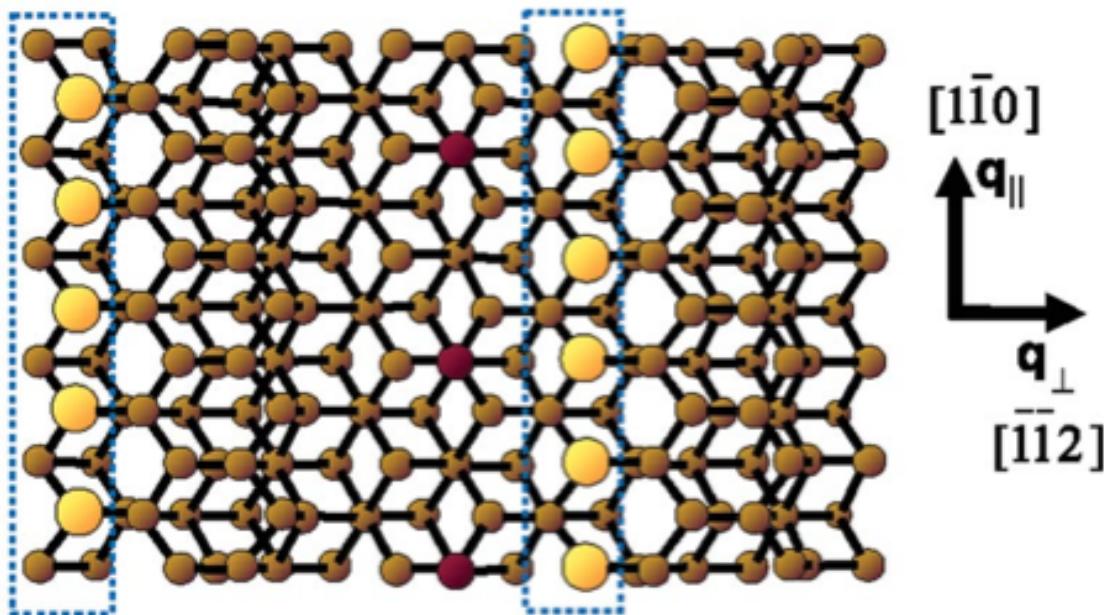
Complete optical absorption

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Sensing with graphene plasmons

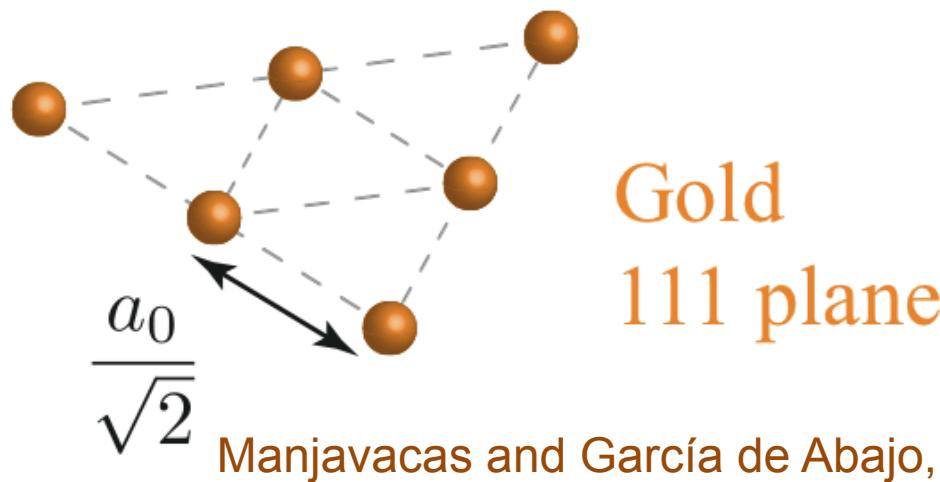
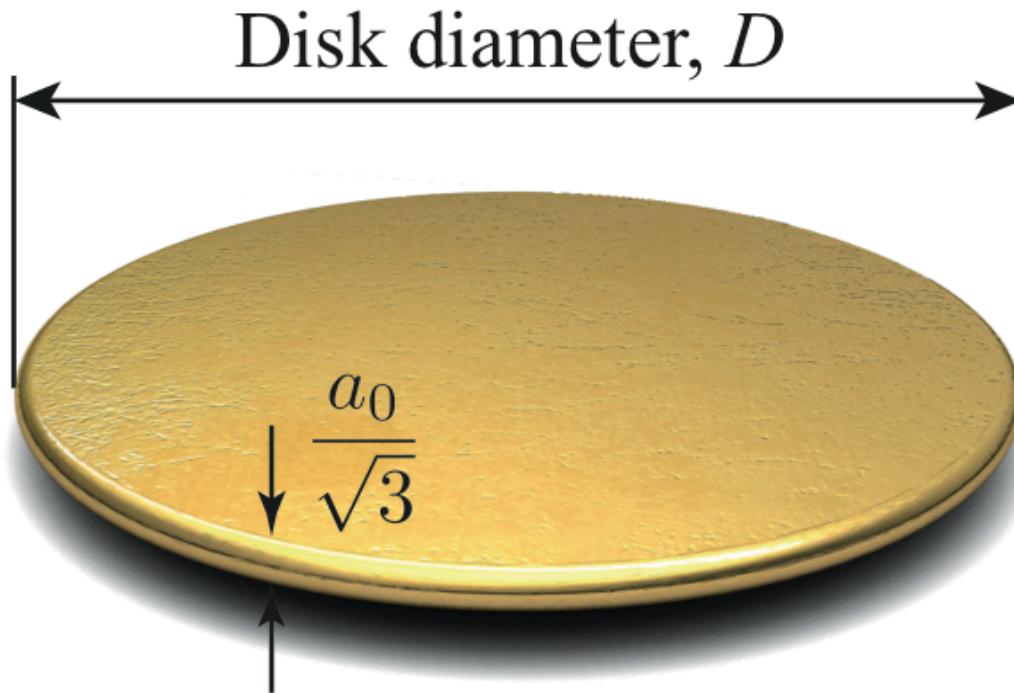
Plasmons in other atomically thin materials

Single-atom-layer metal plasmons

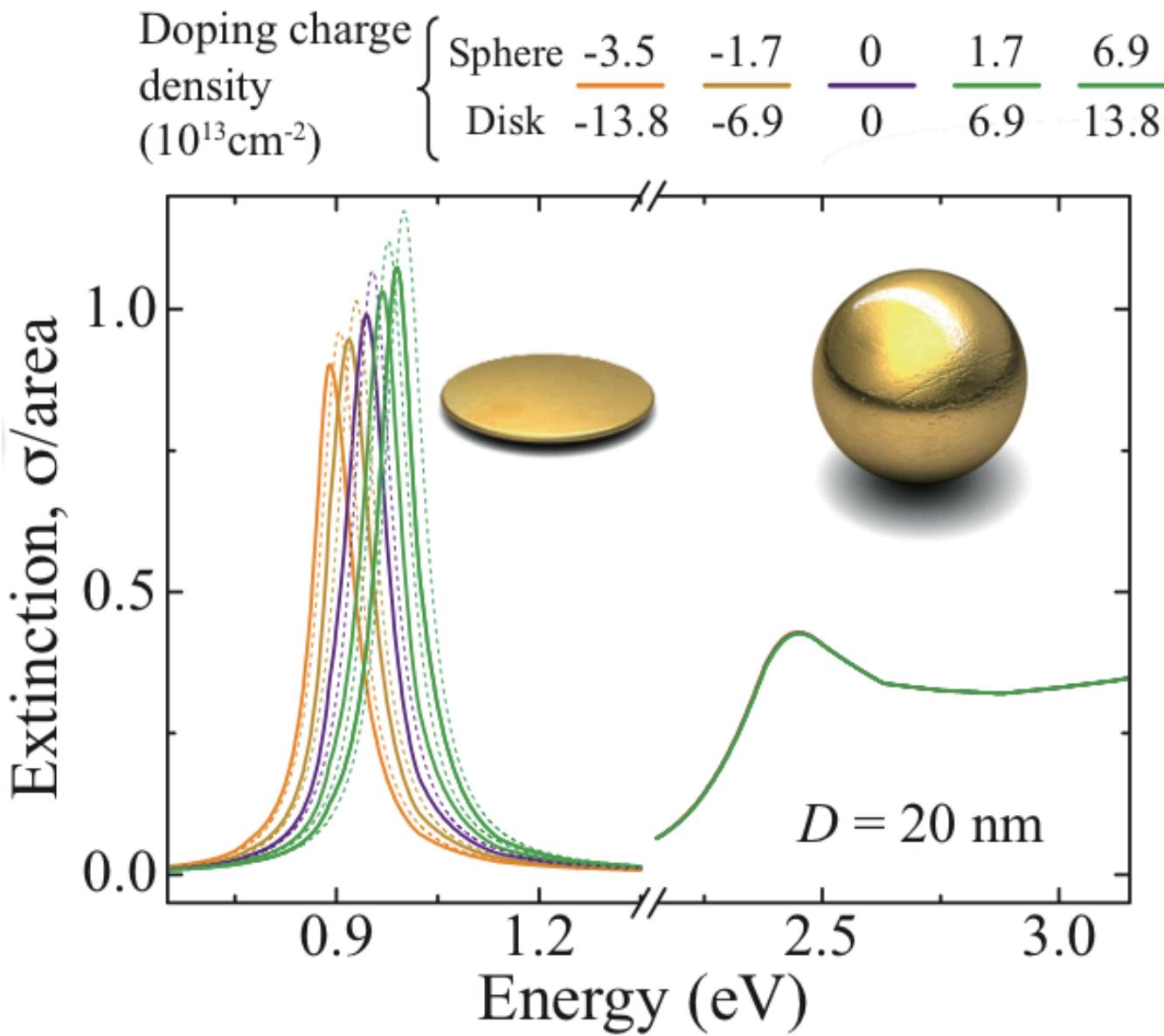


Nagao *et al.*, Phys. Rev. Lett. (2006)

Single-atom-layer metallic structures

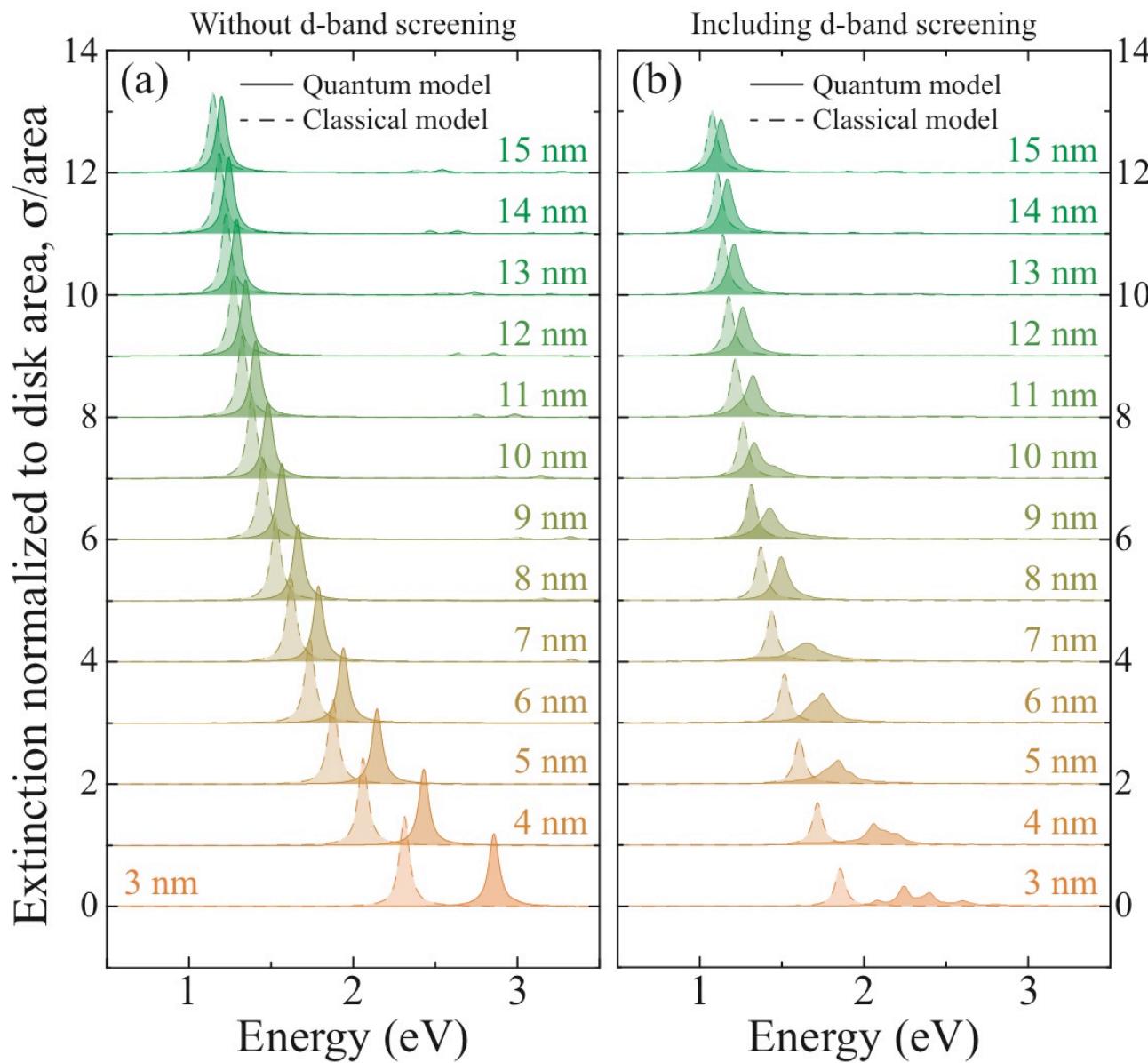


Single-atom-layer metallic plasmons



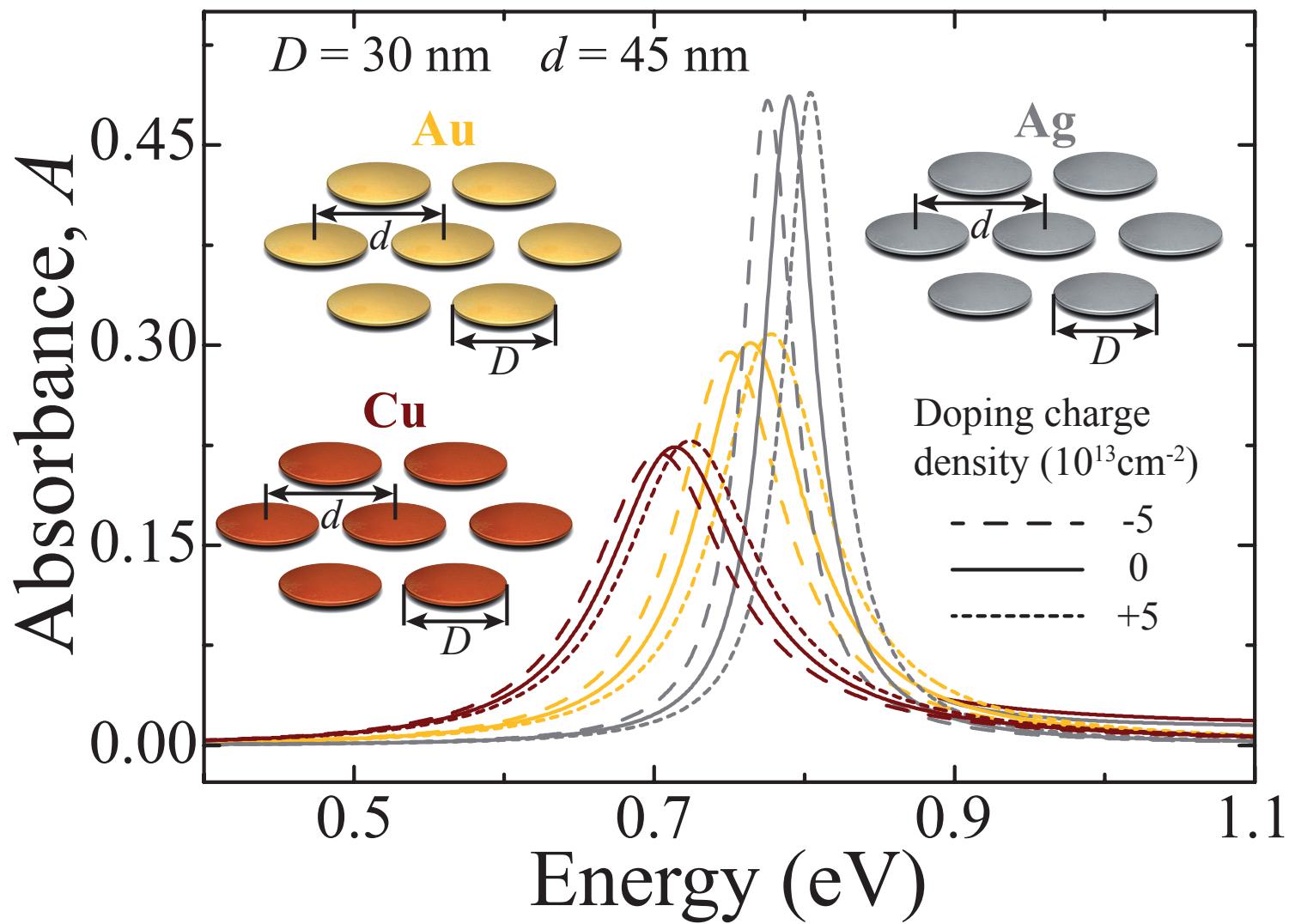
Manjavacas and García de Abajo, Nat. Commun. (2014)

Single-atom-layer metallic plasmons



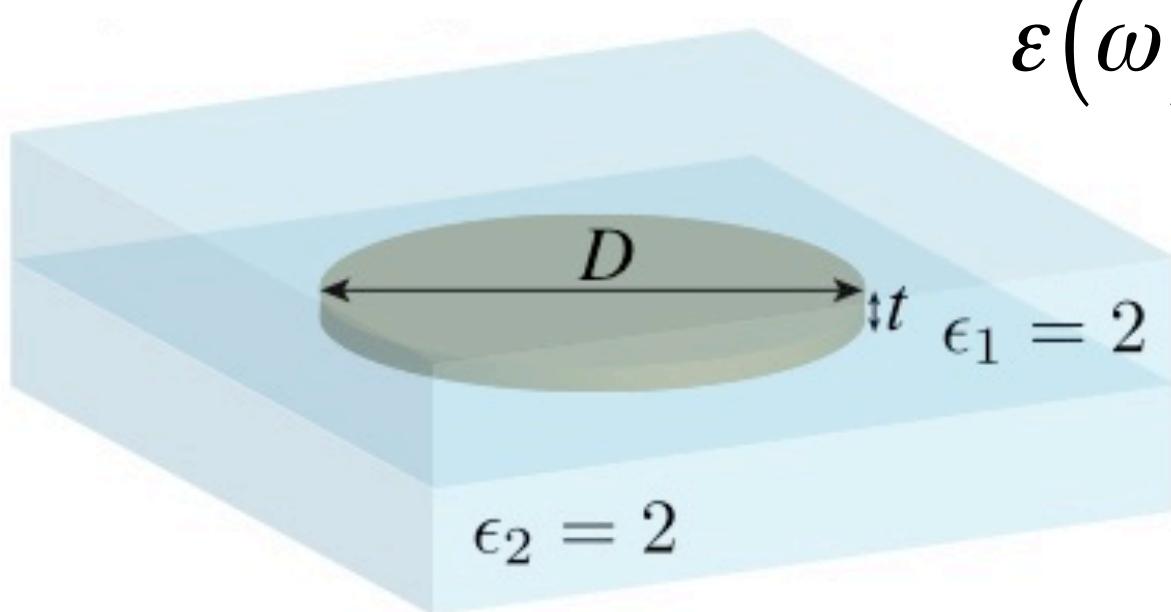
Manjavacas and García de Abajo, Nat. Commun. (2014)

Single-atom-layer metallic plasmons

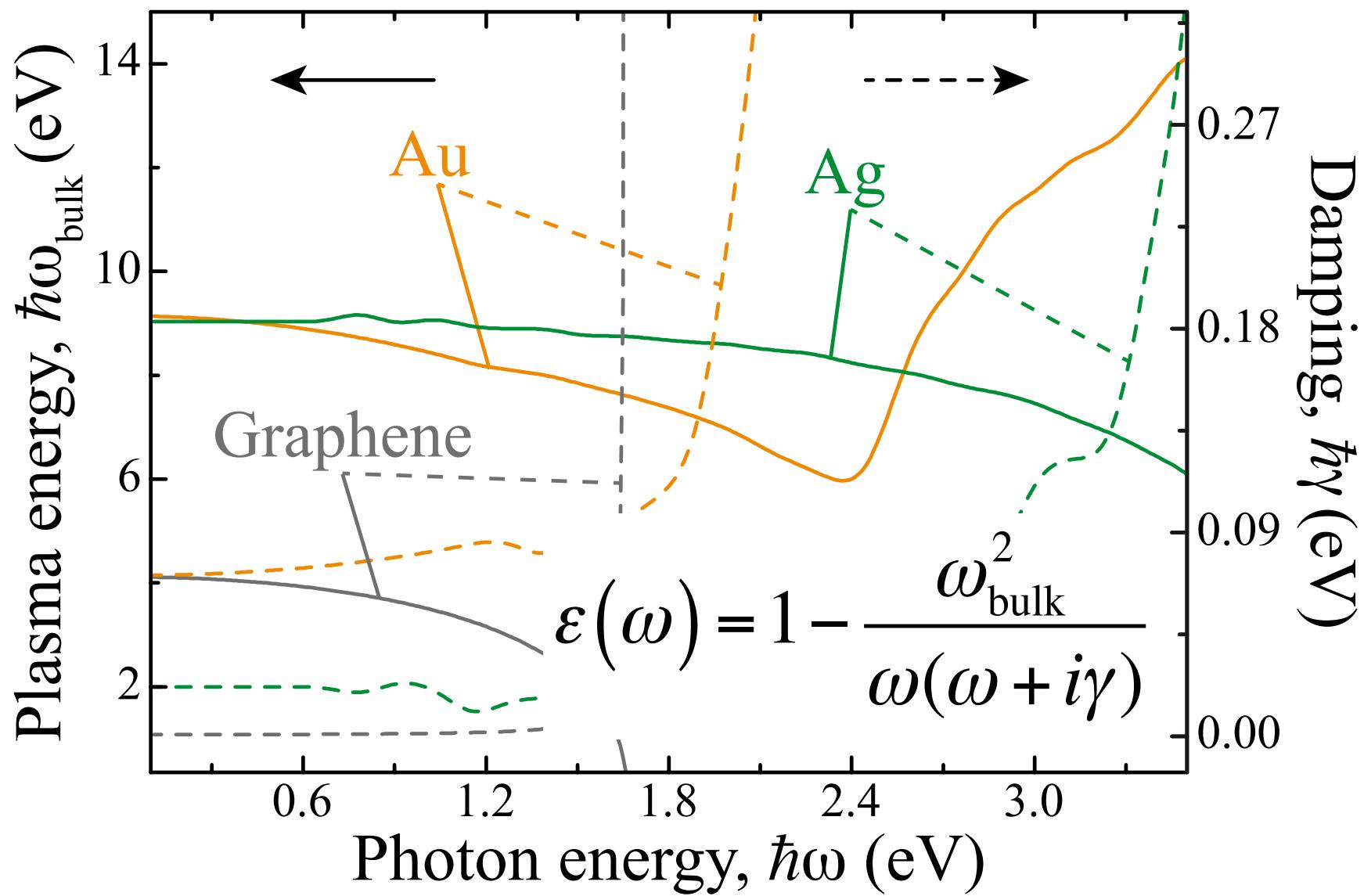


Plasmonics in atomically thin materials

$$\varepsilon(\omega) = 1 - \frac{\omega_{\text{bulk}}^2}{\omega(\omega + i\gamma)}$$

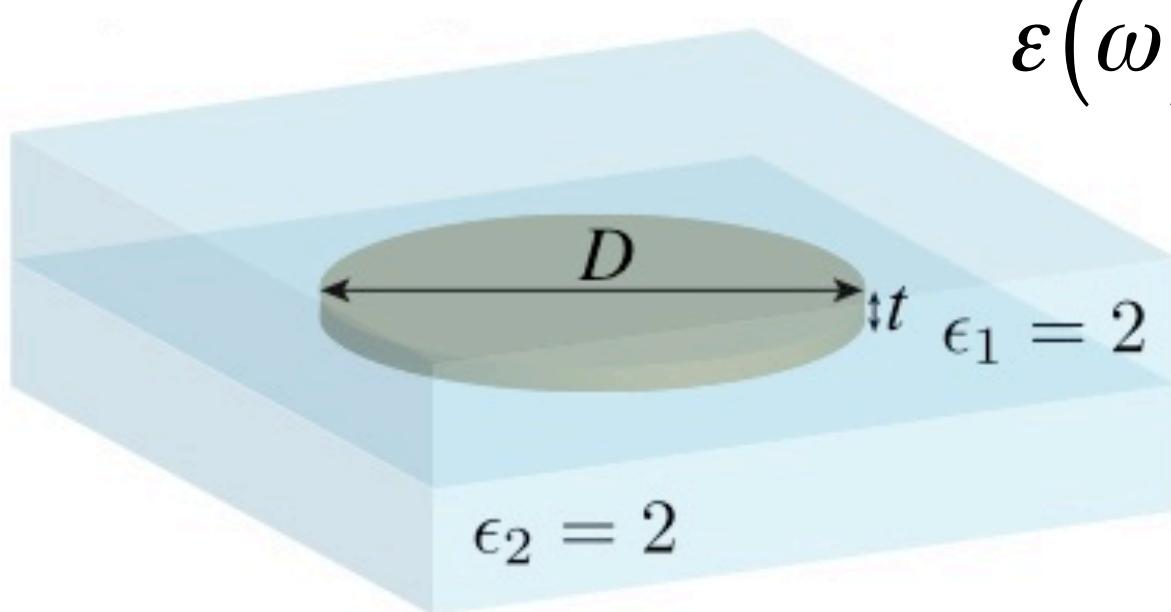


Plasmonics in atomically thin materials



Plasmonics in atomically thin materials

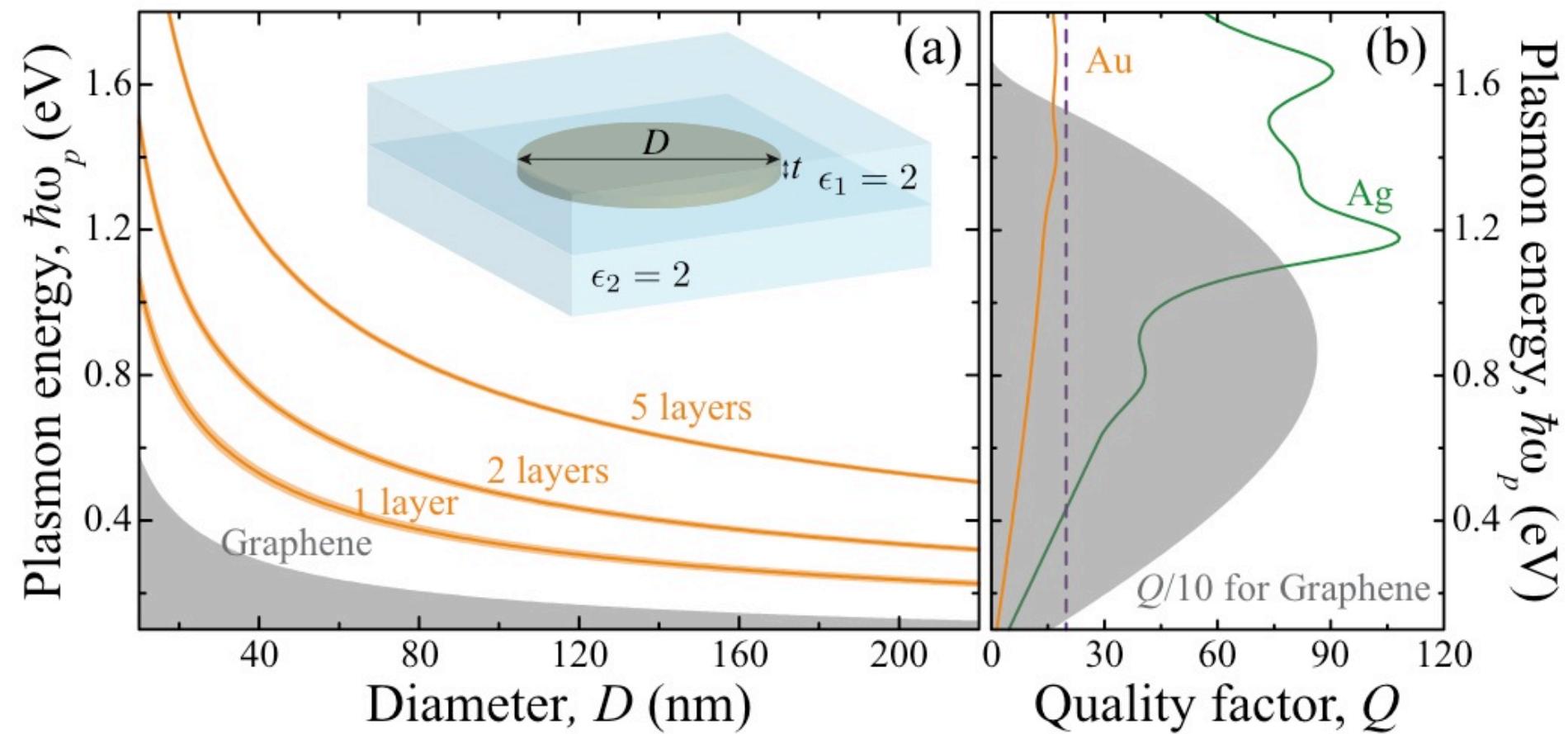
$$\varepsilon(\omega) = 1 - \frac{\omega_{\text{bulk}}^2}{\omega(\omega + i\gamma)}$$



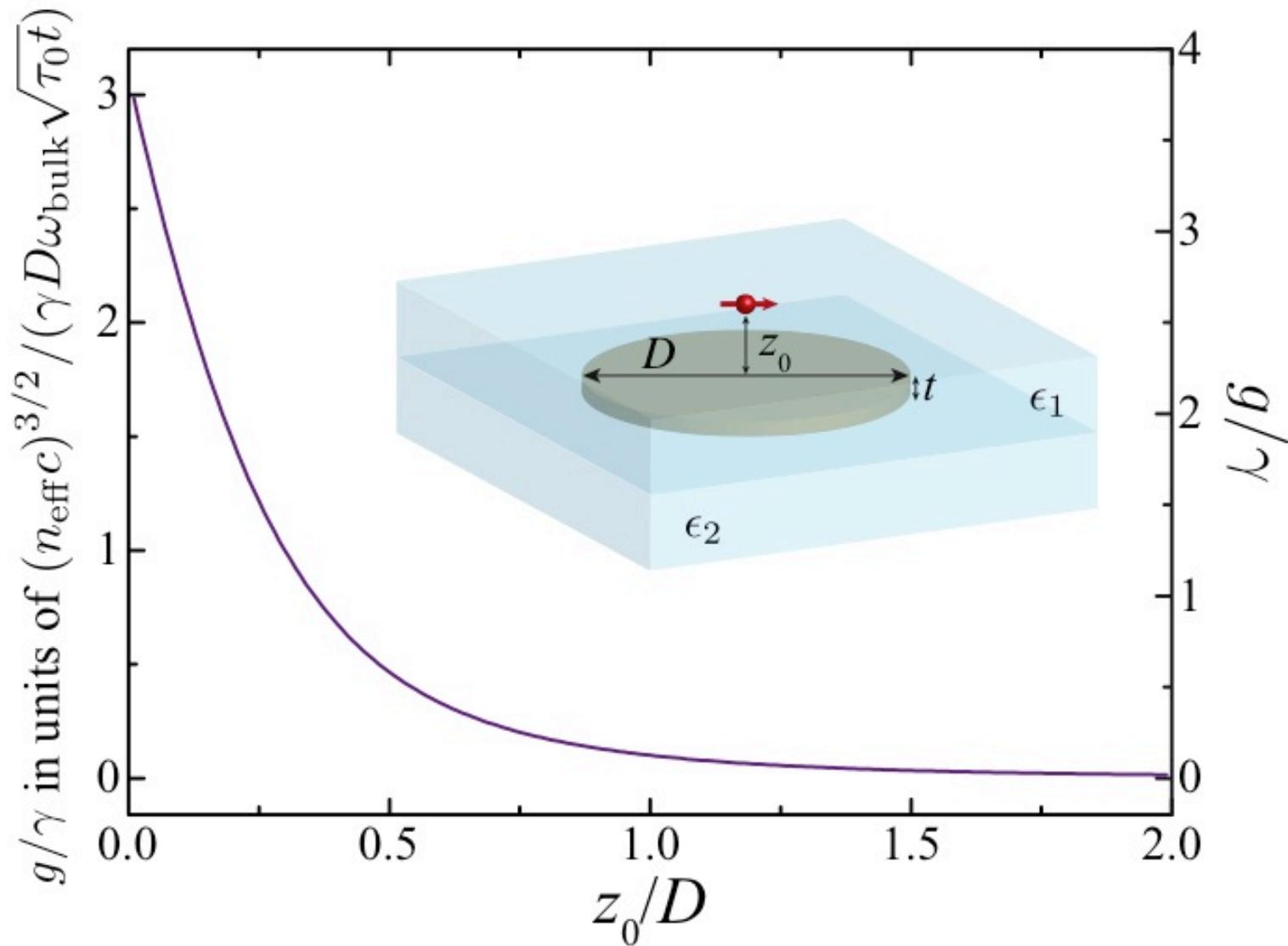
$$\omega_p \approx \frac{\omega_{\text{bulk}}}{n_{\text{eff}}} \sqrt{\frac{3\pi t}{8D}}$$

$$n_{\text{eff}} = \sqrt{(\varepsilon_1 + \varepsilon_2)/2}$$

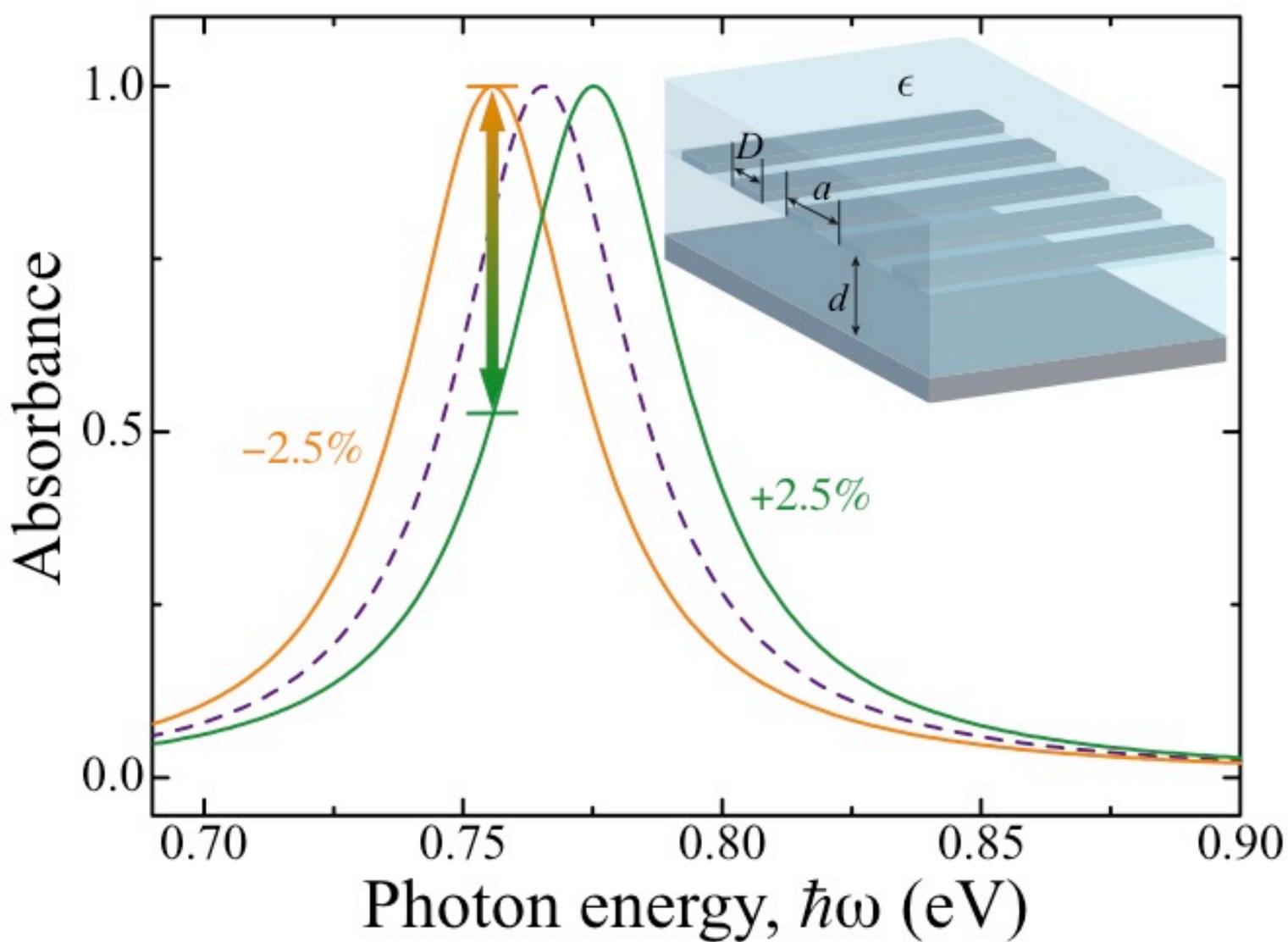
Plasmonics in atomically thin materials



Plasmonics in atomically thin materials



Plasmonics in atomically thin materials

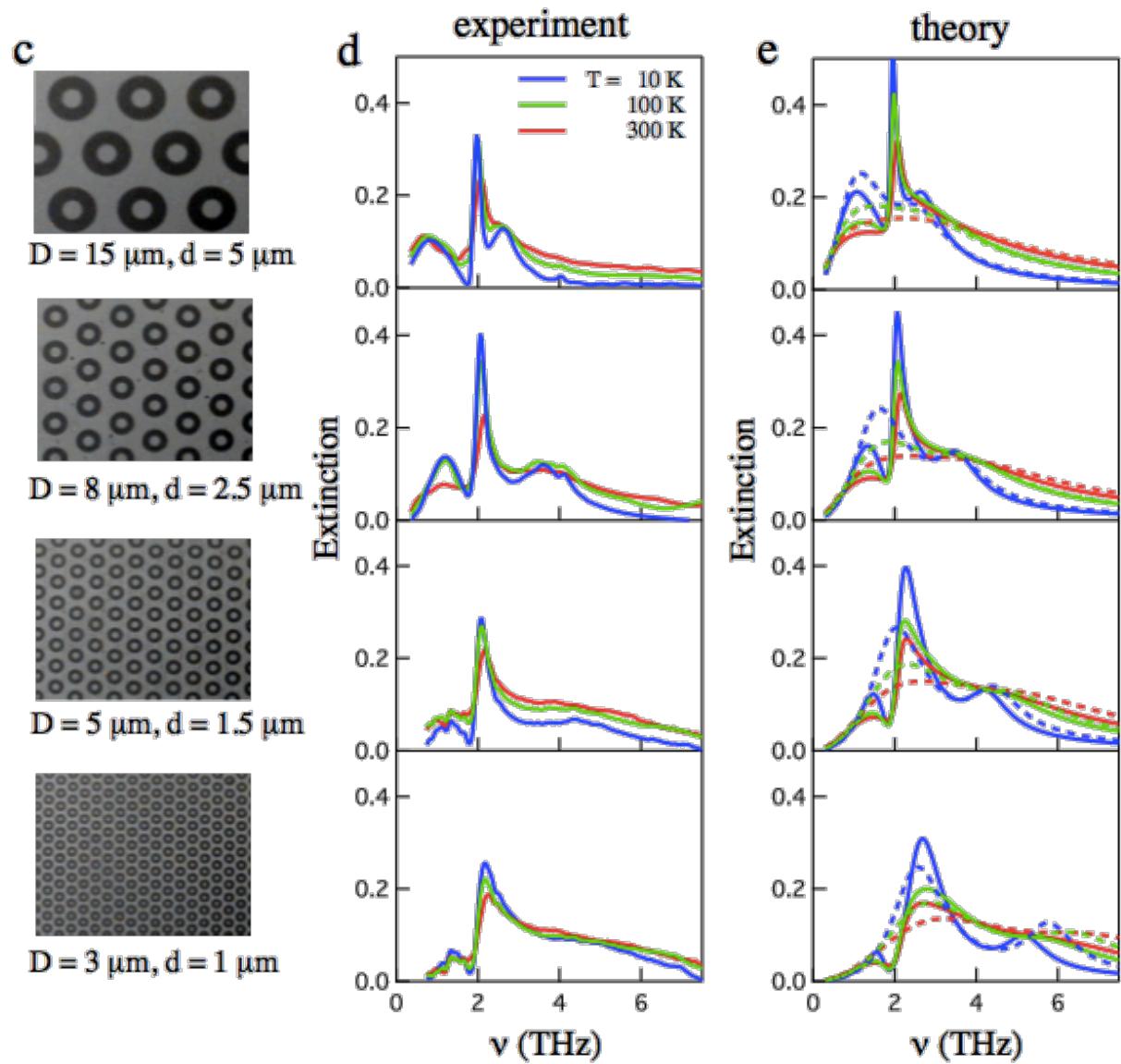


Plasmons in topological insulator rings

2D surface electron band
insulator
2D surface electron band

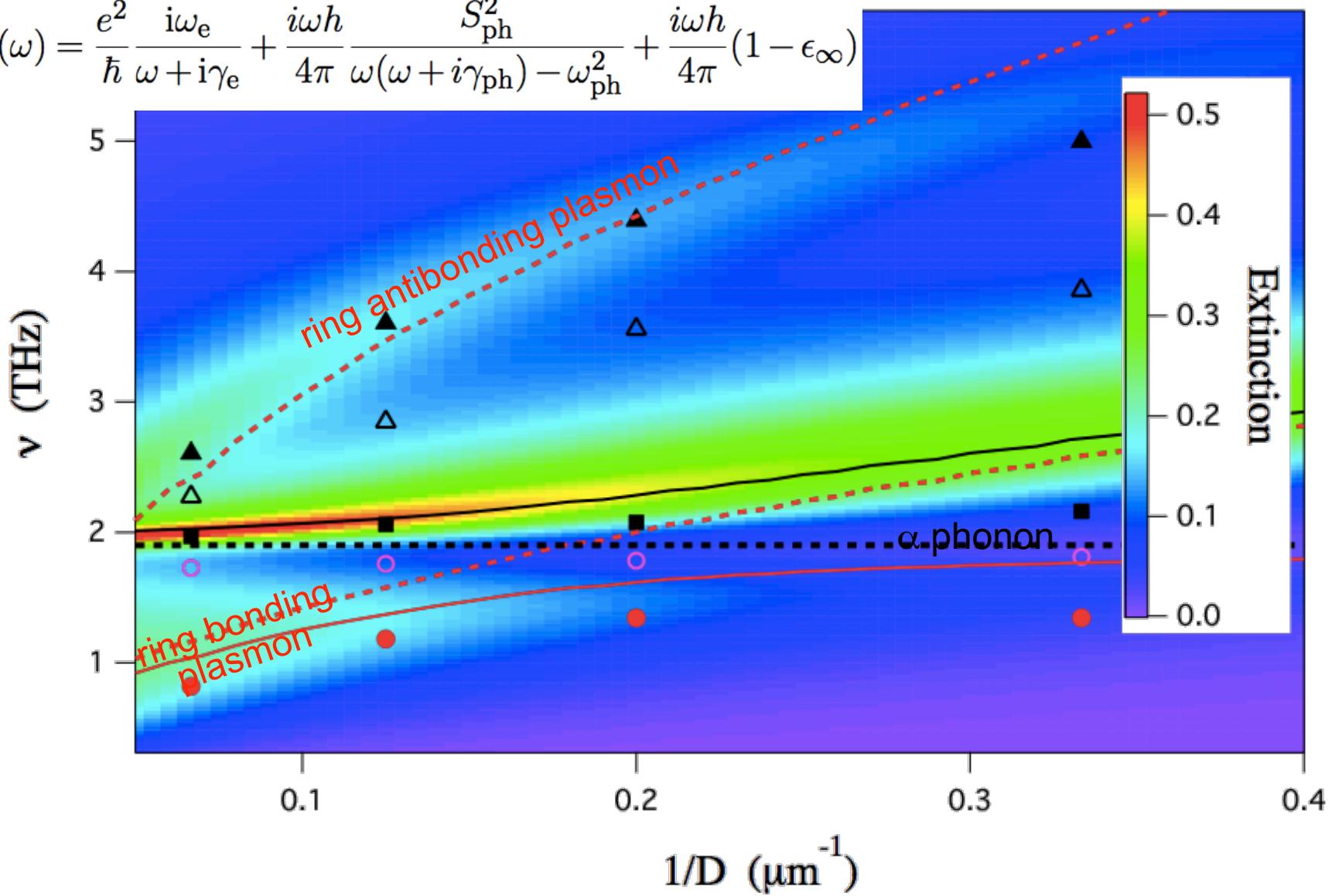
Plasmons in topological insulator rings

2D surface electron band
insulator
2D surface electron band



Plasmons in topological insulator rings

$$\sigma(\omega) = \frac{e^2}{\hbar} \frac{i\omega_e}{\omega + i\gamma_e} + \frac{iwh}{4\pi} \frac{S_{ph}^2}{\omega(\omega + i\gamma_{ph}) - \omega_{ph}^2} + \frac{iwh}{4\pi} (1 - \epsilon_\infty)$$



Further reading

Further reading:

- Myroshnychenko *et al.*, Chem. Soc. Rev. (2008)
- García de Abajo, Rev. Mod. Phys. (2010)
- Koppens, Chang, García de Abajo, Nano Lett. (2011)
- García de Abajo, ACS Photonics (2014) ← arXiv:1402.1969
- Manjavacas and García de Abajo, Nature Commun. (2014)
- García de Abajo and Manjavacas, Faraday Discussions (2015) ← arXiv:1411.4780
- Rodrigo *et al.*, Science (2015) ← arXiv:1506.6800