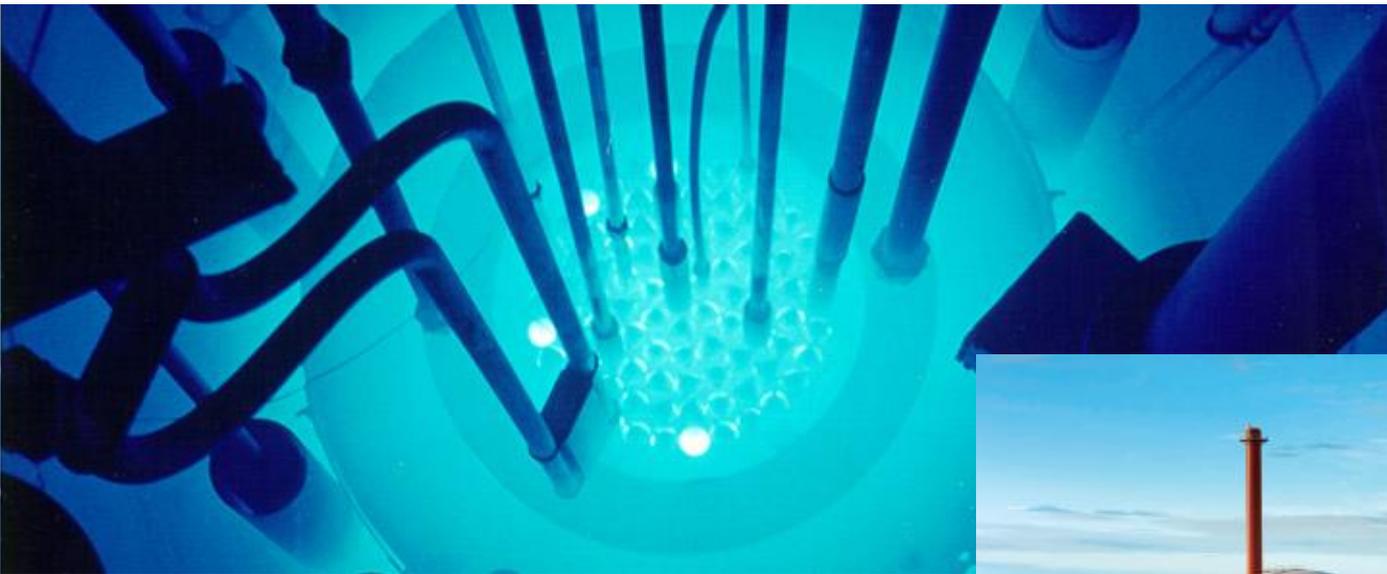


# Energy from nuclear fission: basics



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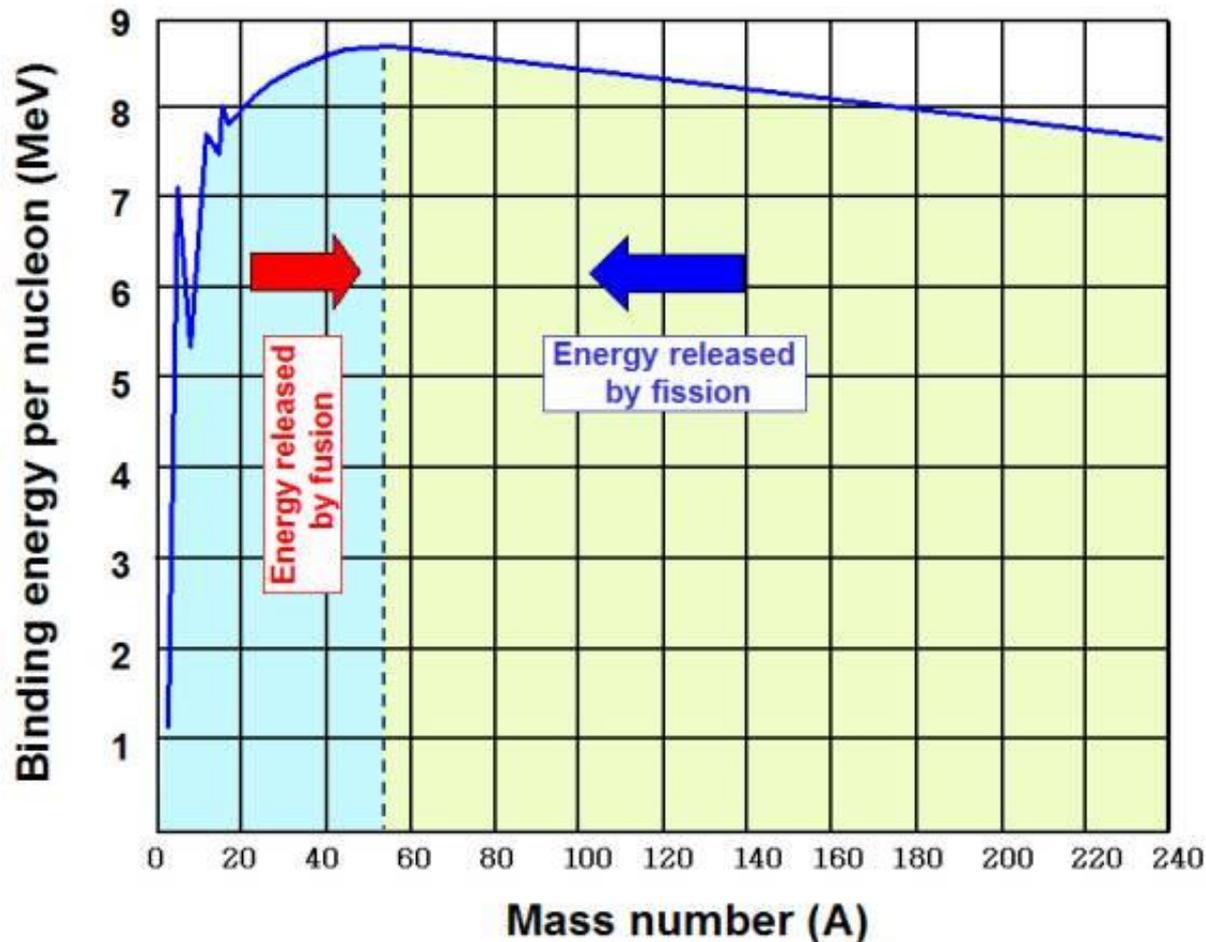
# Why can fission produce energy ?

Nuclear mass and nuclear binding energy

$$M(Z,A) = ZM_p + (A - Z)M_n + B(Z,A)$$

$B(Z,A) < 0$  !!! i.e. a nucleus weighs less than the sum of proton and neutron masses

$$\varepsilon \equiv \frac{|B(Z,A)|}{A}$$



# How can fission produce energy ?

$$M(Z,A) \rightarrow M(Z_1, A_1) + M(Z_2, A_2); \quad Z = Z_1 + Z_2; \quad A = A_1 + A_2$$

$$\text{Energy balance (Q-value)} \quad Q_{fiss} = M(Z, A) - M(Z_1, A_1) - M(Z_2, A_2)$$

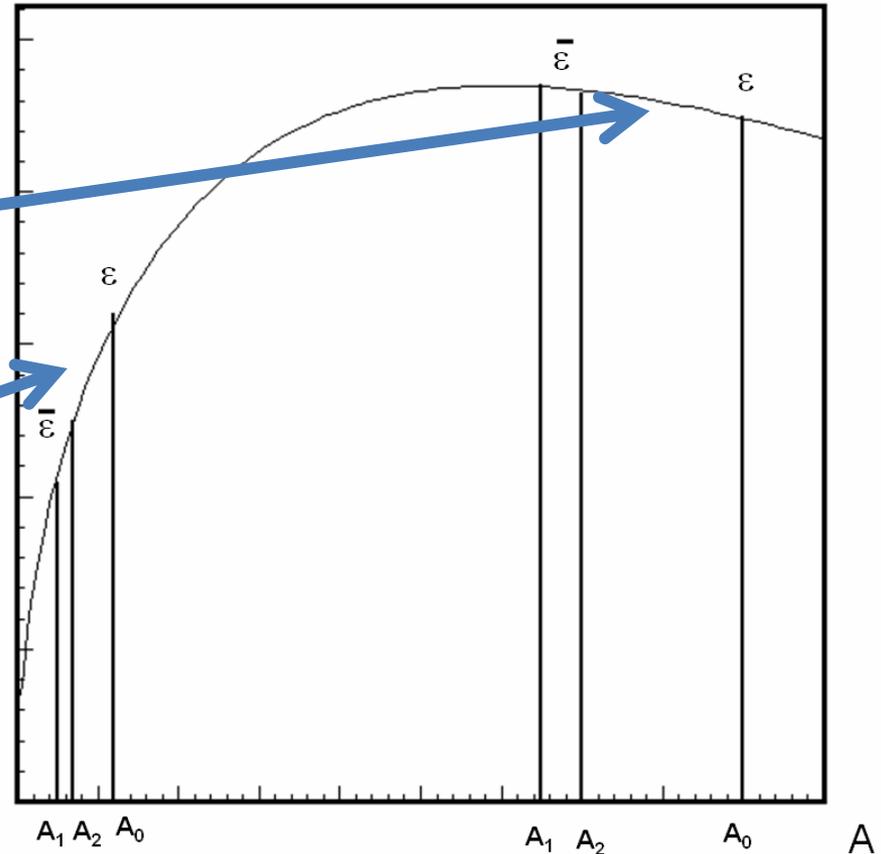
$$= B(Z, A) - B(Z_1, A_1) - B(Z_2, A_2) = -\varepsilon A + \varepsilon_1 A_1 + \varepsilon_2 A_2 = -\varepsilon A + \bar{\varepsilon} A = (\bar{\varepsilon} - \varepsilon) A$$

$$\bar{\varepsilon} = \frac{\varepsilon_1 A_1 + \varepsilon_2 A_2}{A_1 + A_2}$$

$$\varepsilon = |B|/A$$

$$Q_{fiss} > 0$$

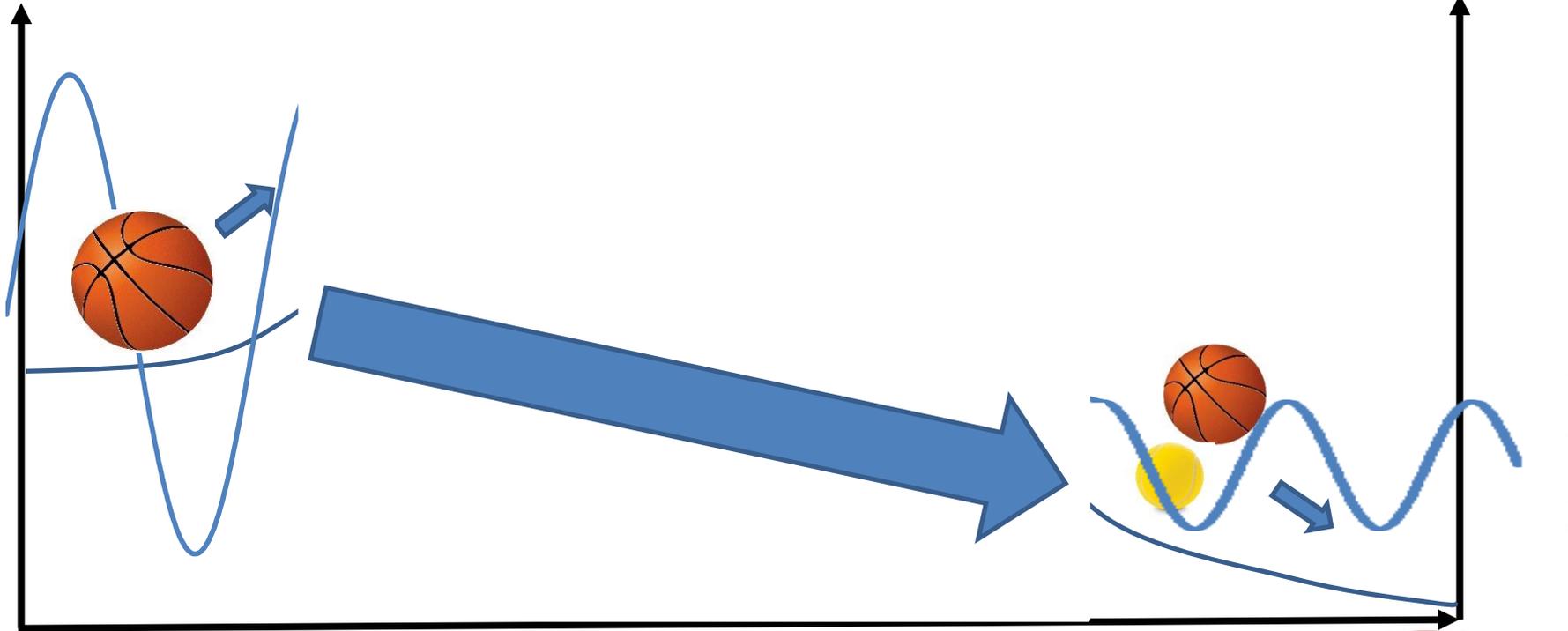
$$Q_{fiss} < 0$$



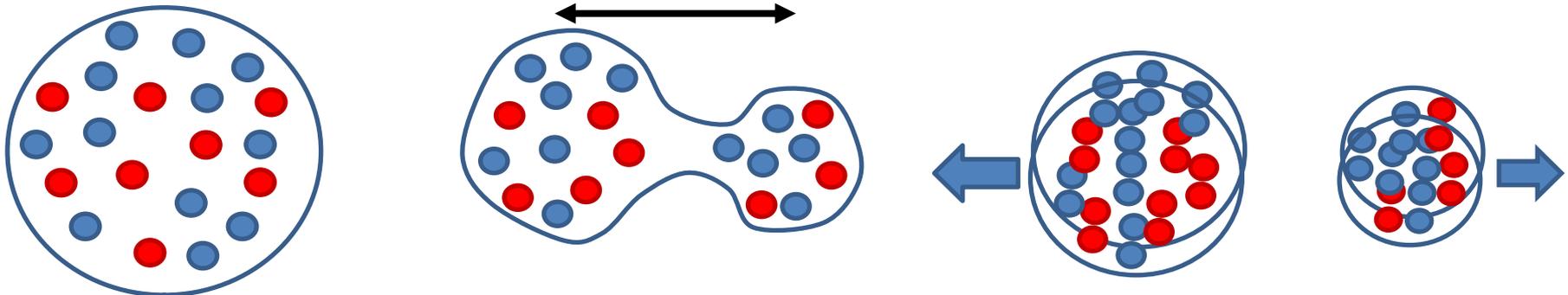
# How to break a nucleus

Fragment kinetic energy

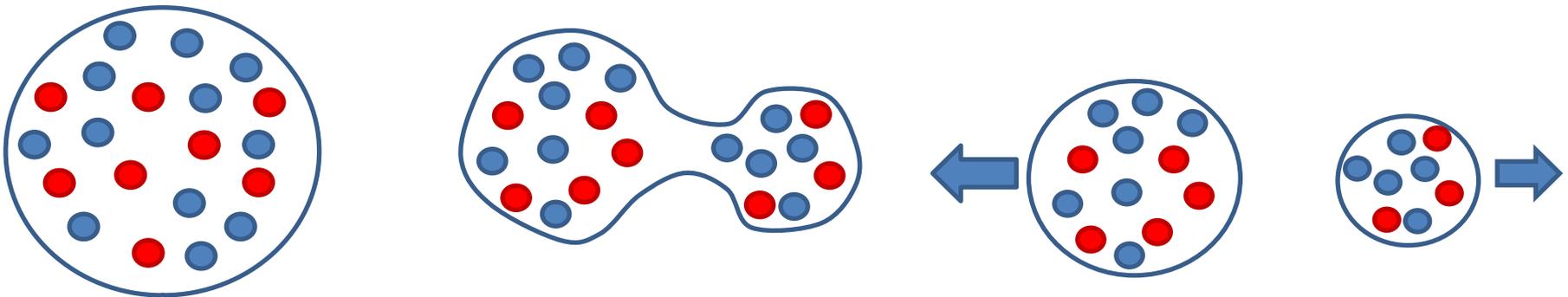
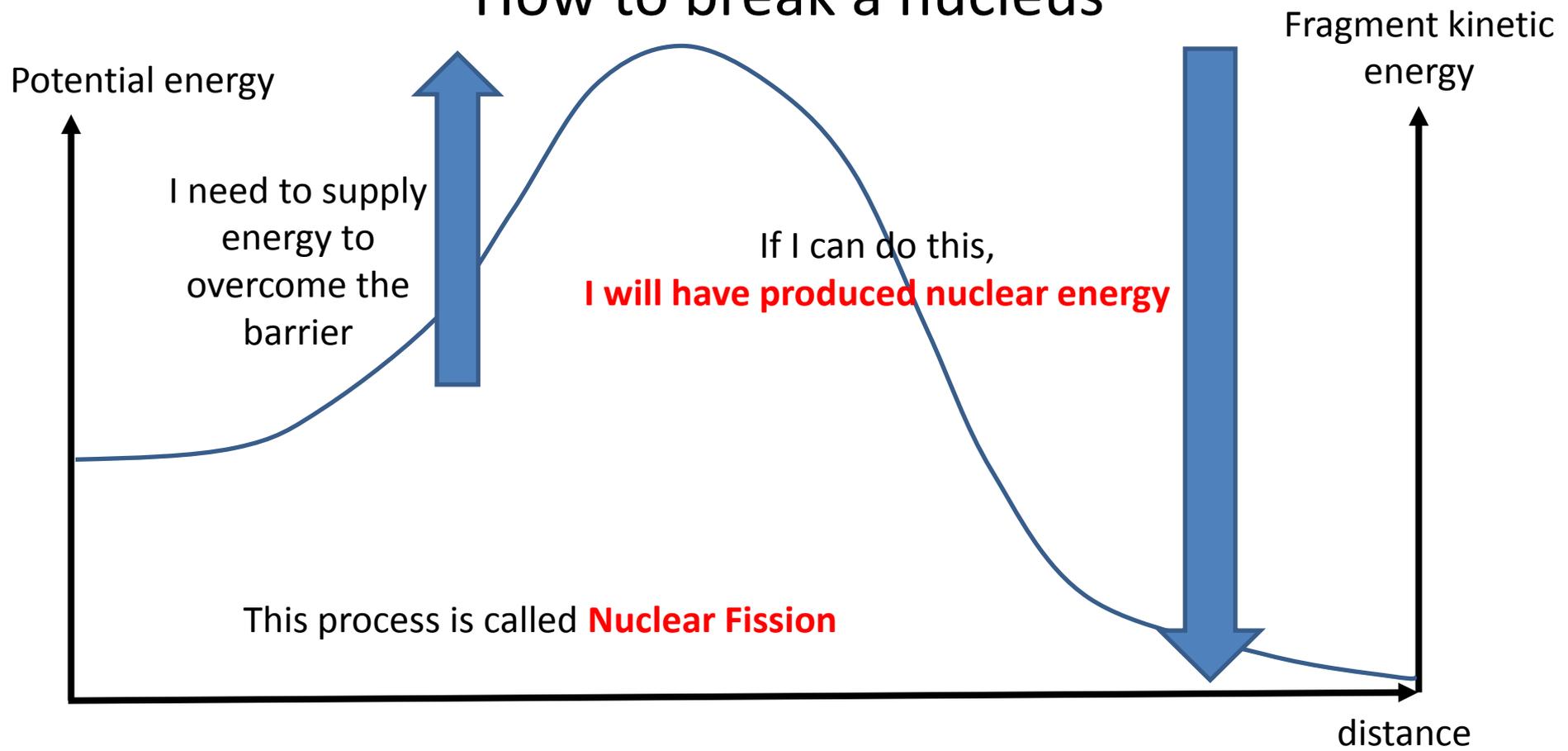
Potential energy



● proton  
● neutron



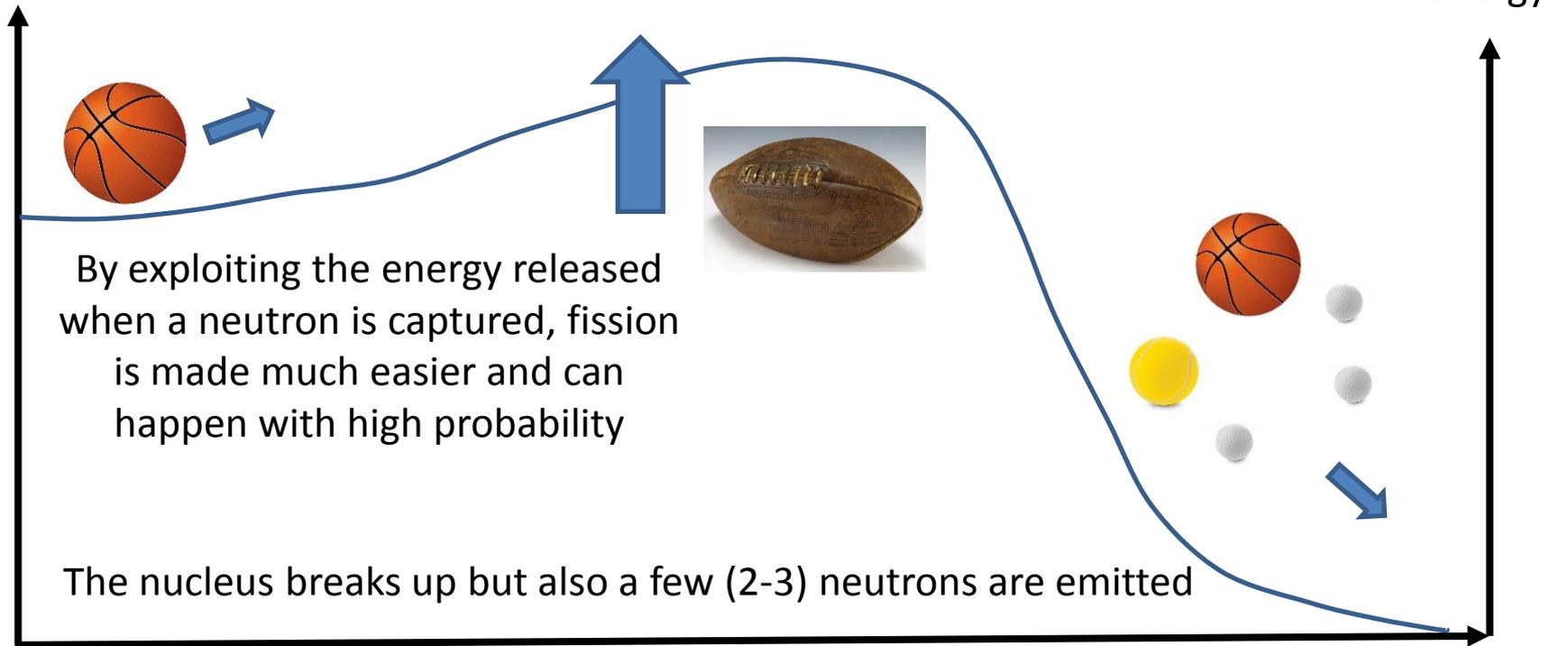
# How to break a nucleus



# A special case, Uranium 235

Potential energy

Fragment kinetic energy

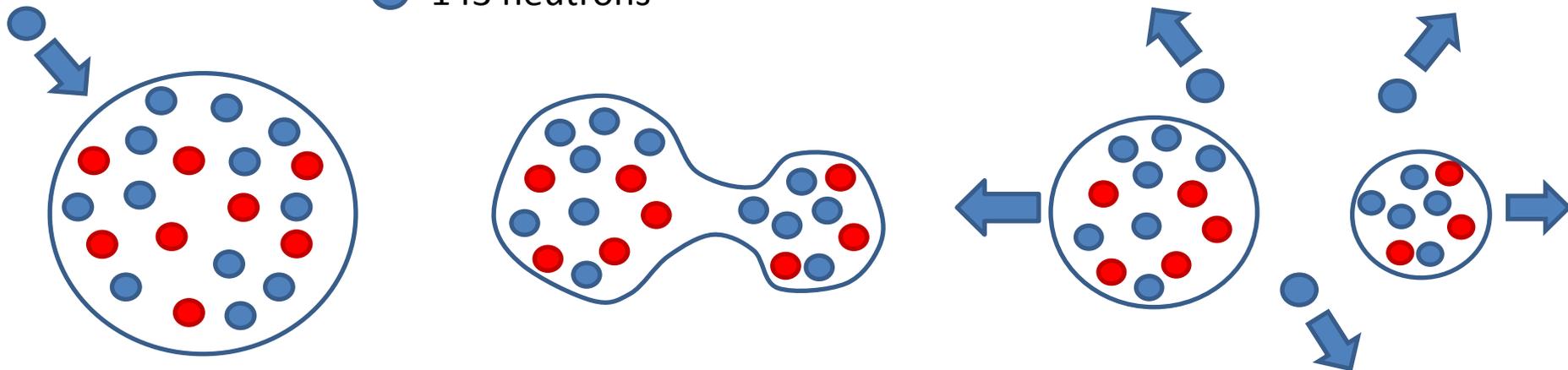


By exploiting the energy released when a neutron is captured, fission is made much easier and can happen with high probability

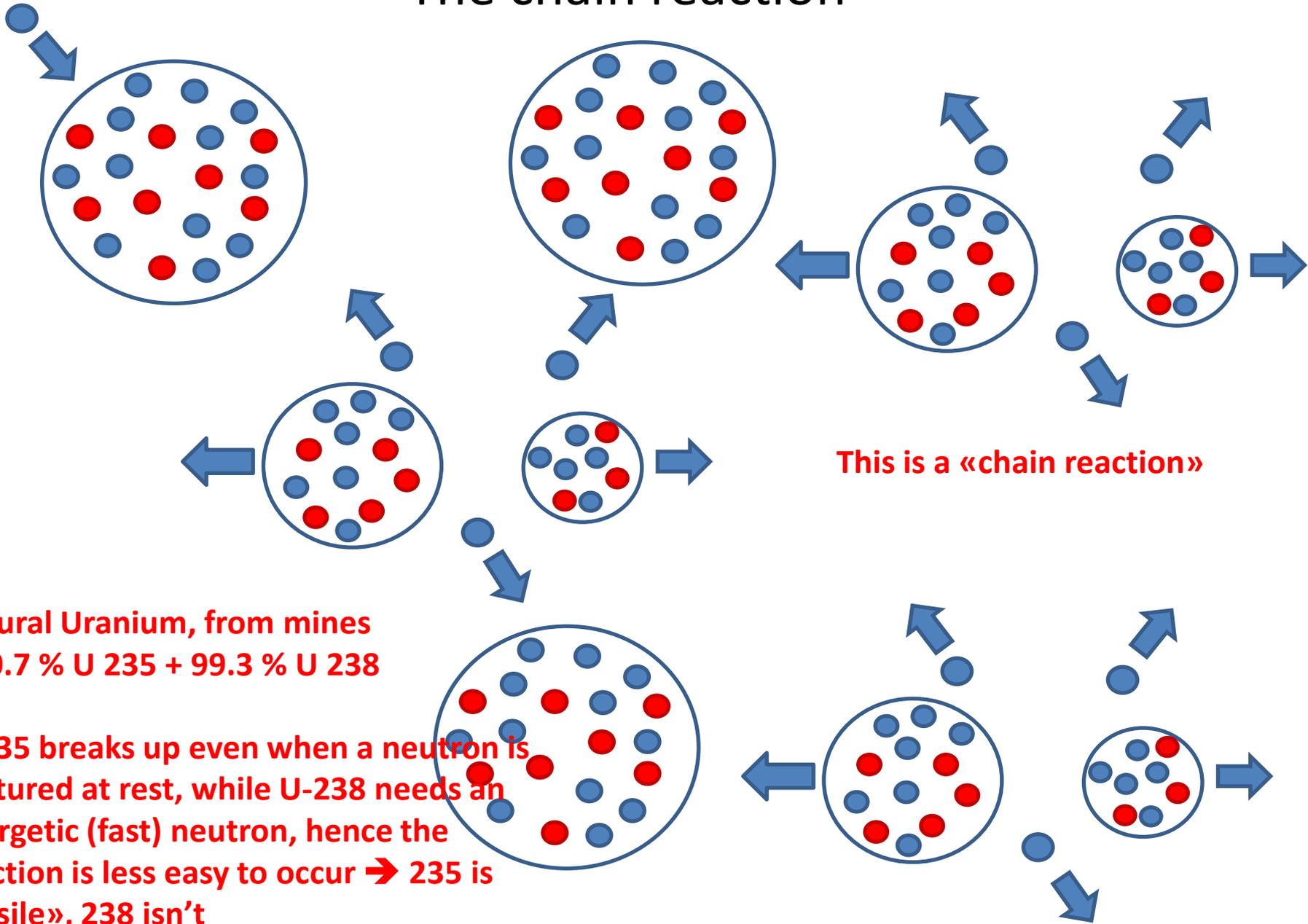
The nucleus breaks up but also a few (2-3) neutrons are emitted

● 92 protons

● 143 neutrons



# The chain reaction



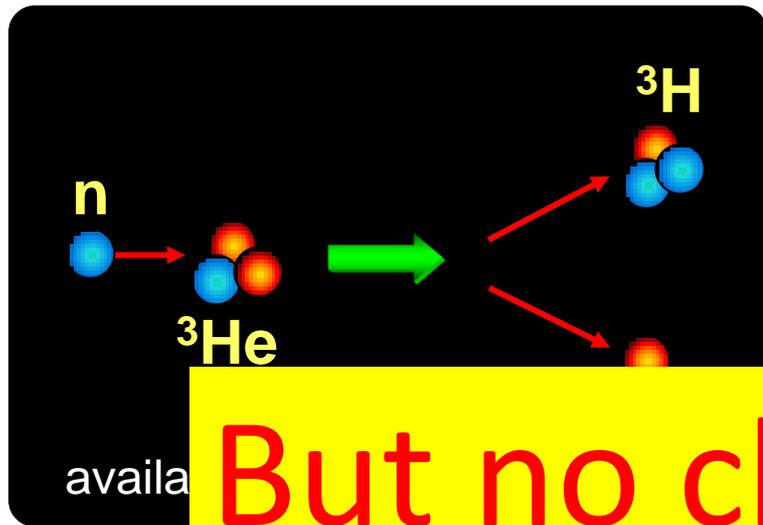
This is a «chain reaction»

Natural Uranium, from mines  
→ 0.7 % U 235 + 99.3 % U 238

U-235 breaks up even when a neutron is captured at rest, while U-238 needs an energetic (fast) neutron, hence the reaction is less easy to occur → 235 is «fissile», 238 isn't

Fragments are moving → kinetic energy → transferred to atoms → heat

# Other neutron absorption processes yielding energy



$\sigma$ (thermal neutrons)  
 $\approx 5330$  b (barn,  $1\text{ b} = 10^{-24}\text{ cm}^2$ ,  $\sigma$  is proportional to the reaction probability, see later)

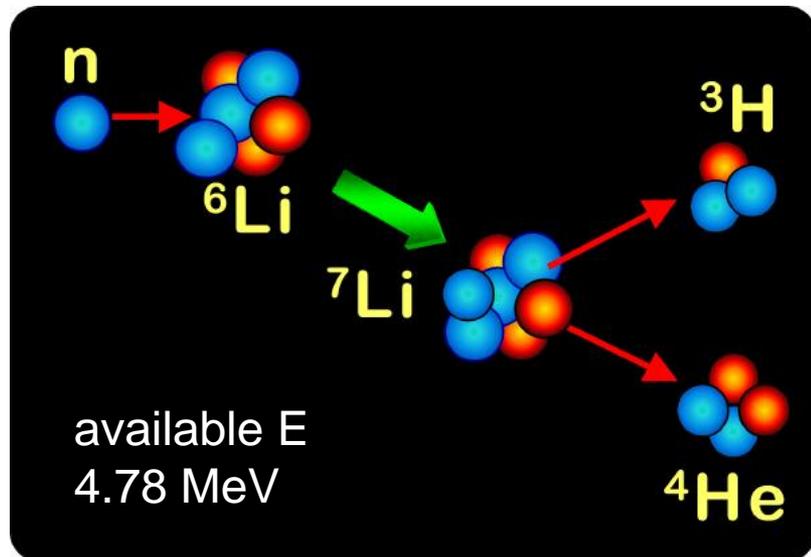
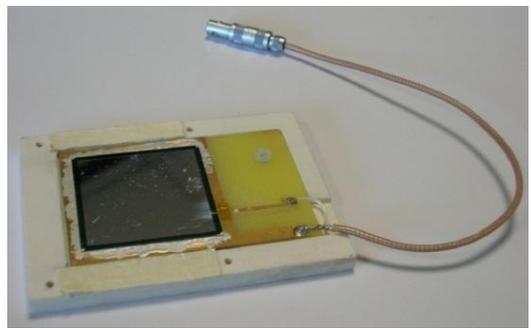
1 MeV = 1 MegaelectronVolt =  $10^6$  electronVolt =  $10^6 \times 1.6 \times 10^{-19}$  Coulomb Volt =

**But no chain reaction**

$\approx 940$  b



neutron detector based on a LiF film



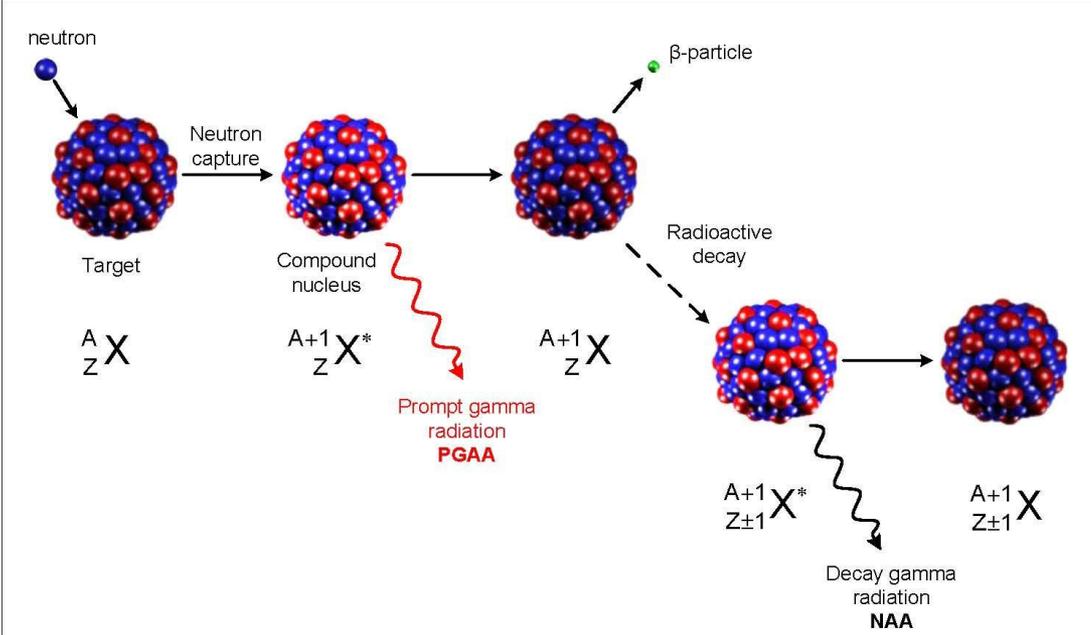
Another very relevant reaction mechanism is **neutron capture**

→ for heavy nuclei, addition of one more neutron can provide several MeV from binding energy

→ capture is **followed by gamma emission** (radiative capture) or **fission**

By quantum mechanical arguments, it is possible to show that at low energies (if the energy gained from the neutron capture is sufficient to produce the phenomenon of interest)

→ **cross section follows a 1/v law, with v being the relative speed (essentially the n speed)**



Example: Plutonium production from Uranium



# Amount of energy and reaction products

When a uranium nucleus fissions into two daughter nuclei fragments, about **0.1 % of uranium mass appears as fission energy of ~200 MeV ( $E=Mc^2$ )**

→ **much bigger than any other exoenergetic nuclear reaction (in absolute terms)**

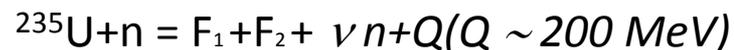
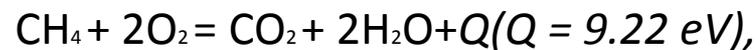
- **~170 MeV** appears as the **kinetic energy of the daughter nuclei**,  
- which fly apart at about 3% of the speed of light

- an **average of 2.5 prompt neutrons are emitted**, with a **mean kinetic energy per neutron of ~2 MeV** (total of 4.8 MeV)

- the **average number of neutrons emitted is called  $\nu$  (order of 2-3)**

- **~25 MeV** are released in form of **prompt gamma ray photons and fission product  $\beta$  decay**

Chemical reactions vs  
nuclear fission



→ *Fission gives between 20 and 50 million times more energy*

# Physics: nuclear cross sections

**Cross section:** quantity that characterizes a nuclear reaction (elastic, inelastic scattering, etc.) connected to the range of the involved forces; **effective area of a nuclear target**

Here we will consider the **total cross section**, defined as follows:

Given a **flux**  $\frac{dN_{in}}{dSdt}$

number of incident particles per unit surface and unit time on a single nucleus (target)

and given an **interaction rate**  $\frac{dN_{reac}}{dt}$

number of interacting particles (scattered or absorbed projectiles) per unit time, then

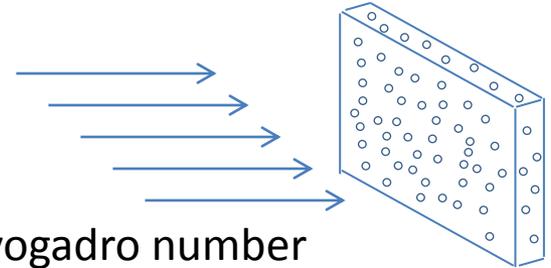
$$\sigma = \frac{\frac{dN_{reac}}{dt}}{\frac{dN_{in}}{dSdt}}$$

$\sigma \rightarrow$  physical dimensions of a surface

# Nuclear cross sections

**Macroscopic target** comprising several nuclei with **density  $\rho$**  (es. gr/cm<sup>3</sup>) and **thickness  $x$** , struck by a particle beam of intensity  $I$  (particles/sec)  $\rightarrow$

$$R = \frac{dN_{\text{reac}}}{dt} = I \frac{\rho x}{A} N_A \sigma$$



where  $A$  is the target atomic weight (es. in gr.) e  $N_A$  is the Avogadro number

$\frac{\rho}{A} N_A$  is the **number density of nuclei** in the target (i.e. number of nuclei per unit volume)

This is all valid for a small thickness  $x$

For a target of arbitrary thickness, first divide it in thin slices of thickness  $dx$   $\rightarrow$

$$dR = \frac{dN_{\text{reac}}}{dt} = I(x) \frac{\rho}{A} N_A \sigma dx$$

$$dI = -I(x) \frac{\rho}{A} N_A \sigma dx$$

$$I(x) = I(0) \exp\left(-\frac{\rho}{A} N_A \sigma x\right)$$

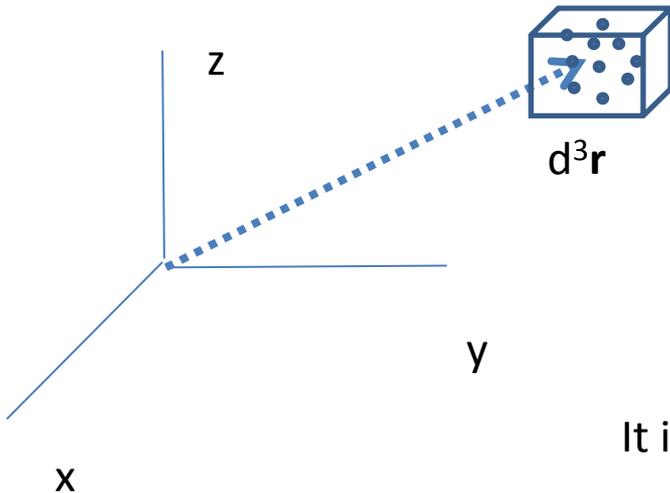
$\rightarrow \Sigma \equiv \frac{\rho}{A} N_A \sigma$  **Macroscopic cross section = prob.ty of interaction per unit length**

$1/\Sigma$  = Mean free path       $\Sigma v$  = Frequency with which reactions occur,  $v$ = projectile speed

# Neutron density and flux

Neutron density  $\equiv n(\mathbf{r}, E, t)$  [ $\text{cm}^{-3}$ ]  $\equiv$

expected number of neutrons with energy between  $E$  and  $E+dE$ , in the volume  $d^3\mathbf{r}$  about  $\mathbf{r}$ , at a time  $t$



Reaction density  $\equiv R(\mathbf{r}, E, t) \equiv$

Number of reactions in the volume  $d^3\mathbf{r}$  about  $\mathbf{r}$ , at a time  $t$ , initiated by neutrons with energy between  $E$  and  $E+dE = n(\mathbf{r}, E, t) \Sigma v$

We give a special name to the quantity  $n(\mathbf{r}, E, t)v$

It is called the **neutron “flux”**  $\phi(\mathbf{r}, E, t) \equiv n(\mathbf{r}, E, t)v$  [ $\text{cm}^{-2} \text{s}^{-1}$ ]

**Reaction density  $\equiv$  number of reactions per unit volume  $\equiv R(\mathbf{r}, E, t) = \Sigma \phi$**

Suppose you've got a reactor with 1 GW thermal power =  $10^9$  Joule/sec

Assume each fission releases order of 200 MeV energy =  $3.2 \times 10^{-11}$  Joule

→ In the reactor the fission rate is about  $3 \times 10^{19}$  fissions/sec

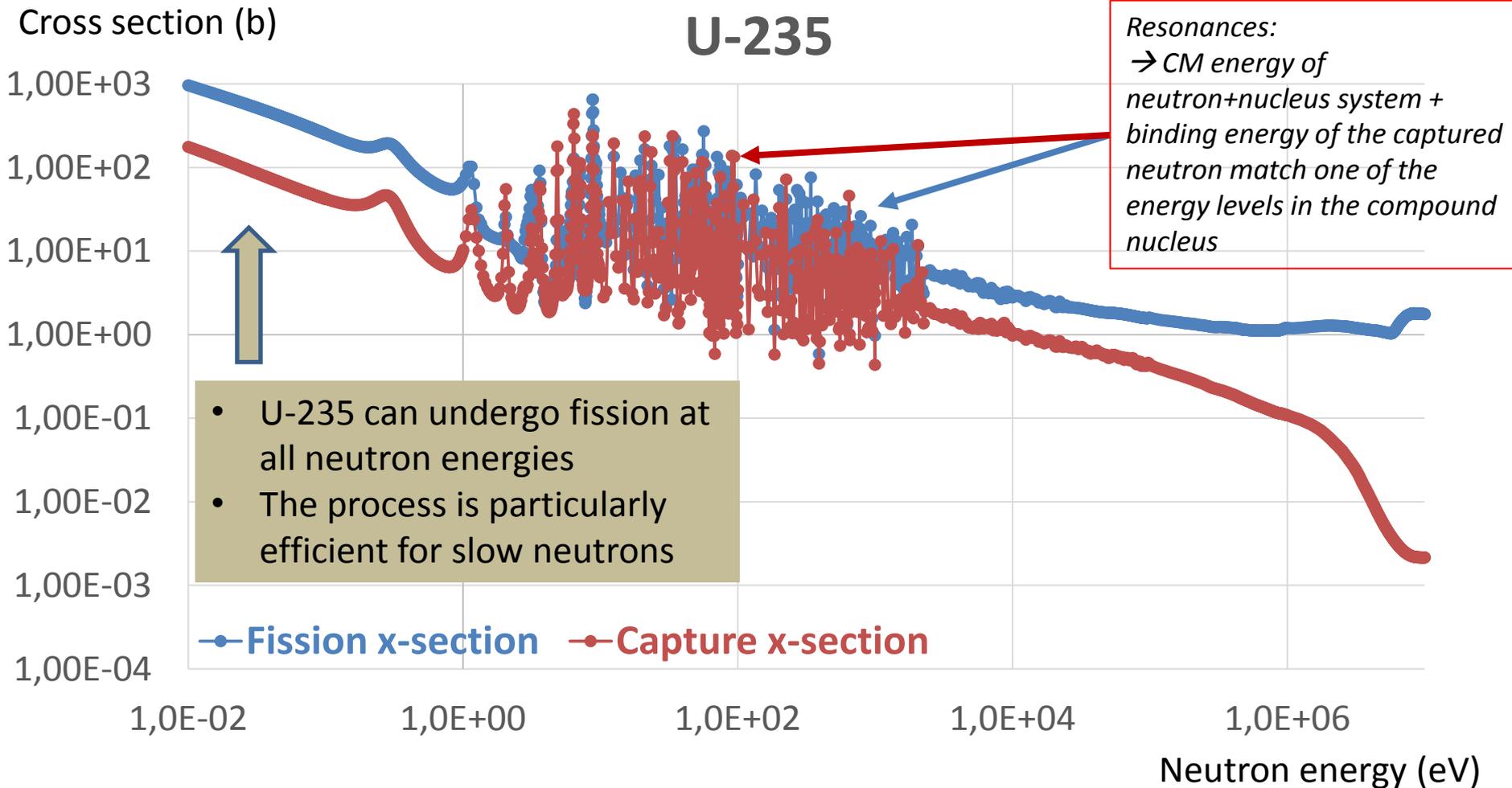
→ Almost  $10^{20}$  neutrons/sec emitted, about  $2 \times 10^{20}$  neutrinos/sec

→  $\phi \sim 10^{14}$  neutrons  $\text{cm}^{-2} \text{s}^{-1}$

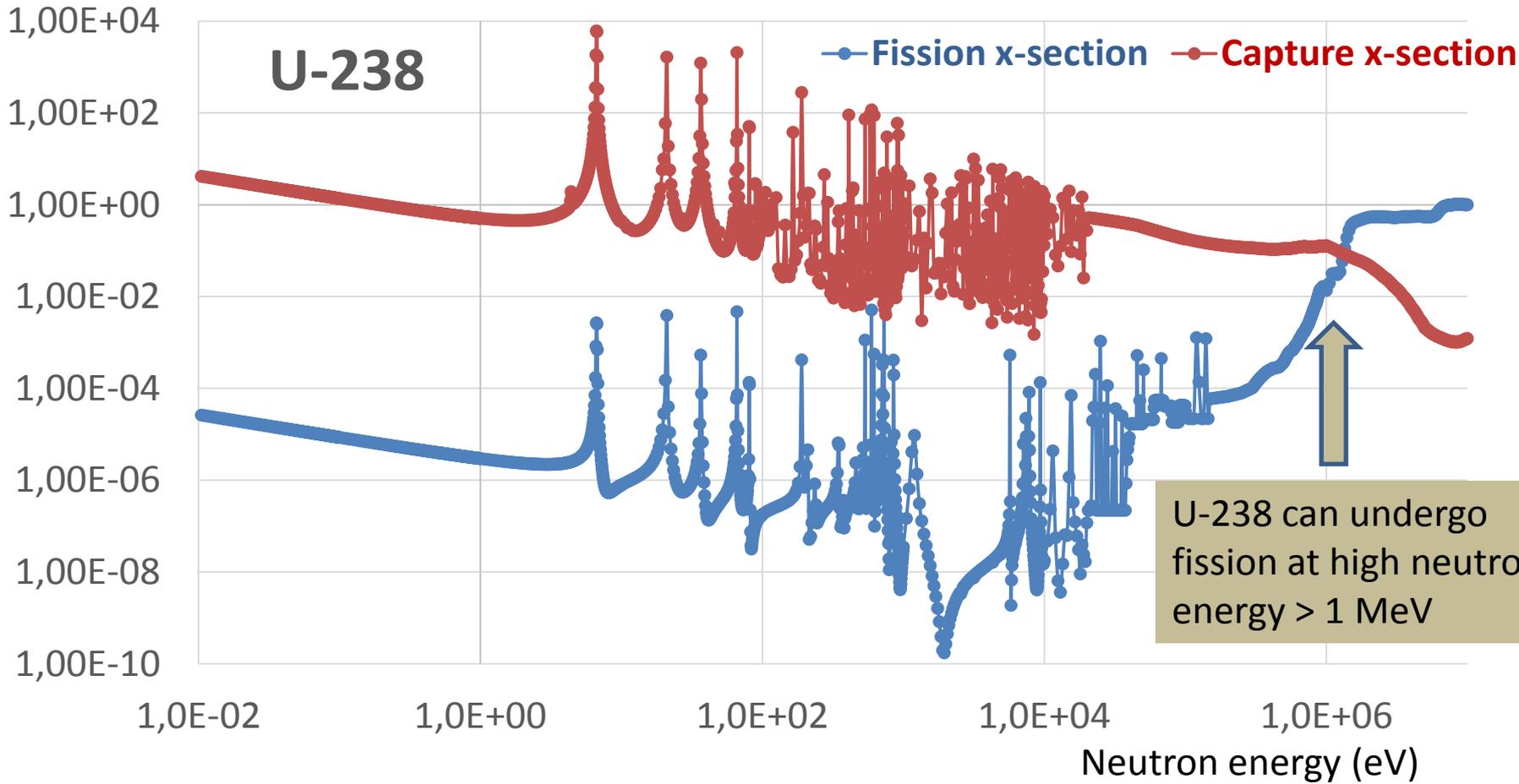
# Nuclear cross sections

Since the nuclear radius is roughly  $10^{-12}$  cm, the geometrical cross sectional area of the nucleus is roughly  $10^{-24} \text{ cm}^2 = 1 \text{ barn}$

Hence we might expect that nuclear cross sections are of the order of  $10^{-24} \text{ cm}^2 \equiv 1 \text{ barn}$   
However, quantum mechanical effects can make nuclear cross sections a lot bigger...

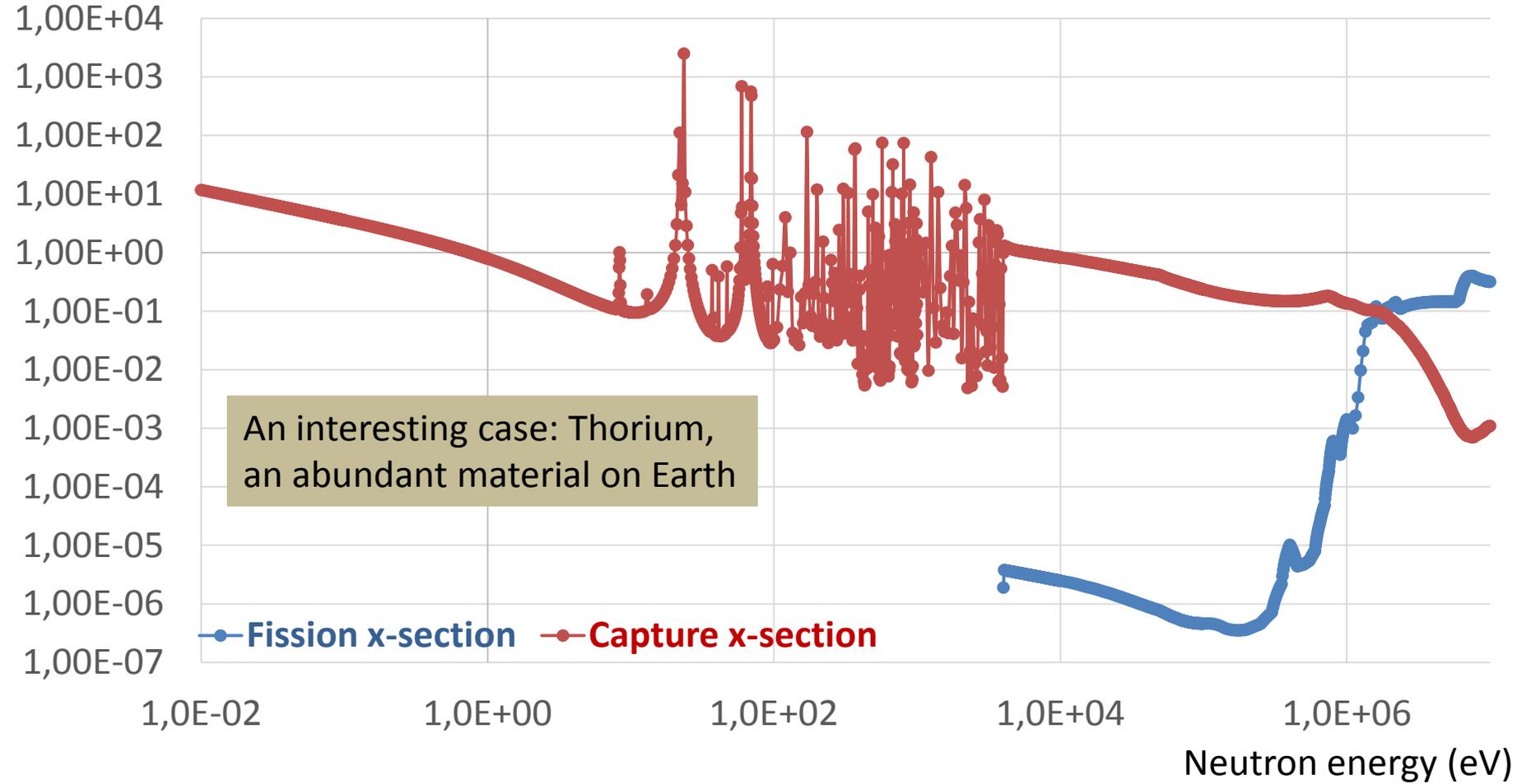


Cross section (b)



Cross section (b)

# Th-232

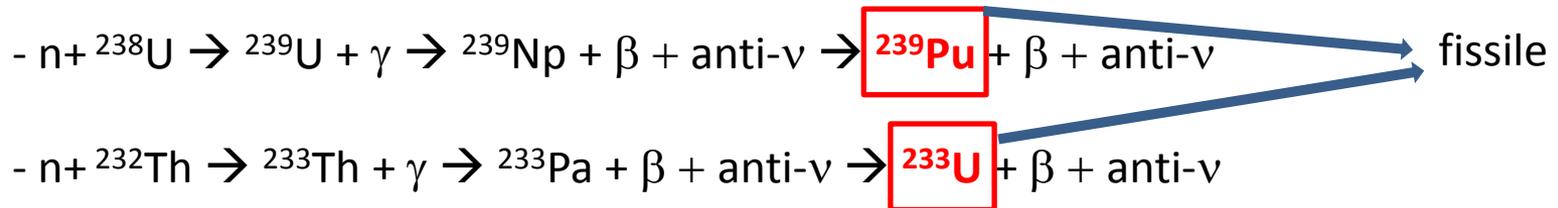


# Fissile, fissionable, fertile isotopes

- Heavy nuclei with a high fission cross section at low (thermal) neutron energies are called **fissile** (e.g.  $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ ,...)

- Those with a non-zero fission cross section only at higher neutron energies are called **fissionable** (e.g.  $^{238}\text{U}$ ,...)

- Those that can produce a fissile isotope via neutron radiative capture and  $\beta$  decay are called **fertile**, i.e. they can be used to **produce fuel** (e.g.  $^{238}\text{U}$ ,...)



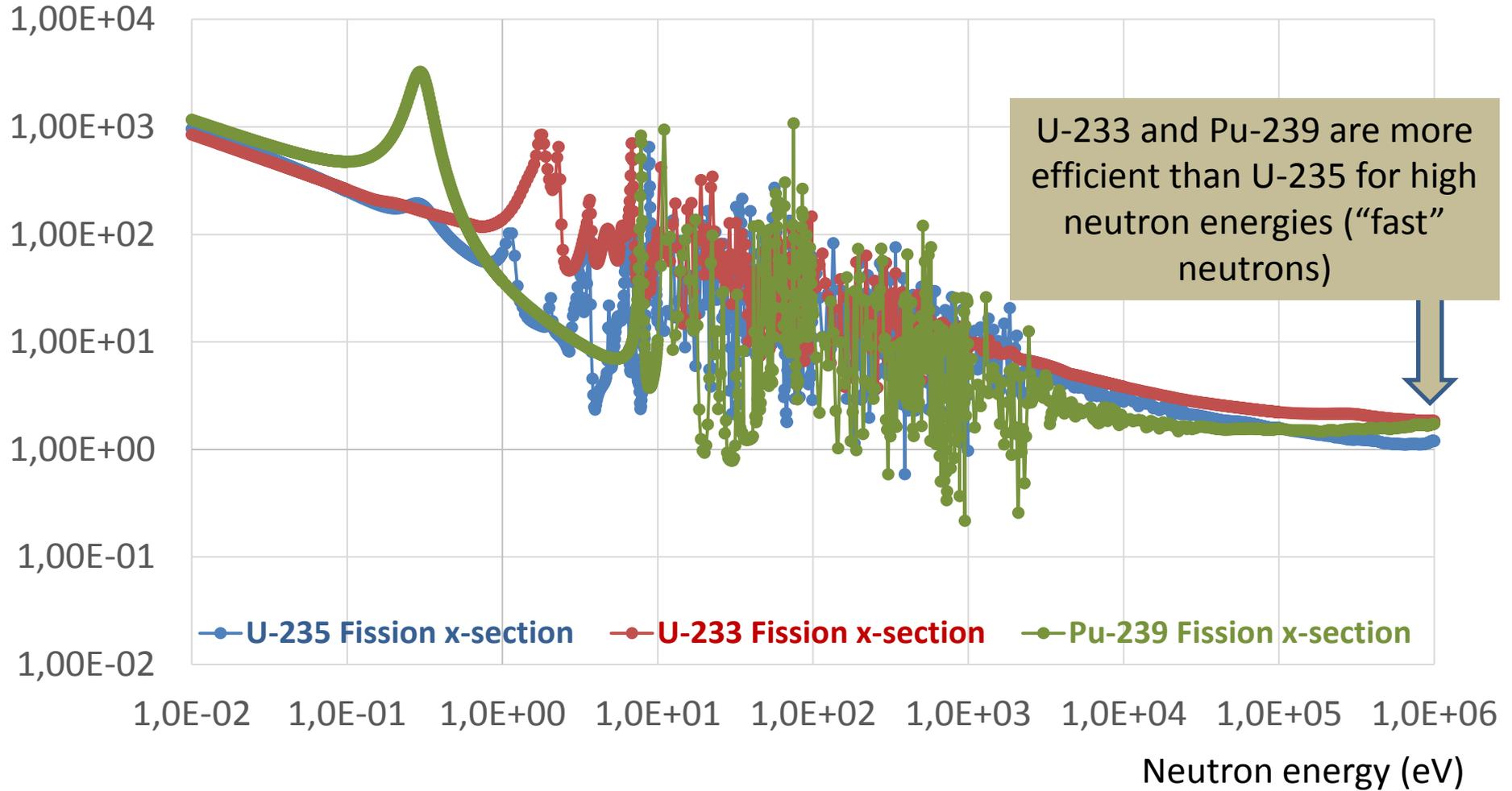
✓ Natural Uranium  $\rightarrow$  0.7 %  $^{235}\text{U}$  + 99.3 %  $^{238}\text{U}$   $\rightarrow$  **most reactors need 3-5 %  $^{235}\text{U}$   $\rightarrow$  “enrichment” process**

✓ Plutonium production is also called “breeding”

✓ Under certain conditions, a reactor can produce more Pu than it consumes  $\rightarrow$  it is called “breeder”

Cross section (b)

U-235, U-233, Pu-239



# Burning-breeding-burning: the Uranium-Plutonium cycle and the long lifetime radioactive waste production (1 GW<sub>e</sub> LWR)



244, 245Cm  
1.5 Kg/yr

241Am: 11.6 Kg/yr  
243Am: 4.8 Kg/yr

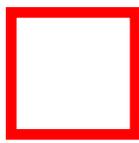
239Pu: 125 Kg/yr

237Np: 16 Kg/yr

LLFP  
76.2 Kg/yr

Fissile fuel  
↑

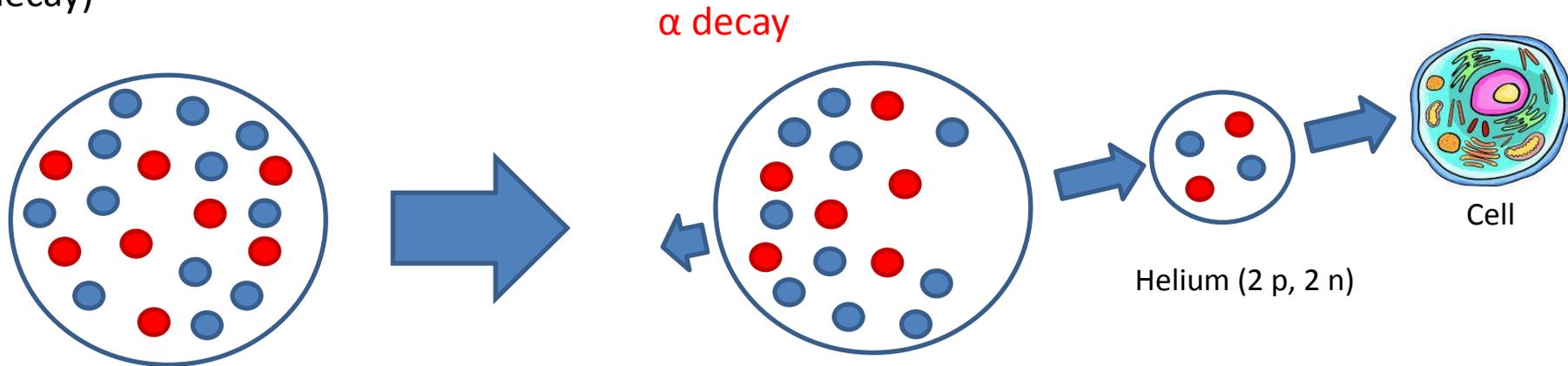
LLFP=Long Life Fission Products



Transuranics = Minor Actinides + Pu

# Transuranics and waste

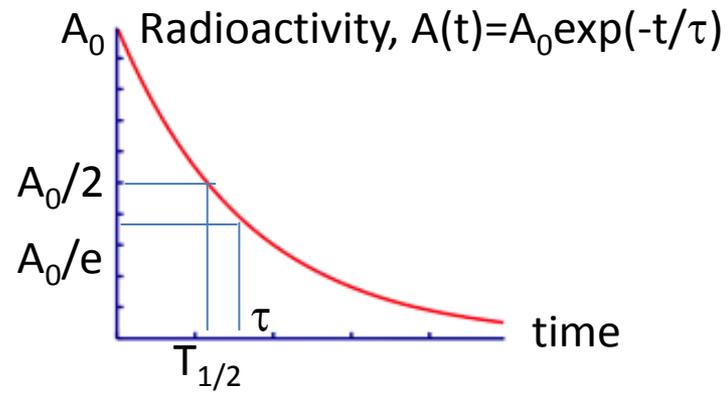
- ✓ Operating a fission reactor means that long-lived radioactive nuclides are produced
- ✓ Many transuranics are long-lived and undergo  $\alpha$  decay (followed by  $\gamma$  emissions)
- ✓ Such radioactive nuclei can be dangerous for the environment and the human health (due to direct exposure in the case of  $\gamma$ 's and due to ingestion or inhalation in the case of  $\alpha$  and  $\beta$  decay)



Uranium 238 (92 protons, 146 neutrons)

Thorium 234 (90 protons, 144 neutrons)

Nuclide	Half-life $T_{1/2}$ (years)
Pu-239	24,000
Pu-242	$3.7 \times 10^5$
Am-241	433



# IAEA Scheme for Classification of Radioactive Waste (2009)

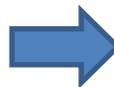
1. Exempt waste (EW) – such a low radioactivity content, which no longer requires controlling
2. Very short-lived waste (VSLW) – can be stored for a limited period of up to a few years to allow its radioactivity content to reduce by radioactive decay. It includes waste containing radionuclides with very short half-lives often used for research and medical purposes
3. Very low level waste(VLLW) – usually has a higher radioactivity content than EW but may, nonetheless, not need a high level of containment and isolation. Typical waste in this class includes soil and rubble with low levels of radioactivity which originate from sites formerly contaminated by radioactivity
4. Low level waste (LLW) - this waste has a high radioactivity content but contains limited amounts of long-lived radionuclides. **It requires robust isolation and containment for periods of up to a few hundred years and is suitable for disposal in engineered near-surface facilities.** It covers a very broad range of waste and may include short-lived radionuclides at higher levels of activity concentration, and also long-lived radionuclides, but only at relatively low levels of activity concentration
5. Intermediate level waste (ILW) – because of its radioactivity content, particularly of long-lived radionuclides, it requires a greater degree of containment and isolation than that provided by near surface disposal. **It requires disposal at greater depths, of the order of tens of metres to a few hundred metres**
6. High level waste (HLW) – this is waste with levels of activity concentration high enough to generate significant quantities of heat by the radioactive decay process or waste with large amounts of long-lived radionuclides that need to be considered in the design of a disposal facility for such waste. **Disposal in deep, stable geological formations usually several hundred metres or more below the surface is the generally recognized option for disposal**

# Breeding and burning: the Thorium-Uranium cycle

	Cm 238 2,4 h	Cm 239 3 h	Cm 240 27 d	Cm 241 32,8 d	Cm 242 162,94 d	Cm 243 29,1 a	Cm 244 18,10 a	Cm 245 8500 a	Cm 246 4730 a
Am 236 ? 3,7 m	Am 237 73,0 m	Am 238 1,63 h	Am 239 11,9 h	Am 240 50,8 h	Am 241 432,2 a	Am 242 141 a	Am 243 7370 a	Am 244 26 m	Am 245 10,1 h
Pu 235 25,3 m	Pu 236 2,858 a	Pu 237 45,2 d	Pu 238 87,74 a	Pu 239 2,411 · 10 <sup>4</sup> a	Pu 240 6563 a	Pu 241 14,35 a	Pu 242 3,750 · 10 <sup>5</sup> a	Pu 243 4,956 h	Pu 244 8,00 · 10 <sup>7</sup> a
Np 234 4,4 d	Np 235 396,1 d	Np 236 22,5 h	<b>Np 237</b> 2,144 · 10 <sup>6</sup> a	Np 238 2,117 d	Np 239 2,355 d	Np 240 7,22 m	Np 241 13,9 m	Np 242 2,2 m	Np 243 1,85 m
<b>U 233</b> 1,592 · 10 <sup>5</sup> a	U 234 0,0055	U 235 0,7200	U 236 120 ns	U 237 16,75 d	U 238 99,2745	U 239 23,5 m	U 240 14,1 h		U 242 16,8 m
Pa 232 1,31 d	Pa 233 2,0 d	Pa 234 1,17 m	Pa 235 24,2 m	Pa 236 9,1 m	Pa 237 8,7 m	Pa 238 2,3 m		148	150
Th 231 25,5 h	<b>Th 232</b> 1,405 · 10 <sup>10</sup> a	Th 233 22,3 m	Th 234 24,10 d	Th 235 7,1 m	Th 236 37,5 m	Th 237 5,0 m			

Fission products

Fission products



Much lower production of Transuranics

## Remember that

- ✓  $1 \text{ GW}(th) = 1 \text{ GW thermal power}$
- ✓  $1 \text{ GW}(e) = 1 \text{ GW electrical power}$
- ✓ *typically, for a fossil-fueled or nuclear power plant, a conversion factor between ~ 30 to 60 % has to be applied to go from thermal to electrical power*

# How much fuel ?

Suppose you've got a **reactor with 1 GW thermal power** ( $1 \text{ GW}_{\text{th}} \rightarrow \sim 300 \text{ Mw}_e$ ) =  $10^9$  Joule/sec

Assume each fission releases order of 200 MeV energy =  $3.2 \times 10^{-11}$  Joule

→ In the reactor the fission rate is about  $3 \times 10^{19}$  fissions/sec

→ which means that e.g.  $3 \times 10^{19}$  (nuclei of  $^{235}\text{U}$ )/sec disappear (actually a bit more because of radiative capture)

Fuel	Istantaneous consumption (per second)	Yearly consumption (90 % load factor)
Uranium	0.012 g	340 Kg
Natural Gas	25 m <sup>3</sup>	700 million m <sup>3</sup>
Crude oil	0.02 tons	0.7 million tons
Lignite	100 Kg	2.8 million tons
Coal	40 Kg	1.1 million tons

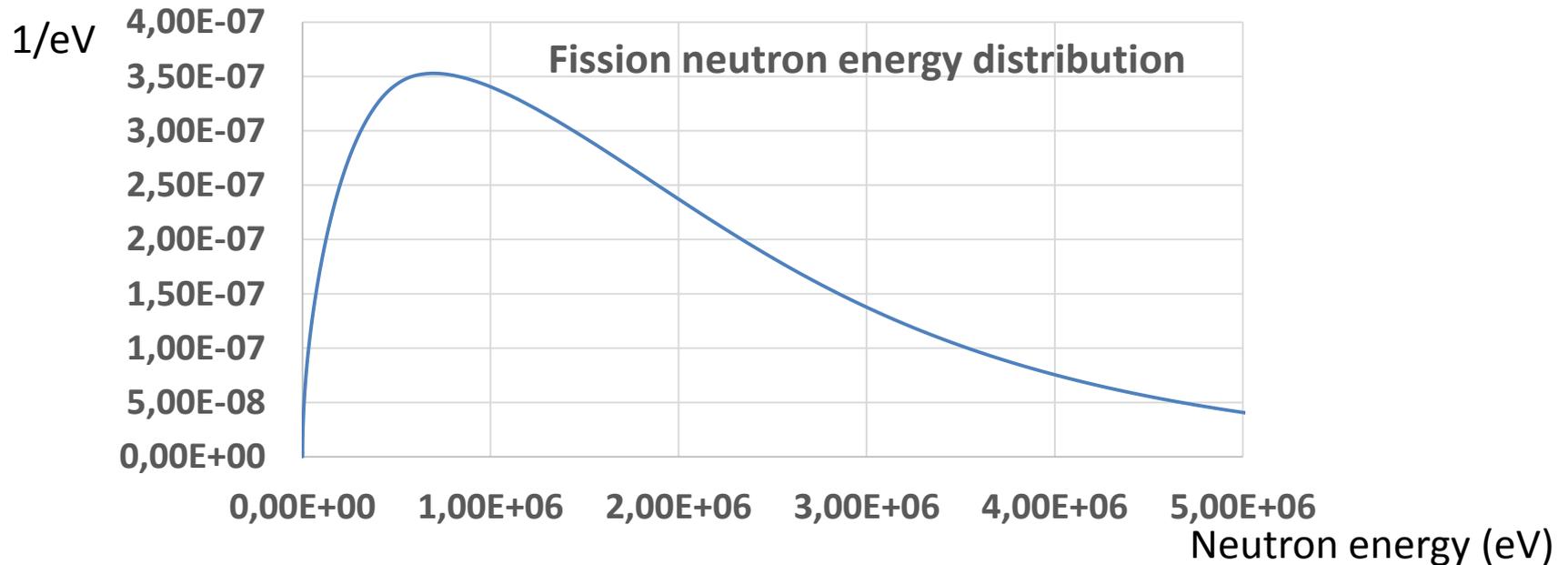
For a thermal reactor (see later) loaded with mixed  $\text{UO}_2$  fuel (density about 11 gr/cm<sup>3</sup>) comprising 4 %  $^{235}\text{U}$  and 96 %  $^{238}\text{U}$ , this corresponds to 8500 Kg of fuel → 0.8 m<sup>3</sup>

**In practice, there has to be much more** as the chain reaction needs the presence of fissile nuclei at all times → the reactor has to be critical at all times

**However,  $^{235}\text{U}$  consumption is partly compensated by Plutonium ( $^{239}\text{Pu}$ ) breeding**

(\* ) load factor=percentage of time when the reactor is actually producing electricity

# Fission spectrum, fast and slow neutrons



It is customary to adopt the following classification:

- **slow neutrons**: those with kinetic energy  $T_n < 1$  eV
- in particular **thermal neutrons** have  $T_n$  around 0.025 eV or 25 meV (the value of  $kT$ , where  $k$  is the Boltzmann constant and  $T$  is the temperature)
- **epithermal neutrons**:  $1$  eV  $< T_n < 100$  keV (0.1 MeV)
- **fast neutrons**:  $0.1$  MeV  $< T_n < 20$  MeV

Obviously neutrons in general can have energies above 20 MeV but this is an extreme limit in reactor physics (e.g. neutrons from D+T fusion have 14 MeV fixed energy)

# Slowing down neutrons (moderation)

It is easy to show in non-relativistic kinematics that **after a scattering off a nucleus with mass number  $A$** , the kinetic energy of the neutron changes according to the ratio

$$\frac{T'_n}{T_n} = \frac{m_n^2 + m_A^2 + 2m_n m_A \cos\theta_{CM}}{(m_n + m_A)^2}$$

Assuming an isotropic CM cross section that does not depend on  $\cos\theta_{CM}$ , the corresponding term averages out to zero, so that we can write on average

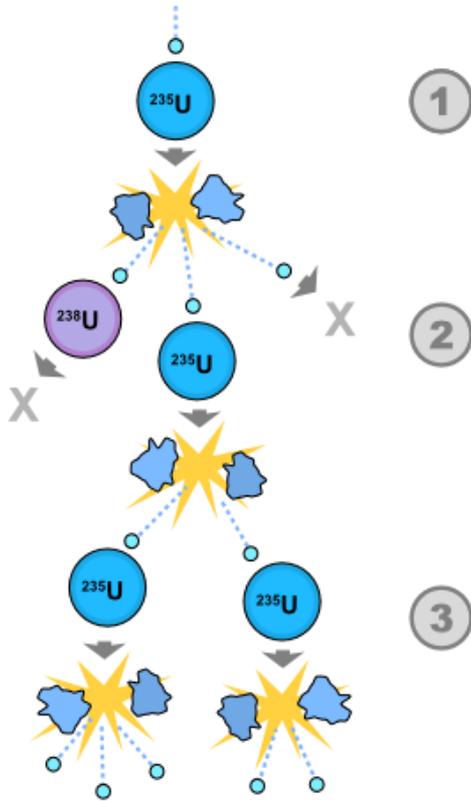
$$\frac{T'_n}{T_n} = \frac{m_n^2 + m_A^2}{(m_n + m_A)^2} \quad \rightarrow \text{Assuming } M_A \cong Am_n \rightarrow \frac{T'_n}{T_n} = \frac{1 + A^2}{(1 + A)^2}$$

For a **heavy nucleus  $A \gg 1$**   $\rightarrow T'_n \cong T_n$  or in other words, the neutron has to undergo many collisions in order to significantly lose energy.

Consider instead the case  **$A=1$**   $\rightarrow$  (target containing hydrogen, i.e. protons as nuclei)  $T'_n = T_n/2$  i.e. on average a neutron will lose half of its energy at each collision and therefore few collisions are sufficient to rapidly decrease its energy

**$\rightarrow$  Moderators = light materials containing hydrogen = water, paraffin or graphite**

# The chain reaction and the critical reactor



The chain reaction:

- must not diverge (more and more fissions at each “generation”)
- must not die away (less and less fissions at each generation)

→ precisely one neutron from each fission has to induce another fission event

The remaining fission neutrons will then either be

- absorbed by radiative capture or
- will leak out from the system

Suppose we can count the number of neutrons in one generation and in the next one  
Then

$$k \equiv \frac{\text{number of neutrons in one generation}}{\text{number of neutrons in the preceding generation}}$$

- The condition  $k=1$  corresponds to a **critical reactor**
- $k>1$  is a **supercritical reactor** (chain reaction diverges)
- $k<1$  is a **subcritical reactor** (chain reaction dies away)

# “Simple-minded” reactor kinetics

$$\frac{dn(t)}{dt} = P(t) - L(t)$$

$n(t)$ =neutron population at time  $t$

$P(t)$ = neutron production at time  $t$  (mainly as fission products)

$L(t)$ =neutron loss (fission+capture+leakage) at time  $t$

All are functions of time as reactor evolves over time

➔ Alternative definition  $k \equiv \frac{P(t)}{L(t)}$       Neutron lifetime  $\equiv \tau \equiv \frac{n(t)}{L(t)}$

➔  $\frac{dn(t)}{dt} = \frac{k-1}{\tau} n(t)$       Let's assume  $k$  and  $\tau$  are time independent (not true...)

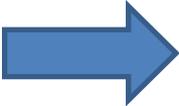
$$n(t) = n_0(t) \exp\left(\frac{k-1}{\tau} t\right)$$

- $k=1 \rightarrow$  steady state  $\rightarrow$  critical reactor
- $k>1 \rightarrow$  increase  $\rightarrow$  supercritical
- $k<1 \rightarrow$  decrease  $\rightarrow$  subcritical

Time constant  $\equiv T \equiv$  Reactor period  $\equiv \frac{\tau}{k-1}$

# Delayed neutrons: crucial for reactor control

Typical neutron lifetime in a thermal power reactor  $\sim 10^{-4}$  sec

If  $k=1.001$    $T=0.1$  sec  power will increase by 2.7 in 0.1 sec !!

Actually, **we neglected** the very small amount ( $< 1\%$ ) of **delayed neutrons**

Emitted by fragments after fission on **time scale from ms to sec**

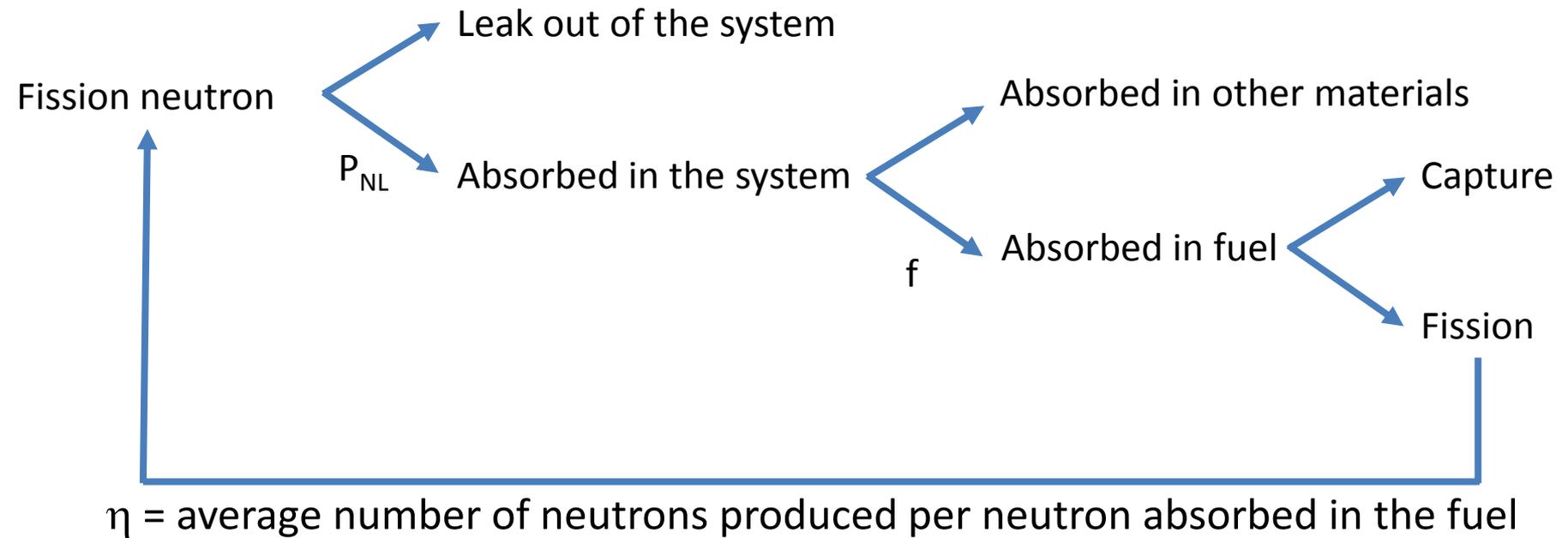
The trick is to **make the reactor critical thanks to that small fraction of neutrons**

→ Delayed neutrons **dominate the reactor response time** making it much longer



Reactor control manageable by absorbers: “control rods”

# Physics of multiplication: path representation



$P_{NL}$  = probability of non-leakage (for a **finite system**)

$f$  = conditional probability that, if neutron will be absorbed, it will be absorbed in fuel

# Physics of multiplication

Multiplication can be written as

$$k = \frac{N_2}{N_1} = \eta f P_{NL}$$

$N_1, N_2$  = number of neutrons in two subsequent generations

$\eta$  = average number of neutrons produced per neutron absorbed in the fuel

where

$$\eta = \nu \frac{\sigma_f^F}{\sigma_a^F}$$

$\sigma_f^F$  = Fission cross section in the fuel  
 $\sigma_a^F$  = Absorption cross section in the fuel  
 $\nu$  = Average number of emitted neutrons

$f$  = conditional probability that, if neutron will be absorbed, it will be absorbed in fuel

$P_{NL}$  = probability of non-leakage

Infinite reactor  $\rightarrow P_{NL} = 1 \longrightarrow k_{\infty} = \eta f$

- ✓ This is a property of the material, not of the geometry
- ✓ For a finite, non-homogenous reactor  $\rightarrow$  **effective k, or  $k_{\text{eff}}$**

# Simple considerations

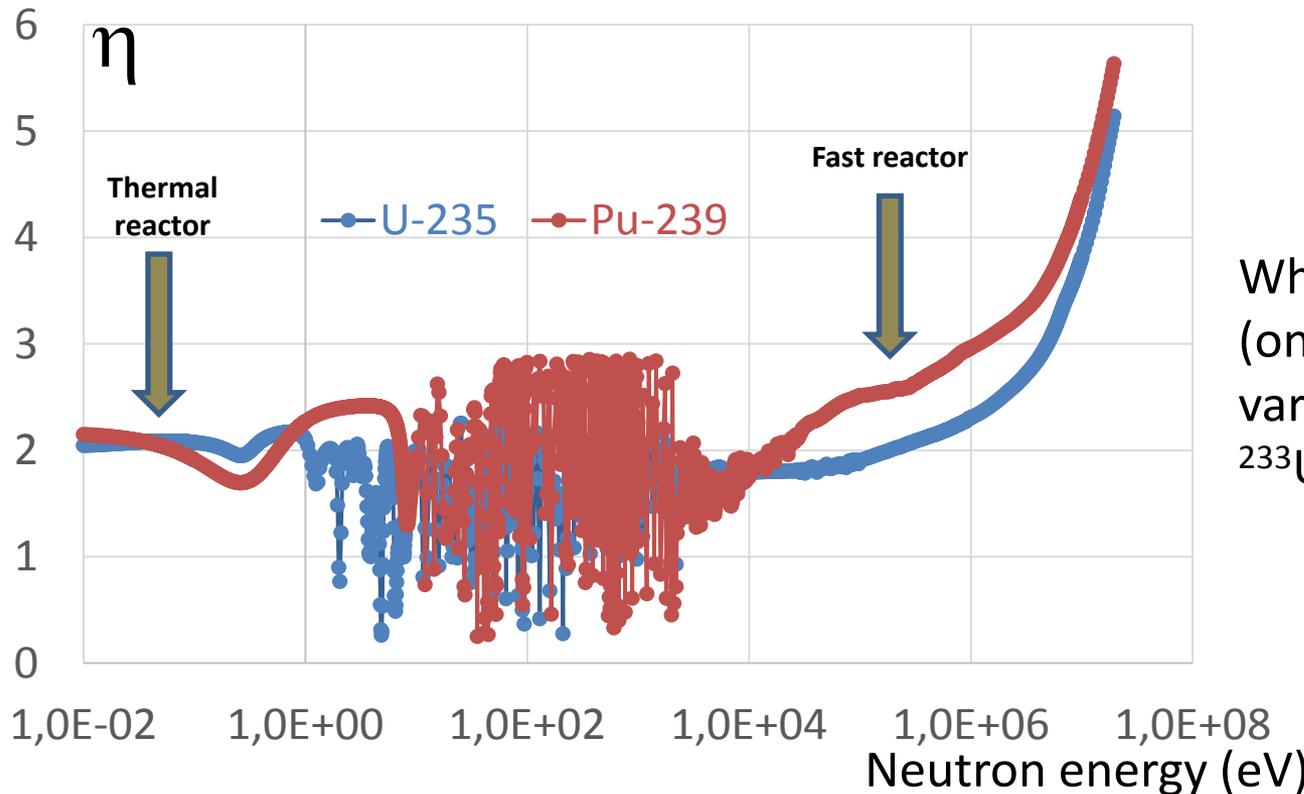
$$k = \frac{N_2}{N_1} = \eta f P_{NL}$$

If  $n$  is absorbed, it is absorbed in the fuel

$$f < 1, P_{NL} < 1$$

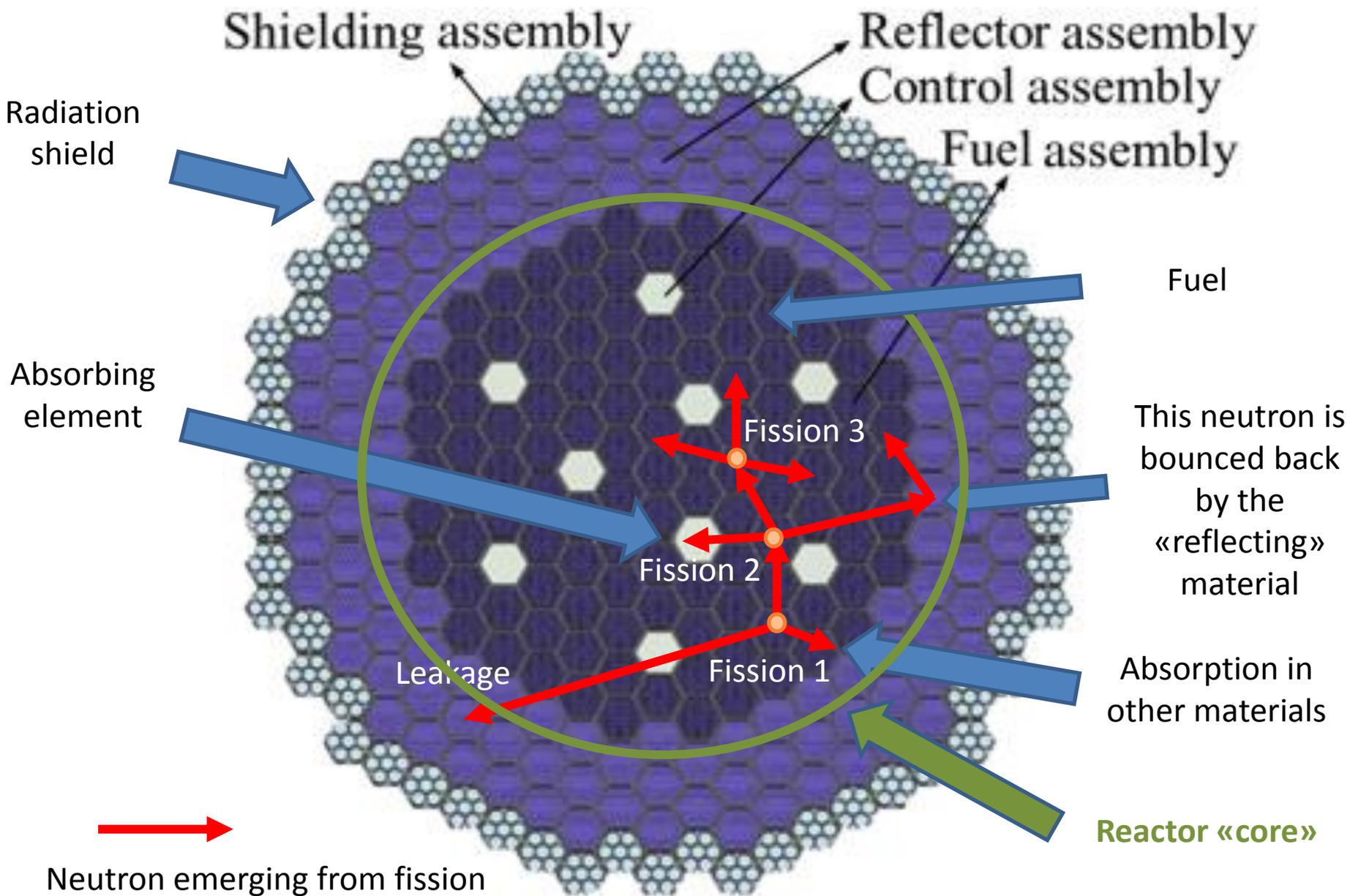


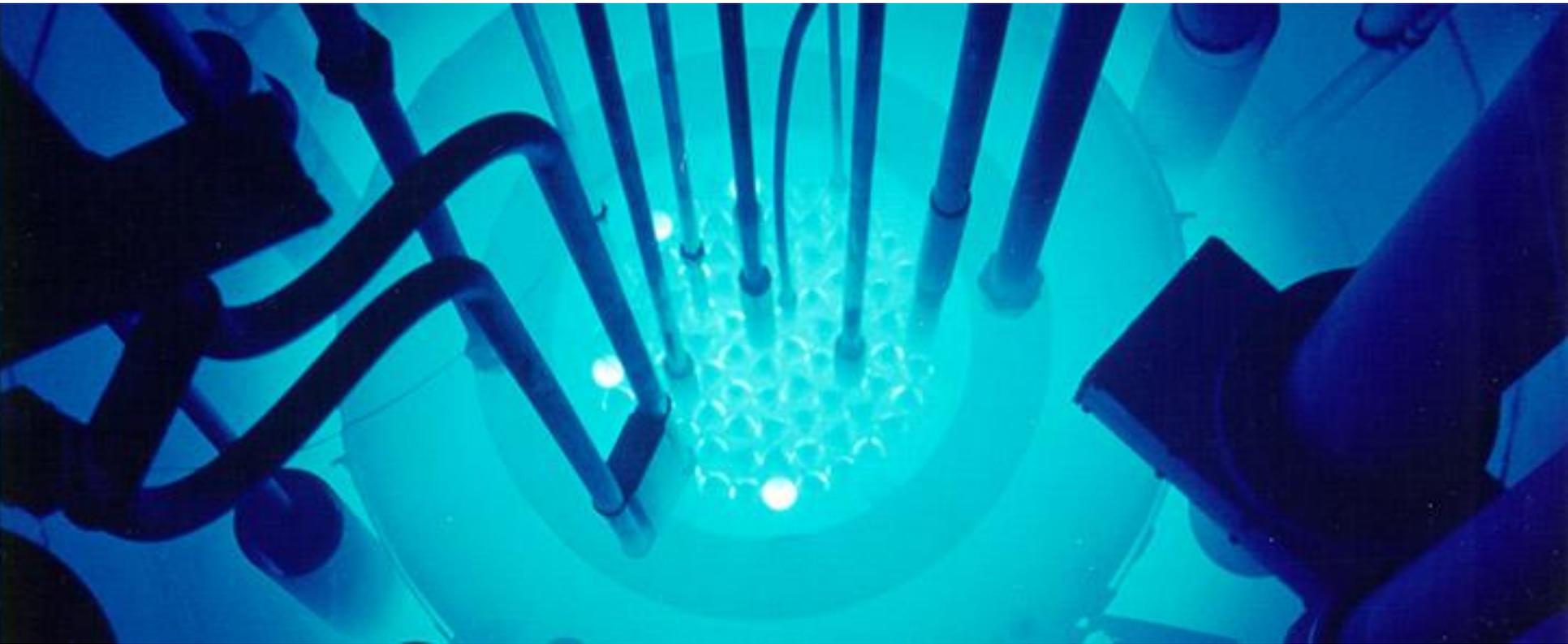
To have  $k \sim 1 \Rightarrow \eta$  significantly  $> 1$



Which is indeed the case  
(on average):  
variation of  $\eta$  with energy for  
 $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ ,  $^{241}\text{Pu}$

# Physics of multiplication: visual representation





# Neutron population and reactor classes

- it is easiest to maintain a fission chain reaction using slow neutrons
- Hence **most nuclear reactors until now (Gen. I to III+)** use **low mass number materials such as water or graphite to slow down or moderate the fast fission neutrons**
- neutrons slow down to energies comparable to the thermal energies of the nuclei in the reactor core
- **Thermal reactor**: average neutron energy comparable to thermal energies
- It requires the **minimum amount of fissile material** for fueling
  - ✓ As an example, a **Light Water Reactor (LWR)** can start with 3 %  $^{235}\text{U}$  + 97 %  $^{238}\text{U}$
  - ✓ **Burn-up** of  $^{235}\text{U}$  is compensated by **breeding** of  $^{239}\text{Pu}$
  - ✓ After 1 year, the core may contain 1 %  $^{235}\text{U}$  + 1 %  $^{239}\text{Pu}$

# Neutron population and reactor classes

However

**the number of neutrons emitted per neutron absorbed in the fuel is largest for fast neutrons**

→ but  $\sigma_f$  is smaller

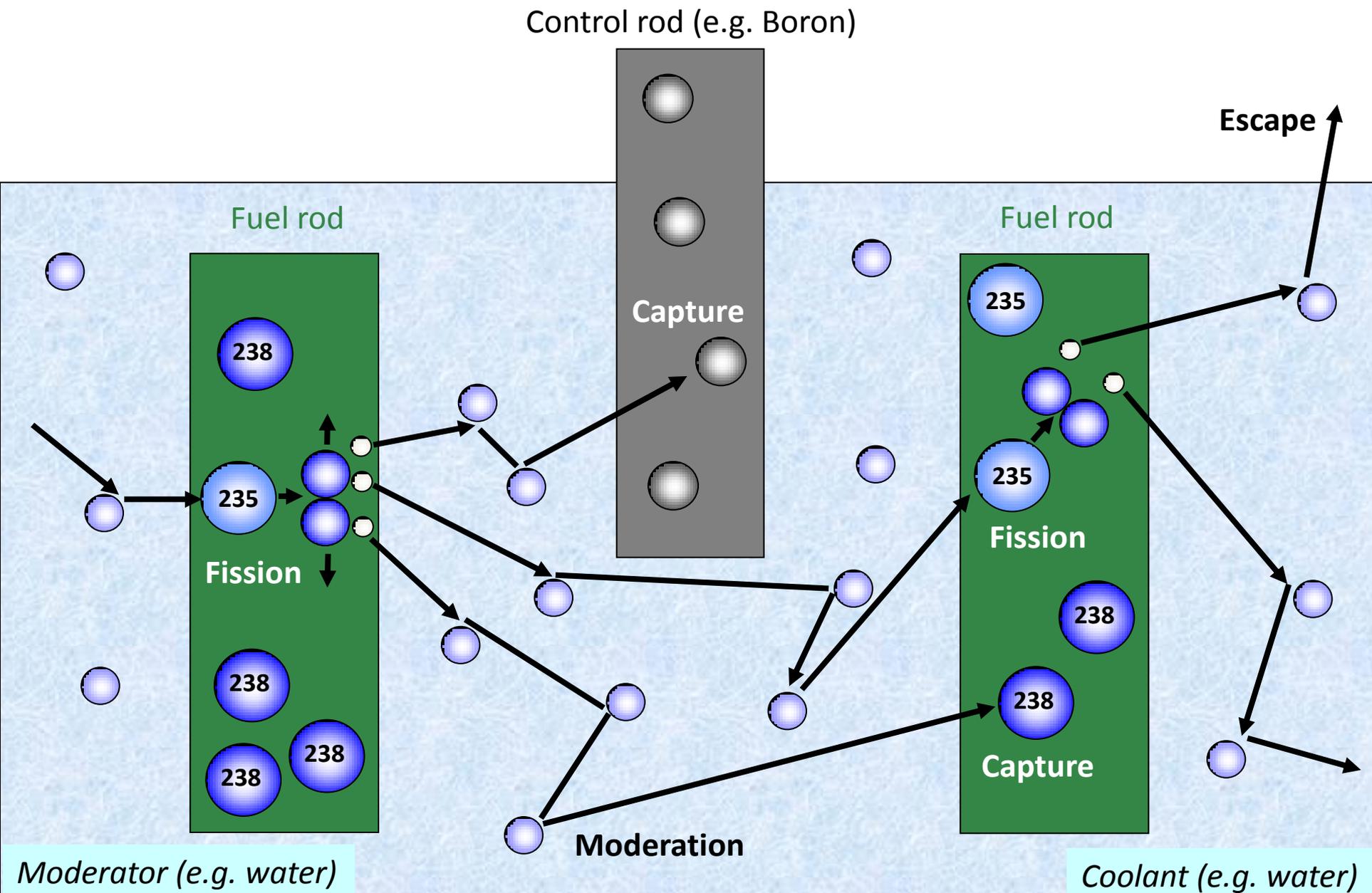
→ **need much more fissile content and higher neutron fluxes** to reach comparable power

→ to keep the neutron energy high, **only high mass-number materials in the core**

→ **Fast reactor**: average neutron energies above 100 keV

→ one can use the "extra" neutrons to **convert or breed new fuel** → "Fast Breeder"

# The thermal reactor





# Nuclear reactor zoo

## Most current reactors

→ **ordinary water** serves as both **coolant** and **moderating material** in the reactor

There are two major types of Light Water Reactors (LWR):

- 1) pressurized water reactors (PWR)
- 2) boiling water reactors (BWR)

In a **PWR** the primary coolant is water maintained under very high pressure (~160 bar)

→ high coolant temperatures ( $> 300^\circ$ ) without steam formation within the reactor

In a **BWR**, the primary coolant water is maintained at lower pressure (~70 bar)

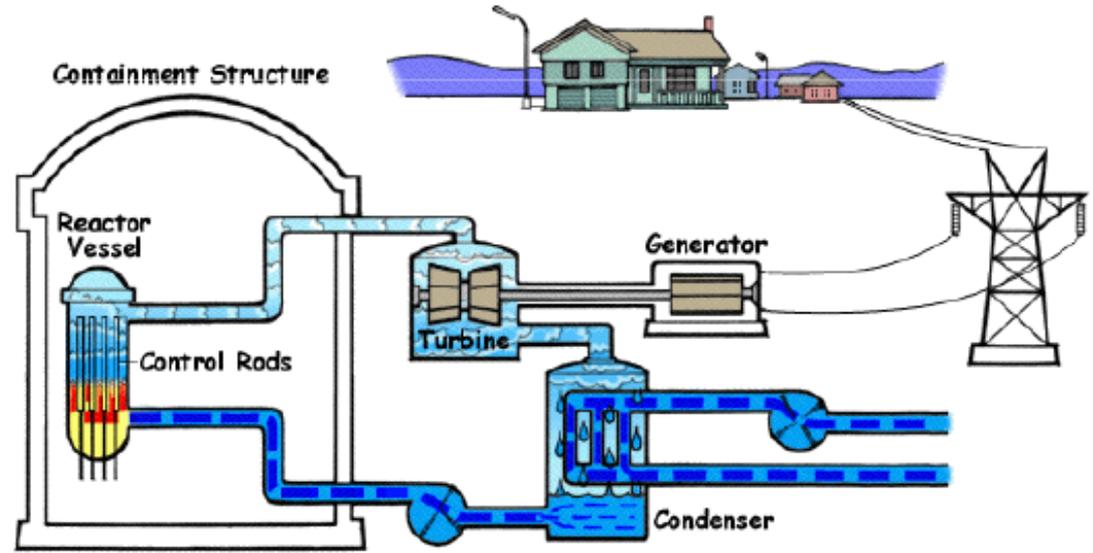
→ appreciable boiling (at  $\sim 285^\circ$ ) and steam within the reactor core itself

→ the reactor itself serves as the steam generator → no secondary loop and heat exchanger

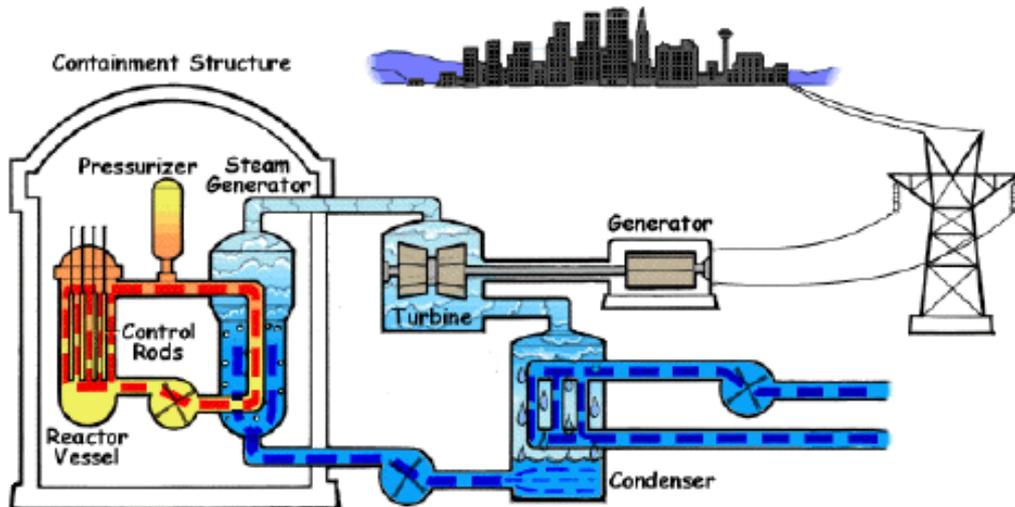
In both PWR and BWR, the nuclear reactor itself and the primary coolant are contained in a **large steel pressure vessel** designed to accommodate the high pressures and temperatures

# BWR and PWR

**BWR**



**PWR**



# Nuclear reactor zoo

## **Heavy water (D<sub>2</sub>O) reactor**

- deuteron has lower neutron capture cross section with respect to hydrogen
- low-enrichment uranium fuels (including natural uranium)
- Developed in Canada in the CANDU (CANadian Deuterium Uranium) series of power reactors and in the UK as Steam Generating Heavy Water Reactors (SGHWR).

## **Gas-based reactors**

- the early MAGNOX reactors developed in the UK: low-pressure CO<sub>2</sub> as coolant
- High-Temperature Gas-cooled Reactor (HTGR, USA): high-pressure helium as coolant
- Pebble-bed concept
- Advanced Gas Reactors (AGR, Germany and UK)

# Decay heat

**Decay heat** is the heat released as a result of radioactive decay: the energy of the alpha, beta or gamma radiation is converted into atomic motion

In nuclear reactors **decay of the short-lived radioisotopes created in fission continues at high power**, for a time after shut down

Heat production comes **mostly from  $\beta$  decay** of fission products

A practical approximation is given by the formula

$$\frac{P}{P_0} = 6.6 \cdot 10^{-2} \left[ \frac{1}{(\tau - \tau_s)^{0.2}} - \frac{1}{\tau^{0.2}} \right]$$

Where P is the decay power,  $P_0$  is the reactor power before shutdown,  $\tau$  is the time since reactor startup and  $\tau_s$  is the time of reactor shutdown measured from the time of startup (in seconds)

 **At shutdown, the heat power is about 6.5 % (~200 MWth for a 1 GWe reactor)  
Sufficient to melt the core....**

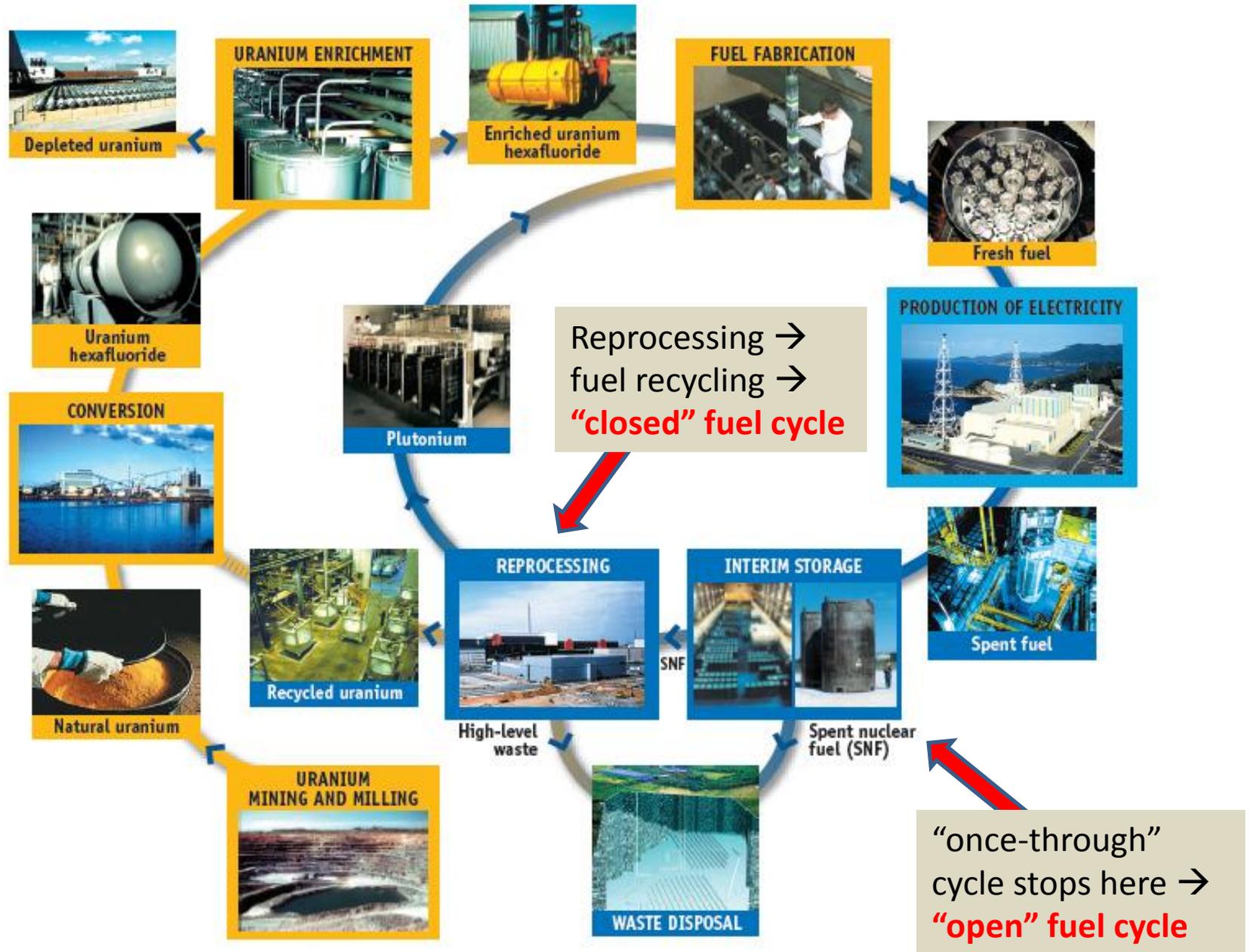
About 1 hour after shutdown, the decay heat will be about 1.5% of the previous core power.  
After a day, the decay heat falls to 0.4%, and after a week it will be only 0.2%

**Spent fuel rods are kept for long time in water pool**, before storage or reprocessing.

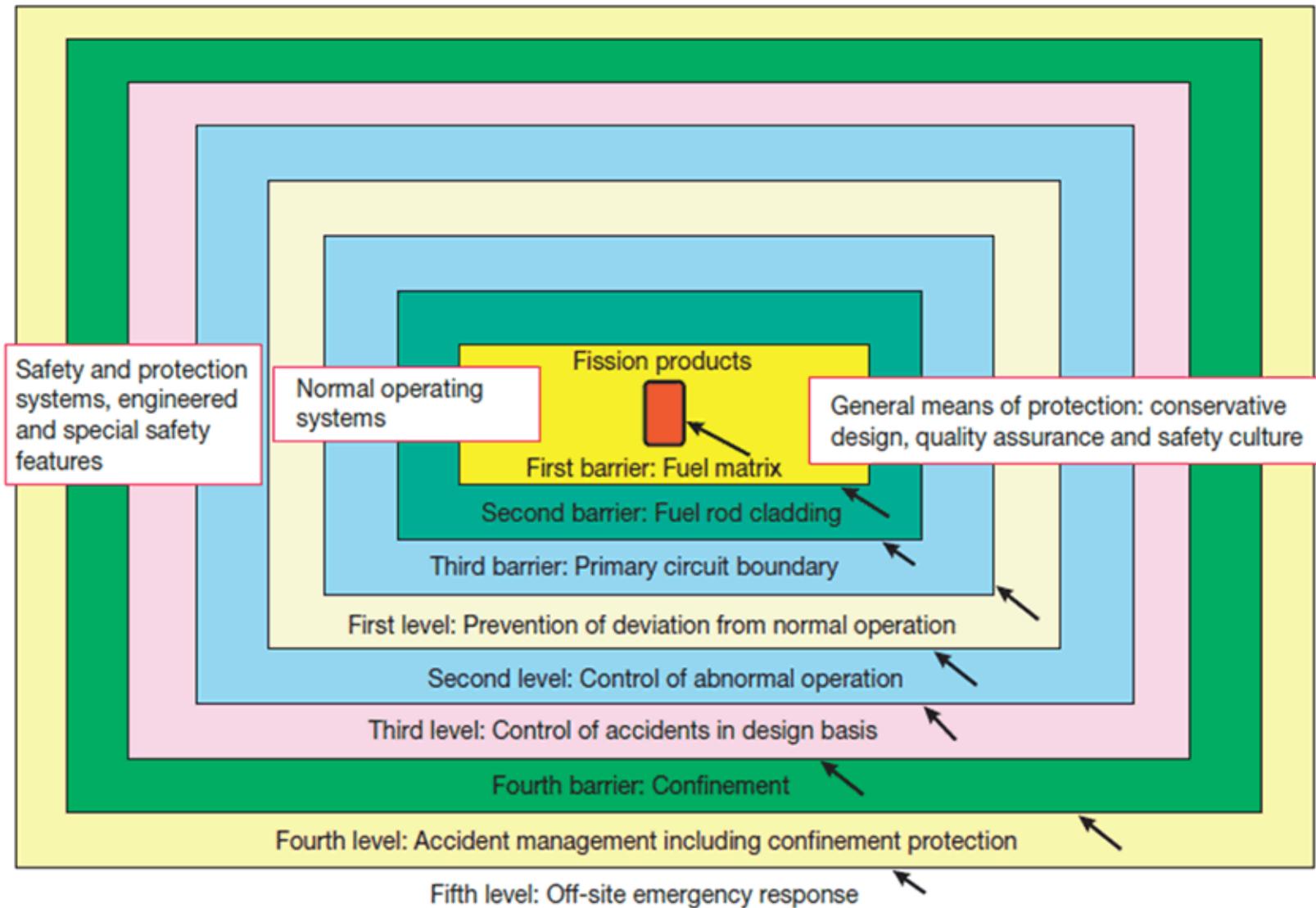
**Removal of decay heat very important → Fukushima...**

**“Heat sink” must not be compromised**

# The nuclear fuel cycle



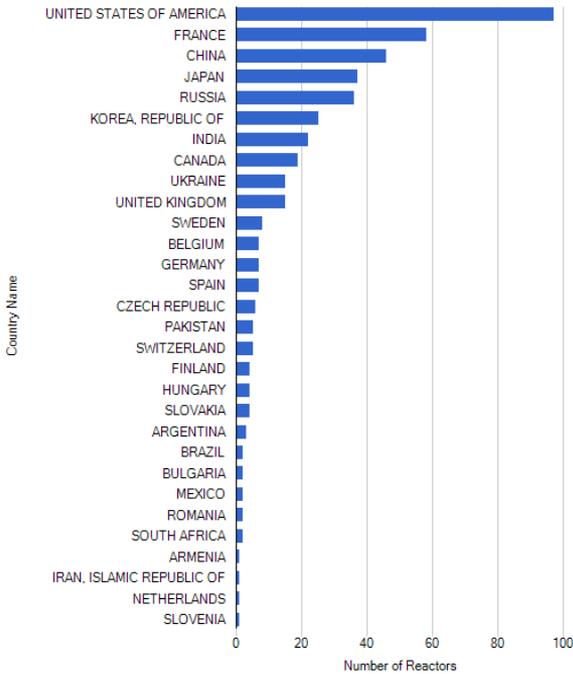
# Safety: defence in depth



Control of abnormal operation should include some (negative) feedback mechanisms:  
e.g. if temperature (power) goes up, reaction cross section goes down

# Nuclear energy today in the world

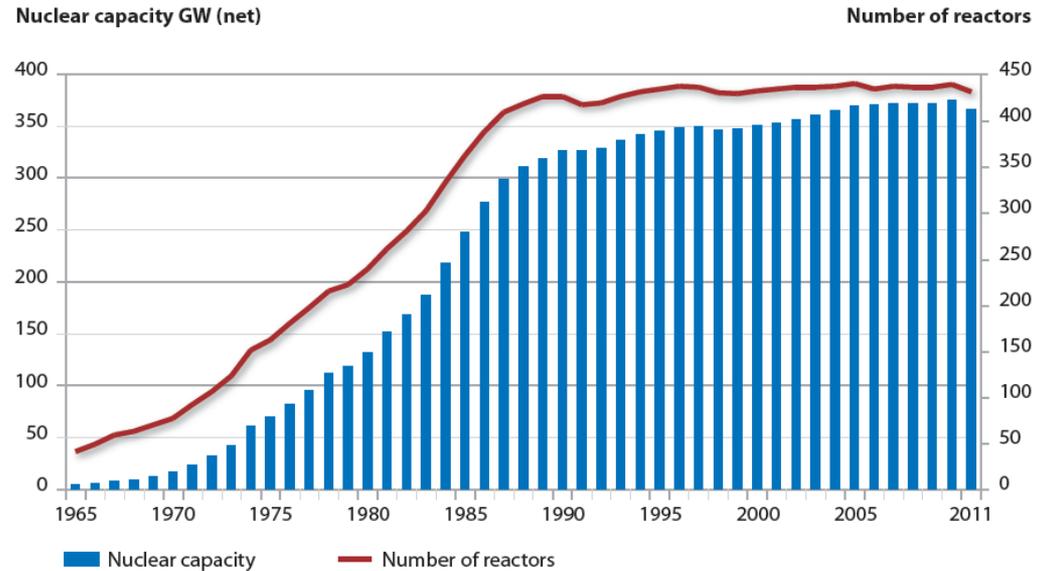
Total Number of Reactors: 449



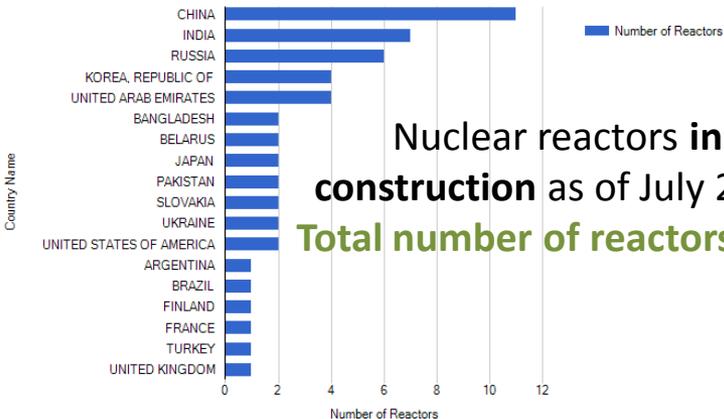
Nuclear reactors **in operation or in long-term shutdown** as of July 2019

**Total number of reactors = 449**

Worldwide nuclear generating capacity and number of operating reactors (1965-2011)



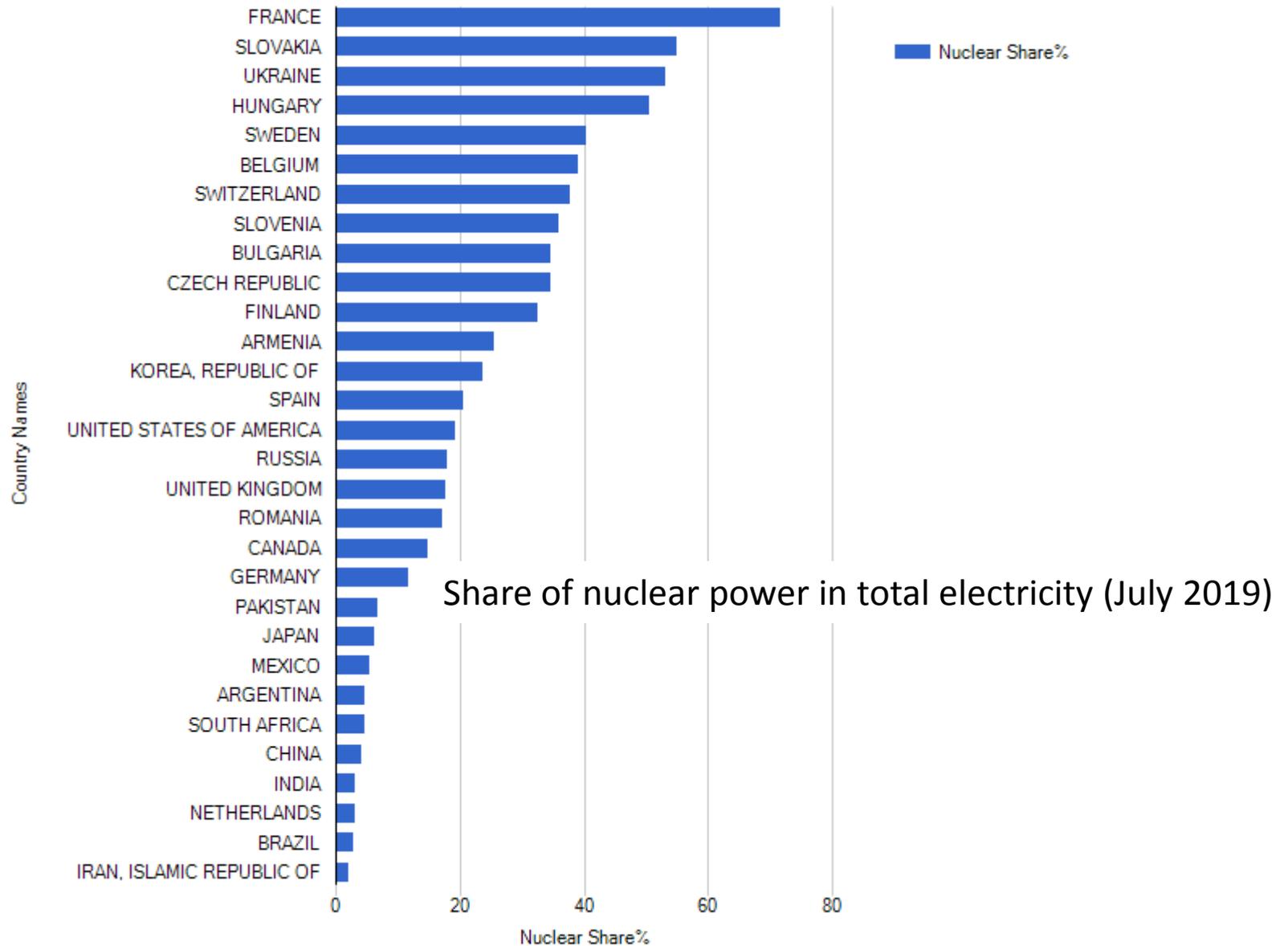
Total Number of Reactors: 54



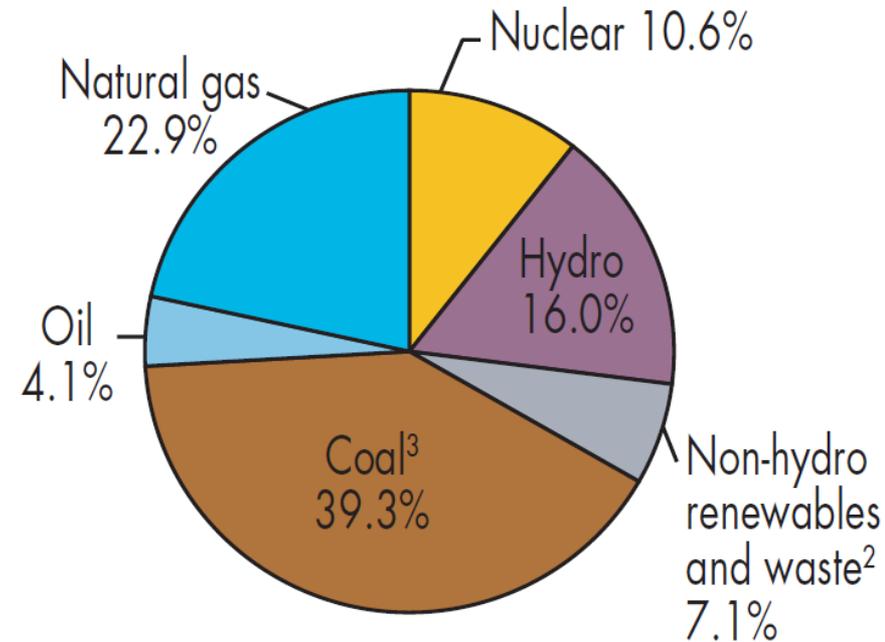
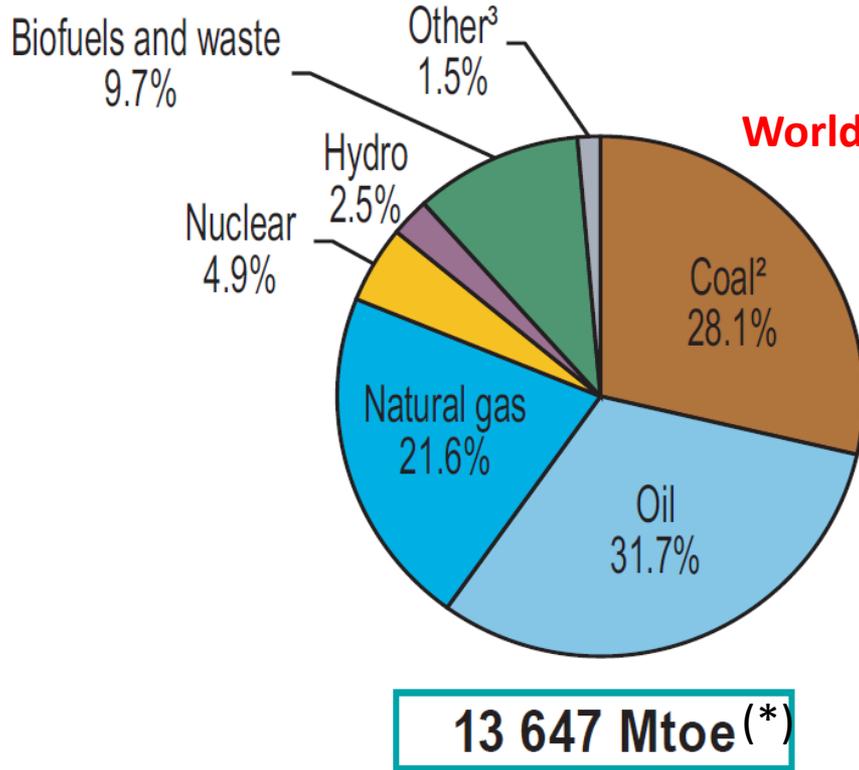
Nuclear reactors **in construction** as of July 2019  
**Total number of reactors = 61**

Source: OECD/NEA – [Nuclear Energy Today 2012](#)

# Share of electricity



# Nuclear energy in the worldwide perspective



## World electricity generation (2015)

1. World includes international aviation and international marine bunkers.
2. In these graphs, peat and oil shale are aggregated with coal.
3. Includes geothermal, solar, wind, tide/wave/ocean, heat and other.

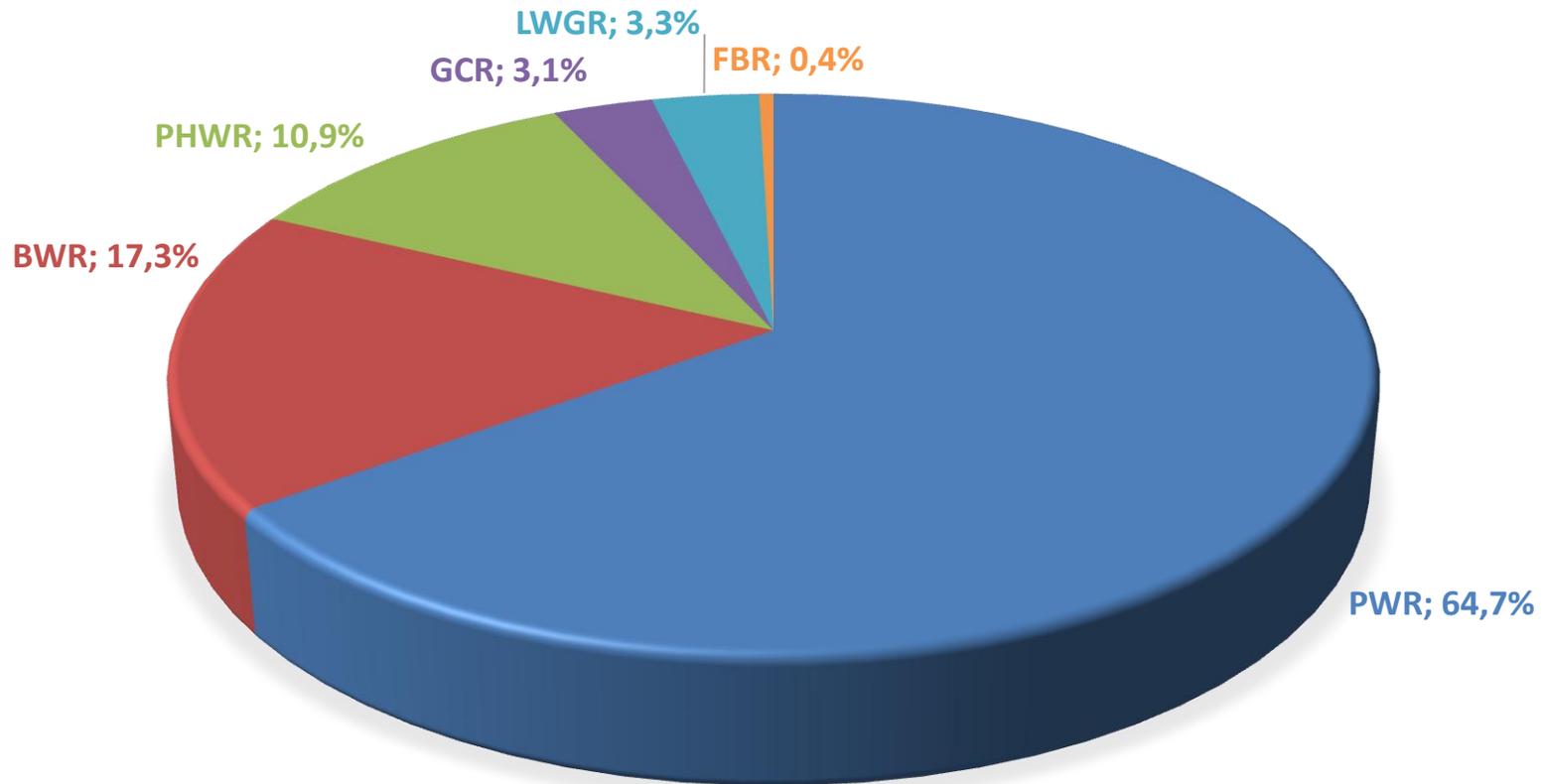
1. Excludes electricity generation from pumped storage.
2. Includes geothermal, solar, wind, tide/wave/ocean, biofuels, waste, heat and other.
3. In these graphs, peat and oil shale are aggregated with coal.

Source: [IEA, Key World Energy Statistics, 2017](#)

(\*) 1 tonne oil equivalent (toe) = 41.868 GJ = 10 Gcal = 11.63 MWh  
 (\*\*) 1 TW =  $10^{12}$  Joule/s, 1 TWh =  $3.6 \cdot 10^{15}$  J

# Reactor types in use worldwide (end of 2016)

## REACTOR TYPES



PWR = Pressurized Water Reactor

BWR = Boiling Water Reactor

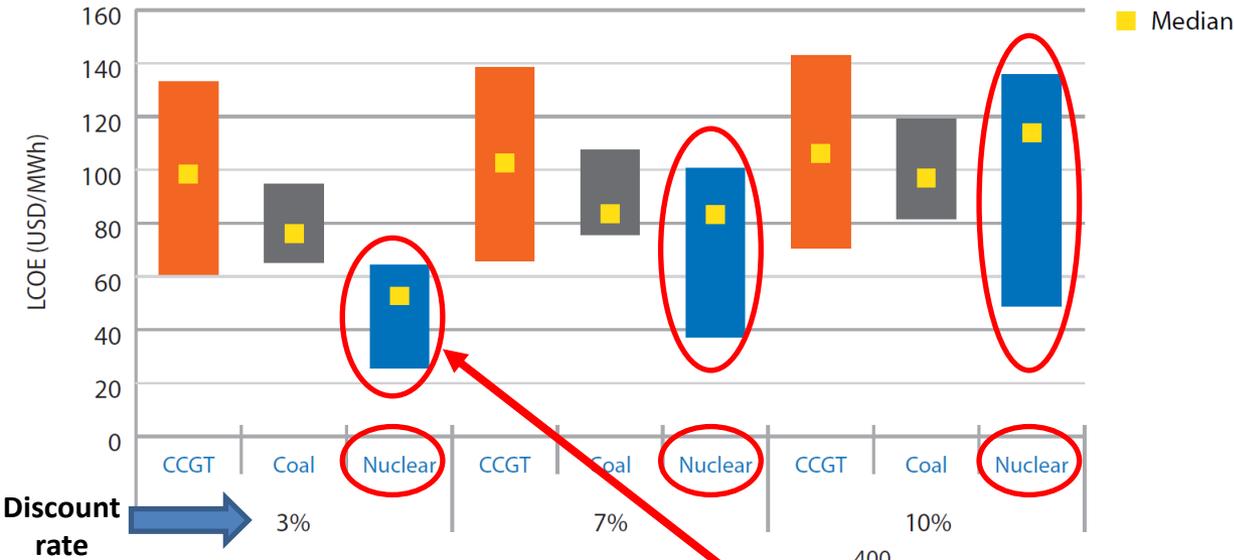
PHWR = Pressurized Heavy Water Reactor

GCR = Gas-Cooled Reactor

LWGR = Light Water cooled, Graphite moderated Reactor

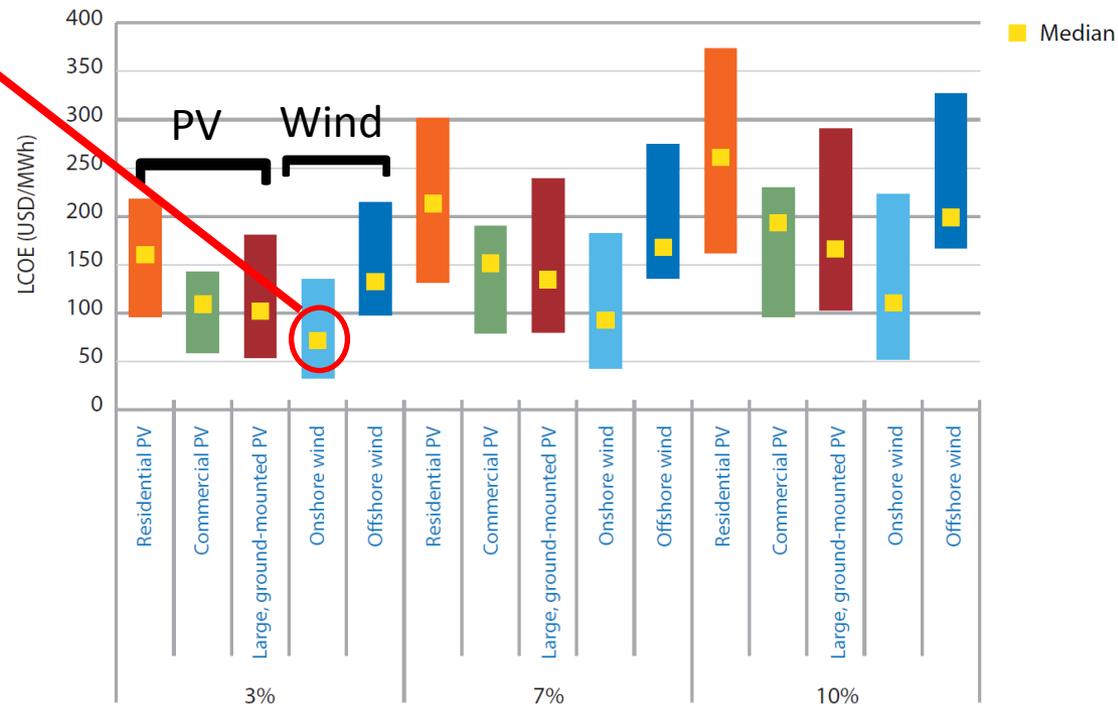
FBR = Fast Breeder Reactor

# Cost of electricity



## LCOE (Levelized Cost Of Electricity) for various technologies (USD/MWh)

- ✓ Measures lifetime costs divided by energy production
- ✓ Calculates present value of the total cost of building and operating a power plant over an assumed lifetime
- ✓ Allows comparison of different technologies with unequal life spans, project size, different capital cost, risk, return, and capacities

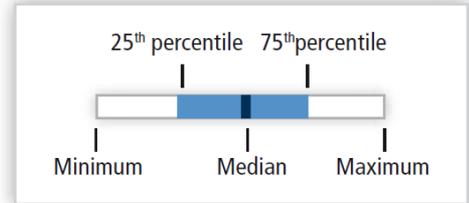
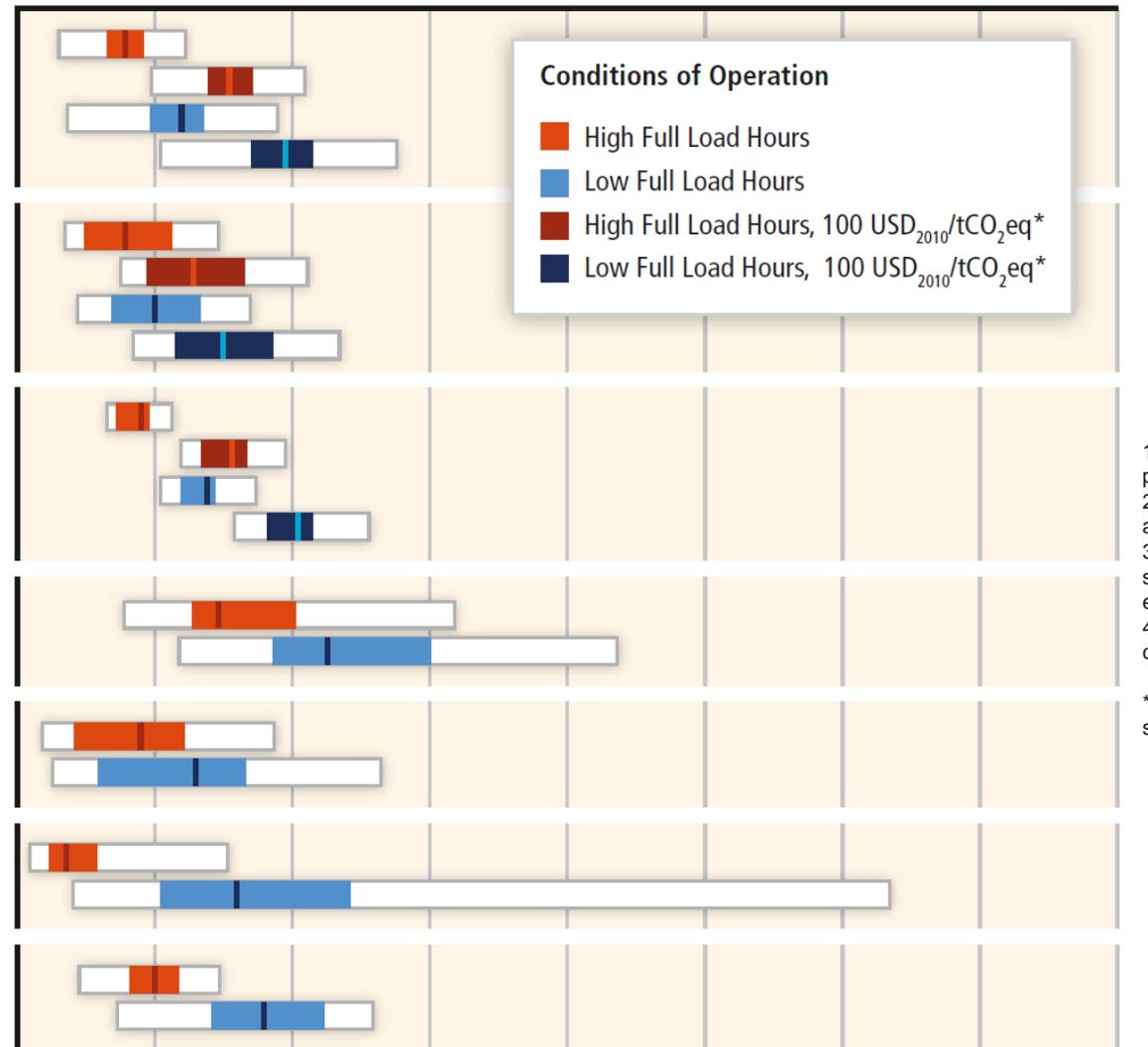


Source:

[IEA/NEA, Projected Costs of Generating Electricity, 2015](#)

# Cost of electricity

Levelized Cost of Electricity at 10% Weighted Average Cost of Capital (WACC) [ $\text{USD}_{2010}/\text{MWh}$ ]



Currently Commercially Available Technologies

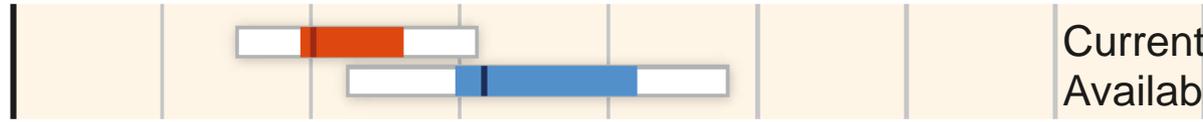
- 1 Assuming biomass feedstocks are dedicated energy plants and crop residues and 80-95% coal input.
- 2 Assuming feedstocks are dedicated energy plants and crop residues.
- 3 Direct emissions of biomass power plants are not shown explicitly, but included in the lifecycle emissions. Lifecycle emissions include albedo effect.
- 4 LCOE of nuclear include front and back-end fuel costs as well as decommissioning costs.

\* Carbon price levied on direct emissions. Effects shown where significant.

Levelized Cost of Electricity at 10% Weighted Average Cost of Capital (WACC) [ $\text{USD}_{2010}/\text{MWh}$ ]

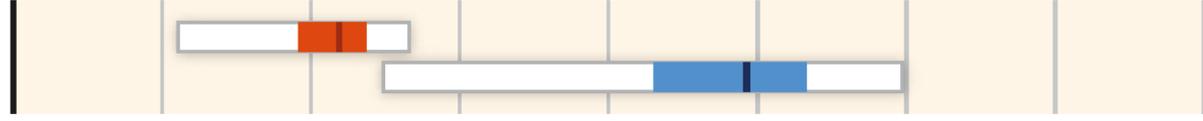
0 100 200 300 400 500 600 700 800

Concentrated Solar Power

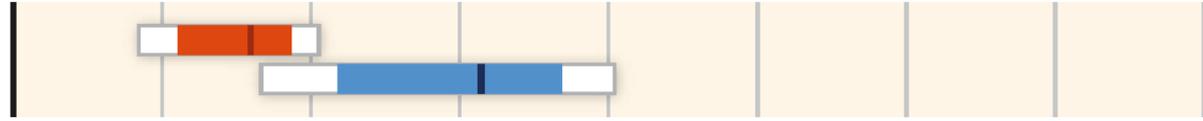


Currently Commercially Available Technologies

Solar PV - Rooftop



Solar PV - Utility



Wind Onshore



Wind Offshore

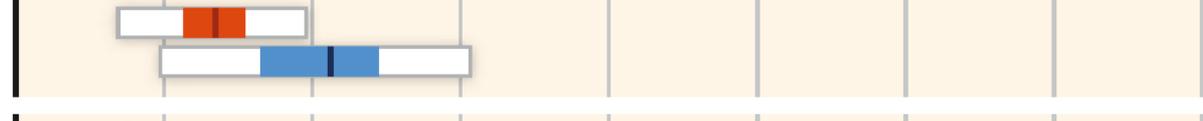


CCS - Coal - Oxyfuel<sup>5</sup>

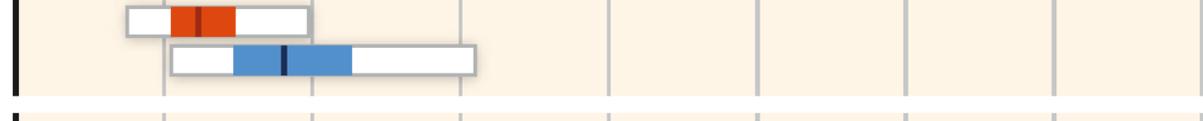


Pre-commercial Technologies

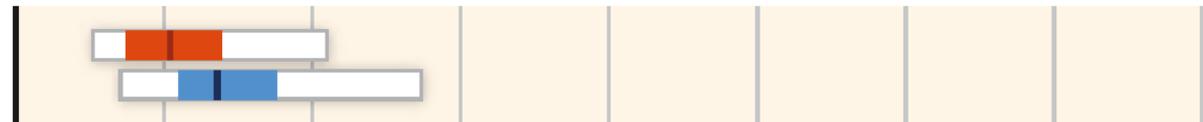
CCS - Coal - PC<sup>5</sup>



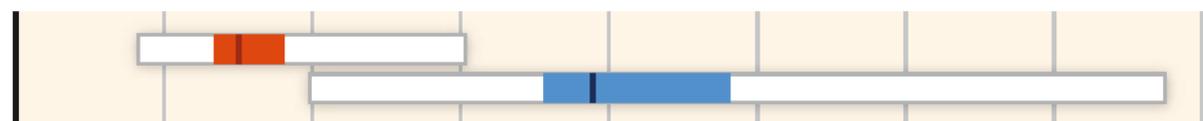
CCS - Coal - IGCC<sup>5</sup>



CCS - Gas - Combined Cycle<sup>5</sup>

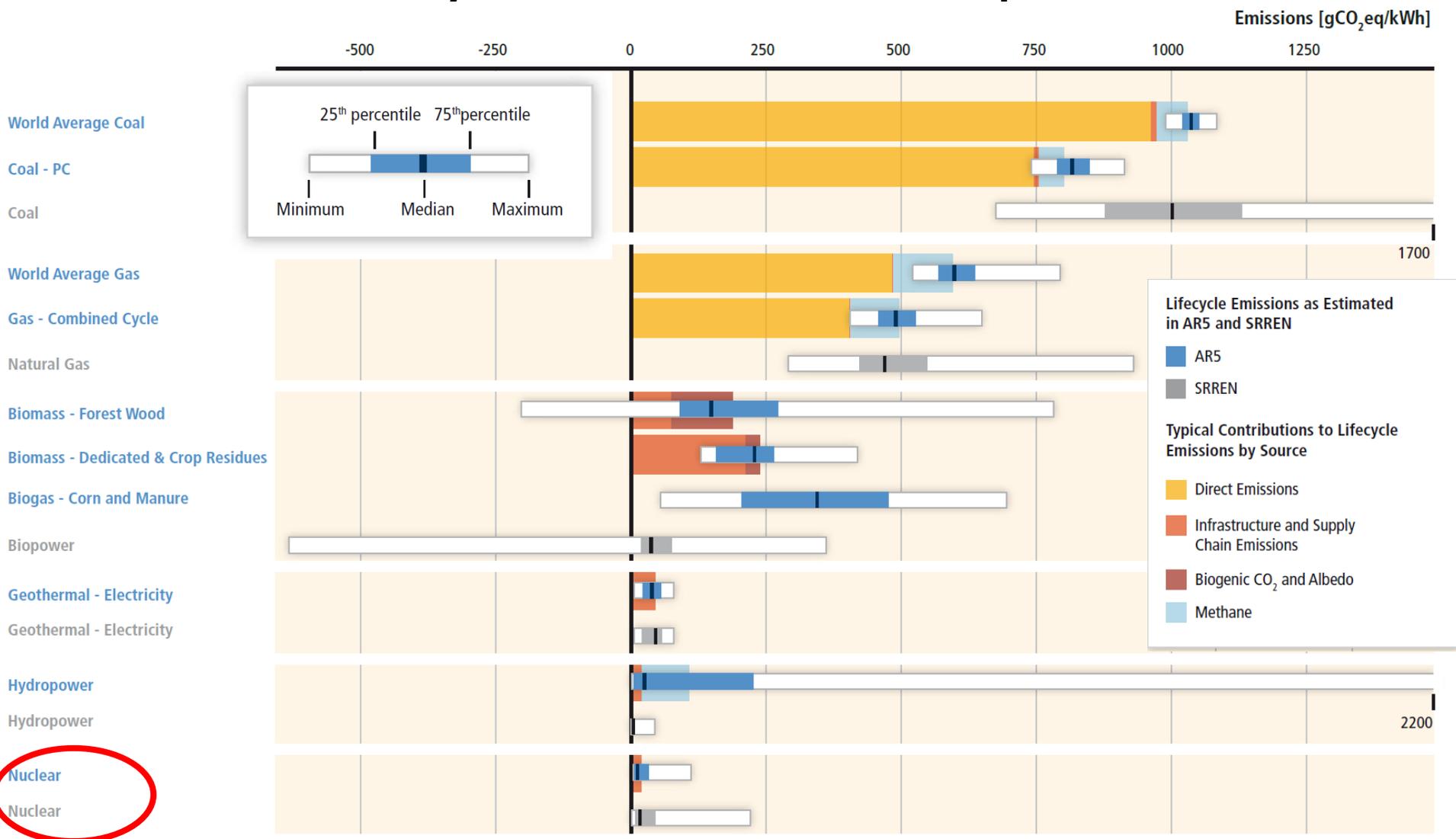


Ocean - Wave & Tidal



<sup>5</sup> Transport and storage costs of CCS are set to 10  $\text{USD}_{2010}/\text{tCO}_2$ .

# Lifecycle emissions compared



[Climate Change 2014 Mitigation of Climate Change](#), Working Group III Contribution to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change (IPCC), p. 71 - Cambridge University Press

© Intergovernmental Panel on Climate Change 2014

Emissions [gCO<sub>2</sub>eq/kWh]

-500      -250      0      250      500      750      1000      1250

Concentrated Solar Power

Concentrated Solar Power

Solar PV - Rooftop

Solar PV - Utility

Solar PV

Wind Onshore

Wind Offshore

Wind Energy

Coal - IGCC

CCS - Coal - Oxyfuel

CCS - Coal - PC

CCS - Coal - IGCC

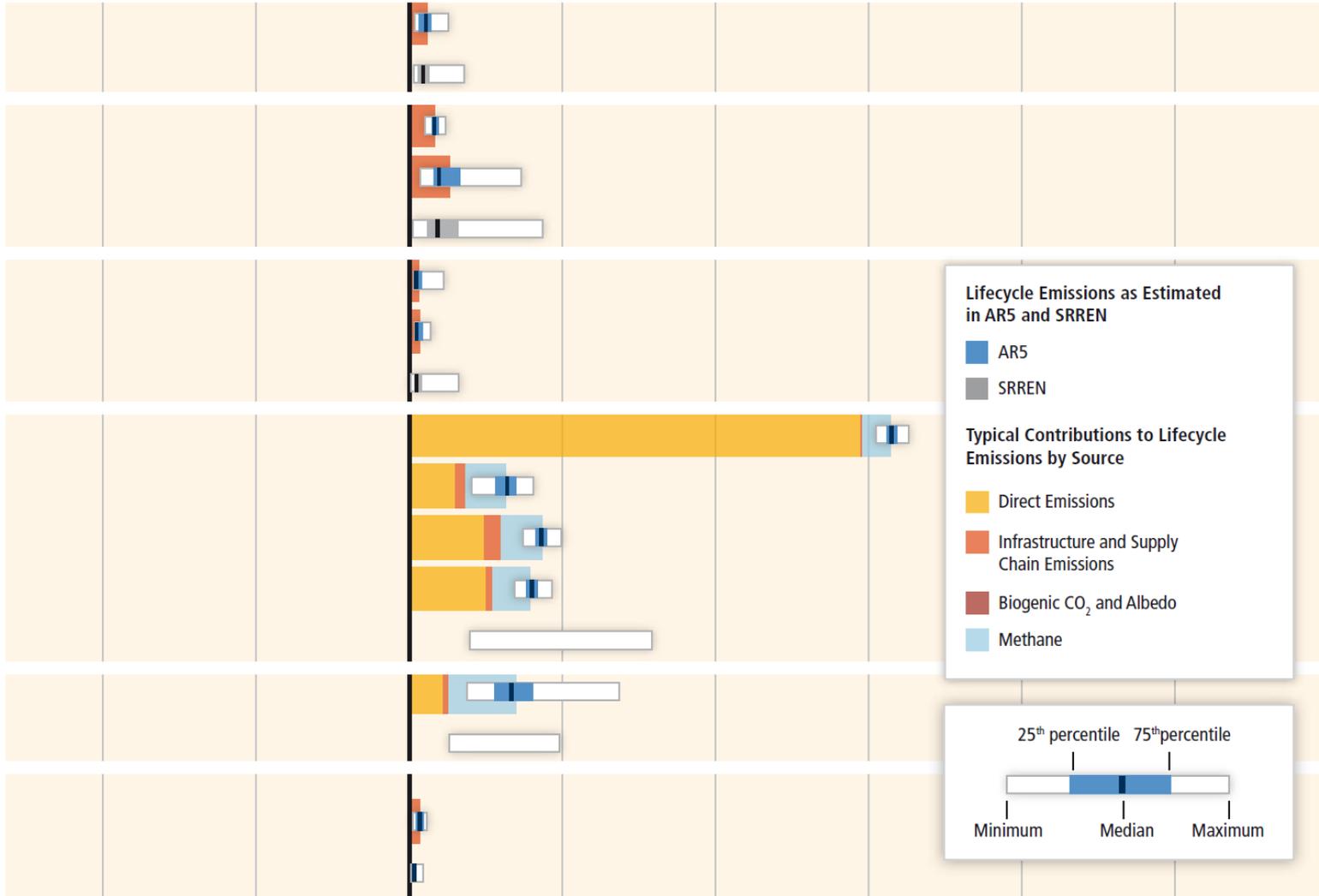
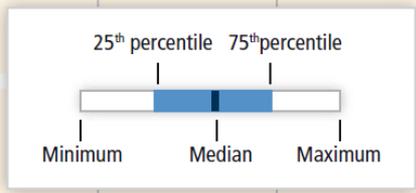
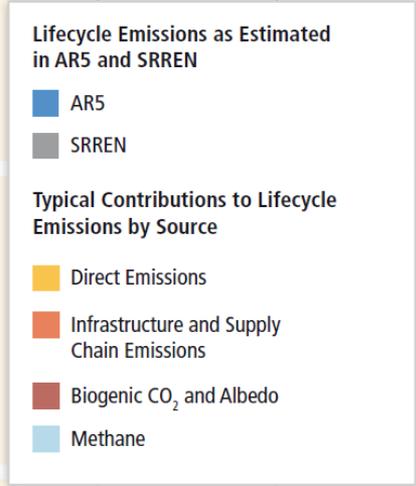
CCS - Coal

CCS - Gas - Combined Cycle

CCS - Natural Gas

Ocean - Wave and Tidal

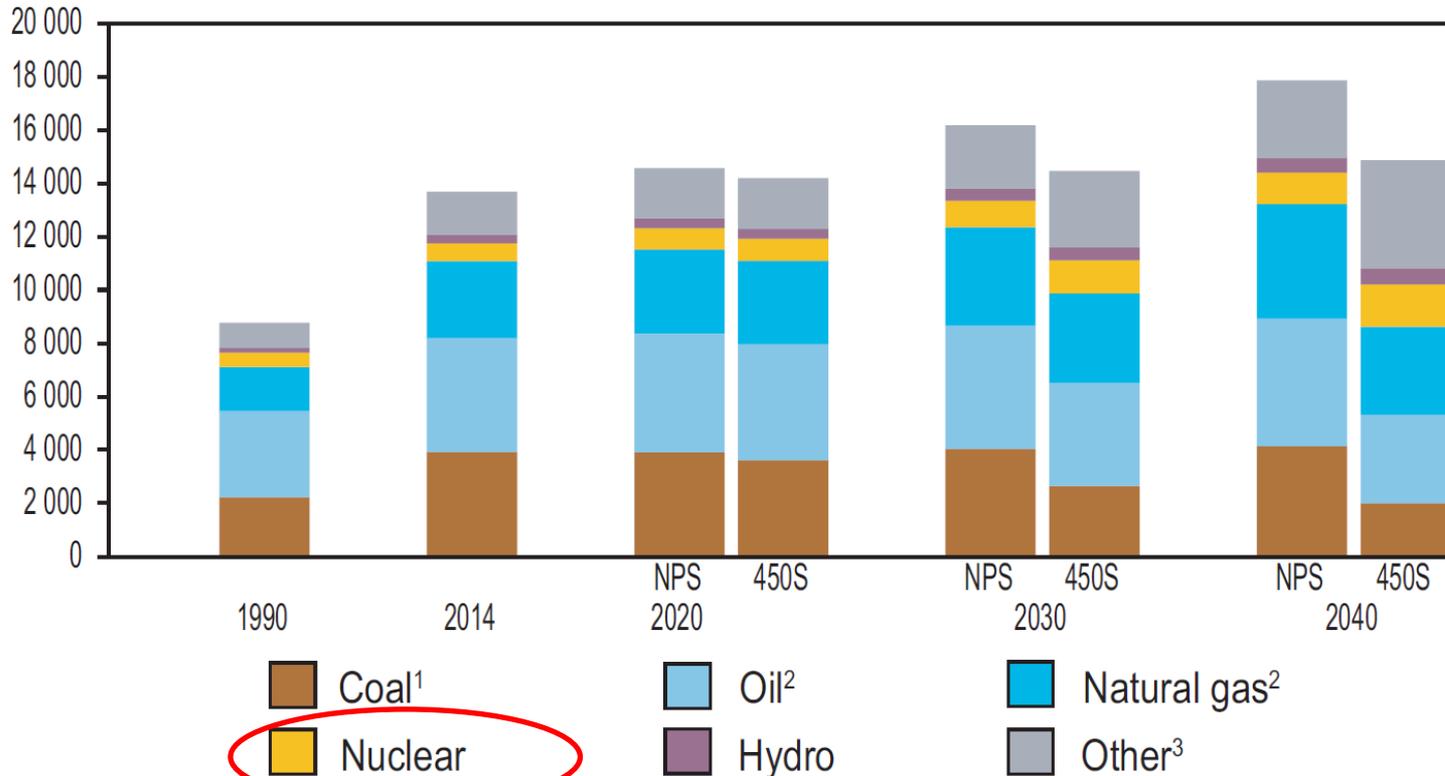
Ocean Energy



# Perspectives and issues

# Worldwide energy trends: projection on energy supply

Total primary energy supply by fuel type (in million tonnes oil equivalent)



NPS: New Policies Scenario  
(based on policies under consideration)

450S: 450 Scenario<sup>4</sup>  
(based on policies needed to limit global average temperature increase to 2 °C)

1. In these graphs, peat and oil shale are aggregated with coal.
2. Includes international aviation and marine bunkers.
3. Includes biofuels and waste, geothermal, solar, wind, tide, etc.
4. Based on a plausible post-2016 climate-policy framework to stabilise the long-term concentration of global greenhouse gases at 450 ppm CO<sub>2</sub>-equivalent.

# How long will U resources last ?

As an example, **fuel fabrication** for a big nuclear power plant with **1000 MWe production**, requires about **160 tons natural U per year**

→ In the **current scheme** with about 450 reactors and **369.000 MWe capacity**, “conventional” (cheap) **reserves would last for another 80 years** (maybe less if average reactor power will increase)

→ Should nuclear power increase as in some of the above scenarios, we should think about (more expensive) resources like phosphates (doable) or U from sea water (still under study)

→ **Switching to fast reactors/Thorium cycle would increase availability to a few 100/few 1000 years**

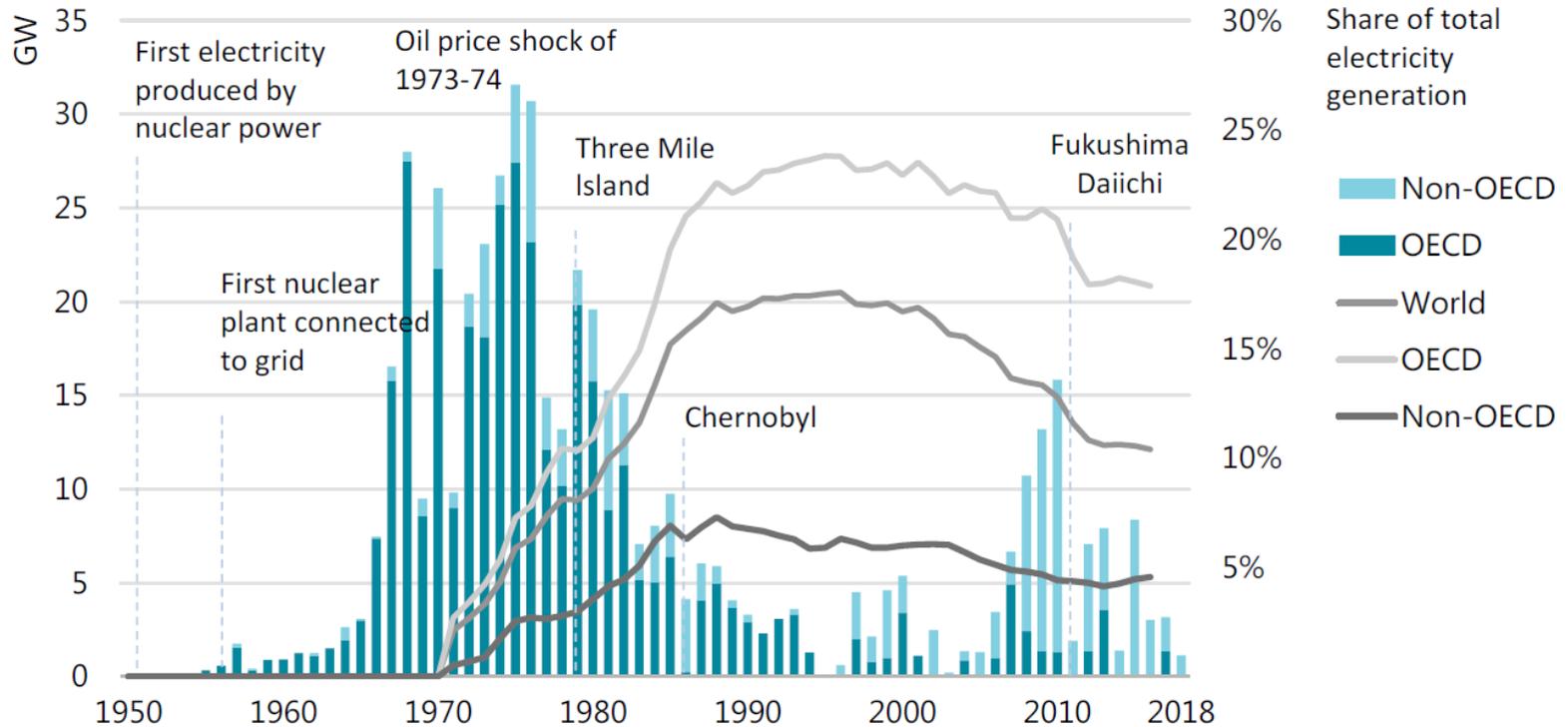
	million tons uranium
Australia	1.14
Kazakhstan	0.82
Canada	0.44
USA	0.34
South Africa	0.34
Namibia	0.28
Brazil	0.28
Russian Federation	0.17
Uzbekistan	0.12
World total (conventional reserves in the ground)	4.7
Phosphate deposits	22
Seawater	4500

Lifetime of uranium resources (in years) for current reactor technology and future fast neutron systems (based on 2006 uranium reserves and nuclear electricity generation rate)

	Identified resources	Total conventional resources	Total conventional and unconventional resources
Present reactor technology	100	300	700
Fast neutron reactor systems	> 3 000	> 9 000	> 21 000

# Reactor ageing

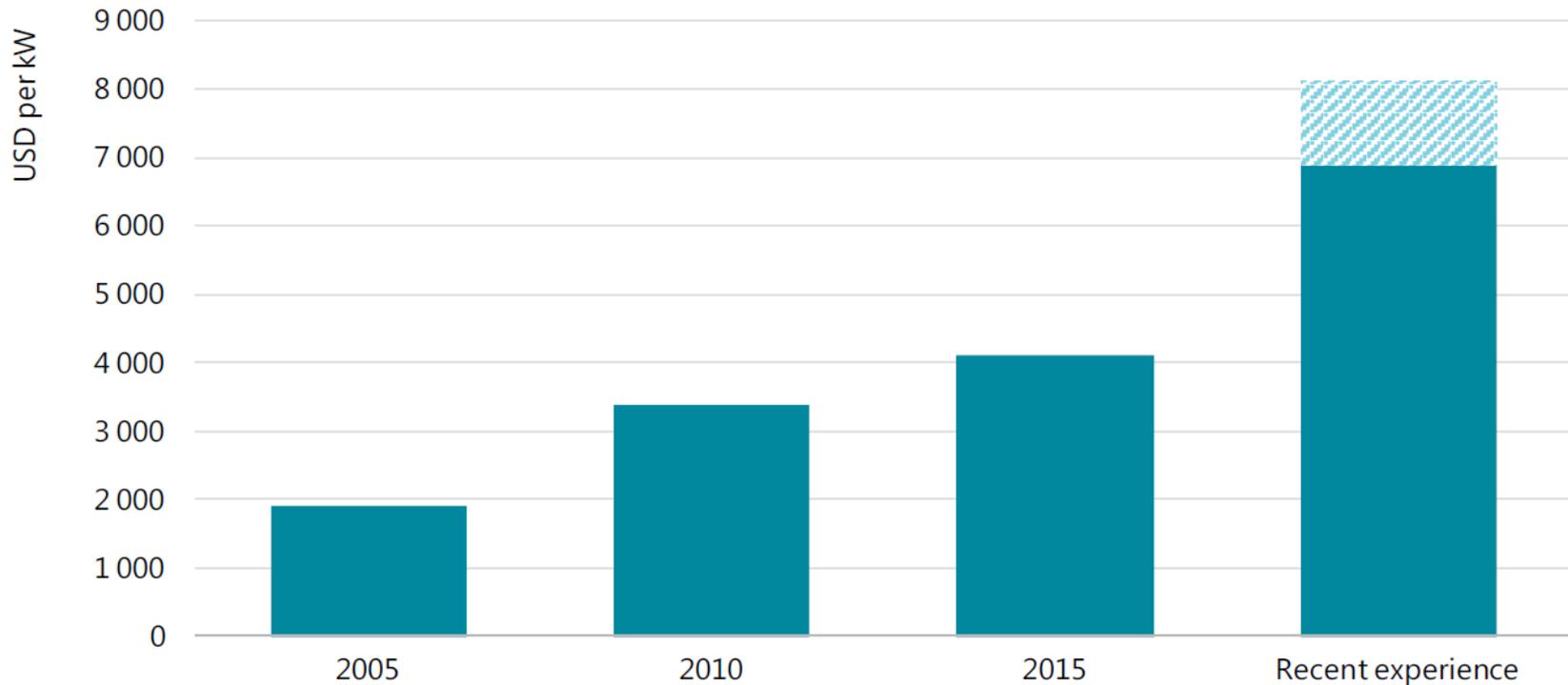
## Reactor construction starts and share of nuclear power in total electricity generation



**Typical lifetime of a plant is 40 to 60 years**  
**→ many are being or are going to be decommissioned**

# Construction costs

## Projected overnight construction cost<sup>1</sup> of nuclear power capacity and recent United States and Western European experience



Source: IEA analysis based on IEA/NEA (2005, 2010 and 2015 editions), Projected Costs of Generating Electricity.

[Nuclear Power in a Clean Energy System](#), IEA 2019

<sup>1</sup>Cost of a construction project if no interest was incurred during construction, as if the project was completed "overnight."

# Market pressure

## NUCLEAR ENERGY INSIDER

Analysis for the nuclear energy community

Home

New Build

Supply Chain

Small Modular Reactors

Operations & Maintenance

## Scientists warn 20% of US nuclear capacity at risk; Toshiba liquidates UK new build company

Nov 14, 2018

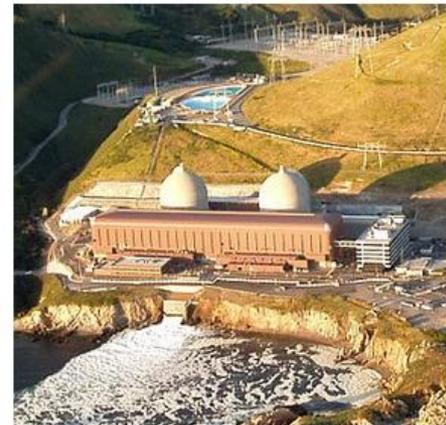
Our pick of the latest nuclear power news you need to know.

### Scientists say 20% of US nuclear capacity unprofitable or set to close

More than one third of operational U.S. nuclear plants, representing 20% of nuclear capacity, are unprofitable or [scheduled to close](#), the Union for Concerned Scientists (UCS) said in a report published November 8.

Nuclear operators face continuing pressure from low wholesale electricity prices, driven by low gas prices and rising renewable energy capacity. The states of New Jersey, New York and Illinois have introduced support mechanisms for nuclear plants but much wider support is required to prevent a hike in carbon emissions, UCS said.

In May, Bloomberg New Energy Finance (BNEF) said more than a [quarter of U.S. nuclear power plants](#) do not earn enough



The Diablo Canyon reactors in California are among 13 U.S. reactors set to close in 2018-2025 and many more could follow. (Image credit: Wikimedia Commons)

# Nuclear waste – how much and what to do ?

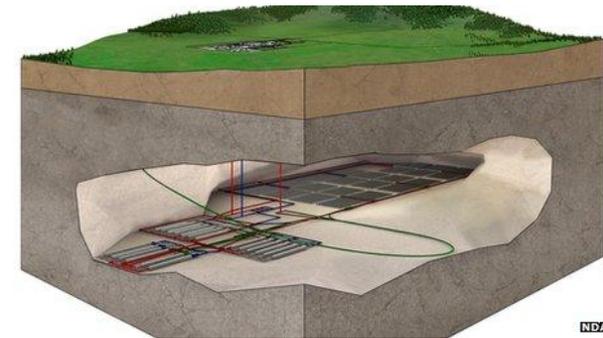
In **1 year**, a **typical** high power **reactor** produces about **1,200 Kg of radioactive material** in the fuel, of which **400 Kg** are long-lived, with half-lives from a few hundred to a few hundred thousand years → they **need to be segregated**

**Spent fuel** assemblies are put in **interim safe storage** for decades, but the same has to be done for the heavily activated structural materials when dismantling a decommissioned plant



Example of spent fuel containers

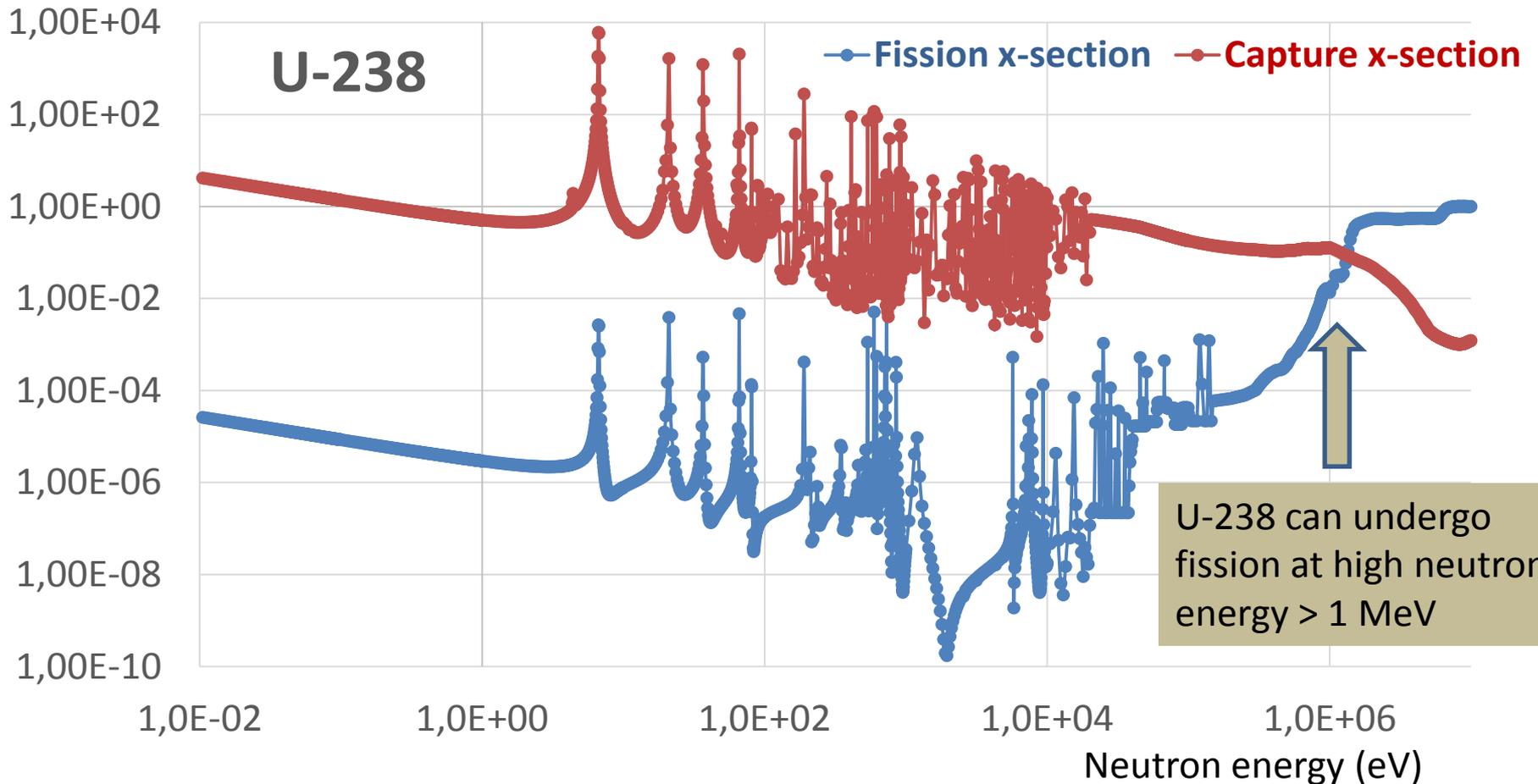
Some countries (most advanced are Finland, Sweden and France) have plans to store spent fuel and other High Level and possibly Intermediate Level Waste in **underground repositories** at a few hundred meters depth: the so-called **geological repositories** → After a few 100,000 years radioactivity dropped to safe levels



**Some countries (France, in particular) recycle the spent fuel** by using specific processes to extract Uranium and Plutonium that can be used to produce fresh fuel (MOX, Mixed Oxide fuel)

# Fast spectrum systems and waste incineration (transmutation)

Cross section (b)



Several **Minor Actinides** are characterized by a **fission threshold** around the **MeV**

➔ Such isotopes can be burnt in **fast reactors** or in **fast Accelerator Driven Systems (ADS)**  
(neutron spectrum from 10 keV to 10 MeV)

➔ See presentation on **Generation IV reactors** by R. Caciuffo and **MYRRHA project** by H. Abderrahim

# Nuclear accidents

The fission process creates radioactive substances that can be dangerous for the environment and for human health → they **must** be contained as much as possible



Chernobyl,  
Soviet  
Union,  
1986

Fukushima, Japan, 2011



**Safety measures** are essential and are subject of continuous research and improvement

# Accidents into perspective...

## Train carrying liquid gas explodes in Italy killing 12

At least 50 injured as freight train derailed in Viareggio and hits homes of sleeping families



▲ The aftermath of the explosion of gas tanks on a derailed train in the Italian town of Viareggio. Photograph: Olycom SPA / Rex Features

The Guardian, 30 June 2009

**africanews.** EN NEWS

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**Mozambique fuel truck explosion: 73 dead, 100s injured**

MOZAMBIQUE

with AFP 17/11/2016

## 'Avian incident' knocks out 84% of massive California solar farm



A solar power facility in Borrego Springs, Calif., on Feb. 11. (Al Seib / Los Angeles Times)

By BLOOMBERG JUNE 20, 2019 | 8:05 AM

An “avian incident” sparked a fire at one of California’s biggest solar farms, affecting 1,200 acres and knocking out 84% of the California Valley Solar Ranch’s generating capacity.

The June 5 incident didn’t damage solar panels at the 250-megawatt power plant, but distribution poles and cables need to be replaced, according to a regulatory filing Wednesday from owner Clearway Energy Inc. The company didn’t say exactly how the blaze was ignited. ...

About 40 megawatts of the San Luis Obispo County facility are in operation, and it’s expected to return to full service by July 1. Clearway expects the incident to cost \$8 million to \$9 million this year, after estimated insurance recovery.

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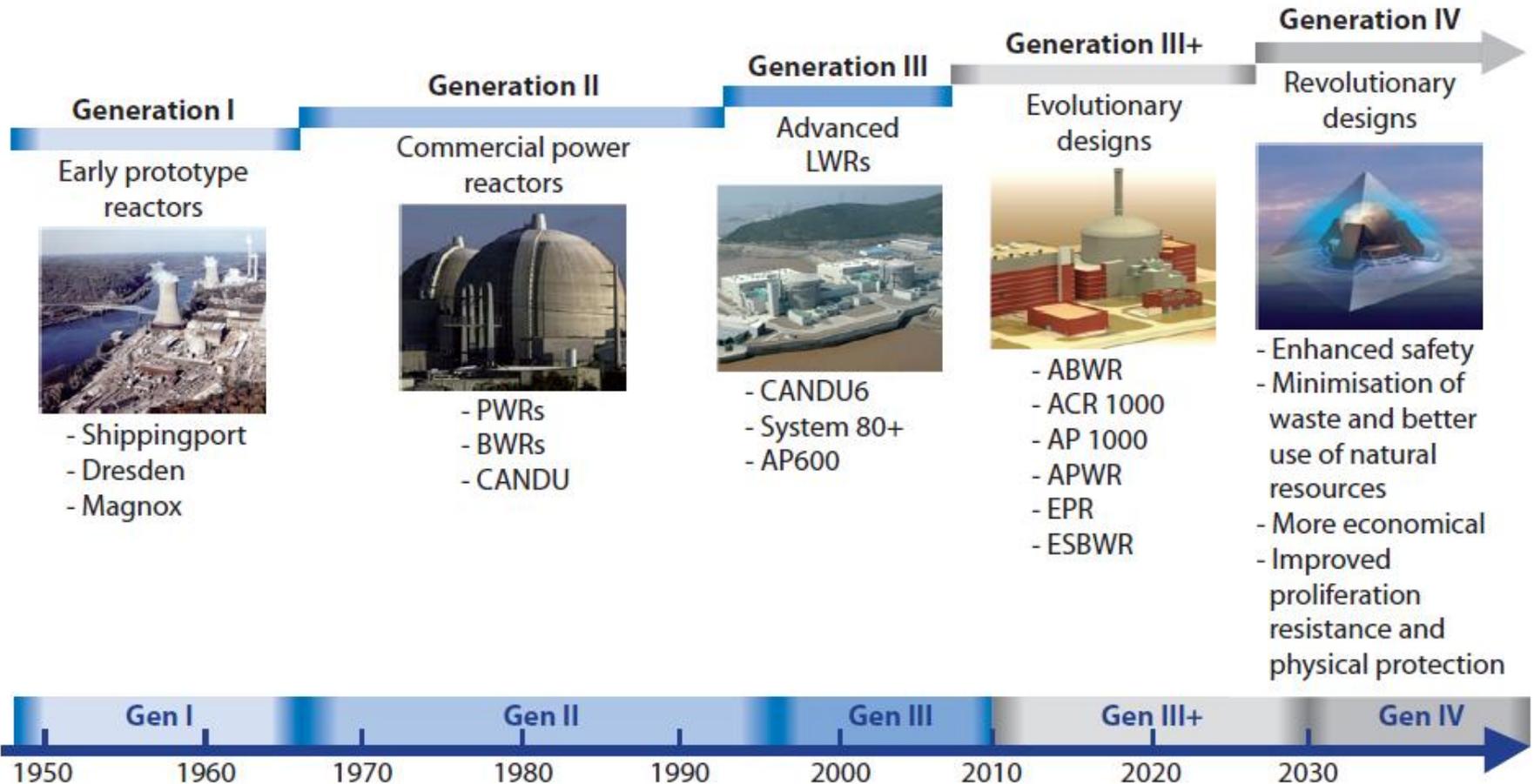
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