## **Quantum fluids of light**











### **Quantum Fluids**

#### Liquid Helium



Helium-4 (boson) Helium-3 (fermion) J.F. Allen (1971)

#### Ultracold atomic condensates



Rubidium-87 (boson) Lithium-6 (fermion)

NIST/JILA/CU-Boulder (1995)

See e.g.,

A. J. Leggett, Quantum Liquids: Bose Condensation and Cooper Pairing in Condensed Matter Systems (2006) S.Giorgini, L.Pitaevskii, and S.Stringari, Rev. Mod. Phys. (2008)

### What about Light?

Light field/beam are composed by a large number of photons but in the vacuum photons do not interact

Optics is typically dominated by single particle behaviuor, however..

- Can we give photons a mass ?
- Can photon-photon interactions make light behave as a fluid ?

In photonic structures

• $\chi^{(3)}$  non linearities  $\implies$  photon-photon interactions •Spatial confinement  $\implies$  effective photon mass

**Collective behaviour of a photonic quantum fluid** 

Optique/Optics

#### **Diffraction non linéaire**

#### Yves POMEAU et Sergio RICA

**Résumé** – Une expérience classique en mécanique des fluides est la formation de structures vorticales à l'arrière d'un obstacle, comme par exemple l'écoulement de Bénard-von-Kármán. Est-il possible d'imaginer une expérience similaire en optique ? C'est-à-dire, en illuminant un obstacle pourrait-on engendrer des structures tourbillonnaires caractéristiques d'un régime pré-turbulent ? Cette Note est consacrée au problème de la génération de vorticité dans les ondes électromagnétiques.

#### Nonlinear diffraction

**Abstract** – A classical experiment in fluid mechanics is the formation of vortical structures in wakes as for instance the Bénard-von-Kármán flow. Is it possible to imagine a similar experiment in optics? i. e. is it possible to generate vortical structures characteristics of a pre-turbulent regime by sending light to an object? This Note is devoted to the problem of generation of vortices in electromagnetic waves.

PHYSICAL REVIEW A

#### VOLUME 60, NUMBER 5

NOVEMBER 1999

#### Bogoliubov dispersion relation and the possibility of superfluidity for weakly interacting photons in a two-dimensional photon fluid

Raymond Y. Chiao\* and Jack Boyce<sup>†</sup> Department of Physics, University of California, Berkeley, California 94720-7300 (Received 3 May 1999; revised manuscript received 22 July 1999)







# Two families of fluids of light



**Cavity configuration** 

Photons fluids in microcavity polaritons

Photon BEC in optical cavity with dye molecules

**Cavity-less configuration** 



Photon fluids in propagating geometry (Rb vapors, photorefractive crystals, thermo-optic liquids)

#### REVIEWS OF MODERN PHYSICS, VOLUME 85, JANUARY-MARCH 2013

### **Quantum fluids of light**

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(published 21 February 2013)





# Outline

### Polaritons

- Introduction
- Superfluidity
- Vortices, solitons and more

Hot Rb Vapors

- > The System
- Superfluid behaviour

Outlook

Fluids of light for analogue physics?

Excitonic polaritons : Mixed light-matter particles

#### Photons confined in an optical cavity

- Very light (m=0 in vacuum)
- Very fast
- No interactions

#### Excitons confined in a quantum well

- Very heavy
- Very slow
- Interactions



Resonance of cavity mode:  $p \lambda/2 = L_c$  $k_z$  is fixed  $E_c$  (

For a motion in the plane of the cavity the photons acquire an effective photon mass

$$E_{C}(k) = Ec(k = 0) + \frac{\hbar^{2}k^{2}}{2Mp_{hot}}$$
  
with  $M_{phot} = \frac{p^{2}\pi^{2}\hbar^{2}}{L_{c}^{2}n^{2}}$ 



# Strong coupling of excitons with photons: polaritons



C. Weisbuch, M. Nishioka, A. Ishikawa, Y. Arakawa, PRL 92

### **Strong Coupling Regime: Cavity Polaritons**

$$H_{k} = E_{cav} (k)\hat{a}_{k}^{\dagger}\hat{a}_{k} + E_{exc} (k)\hat{b}_{k}^{\dagger}\hat{b}_{k} + \frac{\Omega_{R}}{2}(\hat{a}_{k}^{\dagger}\hat{b}_{k} + \hat{b}_{k}^{\dagger}\hat{a}_{k})$$

Strong coupling regime

$$\Omega >> \gamma_{\rm C}, \gamma_{\rm ex}$$

$$\Omega_{\rm R} = 5.1 \text{ meV}$$
  
 $\gamma_{\rm a}, \gamma_{\rm b} \approx 0.1 \text{ meV} \approx 25 \text{ GHz}$ 

Normal modes: *Cavity polaritons* 

E

10

5

$$\hat{p}_{k} = -C_{k}\hat{a}_{k} + X_{k}\hat{b}_{k}$$

$$\hat{q}_{k} = X_{k}\hat{a}_{k} + C_{k}\hat{b}_{k}$$

$$F_{k}(k)\hat{p}^{\dagger}\hat{p}_{k} + F_{k}(k)\hat{q}^{\dagger}\hat{q}_{k}$$

$$\hat{p}_{k}(k)\hat{q}^{\dagger}\hat{q}_{k}$$

$$\hat{p}_{k}(k)\hat{q}^{\dagger}\hat{q}_{k}$$

$$\hat{p}_{k}(k)\hat{q}^{\dagger}\hat{q}_{k}$$

$$\hat{p}_{k}(k)\hat{q}^{\dagger}\hat{q}_{k}$$

 $H_{k} = \mathbf{E}_{\mathrm{LP}} (\mathbf{k}) \hat{\mathbf{p}}_{\mathrm{k}}^{\dagger} \hat{\mathbf{p}}_{\mathrm{k}} + \mathbf{E}_{\mathrm{UP}} (\mathbf{k}) \hat{\mathbf{q}}_{\mathrm{k}}^{\dagger} \hat{\mathbf{q}}_{\mathrm{k}}$ 

#### Observation of the Coupled Exciton-Photon Mode Splitting in a Semiconductor Quantum Microcavity

C. Weisbuch, (a) M. Nishioka, (b) A. Ishikawa, and Y. Arakawa

Research Center for Advanced Science and Technology, University of Tokyo, 4-6-1 Meguro-ku, Tokyo 153, Japan (Received 12 May 1992)







FIG. 3. Reflectivity peak positions as a function of cavity detuning for a five-quantum-well sample at T=5 K. The theoretical fit is obtained through a standard multiple-interference analysis of the DBR-Fabry-Pérot-quantum-well structure.



3316





### **Polaritons Nonlinear Properties**

# When the exciton density rises (strong excitation), interactions between excitons are large.

Hamiltonian for the lower polariton branch:



This yields an effective photon-photon interaction at the output of the cavity

C. Ciuti et al PRB 2000, G. Messin at al PRL 2001

Polaritons are weakly interacting composite bosons

 $P_{+} = -C a + X b$  $P_{-} = X a + C b$ 

Very small effective mass  $m \sim 10^{-5} m_e$ 

Large coherence length  $\lambda_T \sim 1-2 \ \mu m$  at 5K

$$\lambda_T = \left(\frac{2\pi h^2}{mk_B T}\right)^{\frac{1}{2}}$$

and mean distance between polaritons d  $\sim$  0,1-0,2  $\mu$ m

This enables the building of many-body quantum coherent effects : condensation, superfluidity

# **Polariton BEC**



Kasprzak et al. Nature, 443, 409 (2006)

#### Carusotto&Ciuti, Rev. Mod. Phys.85, 299 (2013)

#### Non resonant excitation



# **Boson quantum fluids: polaritons**

#### Coherent propagation



Amo et al., Nature 457, 295 (2009)



#### Long-range order phases



Lai et al., Nature 450, 529 (2007)

#### Vortex and half vortex



Lagoudakis et al., Nature Phys. 4, 706 (2008), and Science 326, 974 (2009)

#### Carusotto&Ciuti, Rev. Mod. Phys.85, 299 (2013)

## Hydrodynamics of polariton quantum fluids



Superfluidity and Cerenkov waves (*Nature Physics 2009*)



### **Resonant excitation**



Dark solitons and vortices (*Science 2011, Nature Photonics 2011*)

### **Excitation & detection**

### EXCITATION

Resonant photon injection

 $I(r,t) \rightarrow n(r,t)$  $\phi(r,t) \rightarrow v(r,t)$ 

### DETECTION

• Imaging of the leaking photons

 $I(r,t) \leftarrow n(r,t)$  $\phi(r,t) \leftarrow v(r,t)$ 

### **Full optical experiment**



- Image of the cavity plane:
  - density map:  $n(x, y) \propto I(x, y)$
  - velocity map:  $\mathbf{v}(x, y) \propto \nabla \phi(x, y)$
- Reshaping of the phase profile of the driving field
  - Use of a Spatial Light Modulator (SLM)
  - Rotating phase ⇒ Rotating fluid

## **Full optical experiment**



### **Microcavity Polaritons: Mean field approach**

### **Generalized Gross-Pitaevskii equation**



### Driven dissipative system, out of equilibrium quantum fluids

### **Steady state solutions: Bistability**



## Study of superfluidity Weak excitations and Bogoliubov dispersion

Weakly excited states : bosonic modes obtained by linearizing the Gross Pitaevskii equation around the steady state solutions

$$\boldsymbol{\psi}(\mathbf{r},t) = \left( \boldsymbol{\psi}_0(\mathbf{r},t) + \boldsymbol{\delta}\boldsymbol{\psi}(\mathbf{r},t) \right)$$

$$i \hbar \frac{\partial}{\partial t} \begin{bmatrix} \delta \psi(\mathbf{r}, t) \\ \delta \psi^*(\mathbf{r}, t) \end{bmatrix} = \mathcal{L}_{Bog} \begin{bmatrix} \delta \psi(\mathbf{r}, t) \\ \delta \psi^*(\mathbf{r}, t) \end{bmatrix}$$

**Bogoliubov operator** 

$$\mathcal{L}_{Bog} = \begin{bmatrix} \frac{\hbar^2 k^2}{2m} + g |\psi_0|^2 & g |\psi_0|^2 e^{2ik_0 x} \\ - g |\psi_0|^2 e^{-2ik_0 x} & - \frac{\hbar^2 k^2}{2m} - g |\psi_0|^2 \end{bmatrix}$$

Look for eigenvalues of the Bogoliubov operator

### **Bogoliubov dispersion**

• Solutions of Bogoliubov equation - healing length  $\xi = \sqrt{\hbar^2/mgn}$ 

$$\begin{split} \hbar\omega_{Bog}(k) &= \pm \sqrt{\frac{\hbar^2 k^2}{2m} \left(\frac{\hbar^2 k^2}{2m} + 2gn\right)} \\ & \left| \psi_0(\mathbf{r}, t) \right| = \sqrt{n} \\ \left(\frac{\hbar^2 k^2}{2m} + 2gn\right) \end{split}$$

- Large k  $(k\xi \gg 1)$ :
- $\hbar\omega_{Bog}(k) =$ - parabolic dispersion
  - "normal" fluid
- Small k (*kξ* ≪ 1) :
  - sonic dispersion
  - superfluidity

Speed of sound:  $c_s = \sqrt{gn/m}$ 

 $\hbar\omega_{Bog}(k) = c_s k$ 



### **Measurements of the Bogoliubov dispersion**

 S. Utsunomiya et al. Nat. Phys. 4, 700 (2008)
 PL

 V. Kohnle et al. PRB 86, 064508 (2012)
 FWM

 P. Stepanov et al., Nat. Com. 10, 3869 (2019)
 PL

 M. Pieczarka et al., Nat. Com. 11, 429 (2019)
 PL

 D. Ballarini et al., Nat. Com. 11, 217 (2020)
 FT of g<sup>1</sup>









P. Stepanov et al., Nat. Com. 10, 3869 (2019)

### **Coherent probe spectroscopy**

- Probe: excitation of small perturbations on top of the polaritons fluid
  - @ different  $k_{pr}$
  - energy scan:  $\Delta \omega_{pr}$  ~100Ghz



• Probe absorption (transmission) when  $(k_{pr}, \omega_{pr}) = (k_{pol}, \omega_{pol})$ 



### **Spectroscopy setup**





AFG: arbitrary function generator SLM: spatial light modulator AOM: acousto-optic modulator DMD: digital micromirror device

- Sample:
  - In cryostat (<4K)</li>
- Pump: excitation of polaritons - Phase and intensity profile reshaped with an SLM
- Probe: scan of the polariton fluid resonances
  - @ different  $k_{pr}$
  - energy scan:  $\Delta \omega_{pr} \sim 100$ GHz
- **Detection:**  $(k, \omega)$  of the probe reflectivity dips
  - $\delta E$  resolution fixed by the laser linewidth
  - $-\delta k$  resolution fixed by the k-space filtering

# Spectroscopy setup



### **Bogoliubov Dispersion**



- $k\xi \gg 1$  parabolic dispersion (same as the linear regime)
- $k\xi \ll 1$  sonic dispersion: fit of the speed of sound  $c_s$

Claude et al., submitted

### **Speed of sound**

• Changing the fluid density (proportional to the detuning  $\delta$ )



• The speed of sound  $c_s$  is proportional to  $\sqrt{n}$ 

Claude et al. arxiv 2112.09903 (2022), submitted

# **Probing the superfluidity**

VOLUME 93, NUMBER 16

PHYSICAL REVIEW LETTERS

week ending 15 OCTOBER 2004

#### Probing Microcavity Polariton Superfluidity through Resonant Rayleigh Scattering

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# **Probing the superfluidity**

We probe the behaviour of the fluid through its interaction with defects





- Polariton density(pump intensity)
- Fluid velocity(excitation angle)
- ✓ Oscillation frequency (laser frequency)





# **Polariton flow around a defect**



# **Transition to the superfluid regime**



Amo et al., Nat. Phys., 5, 805 (2009)

# Čerenkov regime






# Transition to the Čerenkov regime



Amo et al., Nat. Phys., 5, 805 (2009)

# **Speed of sound**



Existence of a well defined speed of sound  $c_s = \sqrt{-g |\psi|^2/m}$ 

$$\sin\vartheta = \frac{c_s}{v_f}$$

Measure of the sound speed

$$c_s = 8.1 x 10^5 m/s$$

#### nature physics

#### LETTERS PUBLISHED ONLINE: 5 JUNE 2017 | DOI: 10.1038/NPHYS4147

# Room-temperature superfluidity in a polariton condensate

Giovanni Lerario<sup>1</sup>, Antonio Fieramosca<sup>1,2</sup>, Fábio Barachati<sup>3</sup>, Dario Ballarini<sup>1\*</sup>, Konstantinos S. Daskalakis<sup>4</sup>, Lorenzo Dominici<sup>1</sup>, Milena De Giorgi<sup>1</sup>, Stefan A. Maier<sup>5</sup>, Giuseppe Gigli<sup>1,2</sup>, Stéphane Kéna-Cohen<sup>3\*</sup> and Daniele Sanvitto<sup>1,6\*</sup>

#### Organic cavity + pulsed excitation





# Superfluidity breakdown: vortices and solitons formation?

The case of spatially extended defects; the size of the defect is larger than the healing length

1' - 1' < c

Acceleration of the fluid near the defect: the Landau criterion is locally violated 
$$v_f = 2v_{\infty}$$

Frisch et al., PRL 69, 1644 (1992)

The currents formed in the fluid passing around a large obstacle can give rise to turbulence in its wake

Quantized vortices Dark Solitons



### **Resonant excitation: shaped pump**



### **Resonant excitation**

✓ Shaped pump: free evolution for the fluid phase

# **Experimental set-up**



### Key points

- CW laser (precise control of the fluid quantum state)
  Mask (free evolution for the superfluid phase)
- Possibility to generate topological excitations



**Resonant excitation** 

 $\checkmark$  Problem: short propagation due to the dissipation

Amo et al., Science, 332, 1167 (2011)

# physics

#### ARTICLES PUBLISHED ON LINE: 3 APRIL 2011 | DOI: 10.1038/NPHYS1959

# Hydrodynamic nucleation of quantized vortex pairs in a polariton quantum fluid

Gaël Nardin\*, Gabriele Grosso, Yoan Léger, Barbara Pietka<sup>†</sup>, François Morier-Genoud and Benoît Deveaud-Plédran



Nardin et al., Nature Phys. 7, 635 (2011)

See also: Sanvitto *et al.*, Nature Phot. **5**, 610 (2011

# Soliton doublet and quadruplet

**Big defect (17μm) >> healing length** 



Low momentum;  $k = 0.2 \mu m^{-1}$  High momentum;  $k = 1.1 \mu m^{-1}$ 

Amo et al., Science, 332, 1167 (2011)

# **Hydrodynamic Dark Solitons: theory**

PRL 97, 180405 (2006)

PHYSICAL REVIEW LETTERS

week ending 3 NOVEMBER 2006

#### **Oblique Dark Solitons in Supersonic Flow of a Bose-Einstein Condensate**

G. A. El,<sup>1,\*</sup> A. Gammal,<sup>2,†</sup> and A. M. Kamchatnov<sup>3,‡</sup>

<sup>1</sup>Department of Mathematical Sciences, Loughborough University, Loughborough LE11 3TU, United Kingdom <sup>2</sup>Instituto de Física, Universidade de São Paulo, 05315-970, C.P. 66318 São Paulo, Brazil <sup>3</sup>Institute of Spectroscopy, Russian Academy of Sciences, Troitsk, Moscow Region, 142190, Russia (Received 21 April 2006; published 1 November 2006)



# Hard to observe in atomic BEC; the dissipation in polariton fluids helps in stabilizing dark solitons

### **Dissipation: short propagation**



### **Dissipation**

✓ Problem: the polariton density decreases rapidly; only short propagation is achieved (about 30- 40  $\mu$ m)

### The idea: to exploit the bistability

Proposal: S. Pigeon et al, NJP, 2018



.A. Baas et al., Phys. Rev. A 69, 23809 (2004)

### Bistability: high polariton density and no phase fixing



### **Dark Soliton Enhanced Propagation**



Up to 150µm propagation distance



### New feature: solitons are parallel each other and to the direction of the flow

G. Lerario et al., Phys. Rev. Research 2, 042041(R) (2020)

# **All-optical imprinting of solitons**



rad

0

SLM phase pattern







Pump phase profile

3

High density regime: the phase of the pump is copied onto the fluid

Density Interferogram

In the bistable region the phase of the fluid is not fixed by the pump: solitons propagate through the bistable region for very long distances

A. Maitre. et al, Phys. Rev. X 10, 4 (2020)

### **Solitons arrays**



Scalable technique to create in a controlled way soliton arrays

### **Colliding Solitons**



Flexible technique to study in a controlled way the soliton interactions

**Light engineering of the polariton landscape:** 

using polariton-polariton interactions

Sample from R. Houdré



#### probe $\sigma$ +



#### control $\sigma$ -



strong field: renormalization of the polariton energy







Probe only No control



Probe + Linear control



Probe + Diagonal control



Probe only No control

10 mu



Probe + Linear control

 $\begin{array}{c} 0.5 \\ (1) \\$ 

Probe + Diagonal control





# Creation of optically controlled traps for polaritons

# **Polariton trap**

A mask is put in the center of the beam and imaged on the microcavity

polariton density

polariton density

Inside the mask: low



## **Vortex-antivortex lattices in optical traps**

#### Small triangular trap

#### Experiment

Theory





Polariton density





Phase

#### Lattice shape fixed by the trap geometry

### **Vortex-antivortex lattices in optical traps**

Increasing the size of the trap, a larger number of hexagonal unit cells is formed



### **Vortex-antivortex lattices in optical traps**

Low density 30

0

10





Phase

High density





**Effects of the interactions** (Hivet et al, PRB 2014)

### Polaritons

- Superfluidity
- Quantized Vortices
- Dark Solitons
- All-optical generation of steady-state topological excitations with macroscopic propagation
- All optical manipulation: polariton landscape, polariton traps

### Paraxial fluids of light in hot atomic vapors



### Quantum fluids of light in propagating geometry

### Paraxial approximation of wave propagation in a Kerr medium:



# **Experimental Implementations**



# Photorefractive crystal

M. Bellec & C. Michel, InPhyNi, Nice J. W. Fleischer, Princeton

# Atomic vapor



D.Faccio - Glasgow



R. Kaiser, InPhyNi, Nice Q. Glorieux, A. Bramati, LKB, Paris

### **Rb** atomic vapor

We work with Rb D2 atomic line (780 nm)

Detuning >> Doppler broadening

We can neglect the fine structure and model the Rb atoms as a twolevel system:

$$\chi^{(3)} = -\frac{4}{3}N(\rho_{bb} - \rho_{aa})^{(eq)}|\mu_{ba}|^4 \frac{1}{\hbar^3 \Delta^3} \frac{T_1}{T_2}.$$
  
Atomic density detuning

By properly choosing the detuning and the atomic density (via the cell temperature) we can have at the same time High enough repulsive non linearities Low absorption (less than 30%)

### **Probing the superfluid behaviour**





- An intense Pump beam creates the
- - We measure the displacement of the perturbation as a function of

### **Probing the superfluid behaviour**



Q. Fontaine et al, Phys. Rev. Lett. 121, 183604 (2018)
### **Probing the superfluid behaviour**



Q. Fontaine, et al. PRL, **121**, 183604 (2018) C. Piekarski, et al. PRL, **127**, 023401 (2021)

## Speed of sound



## Scattering on an optical defect



Q. Fontaine, H. Hu, S. Pigeon, T. Bienaime, E Wu, Giacobino E., A. Bramati, Q. Glorieux - Opt. Express (2019)

## Scattering on an optical defect





## **Turbulence with two counter streaming flows**



Energy cascade, inverse energy cascade, Kelvin-Helmotz instabilities

## Conclusions

✓ Quantum fluid of light in a hot Rb vapor

 Observation of the Bogoliubov dispersion; strong indication of supefluid like behavior in these systems

 Scattering suppression and turbulence measurements

## Outlook: quantum fluids of light for analogue gravity experiments

## See the Kevin Falque's poster

Analogue quantum simulation of field theories on curved spacetimes

Laboratory experiments Black holes Parametric amplification effects: Hawking radiation Zeldovich superradiance Penrose effect Preheating and reheating of early universe

## The team

#### LKB GROUP

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# Thank you for your attention