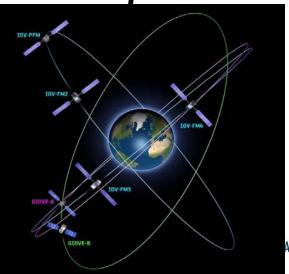


Metrology: from physics fundamentals to quality of life July 2016

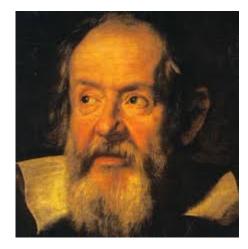
International School of Physics

Precise time scales and navigation systems

Patrizia Tavella Istituto Nazionale Ricerca Metrologica Torino Italy



In 1612 Galileo wrote a letter to the King of Spain, proposing the use of the Juppiter satellites for navigation



"....these stars display conjunctions, separations, eclipses, and other precise configurations...more than 100 a year...and they are so unique, identifiable, and so exact that nobody, of medium intelligence, is not able to use them to estimate the longitude and the position of the ship based on the ephemerids I have computed for the next years to come." Sept 7th, 1612

OBSERVAT. SIDEREAE

Stella occidentaliori maior, ambæ tamen valdè confpicuæ, ac fplendidæ : vtra quæ diftabat à loue fcrupulis primis duobus; tertia quoque Stellula apparere cepit hora tertia prius minimè confpecta, quæ ex parte orientali louem ferè tangebat, cratque admodum exigua. Omnes fuerunt in cadem recia, & fecundum Eclypticæ longitudinem coordinatæ.

Die decimatertia primum a me quatuor confpectæ fuerunt Stellulæ in hac ad louem conftitutione. Erant tres occidentales, & vna orientalis; lineam proximè

ri. = ()+* = Occ:

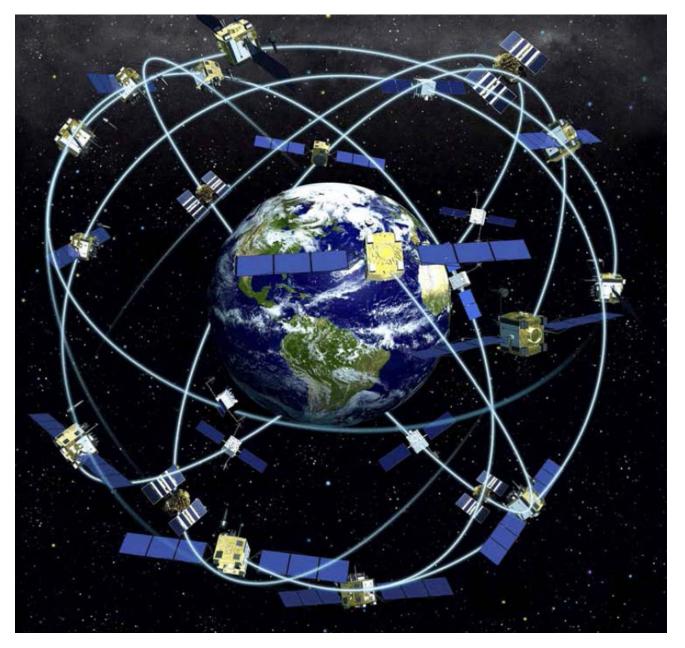
rectam conftituebant; media enim occidétalium paululum à recta Septentrionem verfus deflectebat. Aberat orientalior à loue minuta duo: reliquarum, se louis intercapedines erant fingulæ vnius tantum minuti. Stellæ omnes candem præfe ferebant magnitudinem; ac licet exiguam, lucidiffimæ tamen erant, ac fixis eiufdem magnitudinis longe fplendidiores. Die decimaguarta nubilofa fuit tempeftas.

Die decimaquinta, hora noctis tertia in proximè depicta fuerunt habitudine quatuor Stellæ ad Iouem;

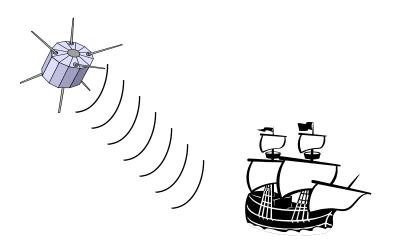
occidentales omnes: ac in eadem proxim recta linea dispositæ; quæ enim tertia à loue numerabatur paululum

Occ.

Navigation by "moon" observation







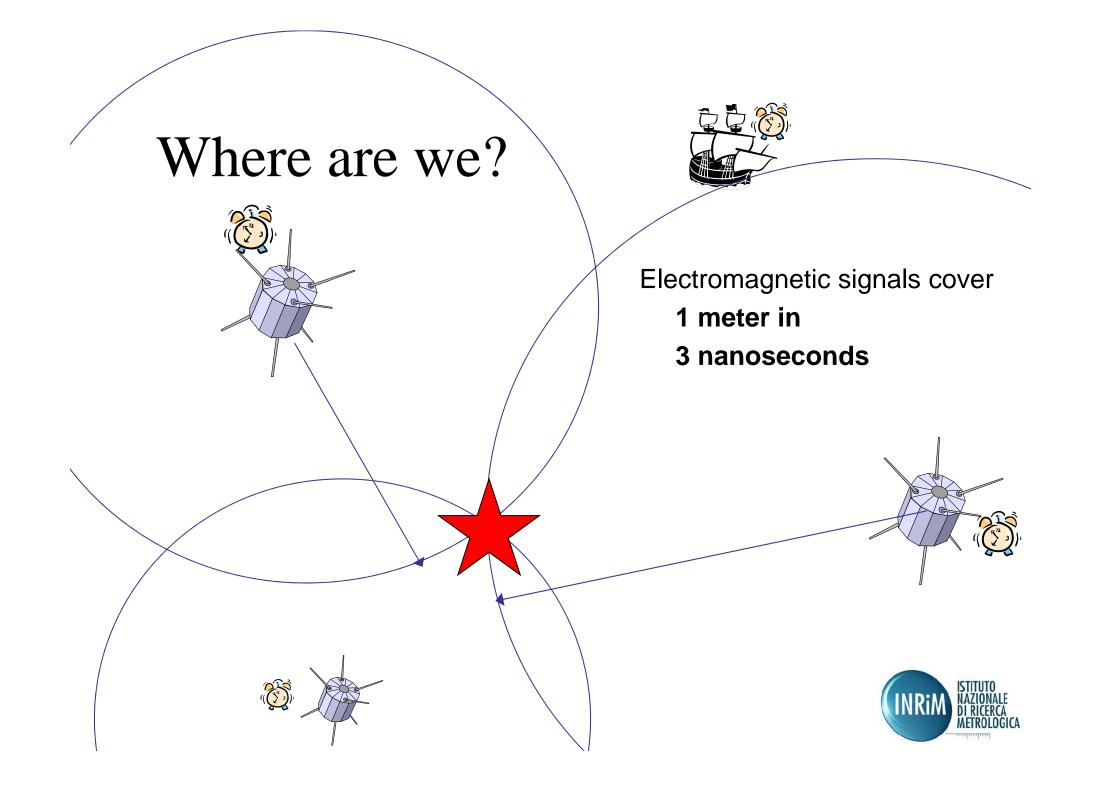
In spherical navigation

position is estimated by measuring *distance* from 3 known fixed points



the *distance* measurement are measurement of the flight *time* of an electromagnetic signal





We therefore need:



good clocks (on Ground and in Space)

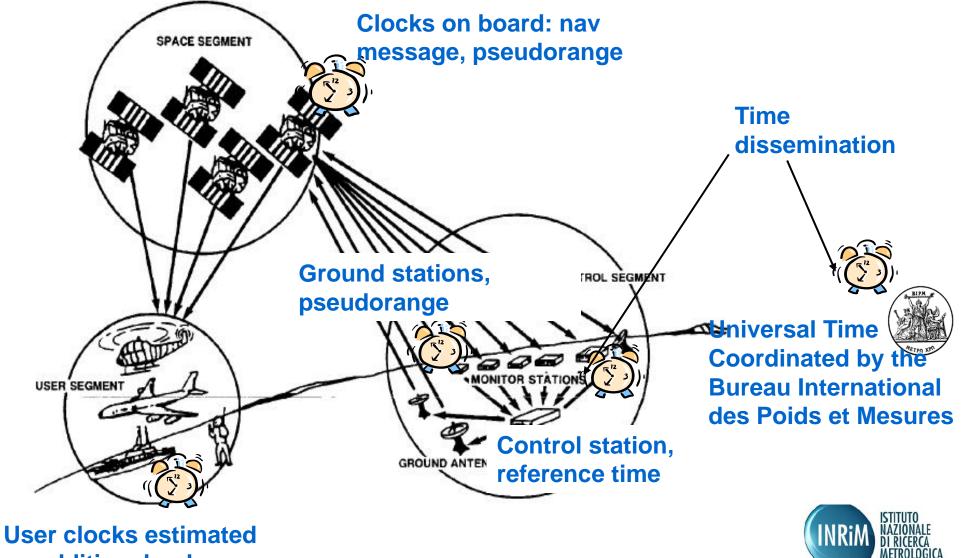
good clock synchronisation system

good reference time scale

good algorithms for clock evaluation in timekeeping and navigation



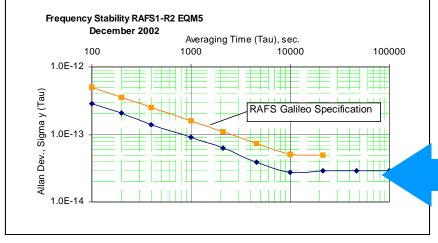
GNSS: Where are the clocks and why?



as additional unknown

Galileo clocks: space





Space Rubidium Atomic Frequency Standard (RAFS)

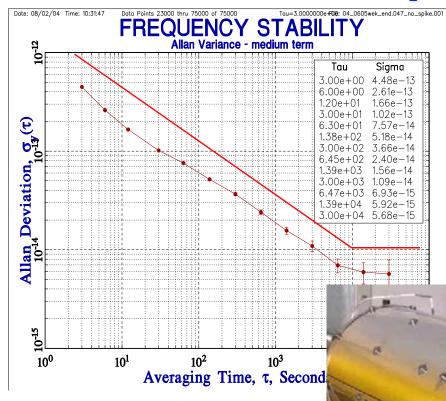


measured data



Galileo clocks: space

SV.



FIRST Space H-Maser Atomic Clocks

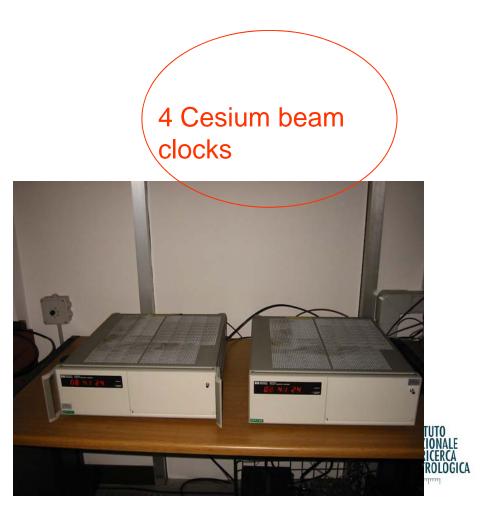




Galileo clocks: ground

Ground Clocks inside the Control Centres



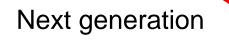


Cryogenic cesium Fountain INRIM ITCsF2

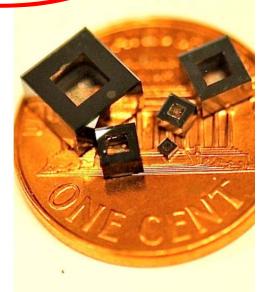
Relative accuracy 2x10⁻¹⁶







Ground clocks

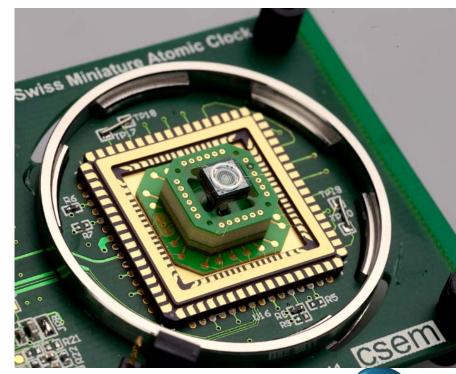


http://www.nist.gov/pml/div688/grp90/index.cfm

They could be implemented in GNSS receivers to improve the positioning (altitude estimate), reduce the noise of the phase measures, allowing holdover navigation ...

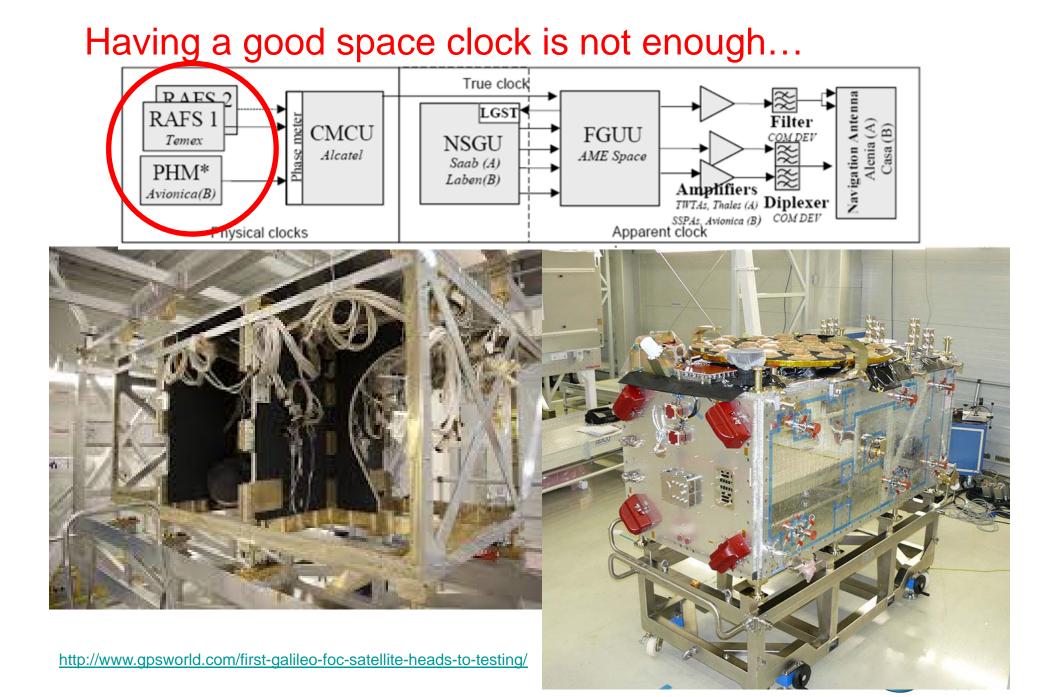
Miniaturized atomic clocks

New conception of miniaturized clocks is leading towards atomic clocks of a few mm dimension



Close-up on the physics package of the Swiss Miniature Atomic Clock , $24x24 \text{ mm}^2$





Relativity effects

With atomic clock on board

relativistic effect are common routine

Travelling clock are slowing down Clock at high altitude are going faster

The relative effect is 10⁻¹³ / km 3 microsec / year for one km in altitude

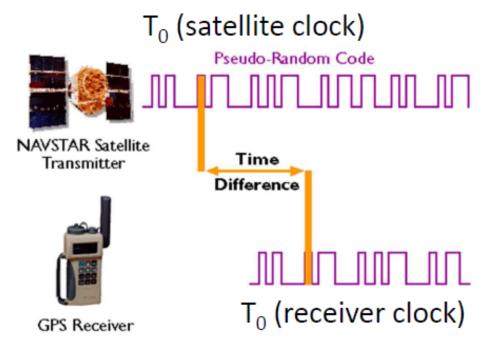
On board GPS/Galileo at 20000 km The effect is about 4 10⁻¹⁰ which means 40 microseconds in a day corresponding to about 10 km error in positioning in one day



The clock signal is emitted from space and then measured on ground

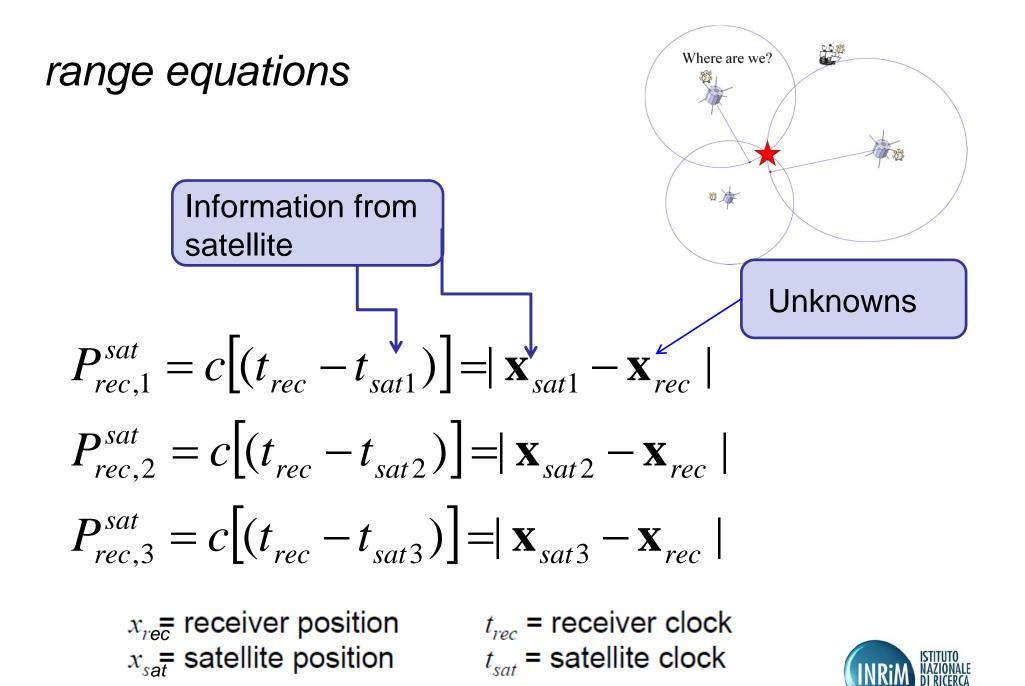
GNSS Code measurement

Courtesy of P.Defraigne, ORB

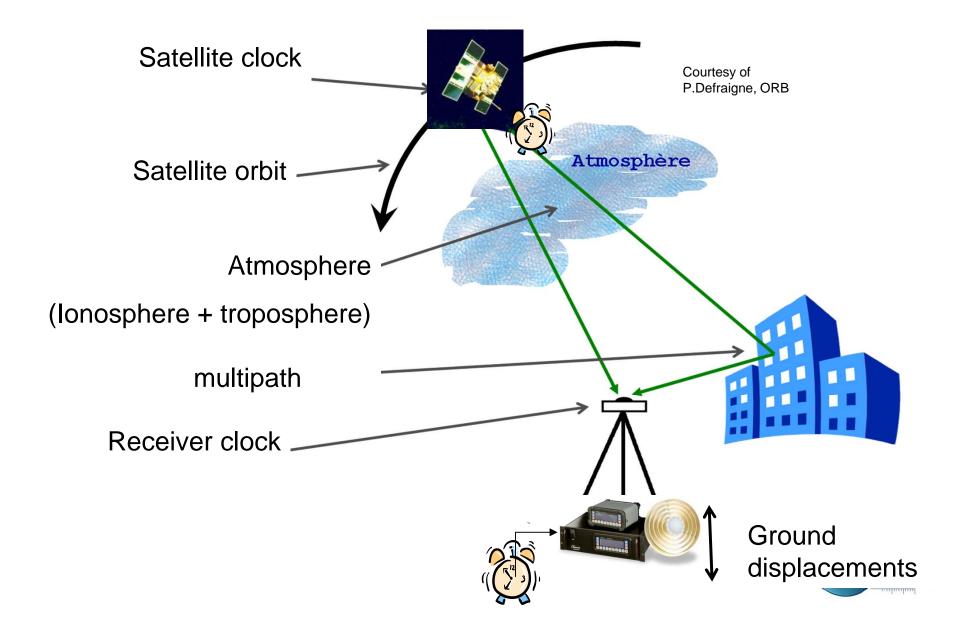


Distance = Speed of Light • Time Difference





From space clock to ground receiver

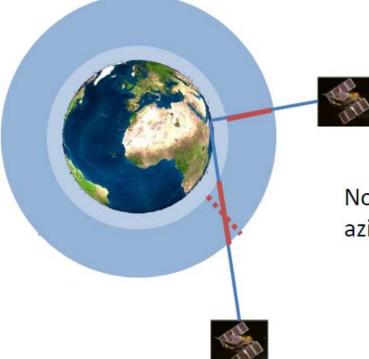


Observation equations Range : Atmosphère $P_{rec,1}^{sat} = c \left[(t_{rec} - t_{sat1}) \right] = |\mathbf{x}_{sat1} - \mathbf{x}_{rec}|$ Unknowns to be Pseudorange : estimated Clock error versus tref $P_{rec,1}^{sat} = c \left[(t_{rec} - t_{sat}) \right] = \int_{\mathbf{x}_{sat}} \mathbf{x}_{rec} | + c \left[(t_{rec} - t_{ref}) \right]$ $\underbrace{(t_{sat} - t_{ref})}_{F} + I_{rec,1} + Tr + \delta_{rec,1} + \varepsilon_{rec,1},$ Hardware delay tropo iono Information from satellite $x_{ro} =$ receiver position t_{rec} = receiver clock t_{ref} = reference time x_{sat} = satellite position t_{sat} = satellite clock **METROLOGICA**

The ionosphere is due to the to solar radiation, which ionizes the atoms and molecules in the upper atmosphere, producing a sea of ions and free electrons

Ionosphere

Layer of electrons and electrically charged atoms and molecules that surrounds the Earth, 50 km \rightarrow ~1000 km.



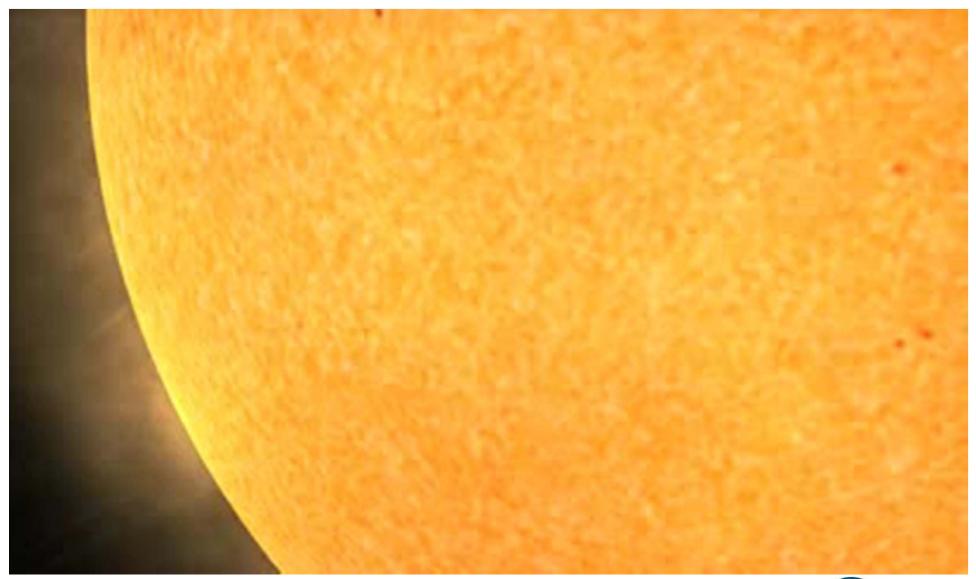
Effects on GNSS signal :

- 0-15 m at high elevation
- Up to 45 m at low elevation

Not same iono for different azimuth-elevation



Solar flares shape ionosphere

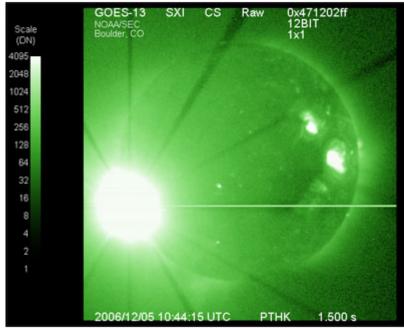




GPS significantly impacted by powerful solar radio burst

NOAA NEWS RELEASE Posted: April 4, 2007

During an unprecedented solar eruption last December, researchers at Cornell University confirmed solar radio bursts can have a serious impact on the Global Positioning System (GPS) and other communication technologies using radio waves. The findings were announced Wednesday in Washington, D.C., at the first Space Weather Enterprise Forum an assembly of academic, government and private sector scientists focused on examining the Earth's ever-increasing vulnerability to space weather impacts.



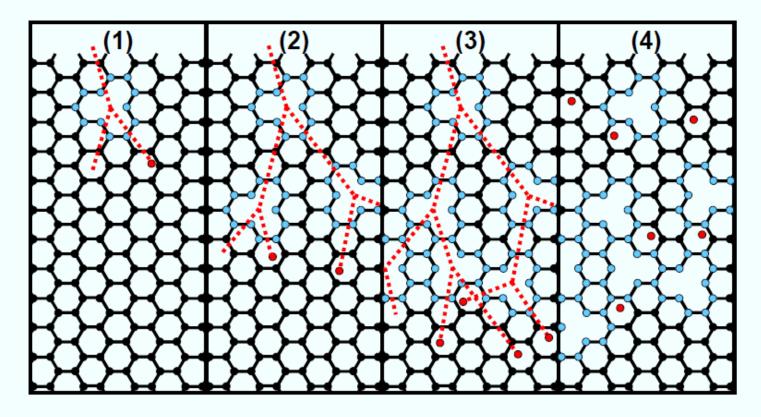
A satellite image of the Dec. 5, 2006, solar flare that caused the following day's intense radio burst that affected GPS systems. Credit: NOAA



https://www.ras.org.uk/news-and-press/news-archive/157-news space-storms-could-threaten-the-uk-power-grid



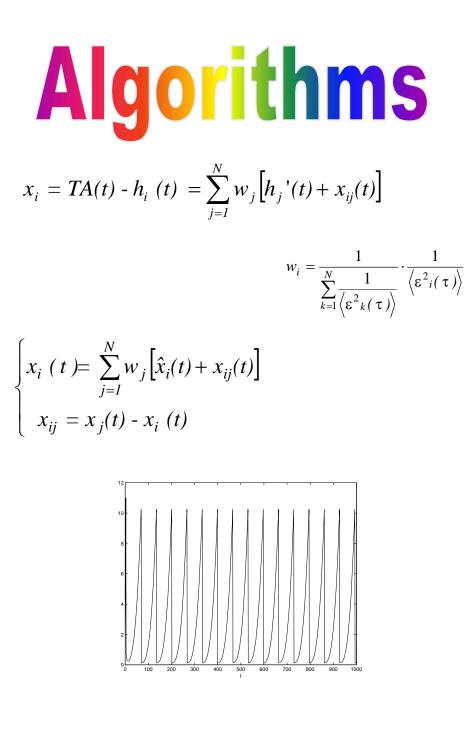
Solar flare effect on quartz clocks Neutron Damage

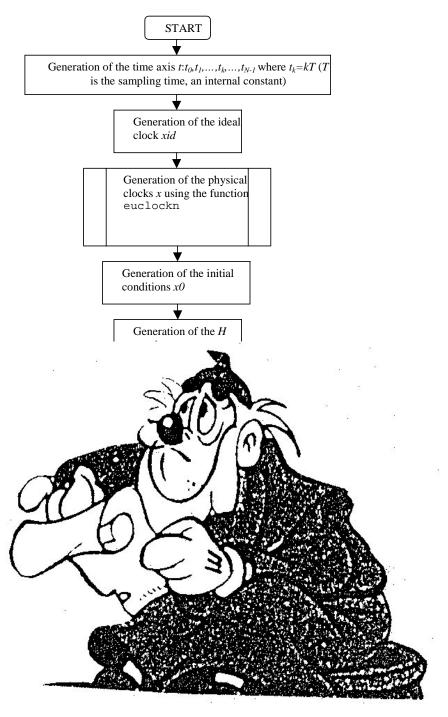


A fast neutron can displace about 50 to 100 atoms before it comes to rest. Most of the damage is done by the recoiling atoms. Net result is that each neutron can cause numerous vacancies and interstitials.

J. Vig, PTTI 2004, Tutorial, http://www.umbc.edu/photonics/Menyuk/Phase-Noise/Vig-tutorial_8.5.2.2.pdf







$$P_{rec,1}^{sat} = c[(t_{rec} - t_{sat})] =$$
Satellite clock error =offset versus the Ref time
$$|\mathbf{x}_{sat} - \mathbf{x}_{rec}| + c[(t_{rec} - t_{ref}) - (t_{sat} - t_{ref})] + I_{rec,1} + Tr + \delta_{rec,1} + \varepsilon_{rec,1},$$

- 1. t_{ref} is the System *Reference* Time to be defined from the *ensemble* of space/ground clocks (as any national ref time scale)
 - □ GPS time is a paper time scale estimated with a Kalman filter and *steered* versus UTC(USNO),
 - Galileo System Time is a weighted average of the ground clocks steered versus UTC
- 2. The offset t_{sat} t_{ref} is estimated by a complex algorithm using the same pseudorange measures and estimating orbits and clocks (Kalman filter in case of GPS, Batch least square in case of Galileo, ...)
- 3. The real time offset t_{sat} t_{ref} transmitted to the user is a prediction based on previous measures



$$P_{rec,1}^{sat} = c[(t_{rec} - t_{sat})] = P_{redicted \ clock \ error} \\ | \mathbf{x}_{sat} - \mathbf{x}_{rec} | + c[(t_{rec} - t_{ref}) - (t_{sat} - t_{ref})] + I_{rec,1} + Tr + \delta_{rec,1} + \varepsilon_{rec,1},$$

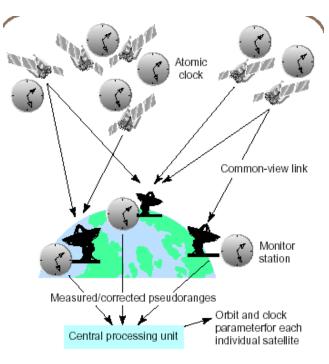
Predicted clock offsets (and predicted orbits) are estimated on ground and uploaded to the satellite

They are transmitted to the user as part of the navigation message and should be valid for a certain period in the future (GPS needs one day validity, Galileo plans 100 minutes validity, ...)

The uploaded navigation message contains

predictions

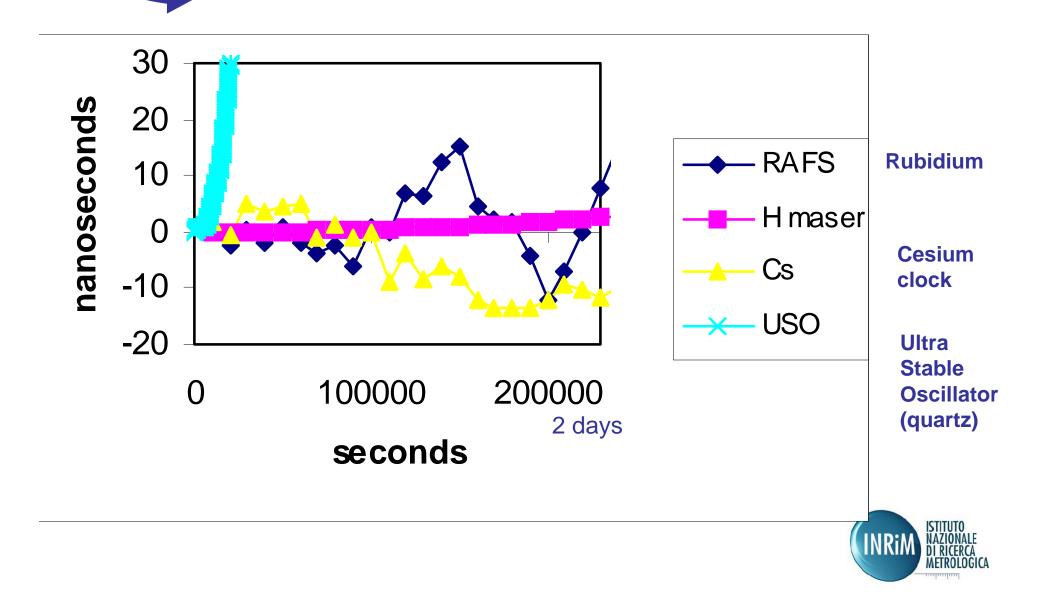
orbit prediction, clock prediction...





After synchronisation, any clock accumulate an error

Galileo requirement for maximum offset = 1.5 ns



The clock signal affected by White and Random Walk
frequency noises plus deterministic drifts can be handled
exactly withtochastic differential equations.stochastic differential equations.Iterative solution useful
for simulations, filter, ...

Phase deviation
Freq component
$$\begin{aligned}
X_1(t_{k+1}) &= X_1(t_k) + X_2(t_k)\tau + a\frac{\tau^2}{2} + \sigma_1 W_{1,k}(\tau) + \sigma_2 \int_{t_k}^{t_{k+1}} W_2(s) ds \\
X_2(t_{k+1}) &= X_2(t_k) + a\tau + \sigma_2 W_{2,k}(\tau)
\end{aligned}$$
with initial conditions
$$\begin{aligned}
X_1(0) &= x_0 \\
X_2(0) &= y_0
\end{aligned}$$
Integration

INRIM INRIM I RICERCA METROLOGICA Stochastic processes helps the clock prediction

Example: White frequency noise

0.015

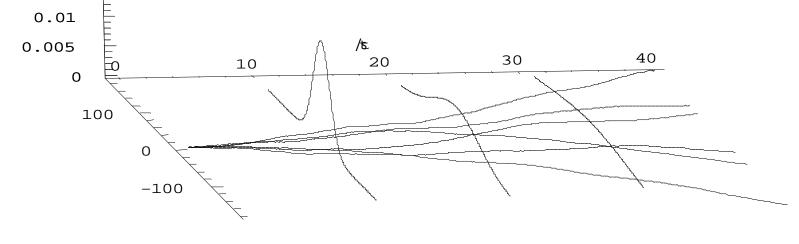


Random walk of phase x(t)

At time t after synchronisation, the time error x(t) is described by a Gaussian probability density with Diffusion coefficient

Diffusion coefficient linked to Allan Deviation

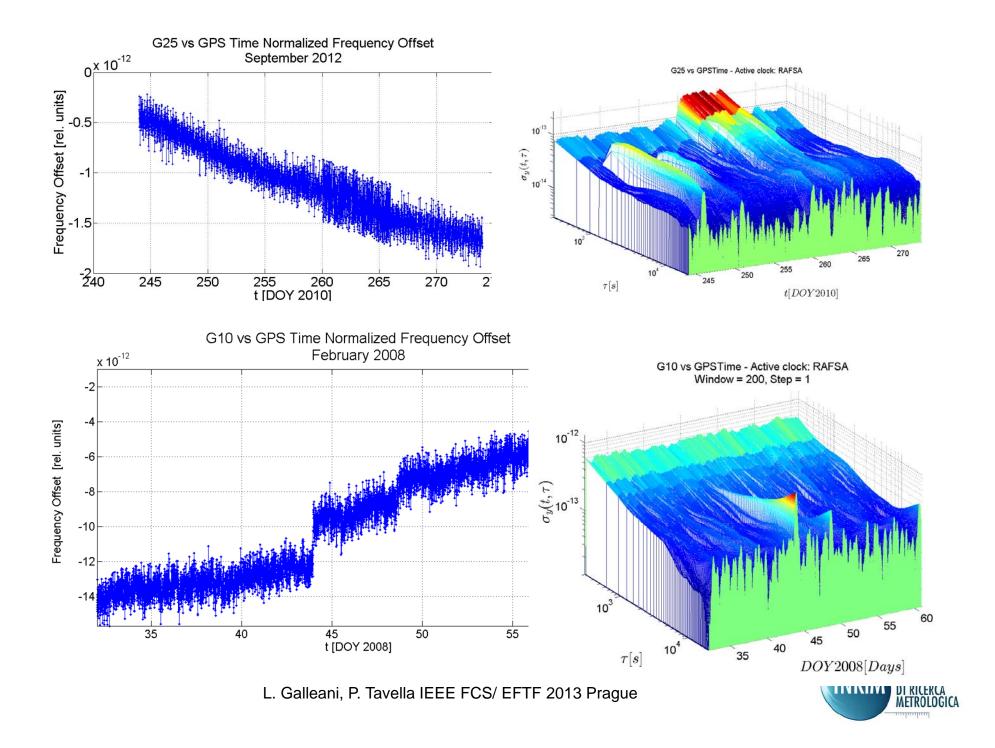
 q_1 t= AVAR(t) · t²

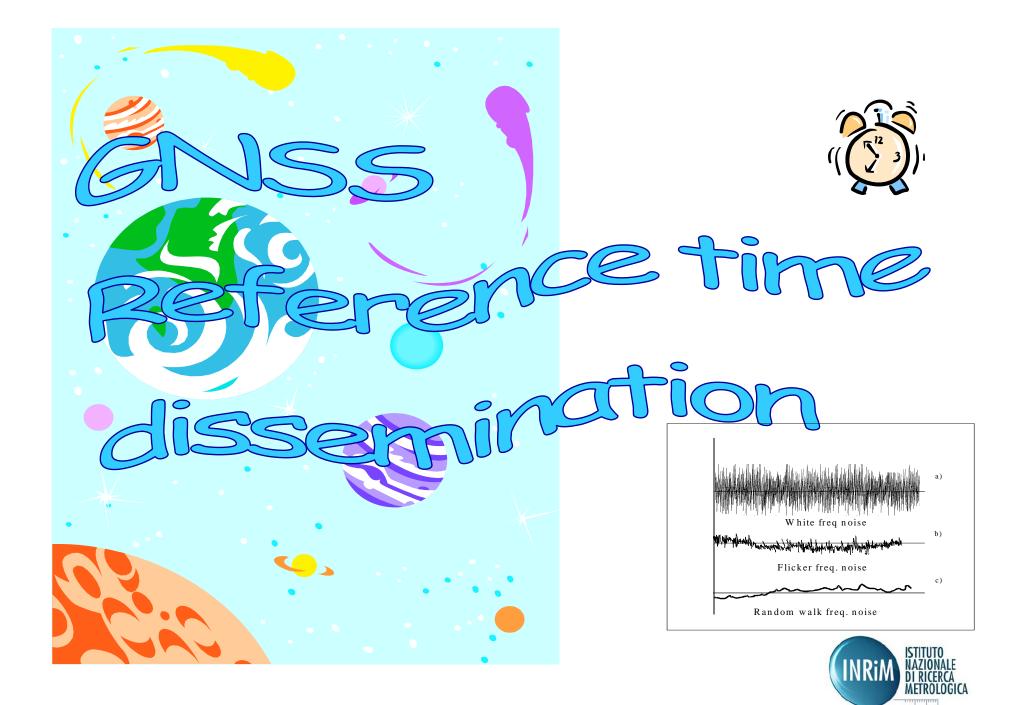




Clock data -580 -600 good clocks: -620 Time Offset [ns] -640 -660 -680 -700 2,5 7,5 12,5 10 15 5 Day Of the Year [days]

CA





 $P_{rec,1}^{sat} = c[(t_{rec} - t_{sat})] =$ The User clock error =offset versus the Ref time is estimated by the receiver $|\mathbf{x}_{sat} - \mathbf{x}_{rec}| + c[(t_{rec} - t_{ref}) - (t_{sat} - t_{ref})] + I_{rec,1} + Tr + \delta_{rec,1} + \varepsilon_{rec,1},$

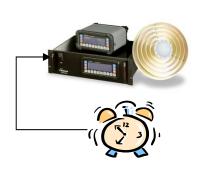
- GNSS receiver and its antenna
 - Timing receiver
 - Fixed (and known) location
 - External frequency reference for receiver
 - Atomic clocks (H-maser, Cesium...)
 - Physical time scale

the difference Local clock - GPS time = $(t_{rec} - t_{ref})$ is estimated

Signals-in-space (SIS) transmitted by the GNSS satellites contains also a prediction of $(UTC_{S/S} - t_{ref})$ as for example the predicted (UTC(USNO) - GPStime) _{S/S}

 $(t_{rec} - t_{ref}) - (UTC_{S/S} - t_{ref})$ allows to estimate Local clock - UTC_{SIS}

The timing user can get UTC_{SIS} from GNSS



A navigation system is also a mean for

UTC time dissemination

What is the Universal Time Coordinated?



For centuries



The time was given by the rotating Earth

on which we set the clock



From 1967

The time is given by atomic clock



used to study Earth rotation



Along centuries...

- day and night are the "natural" time unit
- it was observed that during the year the length of day changes but the "Mean Solar Day" was deemed constant and Universal
- •Universal Second = 1/86400 of rotational day (Mean Solar Time)
 - •1884 Greenwich reference meridian
 - •1925 International Astronomical Union fixes the beginning of the mean solar day at h. 00 and defines the Universal Time



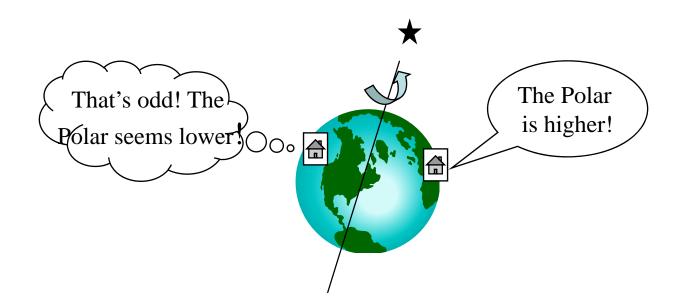


the rotation rate is constant?



Polar motion

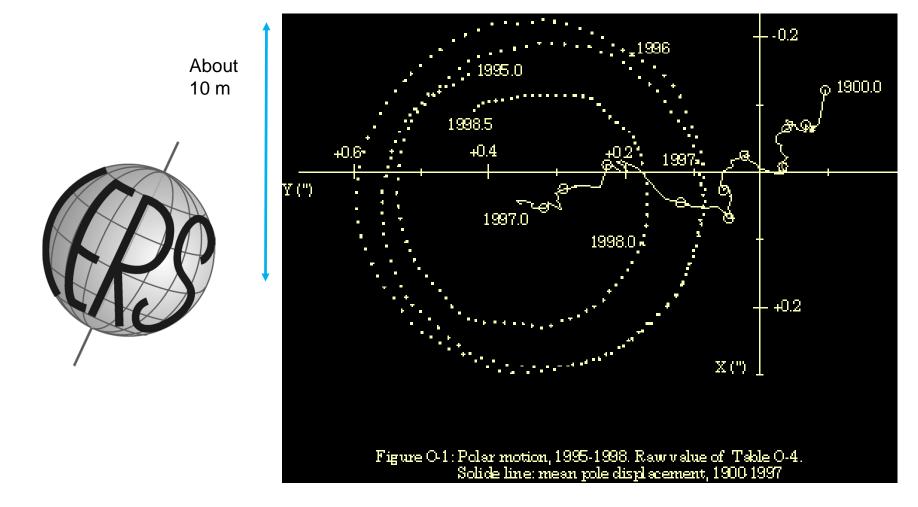
Suspected around 1850 from astronomers



Polar motion can be measured but is not predictable



Polar motion, 1995-1998 Solid line : mean pole displacement,



http://www.iers.org

International Earth Rotation and Reference Systems



Seasonal variation: in summer we spin faster

- A. Scheibe, 1936 in Berlin
- N. Stoyko, 1936 in Paris (BIH)

with crystal clock the day was measured shorter of about 1.2 m

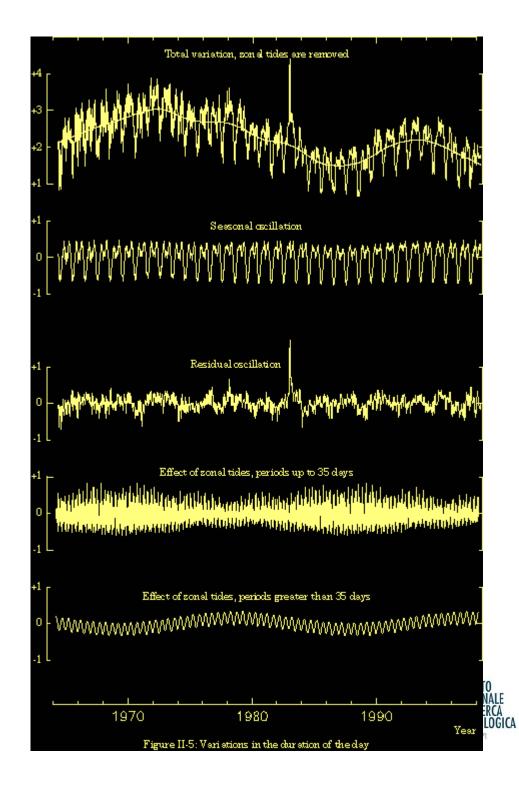




Variations in the duration of the day



http://www.iers.org



Secular slowing down

-8,00 -6,00 Advance of one second per year -4,00 ¥ ms -2,00 0,00 Delay of one second per year 2,00 4,00 1630 1710 1782 1814 1862 1878 1798 1830 1846 1894 1910 1926 1942 1958 Years

ISTITUTO

DI RICERCA METROLOGICA

LENGTH OF DAY exceeding 86400 s

The Universal Time was improved

UT = Universal Time scale

UT1 = Universal Time corrected by polar motion

UT2 = Universal Time scale corrected by seasonal variations

.... (UT not GMT!)



...in 1960

Ephemeris Time



- the "revolution" of the Earth around the Sun is constant.
- •Measuring the longitude of the Sun and using the equation of the apparent Sun orbit
- The new time scale: Ephemeris Time starts from h. 0 UT of January 1st, 1900.
- Time unit is the Ephemeris Second = 1/31 556 925.9747 of the tropical year on day **January 0, 1900**

• any new definition of the Second has to be in agreement with the previous one. For continuity with UT, this is the duration of the second in 1900

> in 1960 this duration was already shorter than 1/86400 of the Mean Solar Day

...in 1967

• Atomic Second = 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the Cs 133 atom

•First comes the second, then the time scale: in 1971: Temps Atomique International TAI, International Atomic Time

Atomic Time • TAI starts from h. 0 UT of January 1st, 1958.

•The length of the atomic second is in agreement with the Ephemeris second

therefore shorter than 1/86400 of the Mean Solar Day So far we have learnt that the Atomic Second is, by definition, shorter than the <u>current</u> Rotational Second (Universal Time)

because it was defined in agreement with the duration of the Rotational Second in 1900 and the Earth is (slowly!) slowing down



The International Astronomical Union recommends time scales and reference frames for the different applications in Geocentric or Solar System Barycentric frames. On the Earth or in the vicinity (50000 km) the reference time scale (1991) is the

Terrestrial Time

The Terrestrial Time is a coordinate time scale defined in a geocentric reference frame (centered at the centre of the Earth), with scale unit the SI second as realised on the rotating geoid, i.e. differing by a constant rate with respect to a geocentric clock.



The International Atomic Time

is an optimal realisation of the Terrestrial Time other realisation are for example TT(BIPM), some TA(k)

But which is **now** the angular position of the





Some users need to know the relationship between the Universal Time UT1 (rotational) and the Atomic Time





The Universal Coordinated Time (UTC) is a trade-off defined with the same time unit as TAI but with insertion of additional leap second

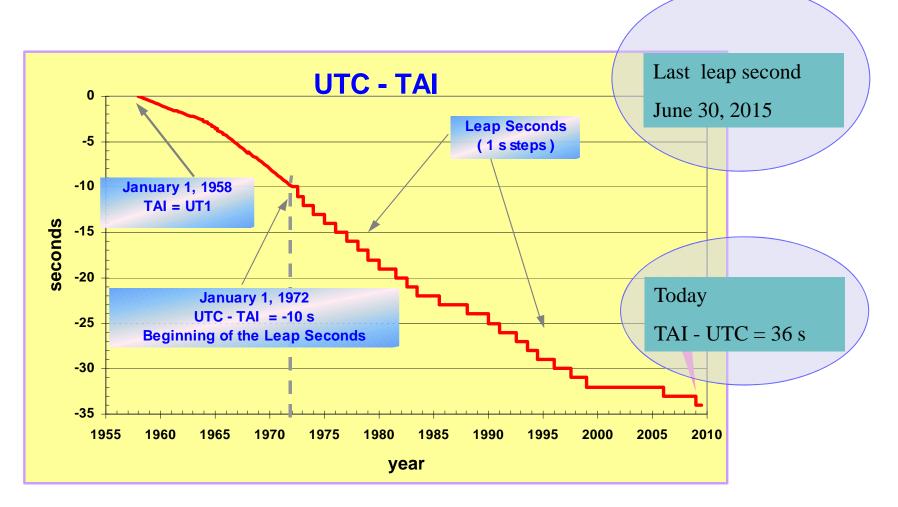
TAI-UTC = n seconds $n = 0, \pm 1, \pm 2, \dots$

Universal Time UT0, UT1, UT2,....

|**UT1-**UTC| < 0.9 s



Universal Coordinated Time and leap seconds





Universal Time Coordinated

is computed at the BIPM in different steps:



= Echelle Atomique Libre = weighted mean of all atomic clocks in the world



= Temps Atomique International = EAL plus frequency steering to maintain the TAI second in agreement with the definition of the second of the International System (SI). This is obtained through the evalation of primary frequency standards



= Universal Time Coordinated = TAI with the addition of leap second to remain close to the rotating Earth



The Universal Time Coordinated is the ultimate time reference (also with a «rapid» version) and it is available in deferred time

Local time scale UTC(k) are realised by national laboratories

in real-time



Idea first raised in public in 1999

Leap seconds are useful or annoying?

Since ancient times, we have used the Earth's rotation to regulate our daily activities. By noticing the approximate position of the sun in the sky, we know how much time was left for the day's hunting or farming, or when we should stop work to eat or prop. First sundials, water clocks, and then mechanical clocks were invented to tell time more precisely by essentially interpolating from noon to noon. As mechanical clocks became increasingly accurate, we discovered that the Earth does not return "It's

INNOVATION

GPS and Leap Seconds Time to Change?

Dennis D. McCarthy, U.S. Naval Observatory William J. Klepczynski, Innovative Solutions International

Just as leap years keep our calendar approximately synchronized with the Earth's orbit about the Sun, leap seconds keep precise clocks in synchronization with the rotating Earth, the traditional "clock" that humans have used to determine time. Coordinated Universal Time (UTC), created by adjusting International Atomic Time (TAI) by the appropriate number of leap seconds, is the uniform time scale that is the basis of most civil timekeeping in the world. The concept of a leap second way introd

seconds. While resetting the GLONASS clocks, the system is unavailable for navigation service because the clocks are not synchronized. If worldwide reliance on satellite navigation for air transportation increases in the future, depending on a system that may not be operational during some critical areas of flight could be a difficulty. Recognizing this problem, GLONASS developers plan to significantly reduce do

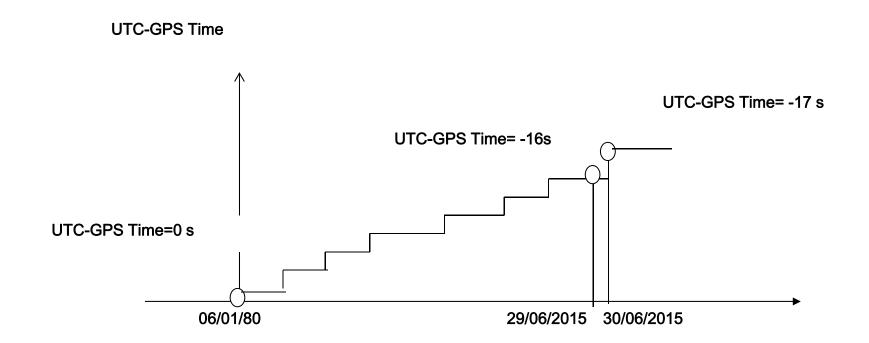


Source: **GPS World** Nov 1999

lational **leasurement** ystem

Global Positioning System: navigation and timing services

GPS time was set in agreement with UTC on h. 00 Jan 6, 1980



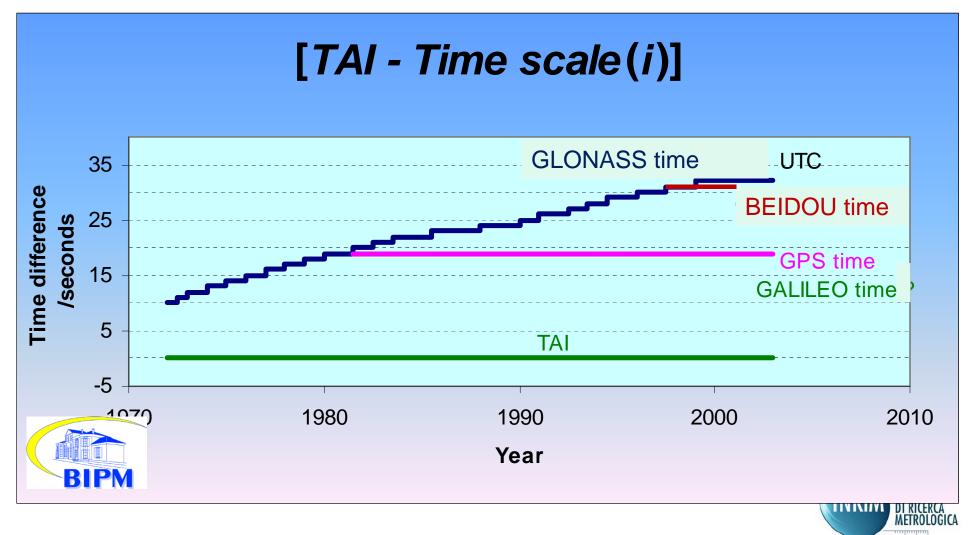
The accumulate time difference between UTC

and GPS time is now of 17 seconds. GPS time is ahead 17 s



Leap seconds in Global Navigation Satellite System time scales

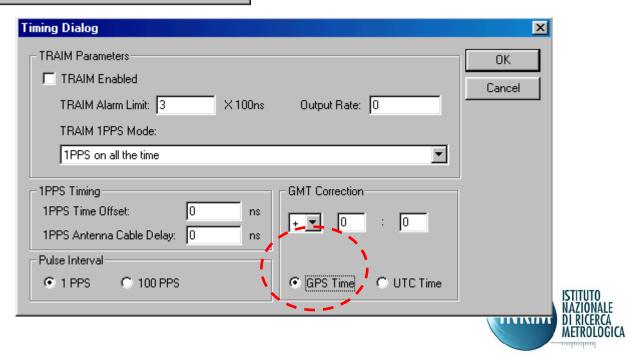
GNSS prefer not to apply leap seconds (except GLONASS), their time scale is easily available all over the world inside the navigation message, reference time scales differ from seconds, source of CONFUSION!!!

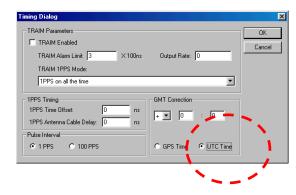


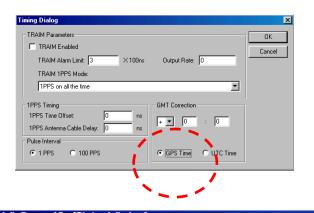
Timing from a MOTOROLA GPS receiver

Timing Dialog			×
TRAIM Parameters TRAIM Enabled TRAIM Alarm Limit: 3 TRAIM 1PPS Mode:	×100ns	Output Rate: 0	OK Cancel
1PPS on all the time		•	
1PPS Timing 1PPS Time Offset: 0 1PPS Antenna Cable Delay: 0	ns ns	GMT Correction	
Pulse Interval 1 PPS 100 PPS		C GPS Time	

UTC or GPS time can be chosen as reference time







Motorola WinOncore12 - [Timing Window] Motorola WinOncore12 - [Timing Window] <u>File View Options Window Help</u> 🕓 <u>F</u>ile <u>V</u>iew <u>O</u>ptions <u>W</u>indow <u>H</u>elp 소율 Ē L. 0 llu abc 0 ll II \bigcirc Msg Satellites Cmd Mon Timing About Signal Navigation Survey Satellites Cmd Mon Signal Navigation Survey Msg Timing About D<u>e</u>O D<u>e</u>O -60 A | N | ID= | ø 0 塾 Ğ ON OFF Þŀ. 0-0 0-0 -60 h. ON OFF 🔊 💦 ID= Ğ ----Time and TRAIM Status | Negative Sawtooth Time and TRAIM Status | Negative Sawtooth TRAIM Setup and Status TRAIM Setup and Status Rate: 0 Rate: 0 TRAIM: Disabled TRAIM: Disabled 300 ns Alarm: 300 ns Alarm: 1PPS Control: Pulse is on all the time 1PPS Control: Pulse is on all the time Solution: Unknown Solution: Unknown Algorithm: Neither possible Algorithm: Neither possible Pulse Status: On Sigma: 65535 ns Pulse Status: On Sigma: 65535 ns Time: 06:50:00 Time: 06:50:16 Pulse Sync: UTC Error: -14 ns Pulse Sync: UTC Error: -14 ns UTC **GPS** Time Time Date: 09/04/2012 Date: 09/04/2012 Time: 06:50:00 UTC _____CMT_Utfset: +00:00 Time: 06:50:16 GPS GMT Offset: +00:00 UTC Offset: 15,999999994 seconds UTC Offset: 15.999999994 seconds Leap Second Pending: None Leap Second Pending: None Present Leap Second: -16 Present Leap Second: -16 Future Leap Second: 16 Future Leap Second: 16 Oscillator and Clock Parameters Oscillator and Clock Parameters Clock Bias: 32 ns Clock Bias: 32 ns. Oscillator Offset: 97668 Hz Oscillator Offset: 97668 Hz 00.0°C Temperature: Temperati 00.0° SVID **GPS Time Estimate** Channel Channel SVID GPS Time sti 01 15 0.000073795 - O. 12 0.000073802 02 О. 302 03 28 0.000073865 Ο. 365 04 27 0.000073795 3795 О. O(05 09 0.000073786 Ο. 0(3786 06 18 0.000073807 0(Ο. 3807 UD 07 22 0.000073807 О. 0(2807 08 17 0.000073818 0. 00 318 09 26 0.000073815

Leap seconds are useful or annoying? The current proliferation of time scales is generating confusion and possible danger



INTERNATIONAL TELECOMMUNICATION UNION

RADIOCOMMUNICATION

STUDY GROUPS

Special Rapporteur Group 7A (SRG 7A) on the Future of the UTC Time Scale

ColloquiumCohloqueiumConTimes Torino, T08 100, Mag-290May 2

Several international organisations created working groups to evaluate this issue. In November 2015 ITU General **Assembly** decided not do change till 2022. ITU would continue to be responsible for the dissemination of time signals via radiocommunication and BIPM for establishing and maintaining the second of the International System of Units (SI) and its dissemination through the reference time scale.



BIPM press release 13 C

The proposed redefinitic

Today, leap seconds keep phase with the slightly var

The possibility of dropping misconceptions in the pop

There are an increasing n second causes serious te



Further lecture...

The proposed redefinition of Coordinated Universal Time, UTC

There is a need to set out clearly the reasons for the change and what is involved. This is the purpose of what follows:

The international character of the world's time scale

The measure of time and its unit the second are matters of international cooperation. Up until the middle of the 20th century, time scales were based on astronomical observations of the rotation of the Earth and the movement of the Earth in its orbit round the Sun. These had been within the purview of astronomers for centuries and, since the 1920s, had been the concern of the International Astronomical Union (IAU). With the invention of the atomic clock in 1955, however, everything began to change. By then, the irregular rate of rotation of the Earth and the practical difficulties in the realization of ephemeris time, based on the period of the Earth's orbit round the Sun, made it necessary to move to a time scale based on the atomic clock.

http://www.bipm.org/utils/en/pdf/Press_Release_UTC_13October.pdf

UTC for the 21st century

November 2011 at The Royal Society at Chicheley Hall,

Organised by Dr Terry Quinn and Dr Felicitas Arias

http://royalsociety.org/events/2011/utc-21-century/

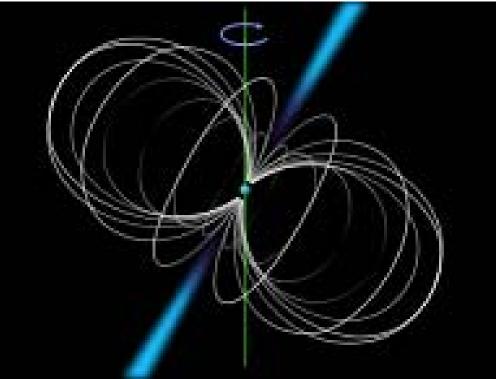
Metrologia

Special issue on "modern time scales" 48 (2011) S121–S124



Time and navigation will return in space? Pulsar: a rotating star A clock in space? TUTO Ionale Iicerca Rologica

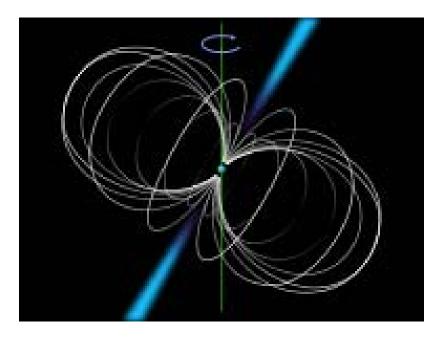
Pulsar



- Neutron star
- 20 km as diameter
- 1,4 time the solar mass
- in our Galaxy, thousand light years apart
- some spinning with millisecond period
- emitting radiowave as a lighthouse



Pulsar



- The rotation is highly stable
- Every millisecond we see a radio pulse

Is it a "clock"?



Many different difficulties:

- The rotation period is slowing down
- The pulse has to cross 10¹⁶ km of interstellar region
- The Earth is a rotating observatory





But...

Pulsar

Nobel Prize to Taylor and Hulse for gravitational wave detection (1993)

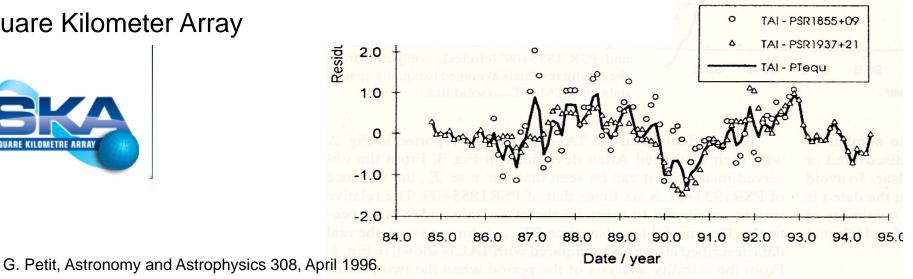
some ideas on the long term instabilities of atomic clocks

Pulsar is the hot topic:

new decades of observations are now available, tens of millisec pulsars will be discovered by the

Square Kilometer Array





he Nobel Prize in Physics 1993

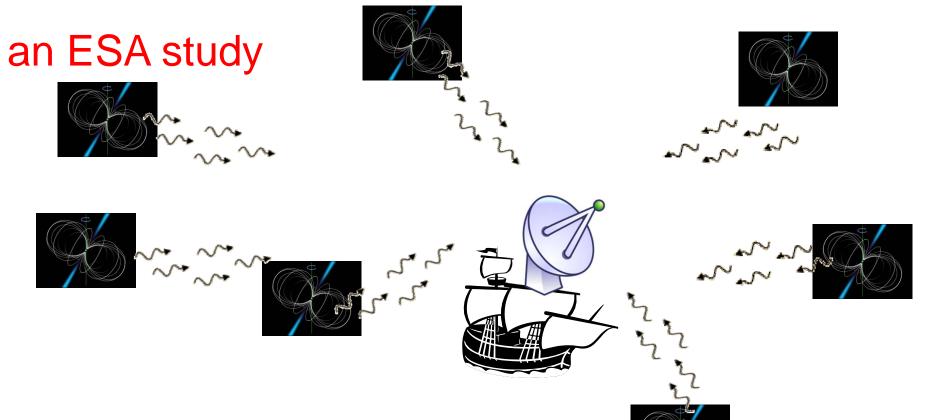
Joseph H. Taylor Jr. - Facts

Share this: 📑 👫 🗾 🛨 🔄 🖃

R. Breton et al Science 4 July 2008, A. Papitto, Nature 09/2013



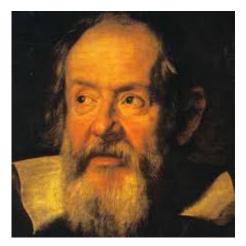
Pulsars for extraterrestrial space navigation?



The position is estimated by comparing measured pulse arrival times with respecty to expected pulse arrival times using information from a pulsar database



The letter to the King of Spain in 1612 still alive...



These stars display conjunctions, separations, eclipses, and other configurations...more than 100 a year...and they are so unique, identifiable, and so exact that nobody, of medium intelligence, is not able to use them to identify the longitude and the position of the ship based on the ephemerids I have computed for the next years to come.

OBSERVAT. SIDEREAE

Stella occidentaliori maior, ambæ tamen valdè confpicuæ, ac fplendidæ : vtra quæ diftabat à loue fcrupulis primis duobus; tertia quoque Stellula apparere cepit hora tertia prius minimè confpecta, quæ ex parte orientali louem ferè tangebat, cratque admodum exigua. Omnes fuerunt in cadem recta, & fecundum Eclypticæ longitudinem coordinatæ.

Die decimatertia primum a me quatuor confpectæ fuerunt Stellulæ in hac ad louem conftitutione. Erant tres occidentales, & vna orientalis; lineam proximè

* O*** Occ:

rectam conftituebant; media enim occidétalium paululum à recta Septentrionem verfus deflectebat. Aberat orientalior à loue minuta duo: reliquarum, se louis intercapedines erant fingulæ vnius tantum minuti. Stellæ omnes candem præfe ferebant magnitudinem; ac licet exiguam, lucidiffimæ tamen erant, ac fixis eiufdem magnitudinis longe fplendidiores.

Die decimaquarta nubilofa fuit tempeftas.

Die decimaquinta, hora noctis tertia in proximè depicta fuerunt habitudine quatuor Stellæ ad Iouem;

occidentales omnes: ac in eadem proxim recta linea disposita; qua enim tertia à loue numerabatur paululum

Occ.

Mostafa Fatemi



Mayo Cinic, USA reveal email address January 1, 2016 through June 30, 2017. "Medical Utrasound Technology: From Pulse

After an introduction on the trend of diagno ultrasound radiation force. Next, the result applications will be presented.

Patrizia Tavella



Istituto Nazionale Ricerca Metrologica INRIN reveal email address July 1, 2015 through December 31, 2016 "Precise Time Scales and Navigation System

View their reports

Susan Trolier-McKinstry



Pennsylvania State University, USA reveal email address January 1, 2015 through June 30, 2016 "Piezoelectric Films for Microelectromechani

View their reports



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