

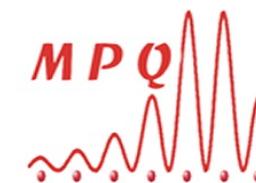
Quantum electron transport controlled by cavity vacuum fields

Cristiano Ciuti

*Université Paris Cité, CNRS,
Laboratoire Matériaux et Phénomènes Quantiques, France*

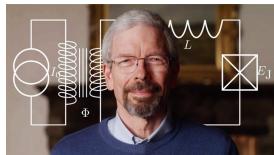


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Paris Cité



@Varennna
QFLM2022

Connection to previous lectures and keywords



Steve Girvin: circuits and QED vacuum fluctuations



Tomoki Ozawa: edge states and topology



Nicola Regnault: 2D electron systems, Landau levels, topology



Atac Imamoglu: light-matter interaction in 2D electron gases

References of work presented today

Experiments and theory:

F. Appugliese, J. Enkner, G. L. Paravicini-Bagliani, M. Beck, C. Reichl, W. Wegscheider, G. Scalari, CC, J. Faist,

Breakdown of topological protection by cavity vacuum fields in the integer quantum Hall effect,

Science 375, 1030 (2022)

Theory:

CC, *Cavity-mediated electron hopping in disordered quantum Hall systems*,
PRB 104, 155307 (2021)

G. Arwas and CC, *Quantum electron transport controlled by cavity vacuum fields*,
arXiv:2206.13432

Acknowledgements

ETH zürich



Felice Appugliese



**Josephine
Enkner**

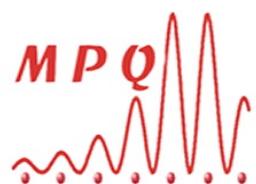


Giacomo Scalari



Jérôme Faist

 Université
Paris Cité



Geva Arwas

Introduction

Quantum vacuum

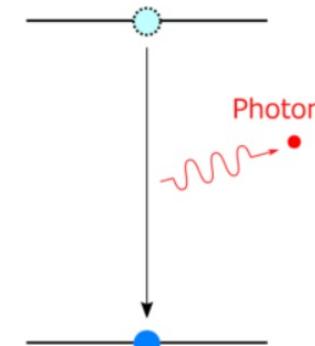
Quantum vacuum is not empty, but filled with fluctuating fields



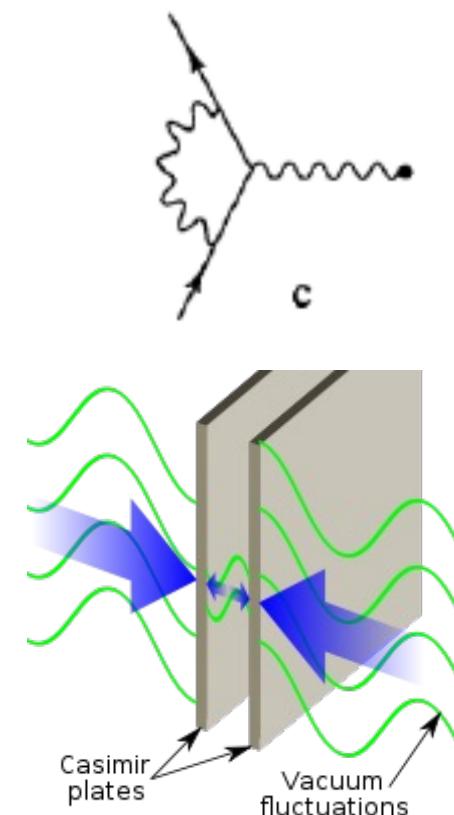
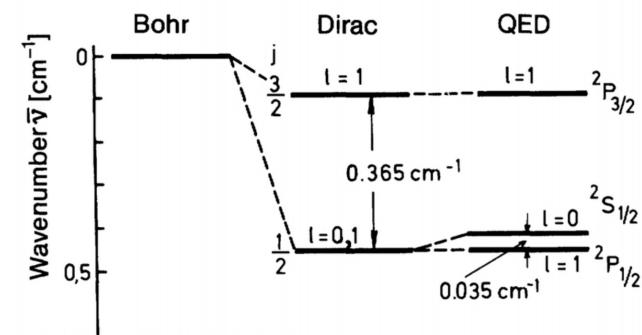
@Pete Linforth

Famous effects due to electromagnetic quantum vacuum

Spontaneous photon emission (luminescence)

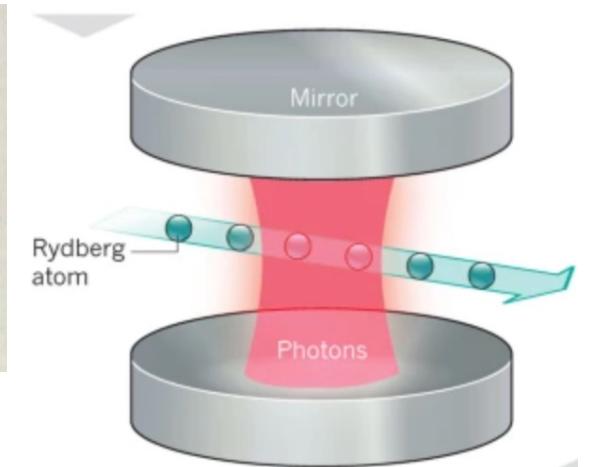
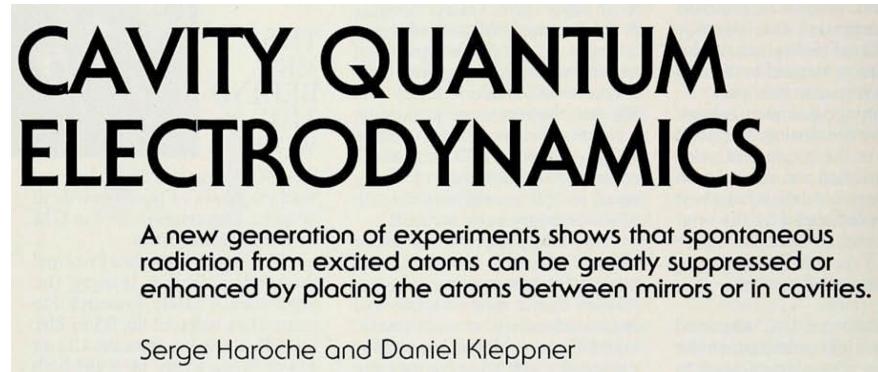


Lamb shift of the hydrogen atom



Casimir forces

Enhancing vacuum effects by spatial confinement: cavity QED



$$E_0 \propto \frac{1}{\sqrt{V}}$$

↑
Vacuum electric field fluctuation

↑
Mode volume

Vacuum field increases with decreasing mode volume

Emerging topic: manipulation of matter by vacuum fields

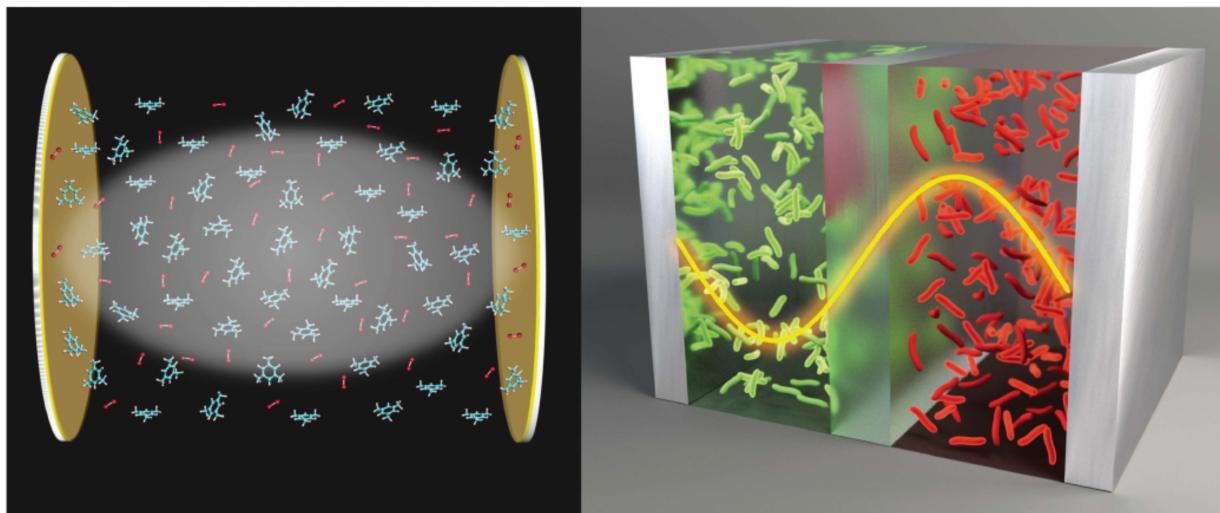
RESEARCH

REVIEW SUMMARY

LIGHT-MATTER COUPLING

Manipulating matter by strong coupling to vacuum fields

Francisco J. Garcia-Vidal*, Cristiano Ciuti*, Thomas W. Ebbesen*



Modification of:

- Condensed matter phases
- Transport properties
- Chemical reactions
-

Garcia-Vidal, C. Ciuti, Ebbesen, Science 373, 178 (2021)

Other recent reviews

Applied Physics Reviews

REVIEW

scitation.org/journal/are

Cavity quantum materials

Cite as: Appl. Phys. Rev. **9**, 011312 (2022); doi: [10.1063/5.0083825](https://doi.org/10.1063/5.0083825)

Submitted: 30 December 2021 · Accepted: 31 January 2022 ·

Published Online: 25 February 2022



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Export Citation



CrossMark

F. Schlawin,^{1,2}  D. M. Kennes,^{1,3}  and M. A. Sentef^{1,a} 

Perspective

Strongly correlated electron–photon systems

<https://doi.org/10.1038/s41586-022-04726-w>

Received: 2 December 2020

Accepted: 2 December 2021

Published online: 25 May 2022

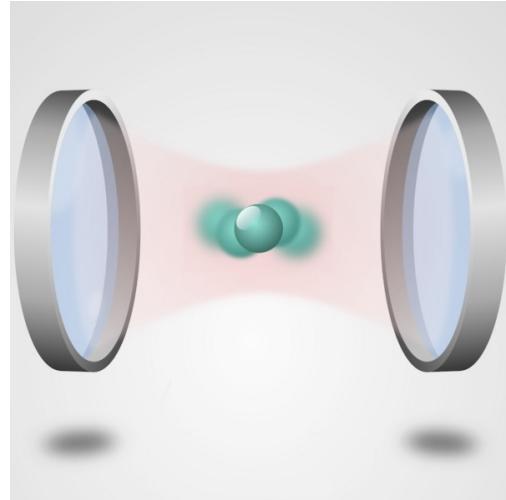


Jacqueline Bloch¹, Andrea Cavalleri², Victor Galitski³ , Mohammad Hafezi⁴ & Angel Rubio^{2,5}

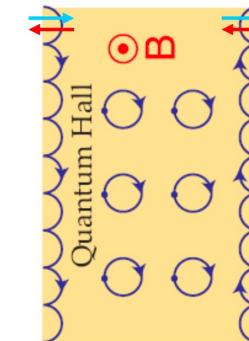
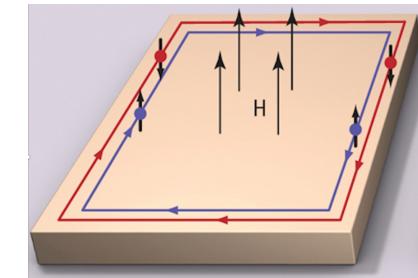
An important goal of modern condensed-matter physics involves the search for states of matter with emergent properties and desirable functionalities. Although the tools for material design remain relatively limited, notable advances have been recently achieved by controlling interactions at heterointerfaces, precise alignment of low-dimensional materials and the use of extreme pressures. Here we highlight a paradigm based on controlling light–matter interactions, which provides a way to manipulate and synthesize strongly correlated quantum matter. We consider the case in which both electron–electron and electron–photon interactions are strong and give rise to a variety of phenomena. Photon-mediated superconductivity, cavity fractional quantum Hall physics and optically driven topological phenomena in low dimensions are among the frontiers discussed in this Perspective, which highlights a field that we term here ‘strongly correlated electron–photon science’.

Cavity-control of quantum Hall systems

Cavity Quantum Electrodynamics CQED



Quantum Hall Effect (QHE)



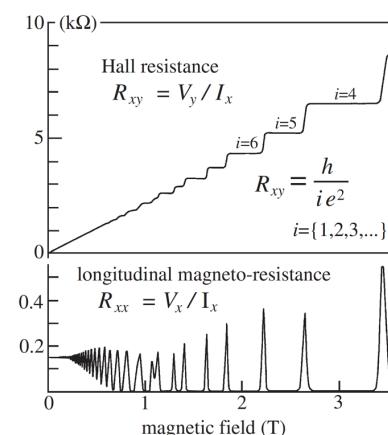
Lamb shift, Casimir,...
Enhanced light matter-interaction
Vacuum Rabi oscillations,...

CAVITY QUANTUM ELECTRODYNAMICS

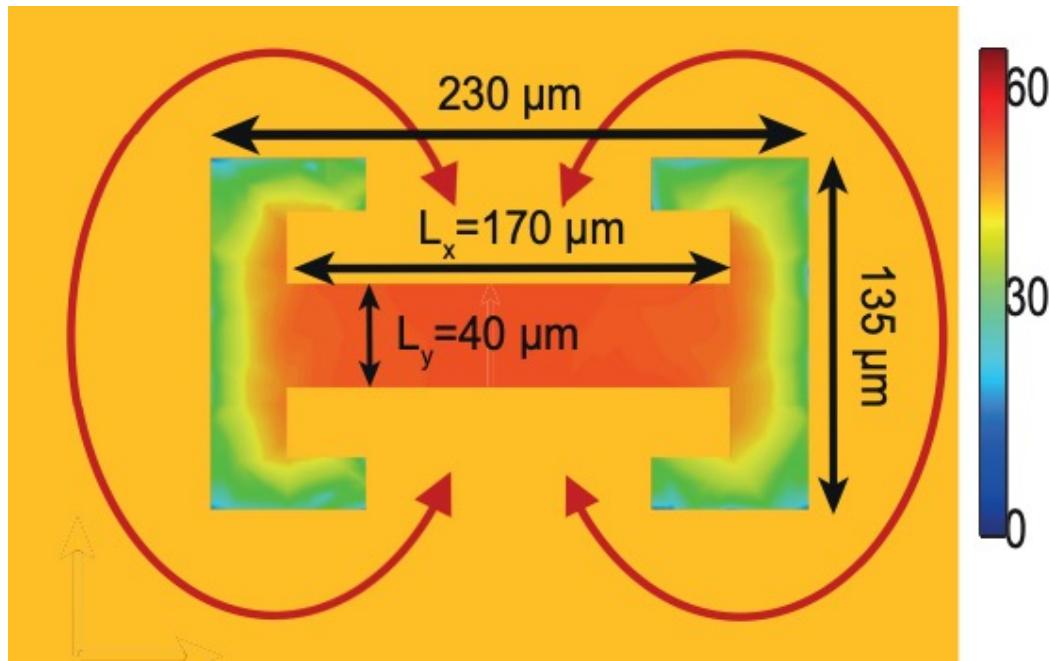
A new generation of experiments shows that spontaneous radiation from excited atoms can be greatly suppressed or enhanced by placing the atoms between mirrors or in cavities.

Serge Haroche and Daniel Kleppner

Paradigmatic Topological Insulator



Giant vacuum fields with split-ring resonators

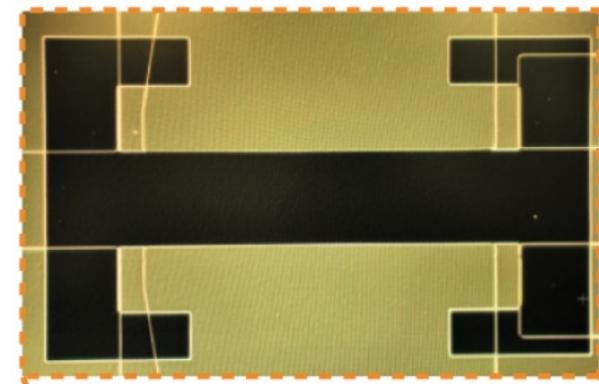


LC-like resonator

**Strong vacuum electric fields
in the capacitive gap**

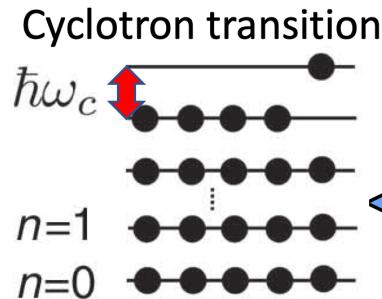
Deeply subwavelength mode confinement

$$10^{-10}(\lambda/n)^3 < V < 10^{-4}(\lambda/n)^3$$



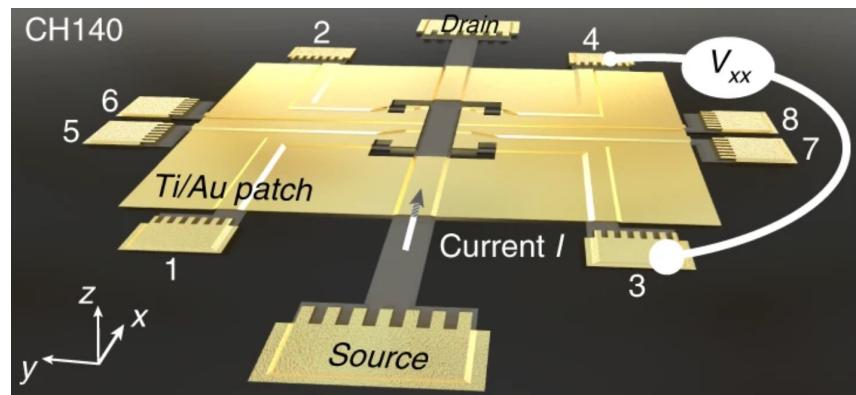
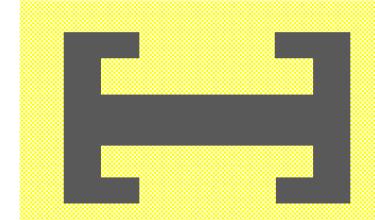
Courtesy of J. Faist's group @ ETH

The new frontier: 2D electron gas in split-ring resonators



Electron-photon interaction

Split-ring resonator



Optics: Landau polaritons

Hagenmüller, De Liberato, CC, PRB (2010)
Scalari et al, Science (2012)

...

See next talk by
J. Mornhinweg and references therein

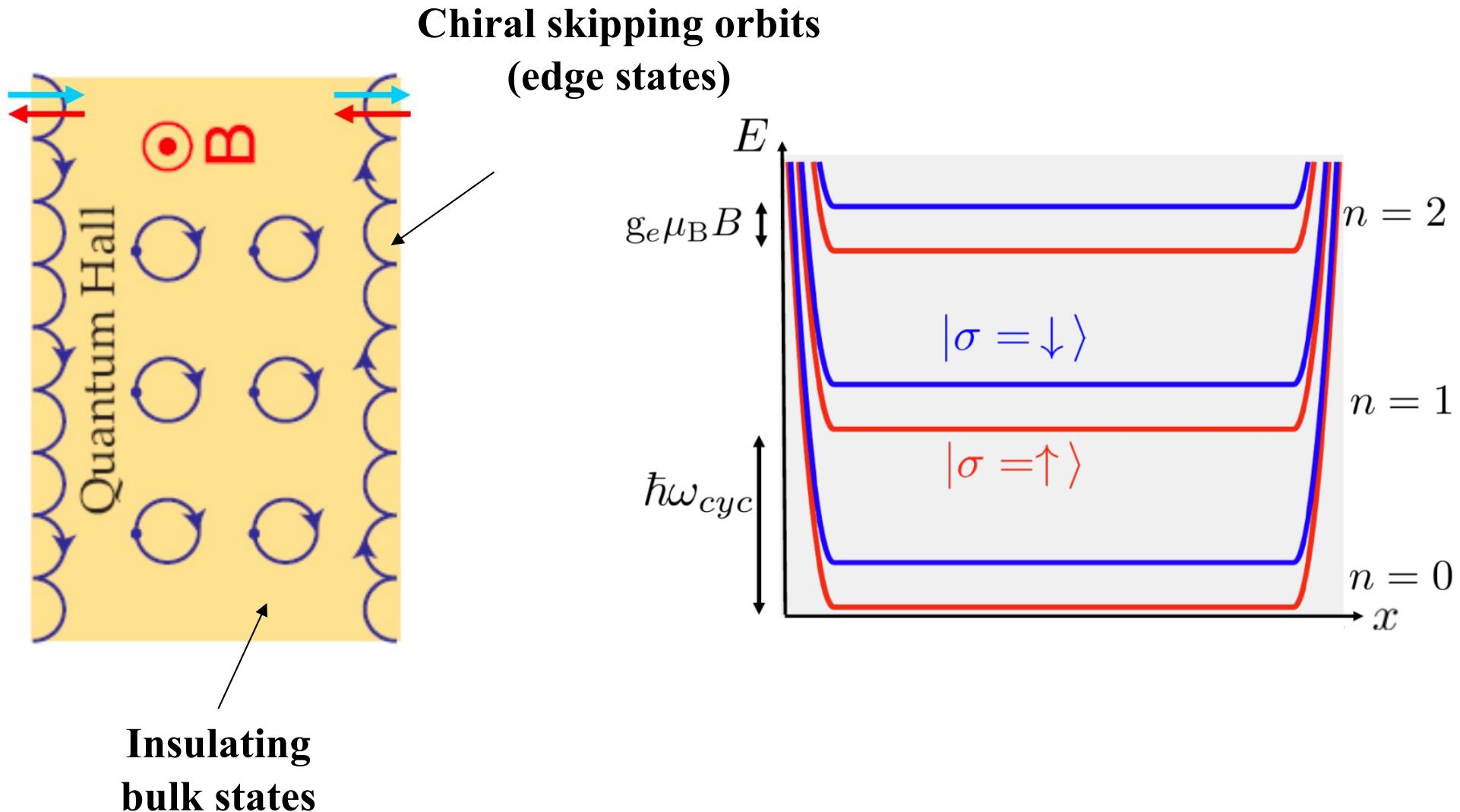
Magneto-transport: Shubnikov-de Haas regime

Paravicini-Bagliani et al., Nature Physics (2019)

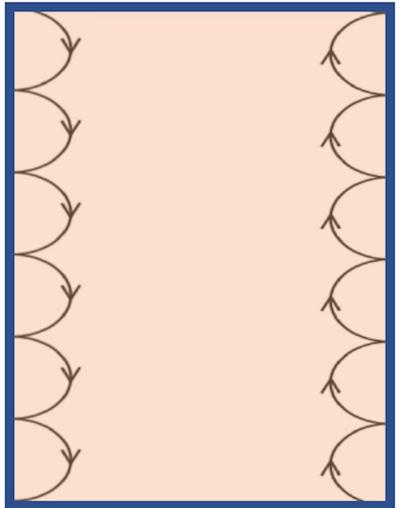
Bartolo & CC, PRB (2018)

Can the **cavity quantum vacuum** fluctuations
modify quantum Hall physics?

Quantum Hall transport: edge picture



Integer quantum Hall: edge transport picture

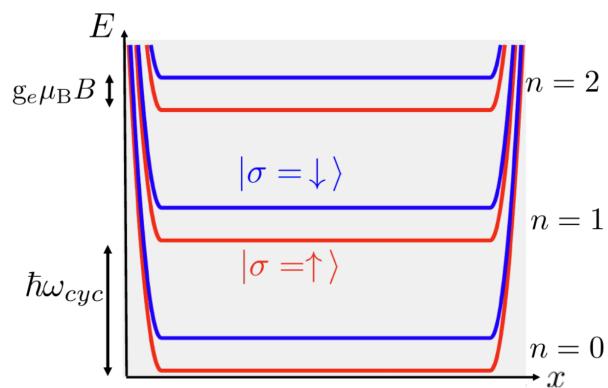


- Localized bulk states do not contribute to transport
- **No back-scattering for chiral 1D edge channels**

Landauer formula

$$G_H = \frac{e^2}{h} \sum_{n,\sigma} T_{n,\sigma}(E_F)$$

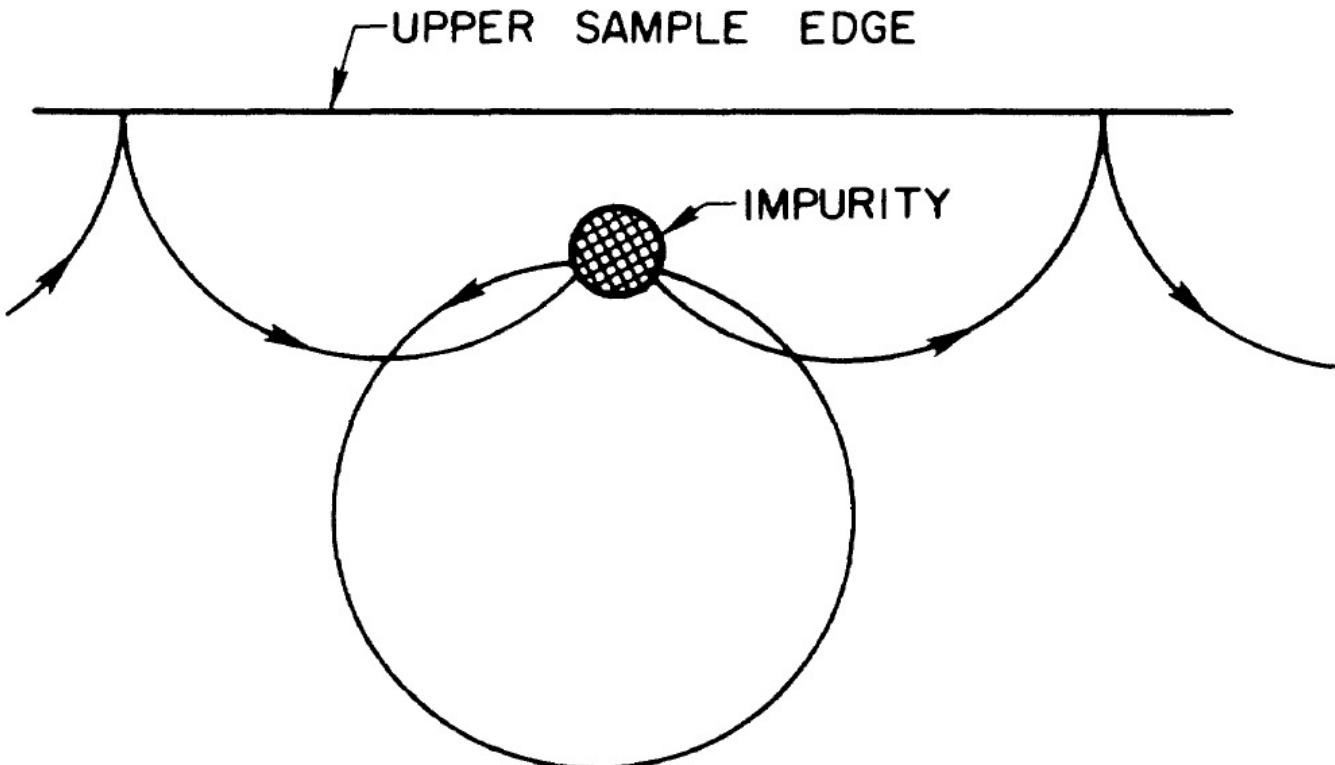
$$T_{n,\sigma} = 1$$



Edge transport is topologically protected

The only way would be for an electron in one edge state to scatter to the other side

Absence of backscattering for chiral edge states

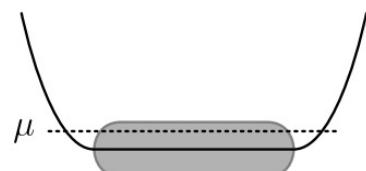
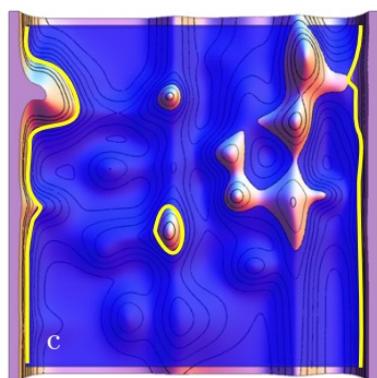


M. Büttiker, Phys. Rev. B 38, 9375 (1988)

Quantization of conductance is topological property



A mug or a donut have one hole



When edge states have no back-scattering,
number of edge channels is what matters

Resistance metrology: QH is topologically robust

Séminaire Poincaré 2 (2004) 39 – 51

Séminaire Poincaré

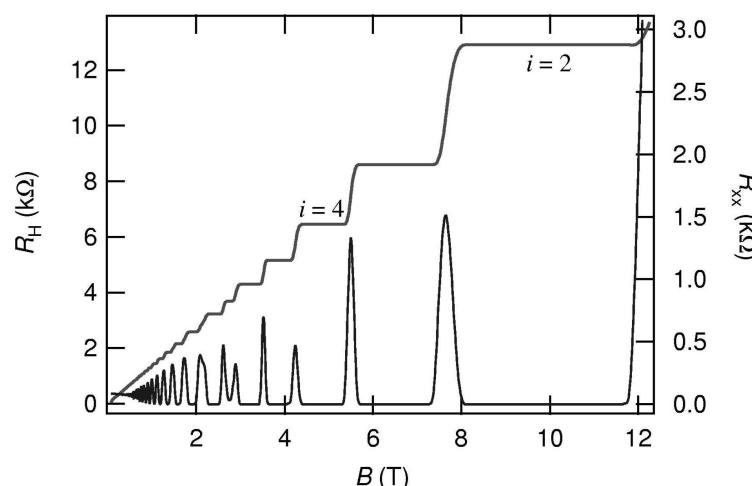
The Quantum Hall Effect as an Electrical Resistance Standard*

B. JECKELMANN and B. JEANNERET
Swiss Federal Office of Metrology and Accreditation
Lindenweg 50
CH-3003 Bern-Wabern
Switzerland

Abstract. The quantum Hall effect (QHE) provides an invariant reference for resistance linked to natural constants. It is used worldwide to maintain and compare the unit of resistance. The reproducibility reached today is almost two orders of magnitude better than the uncertainty of the determination of the ohm in the International System of Units SI. This article is a summary of a recently published review article which focuses mainly on the aspects of the QHE relevant for its metrological application.

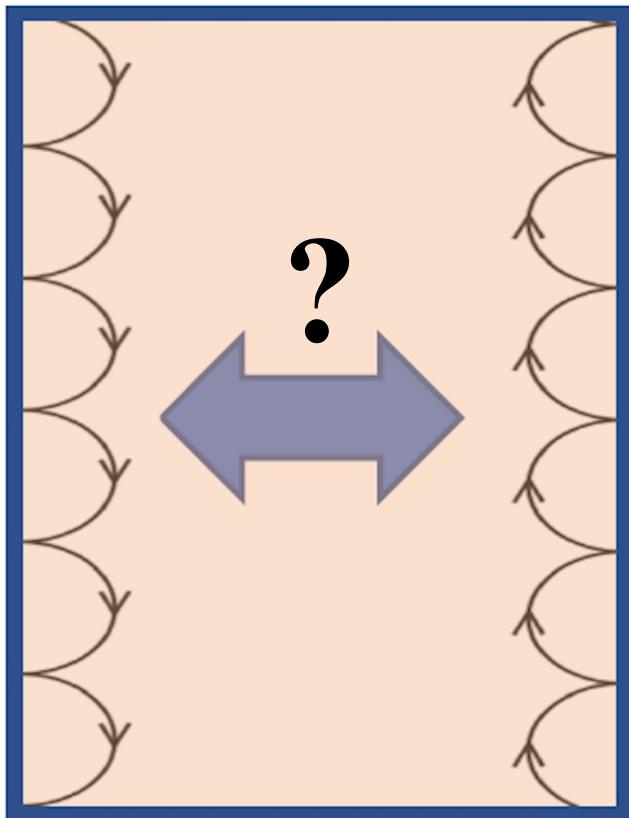
Metrological accuracy....

$$\frac{\overline{i \cdot R_H(i)}}{2 \cdot R_H(2)} = \underline{\underline{1 - (1.2 \pm 2.9) \cdot 10^{-10}}}, \quad i = 1, 3, 4, 6, 8.$$



Giant vacuum fields a threat to the topological protection?

Can **cavity vacuum fluctuations**
induce a **inter-edge coupling**?



All in all, we have.....

- 1) Cavity vacuum field is all over the 2D electron gas
- 2) Topological robustness not immune
to non-local perturbations

Experiments (collaboration with Faist's group at ETH Zürich)

ETHzürich



Felice Appugliese



**Josephine
Enkner**



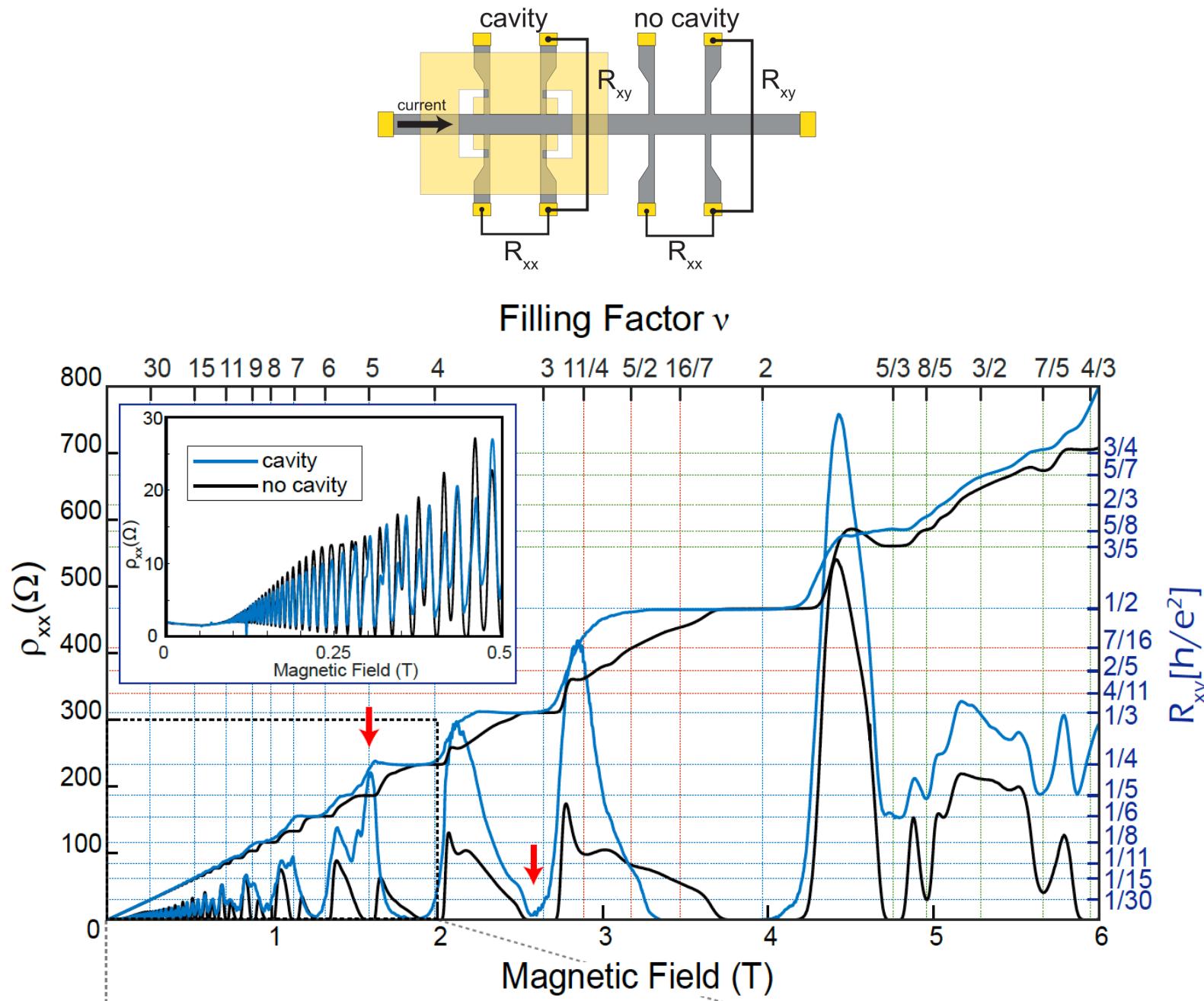
Giacomo Scalari



Jérôme Faist

F. Appugliese, J. Enkner, G. L. Paravicini-Bagliani, M. Beck, Ch. Reichl, W. Wegscheider, G. Scalari, C. Ciuti, J. Faist, Science 375, 1030 (2022)

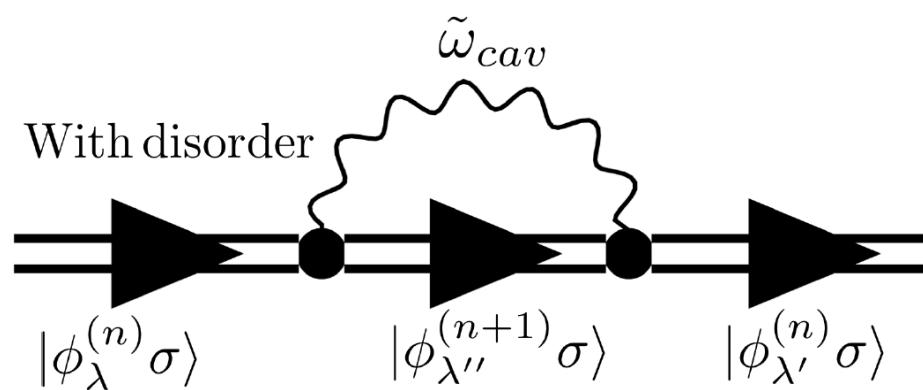
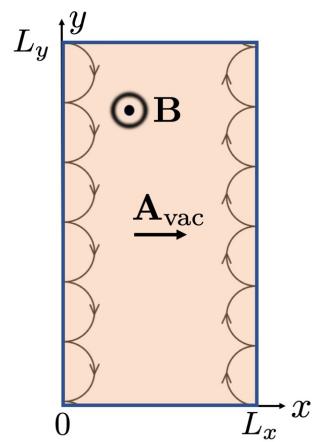
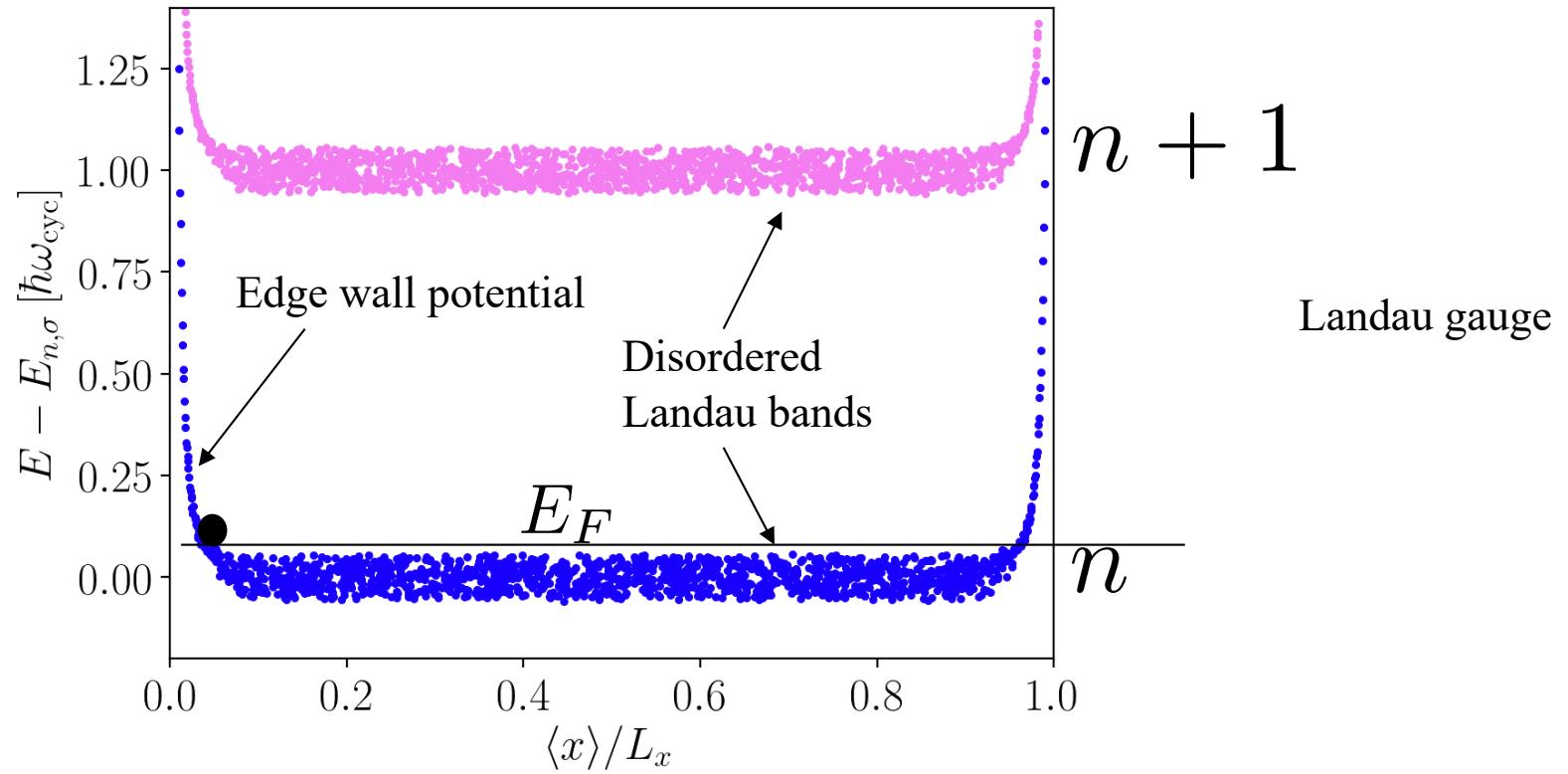
Breakdown of the topological protection of integer QH effect



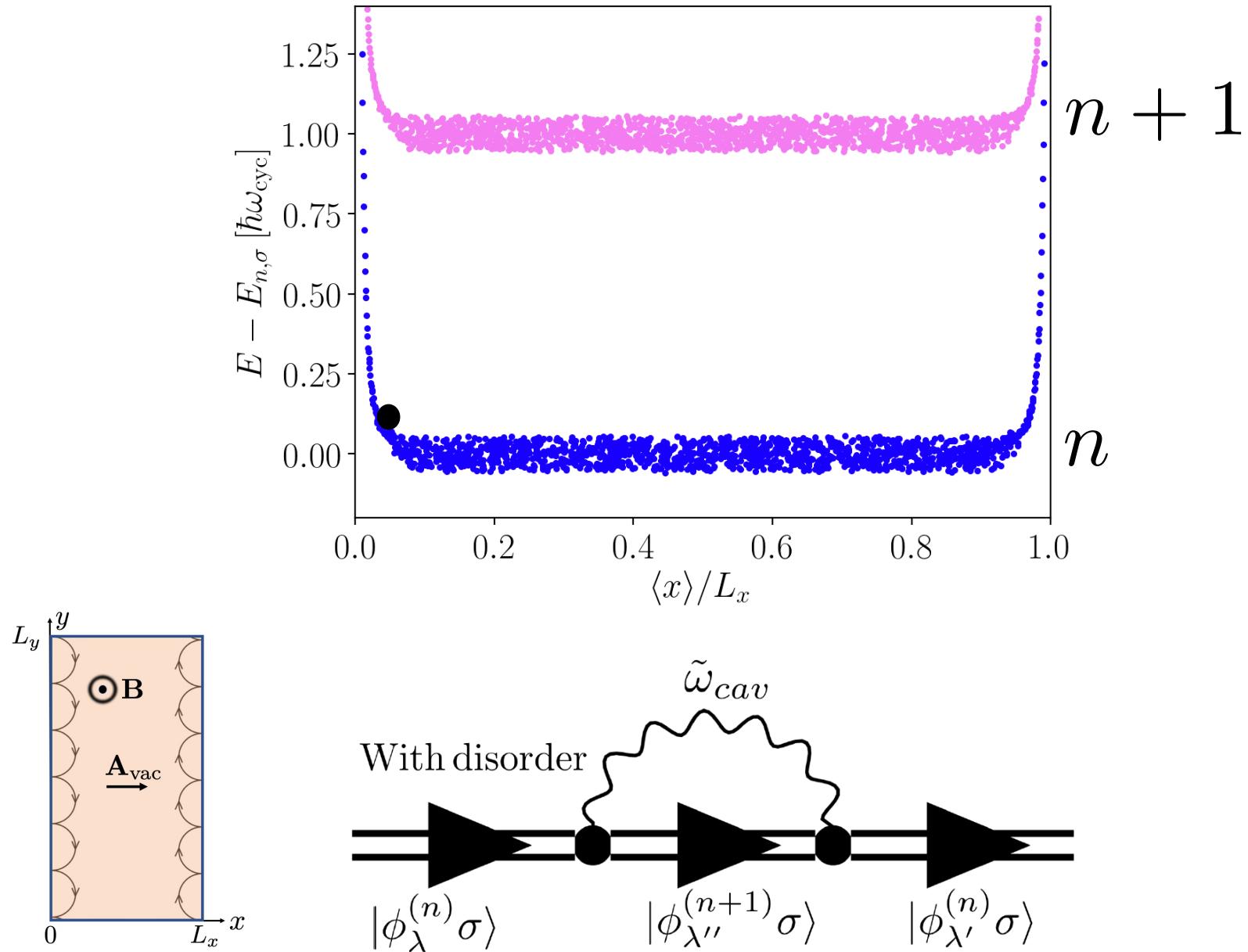
Cavity-mediated electron hopping in disordered electron quantum Hall systems

CC, PRB 104, 155307 (2021)

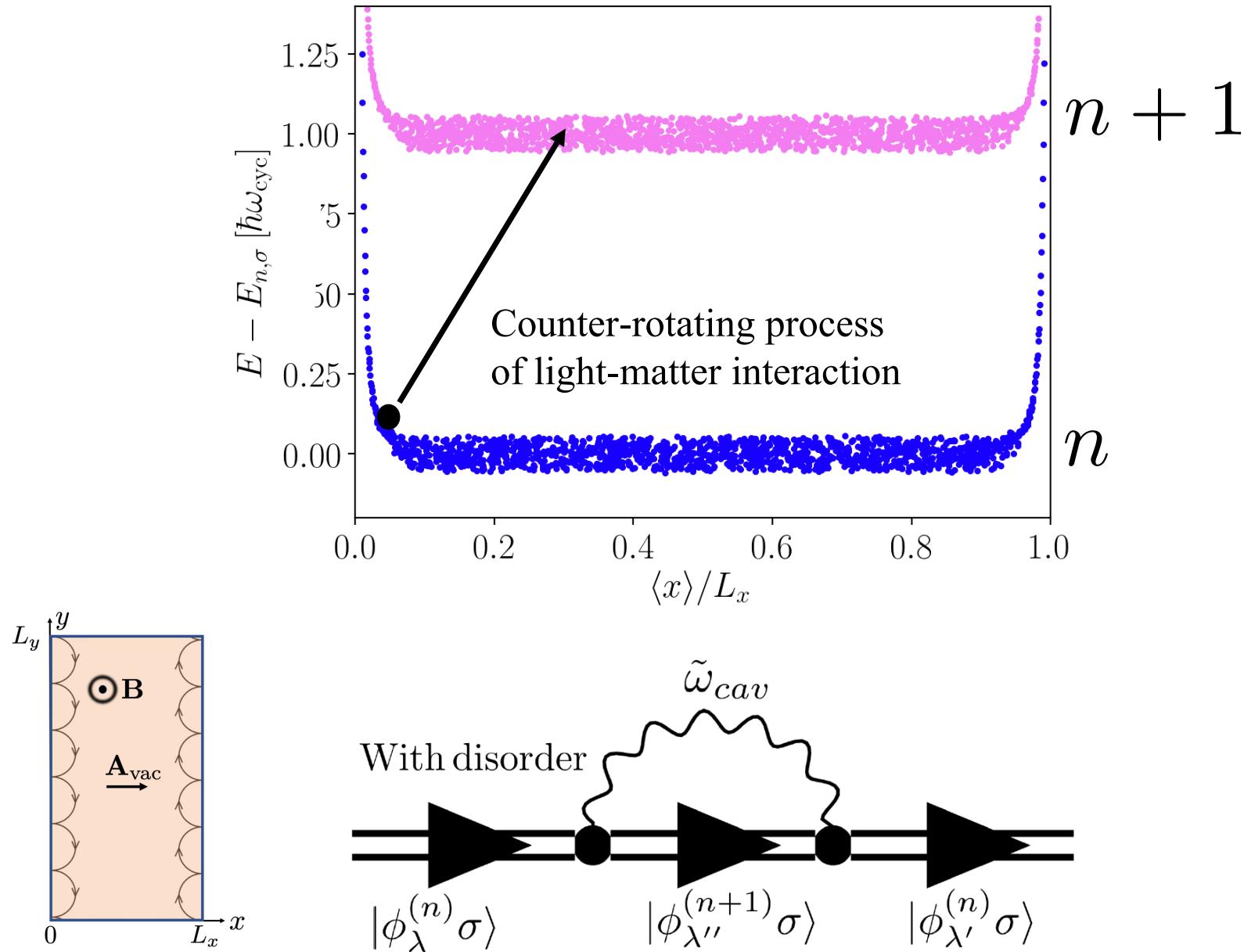
Cavity-mediated electron hopping with disordered Landau levels



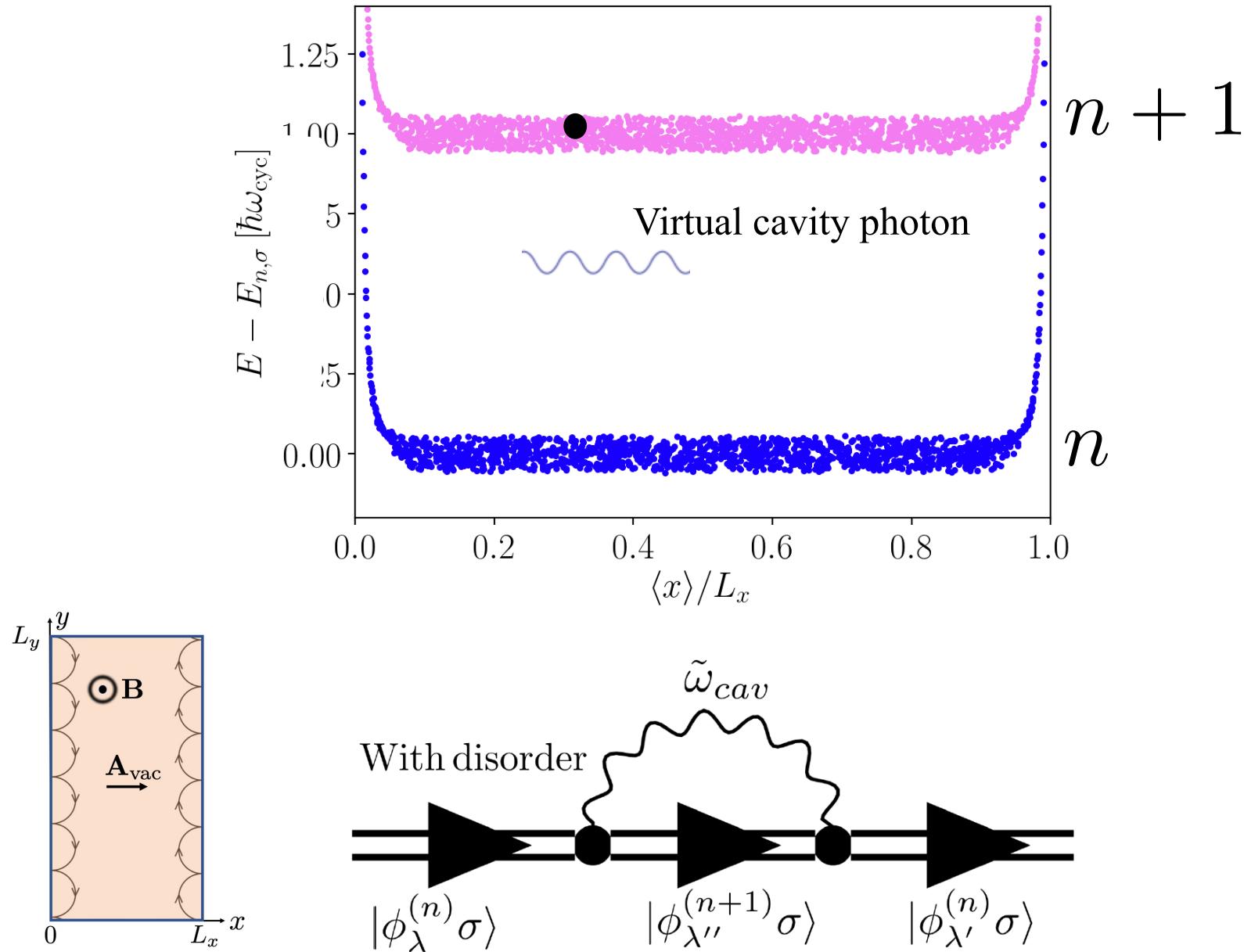
Yes ... The physical mechanism



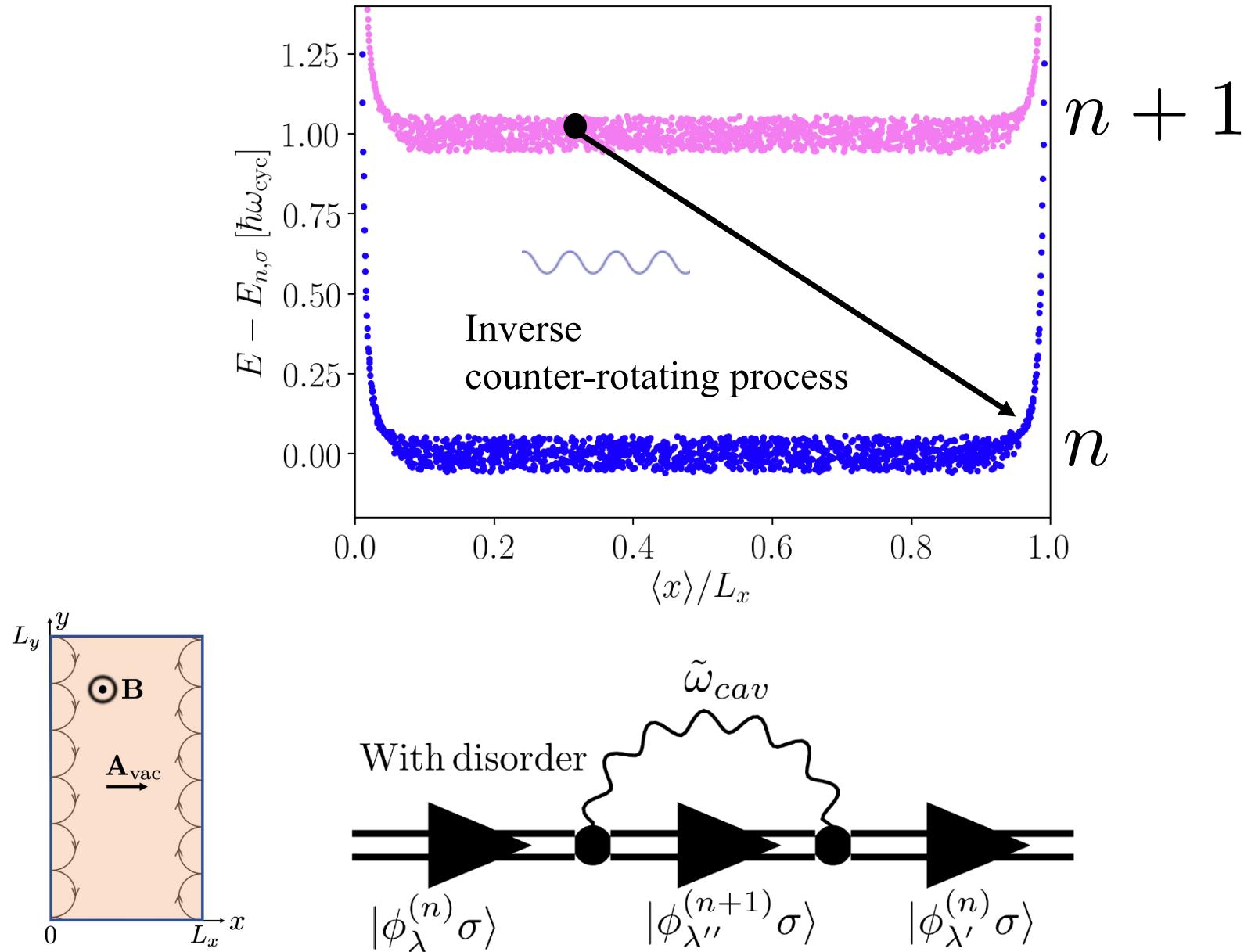
Yes... The physical mechanism



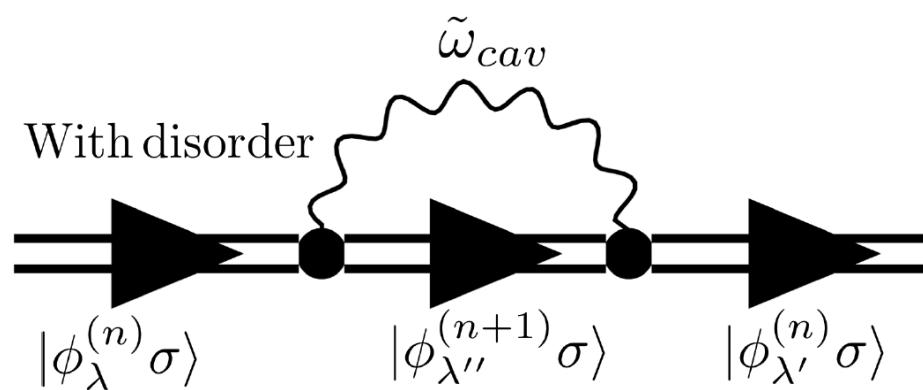
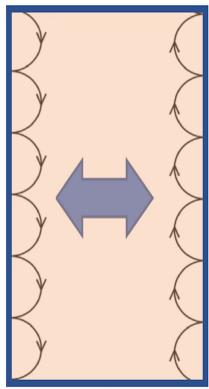
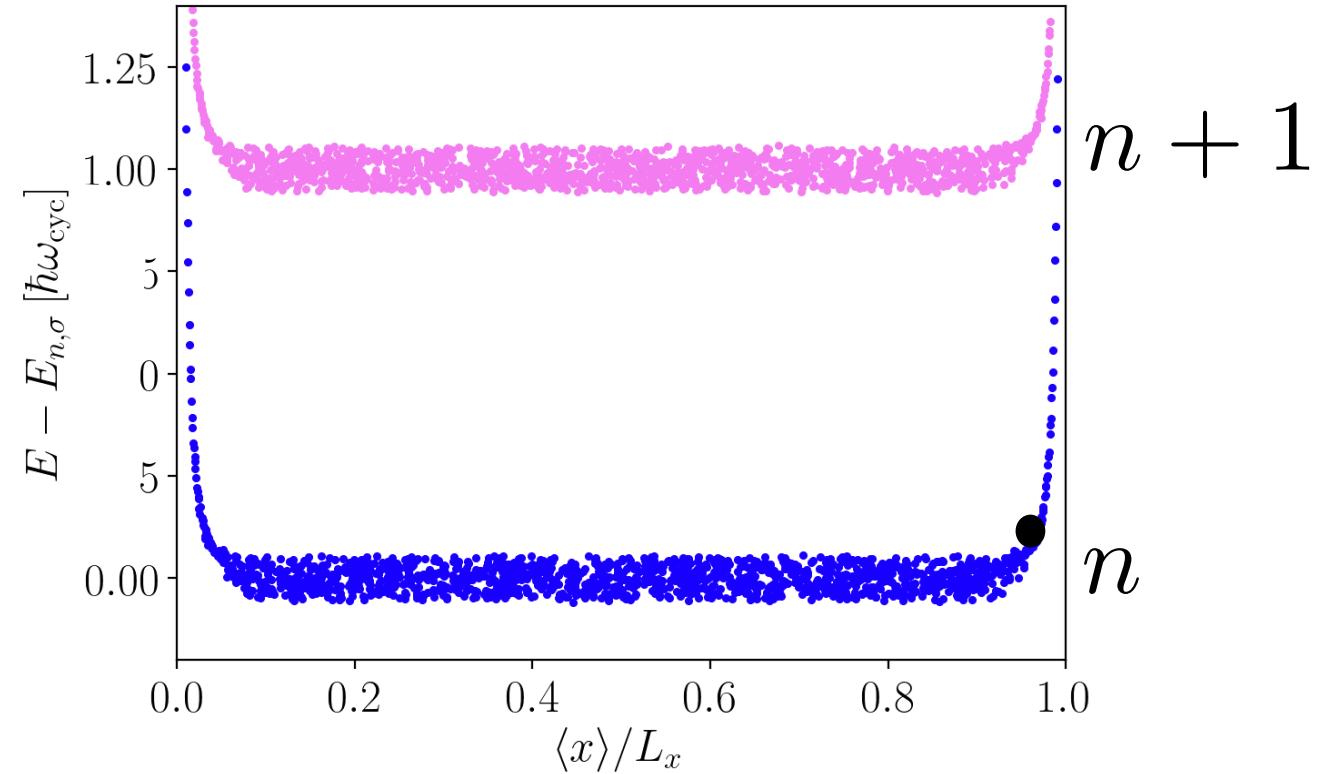
Yes... The physical mechanism



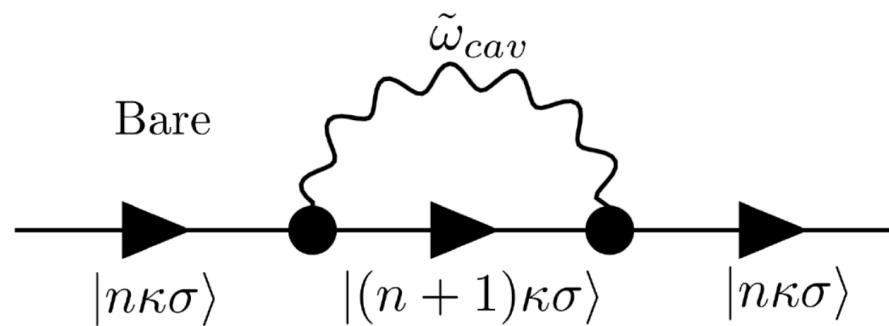
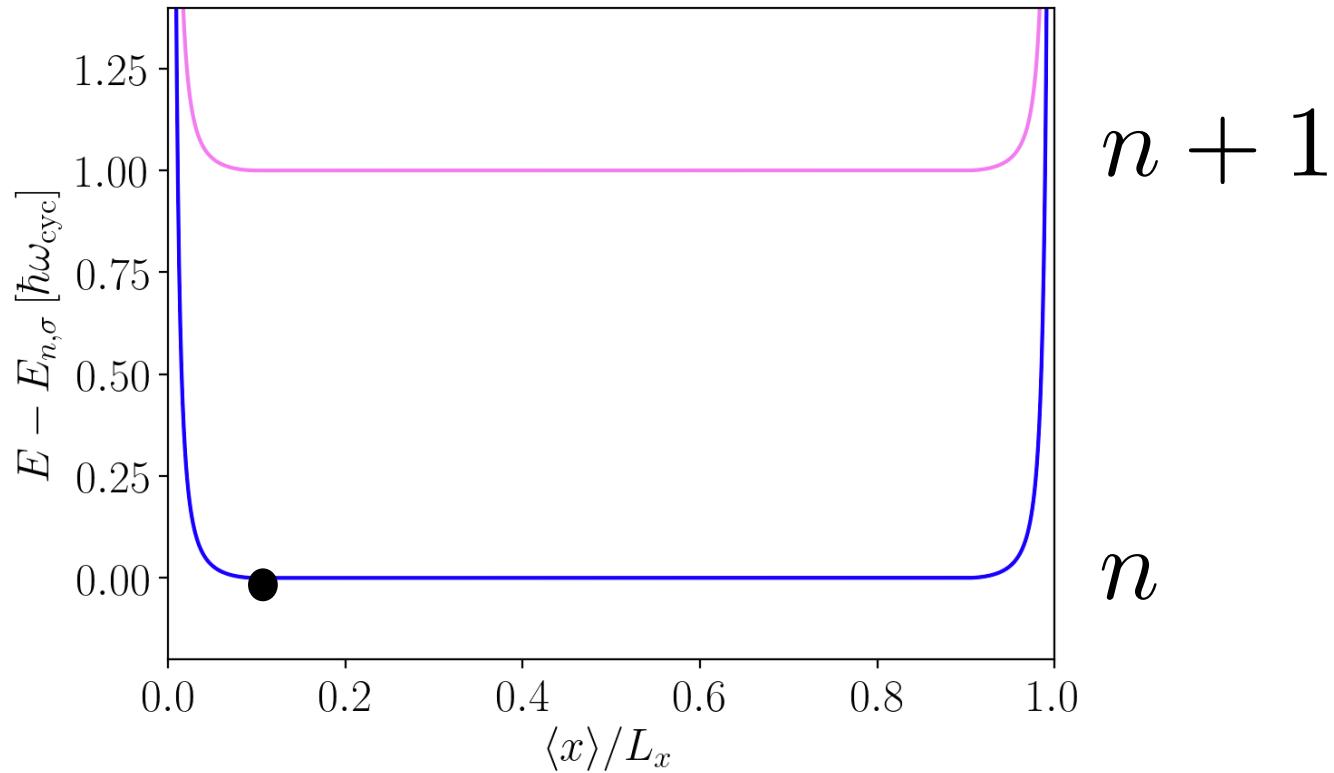
Yes... The physical mechanism



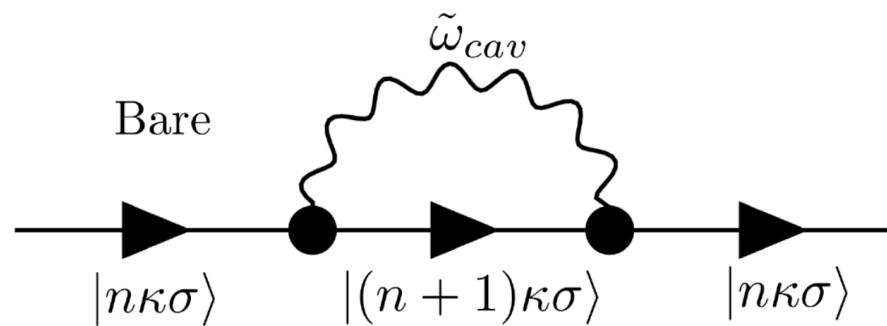
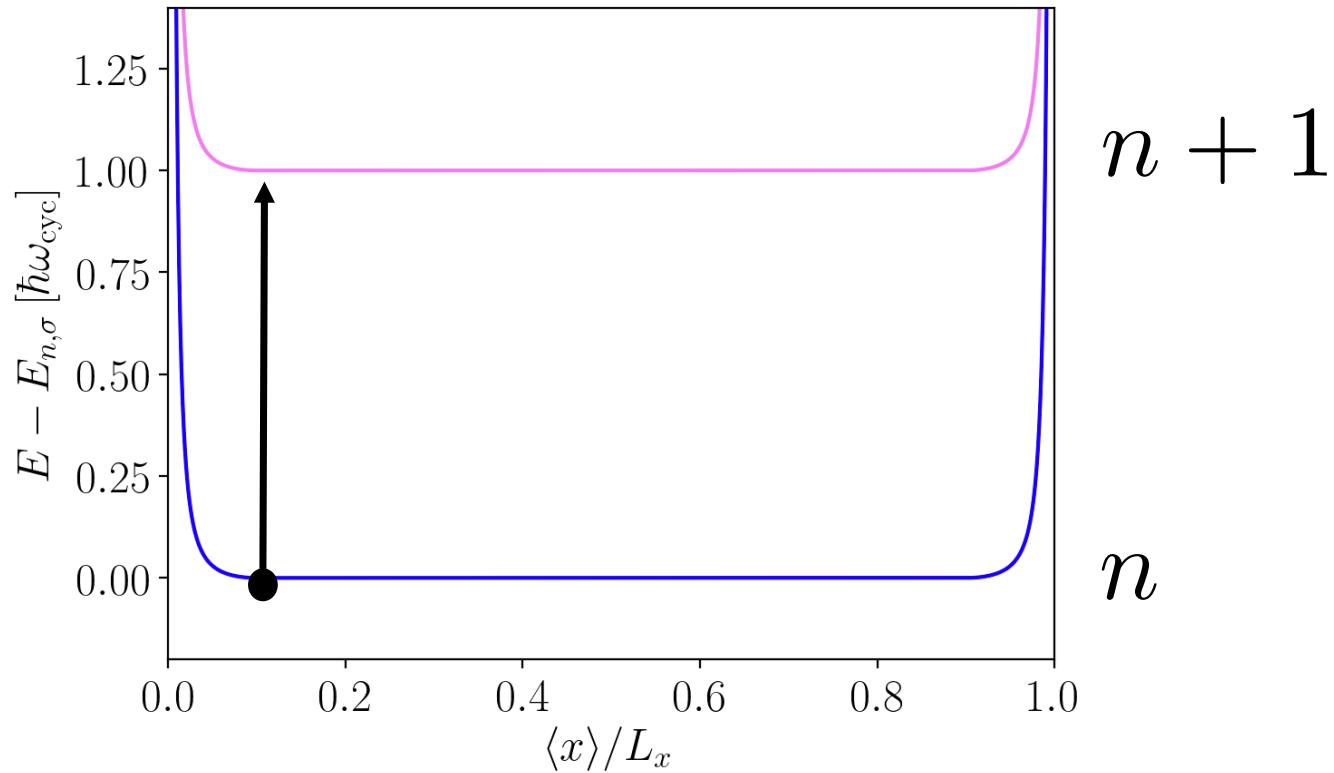
Cavity-mediated hopping via the exchange of a virtual cavity photon



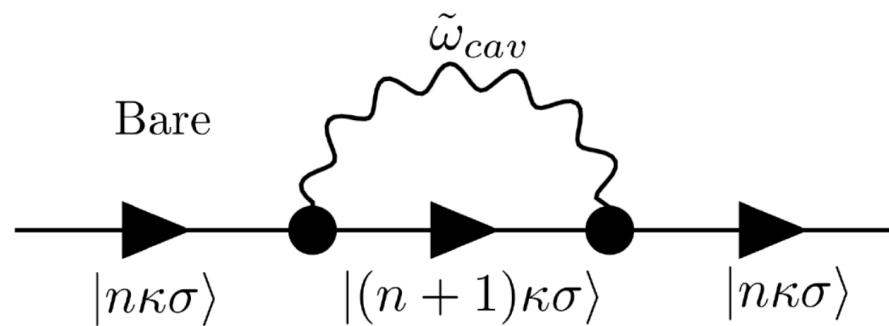
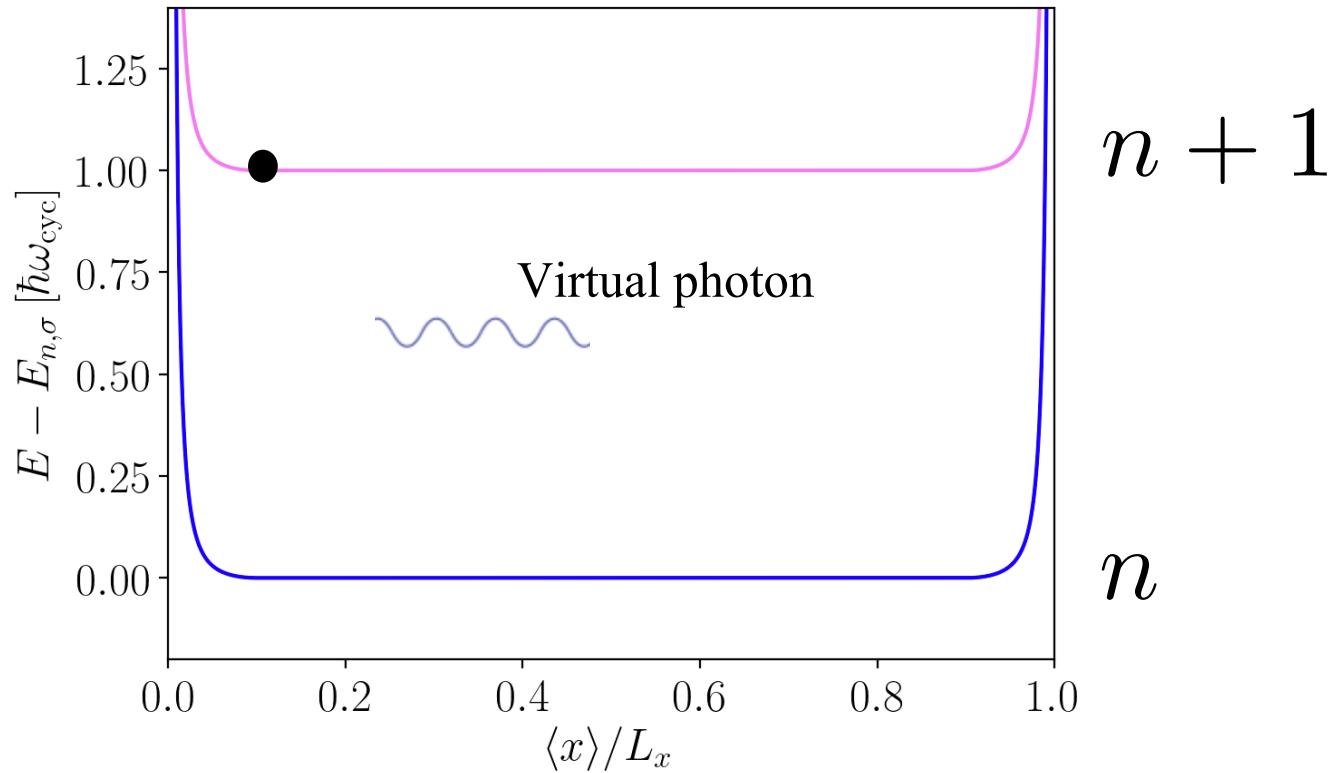
Important: no disorder, no cavity-mediated hopping!



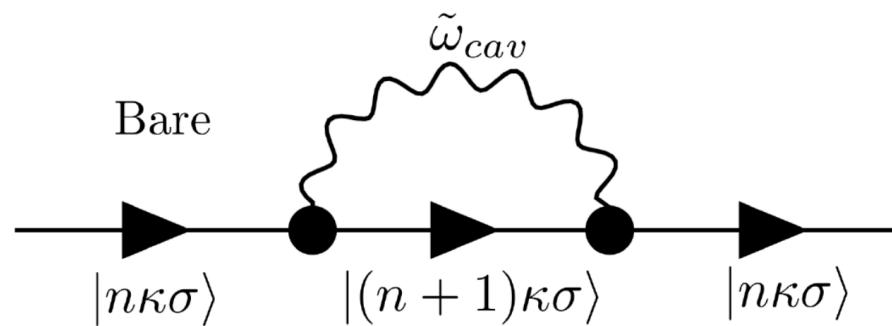
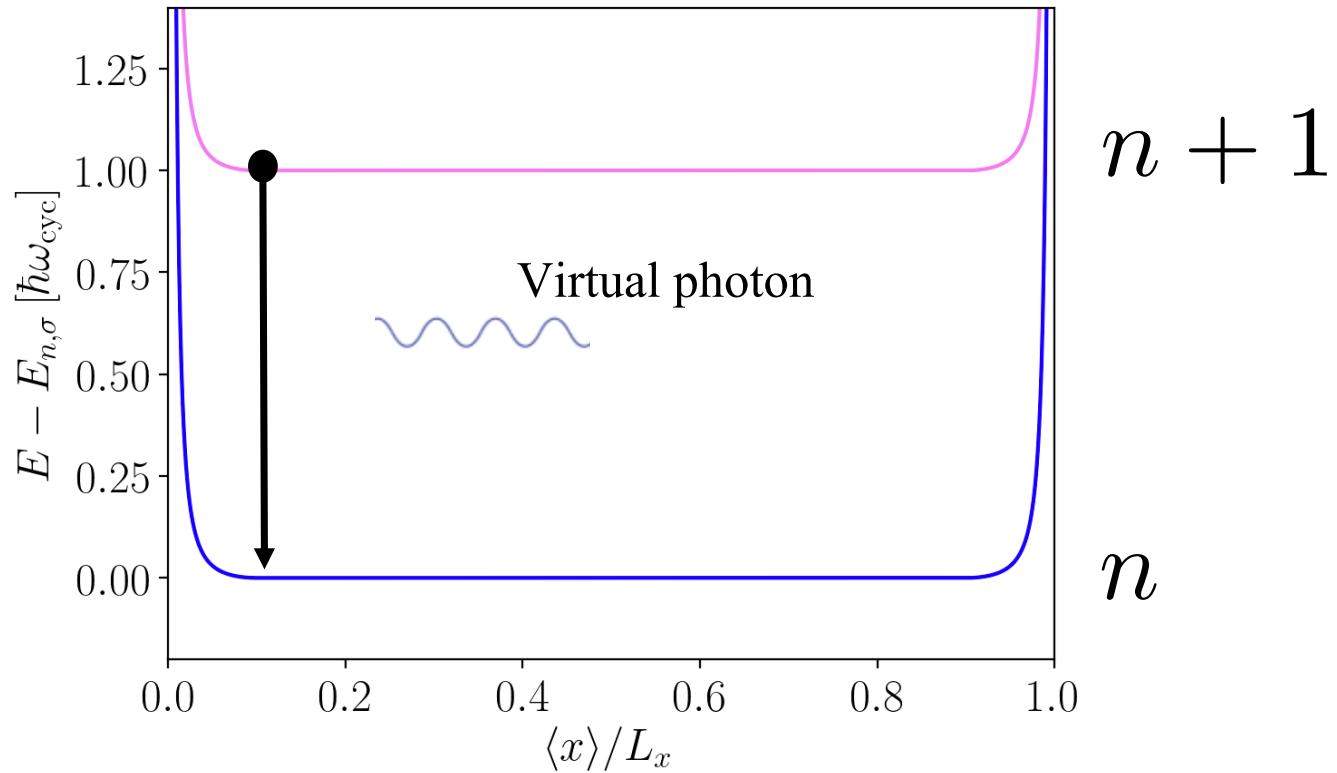
Important: no disorder, no cavity-mediated hopping!



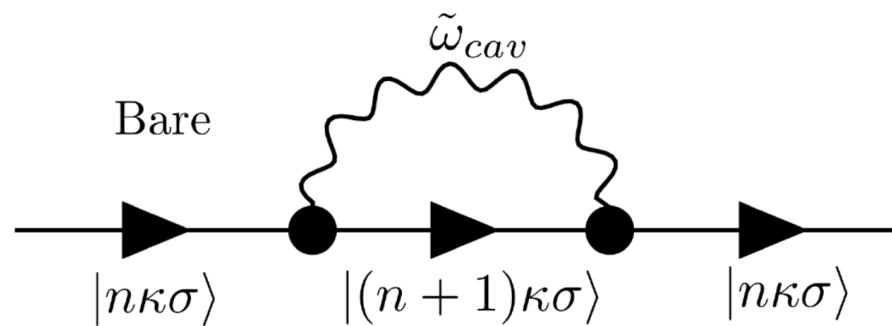
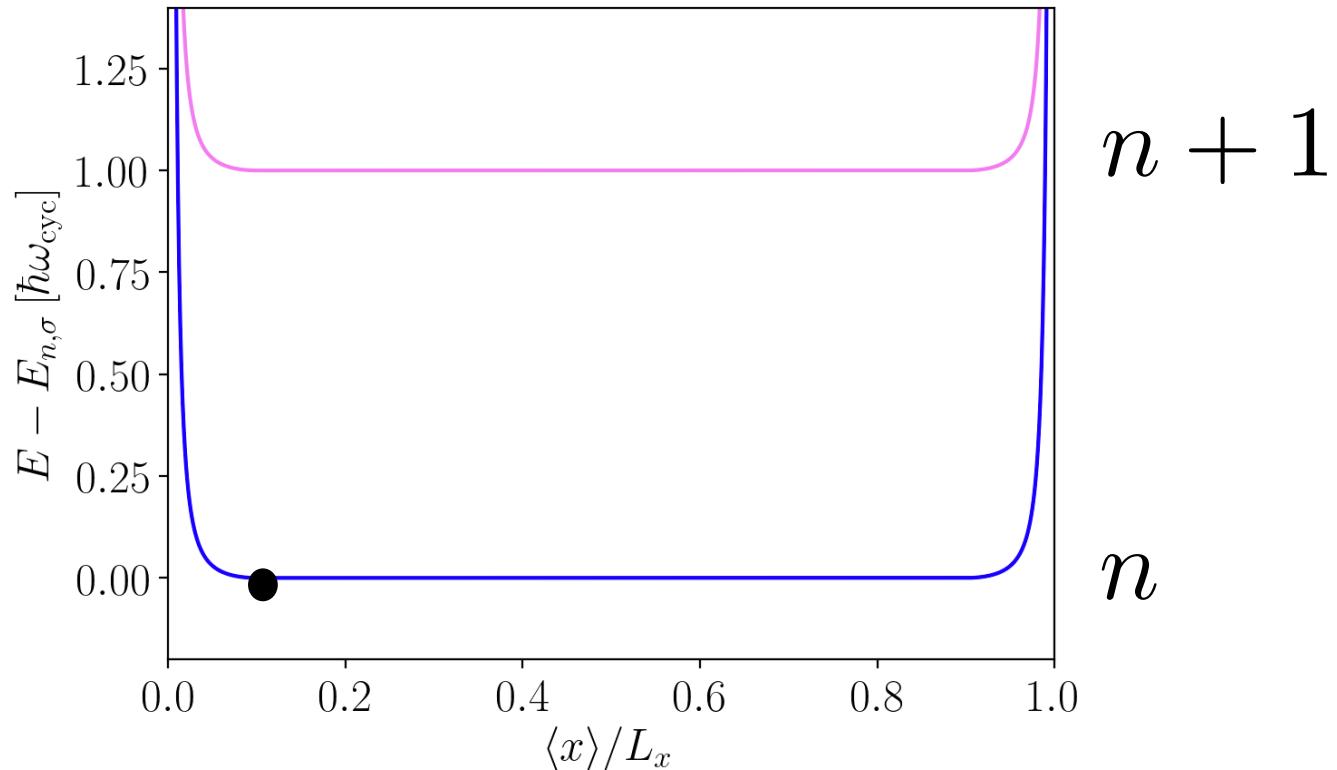
Important: no disorder, no cavity-mediated hopping!



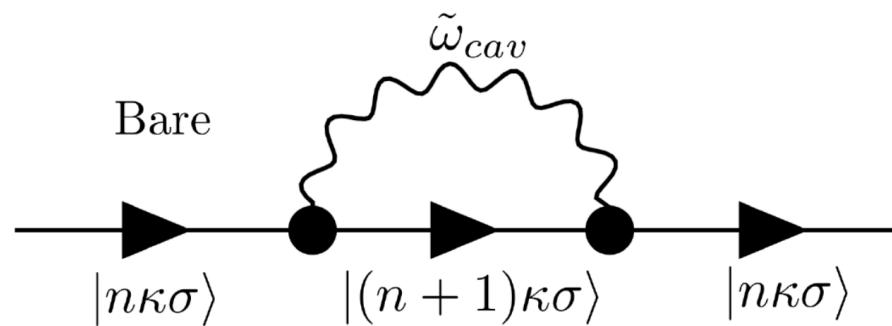
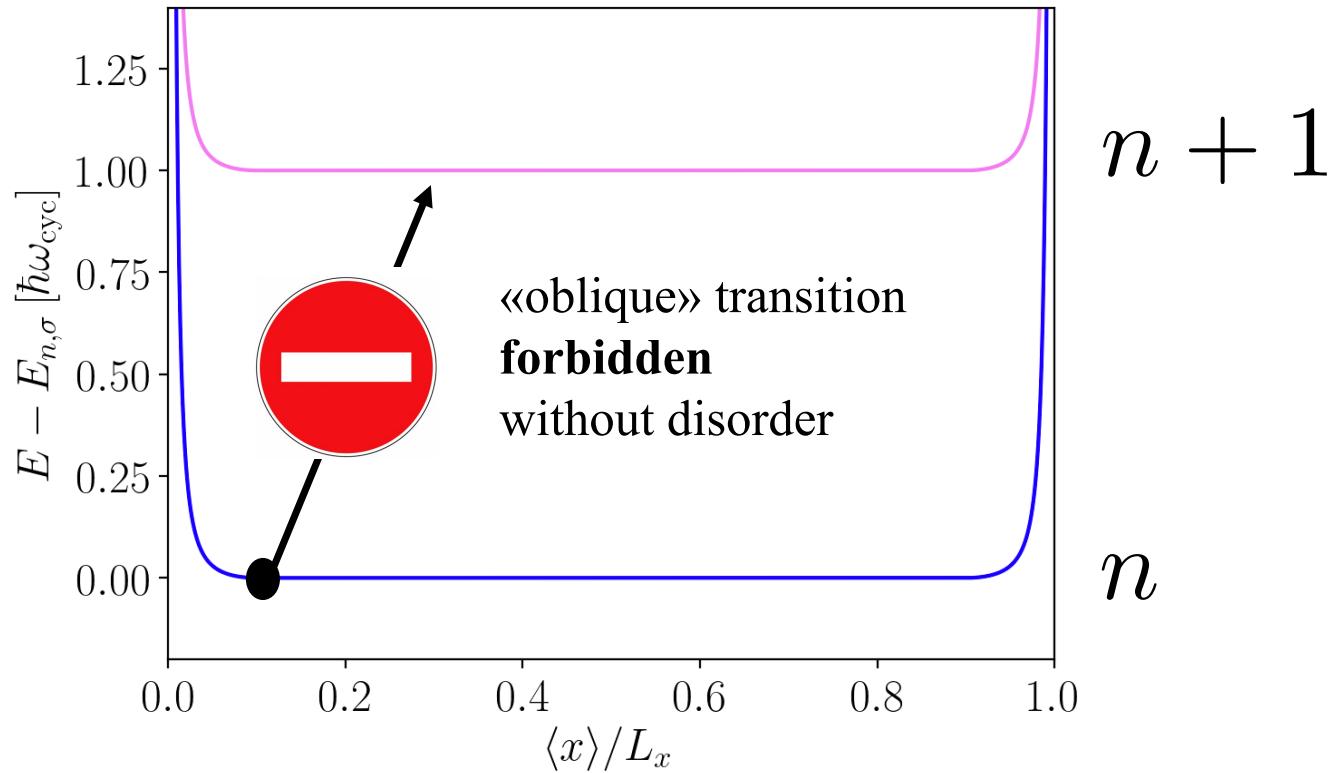
Important: no disorder, no cavity-mediated hopping!



Important: no disorder, no cavity-mediated hopping!



Important: no disorder, no cavity-mediated hopping!



Summarizing the final Hamiltonian

Single-particle Hamiltonian in terms of disordered eigenstates (wall included)

$$\hat{H}_{\text{sp}} = \hat{H}_{\text{el}} + \hat{H}_{\text{dis}} = \sum_{n,\kappa,\sigma} \left(\epsilon_{n,\lambda} + \frac{1}{2} \sigma g_e \mu_B B \right) \hat{d}_{n,\lambda,\sigma}^\dagger \hat{d}_{n,\lambda,\sigma},$$

Renormalized cavity mode (due to diamagnetic term)

$$\hat{H}_{\text{mode}} = \hat{H}_{\text{cav}} + \hat{H}_{\text{dia}} = \hbar \tilde{\omega}_{\text{cav}} \hat{\alpha}^\dagger \hat{\alpha}$$

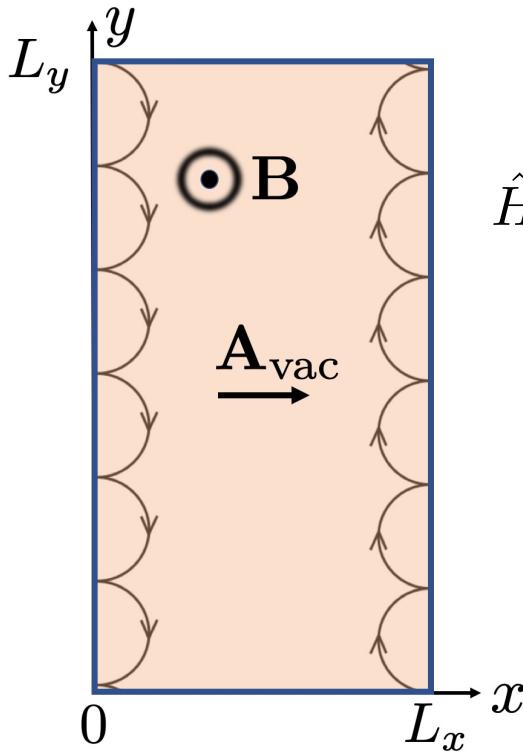
Interaction between disordered eigenstates and renormalized mode

$$\hat{H}_{\text{para}} = \sum_{n,\lambda,\lambda'',\sigma} (-i) \hbar \tilde{g}_{\lambda,\lambda''}^{(n,n+1)} (\hat{\alpha} + \hat{\alpha}^\dagger) \hat{d}_{n+1,\lambda'',\sigma}^\dagger \hat{d}_{n,\lambda,\sigma} + \text{h.c.}$$



Renormalized interaction (disorder + diamagnetic term)

Coupling constant modified by disorder and diamagnetism



$$\hat{H}_{\text{para}} = \sum_{n,\lambda,\lambda'',\sigma} (-i)\hbar\tilde{g}_{\lambda,\lambda''}^{(n,n+1)} (\hat{\alpha} + \hat{\alpha}^\dagger) \hat{d}_{n+1,\lambda'',\sigma}^\dagger \hat{d}_{n,\lambda,\sigma} + \text{h.c.}$$

**Renormalized vacuum Rabi frequency
(disorder and diamagnetic)**

$$\tilde{g}_{\lambda,\lambda''}^{(n,n+1)} = \tilde{g}\sqrt{n+1} \sum_{\kappa} \langle \phi_{\lambda''}^{(n+1)} | n+1 \kappa \rangle \langle n \kappa | \phi_{\lambda}^{(n)} \rangle$$

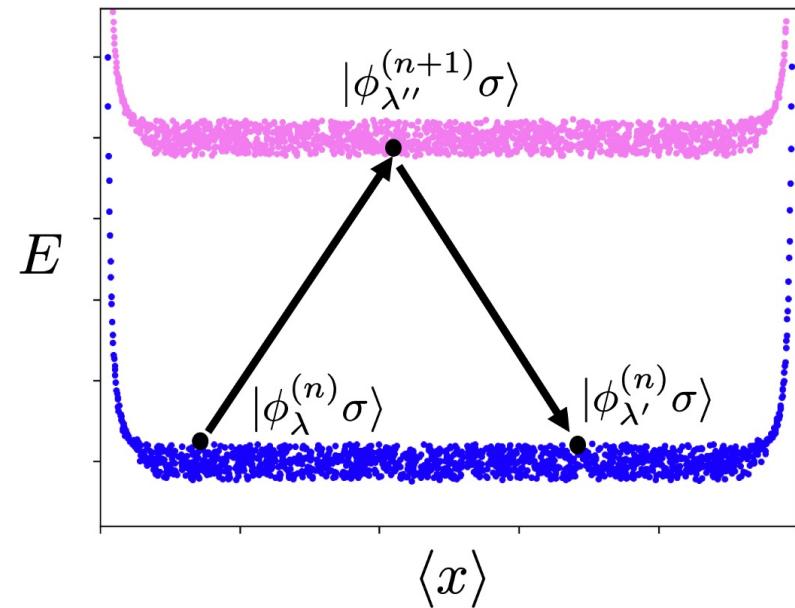
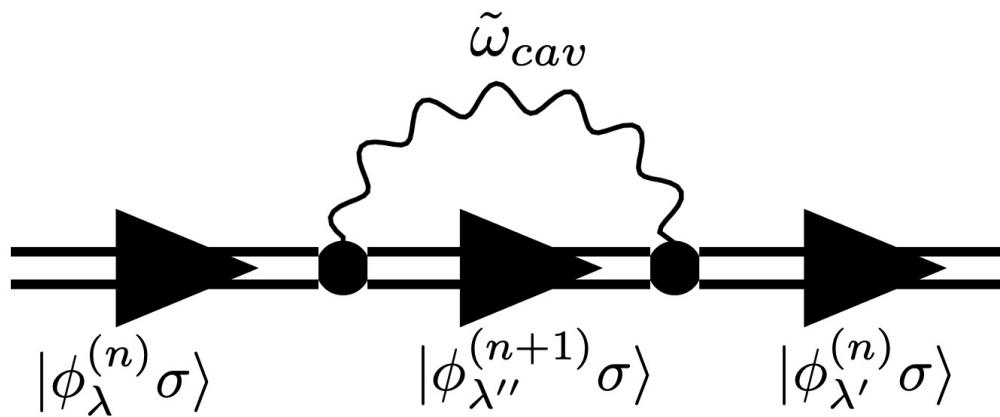
$$\hat{\mathbf{A}} = A_{\text{vac}} \mathbf{e}_x (\hat{\alpha} + \hat{\alpha}^\dagger)$$

Vector potential operator

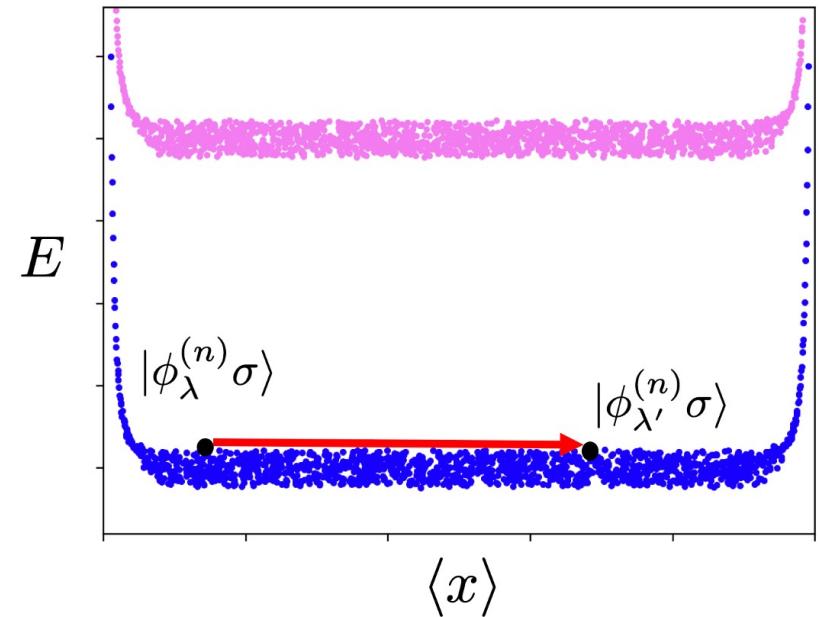
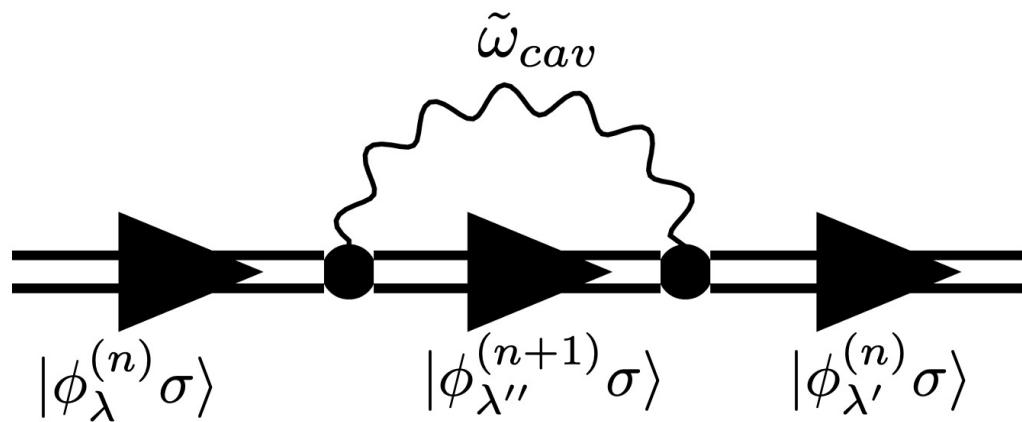
$$g = \frac{eA_{\text{vac}}}{\hbar} \sqrt{\frac{\hbar\omega_{\text{cyc}}}{2m}}$$

$$\tilde{g} = g \sqrt{\omega_{\text{cav}}/\tilde{\omega}_{\text{cav}}}$$

Cavity-mediated hopping between disordered Landau states



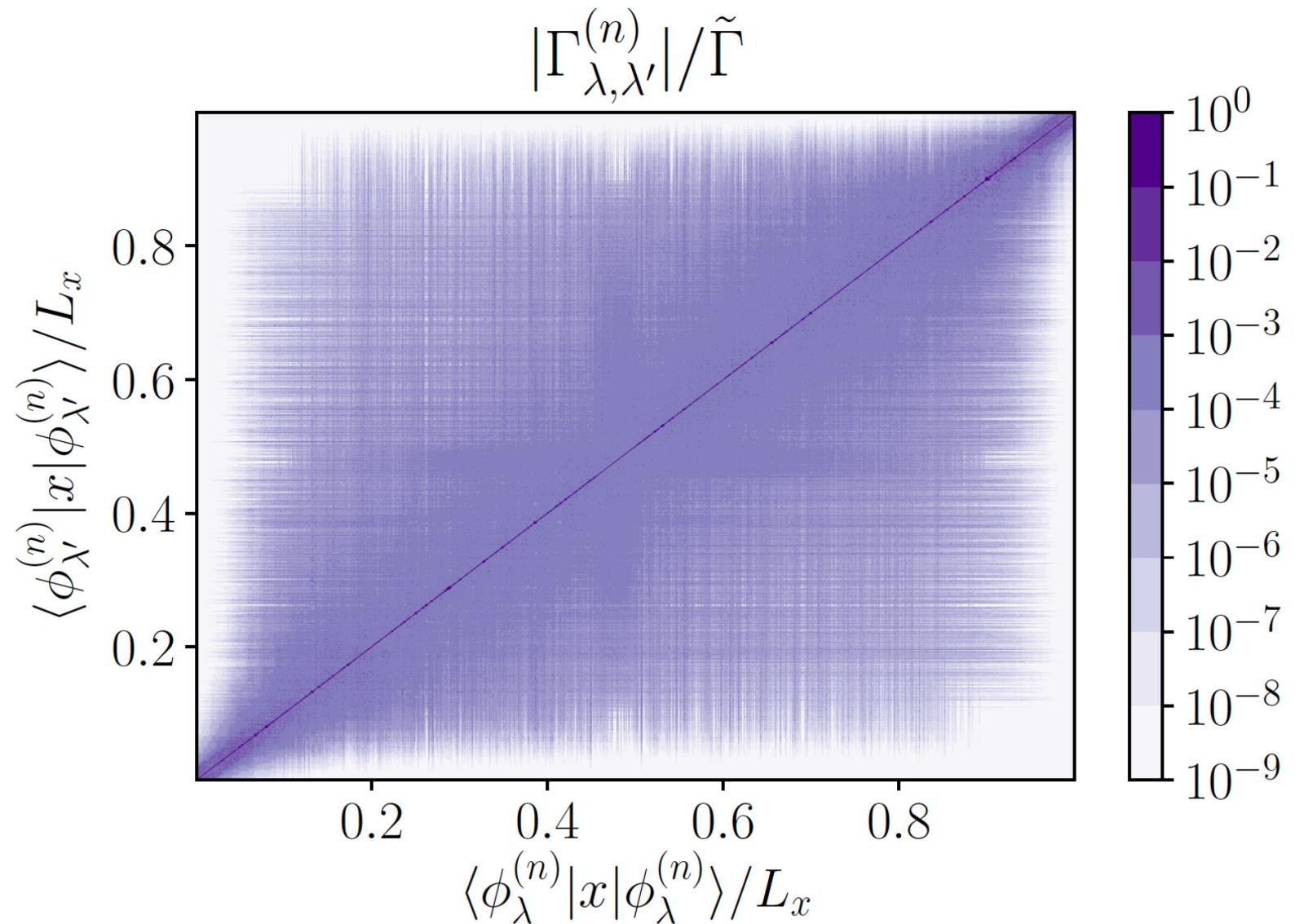
Effective hopping coupling



Effective cavity-mediated hopping (lowest order perturbation theory)

$$\Gamma_{\lambda, \lambda'}^{(n)} \simeq \sum_{\lambda''} \frac{\hbar^2 \tilde{g}_{\lambda, \lambda''}^{(n, n+1)} \tilde{g}_{\lambda', \lambda''}^{(n, n+1) \star}}{\epsilon_{n, \lambda} - \epsilon_{n+1, \lambda''} - \hbar \tilde{\omega}_{\text{cav}}}$$

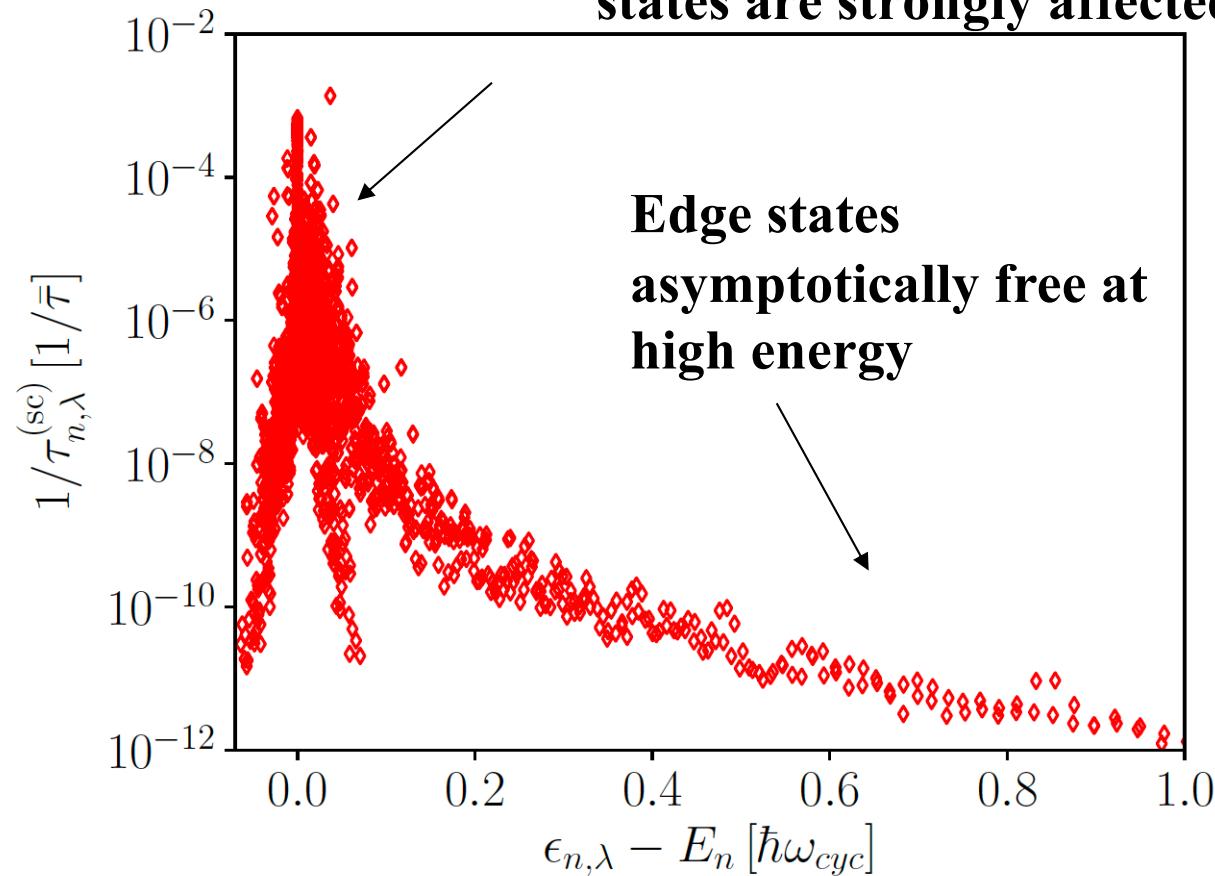
Long-range interaction



Cavity mediate-scattering rate

$$\frac{1}{\tau_{n,\lambda}^{(sc)}} = \frac{2\pi}{\hbar} \sum_{\lambda' \neq \lambda} |\Gamma_{\lambda,\lambda'}^{(n)}|^2 \delta(\epsilon_{n,\lambda} - \epsilon_{n,\lambda'})$$

**Edge states close to bulk
states are strongly affected**



$$\frac{1}{\bar{\tau}} \equiv \frac{2\pi}{\hbar} \tilde{\Gamma}^2 \frac{N_{\text{deg}}}{\hbar\omega_{\text{cyc}}}$$

Characteristic rate

Achilles' heel of the integer quantum Hall effect

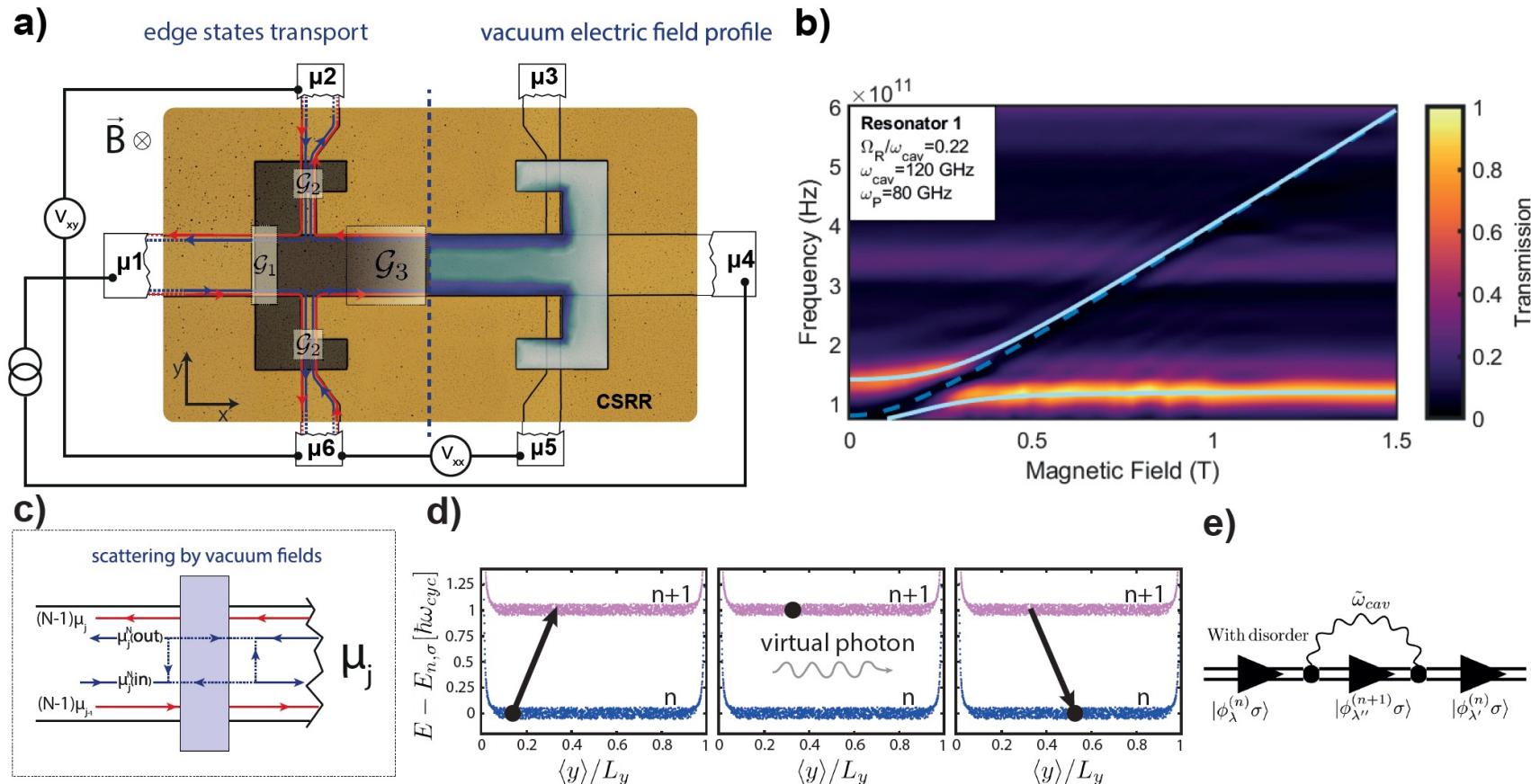
**Topological insulator
(integer quantum Hall system)**



**Non-local
perturbation
(inter-edge)**

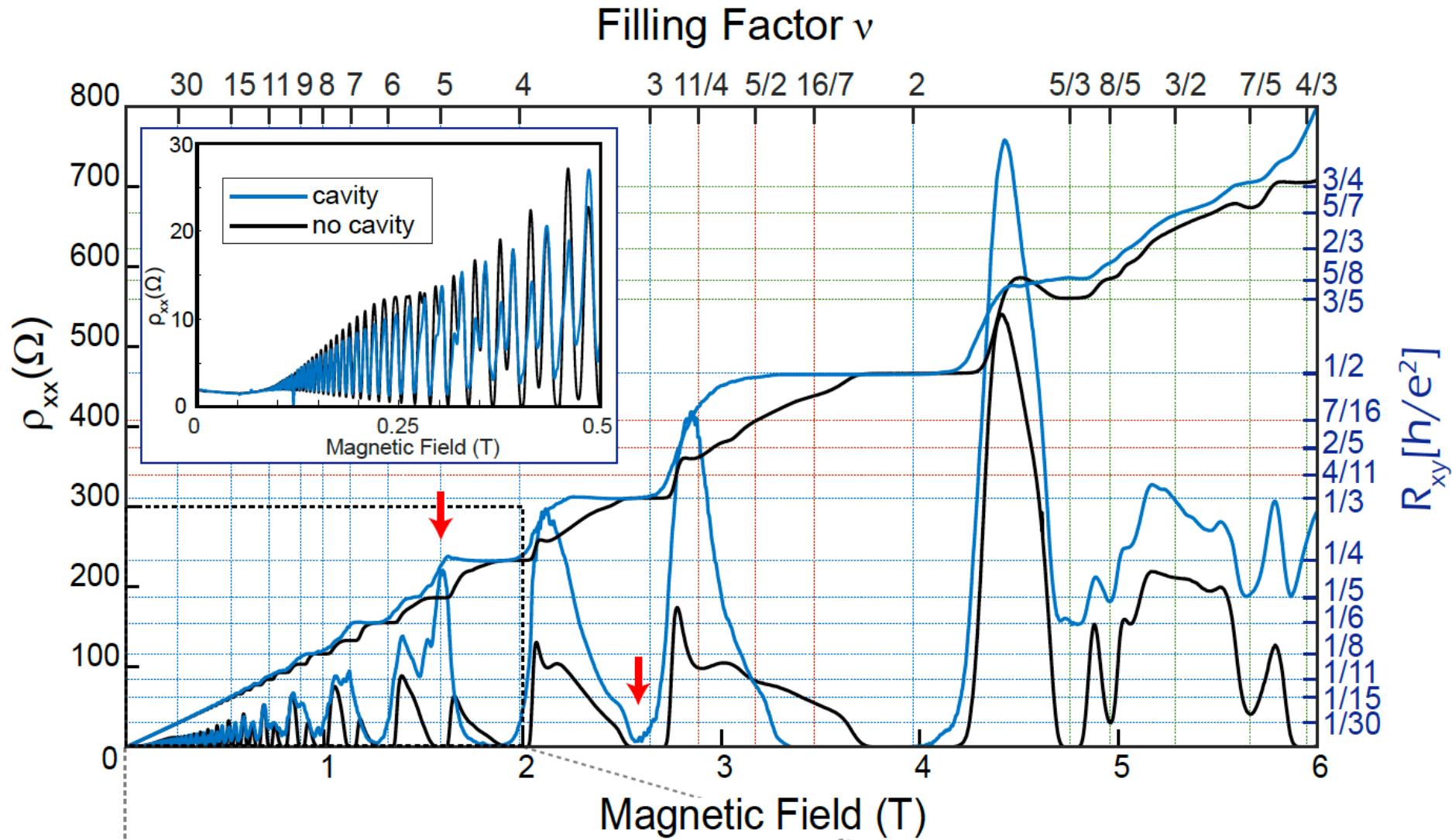


Experiments: J. Faist's group @ ETH Zürich

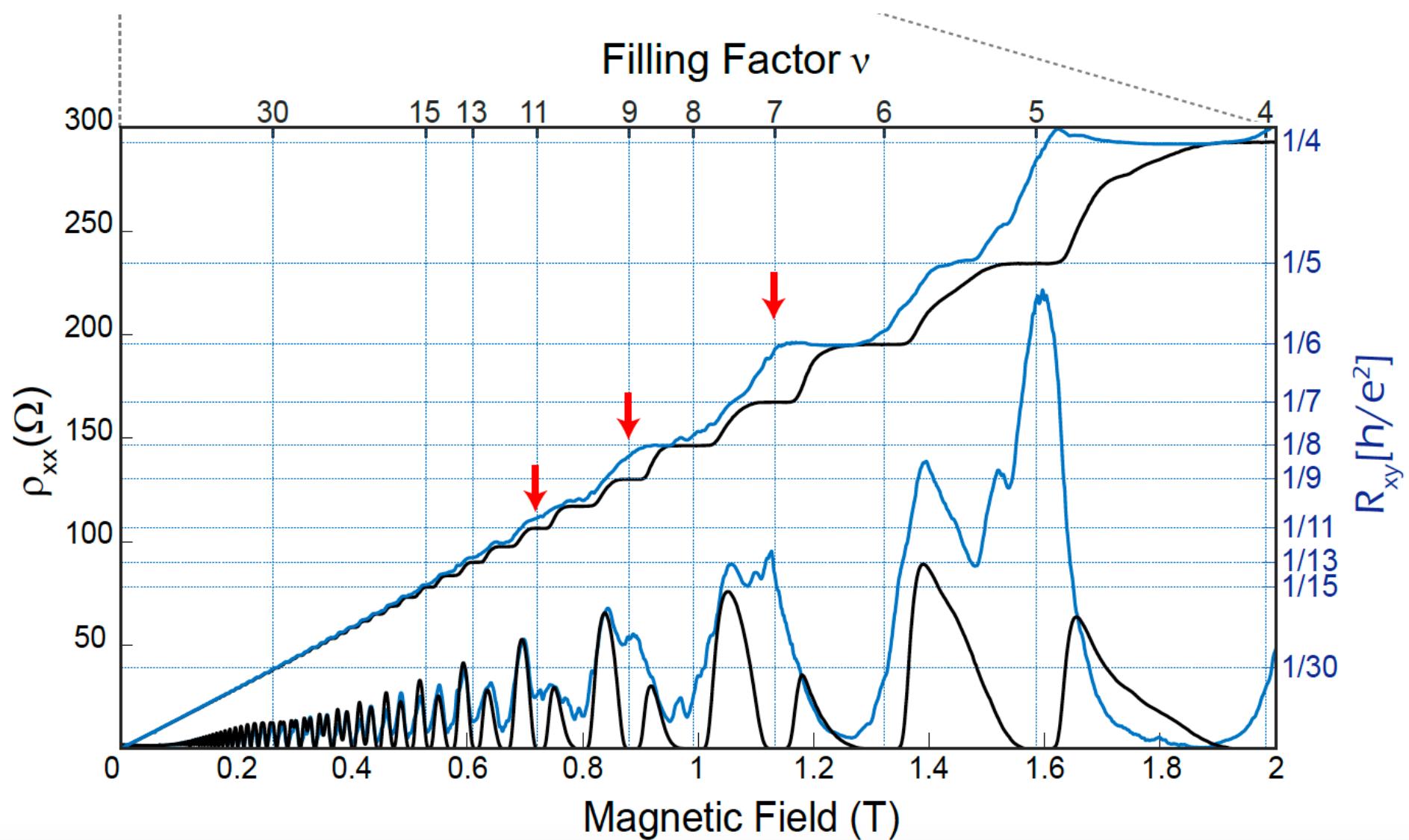


F. Appugliese, J. Enkner, G. L. Paravicini-Bagliani, M. Beck, Ch. Reichl, W. Wegscheider, G. Scalari, C. Ciuti, J. Faist, Science 375, 1030 (2022)

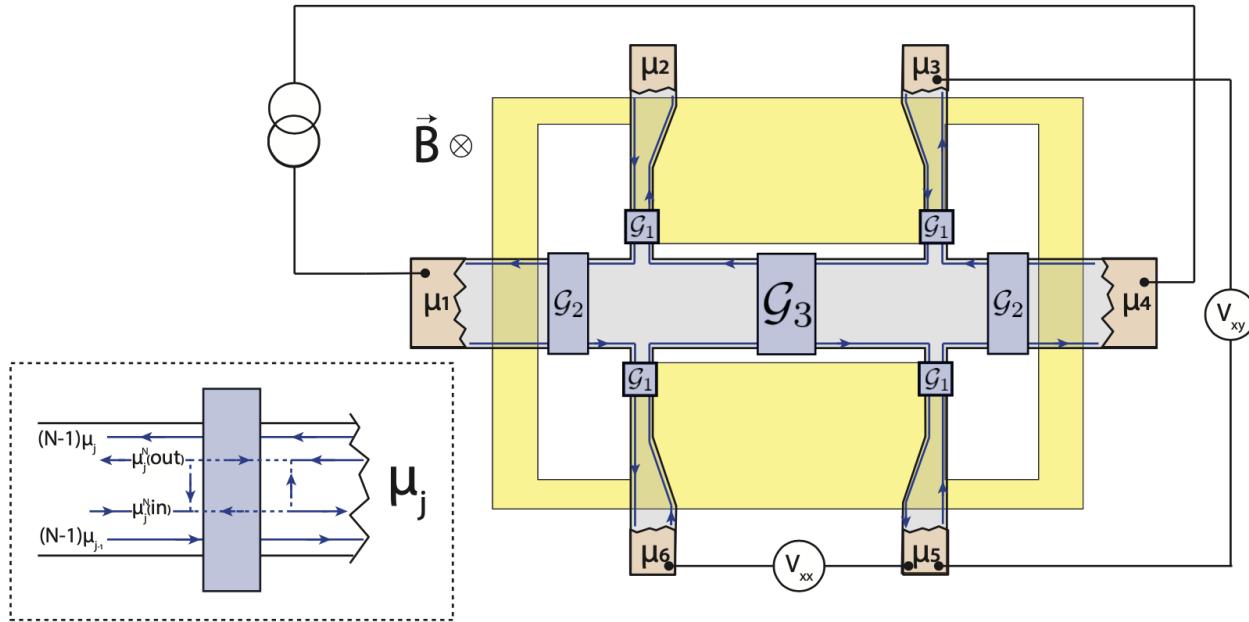
Experiments: J. Faist's group @ ETH Zürich



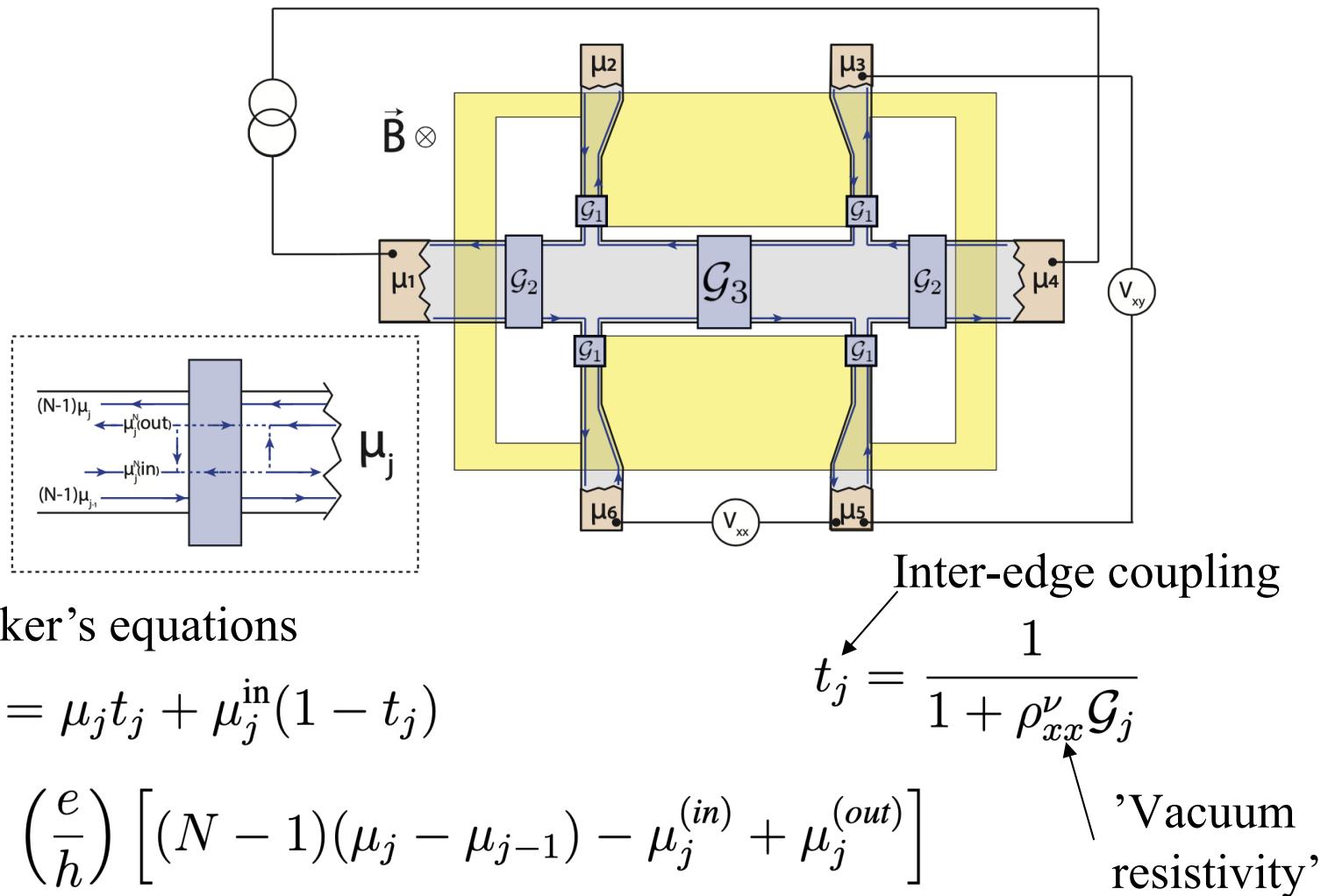
QH Plateaux at odd integer filling are destroyed....



Transport via the Büttiker formalism with inter-edge coupling



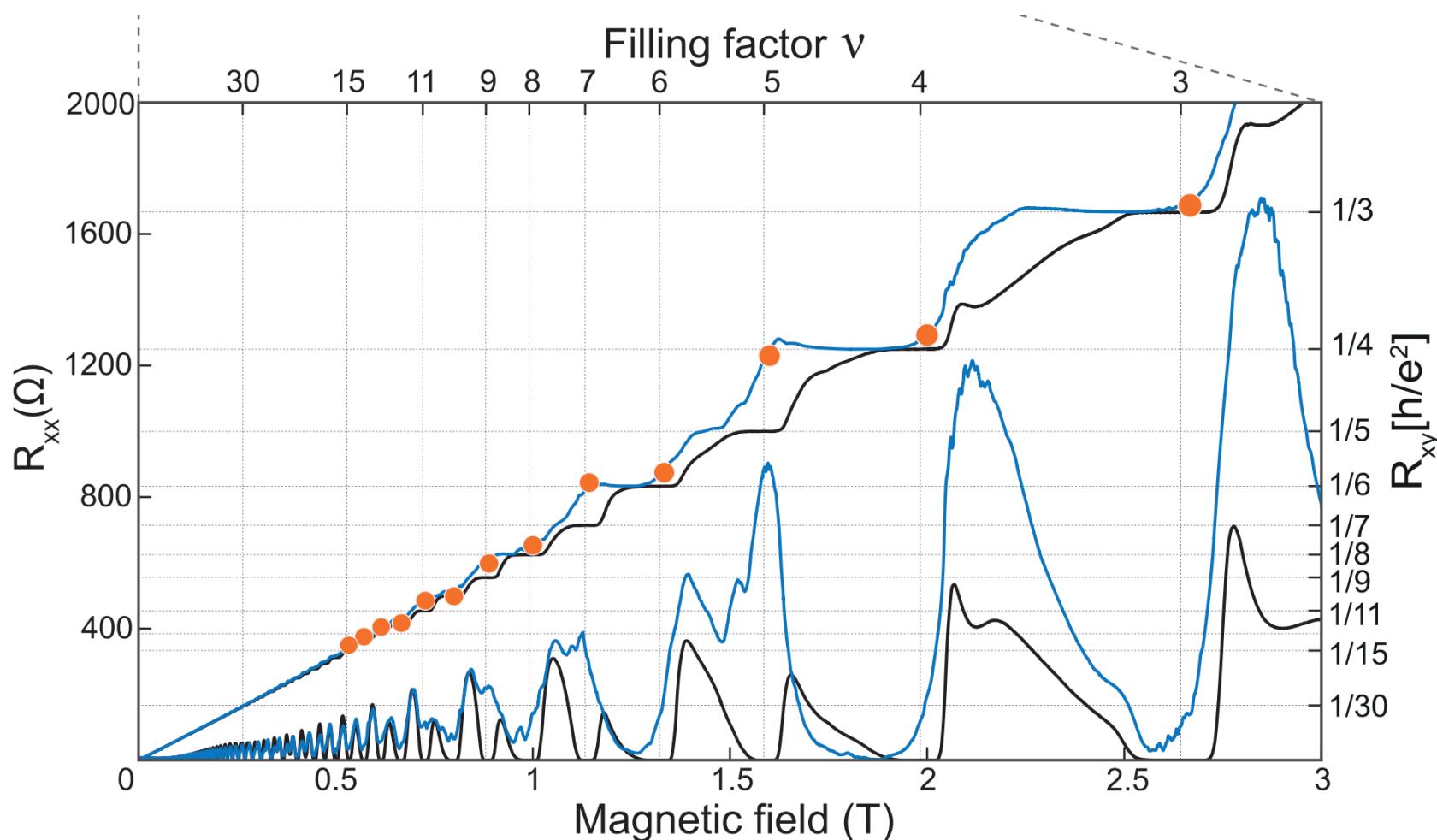
Multiprobe network model with inter-edge coupling



P. McEuen et al., PRL 64, 2062 (1990).

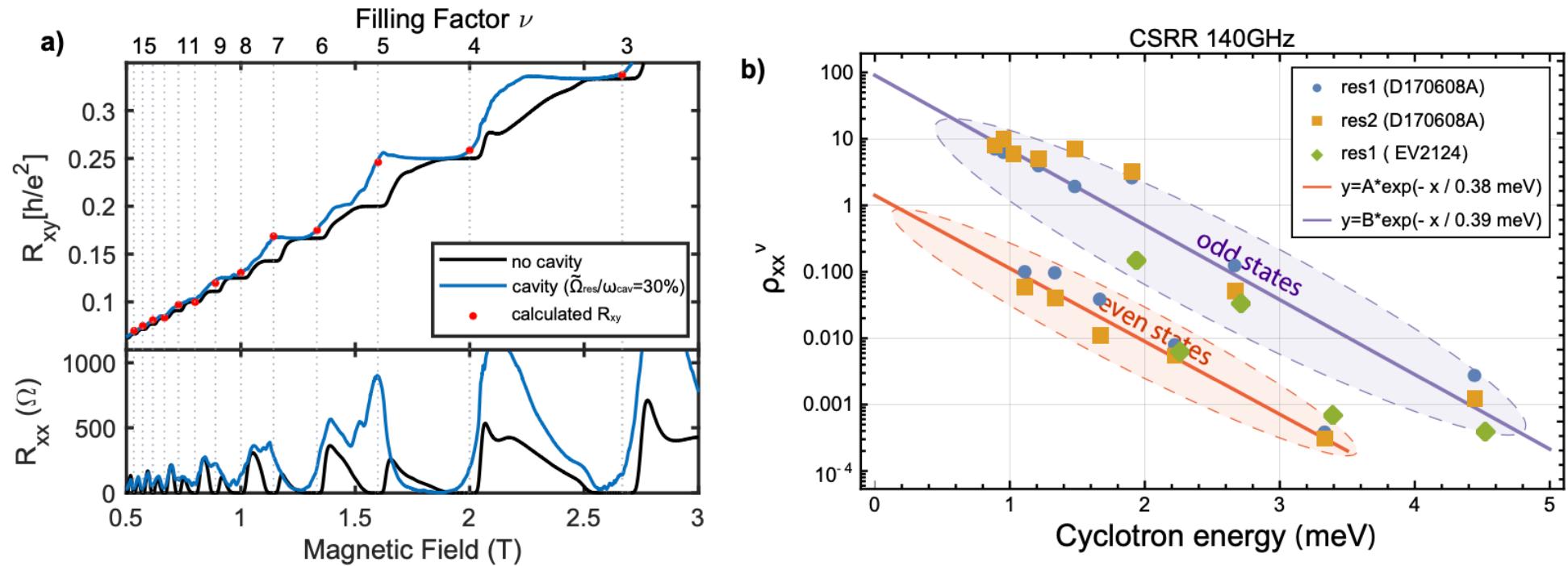
A. Szafer, A. D. Stone, P. McEuen, B. Alphenaar, *Granular Nanoelectronics* (Springer, 1991), pp. 195–222

Predictions of the model at integer filling factors



- 1) Inter-edge coupling fitted from longitudinal resistance
- 2) Transverse Hall resistance predicted without adjustable parameters

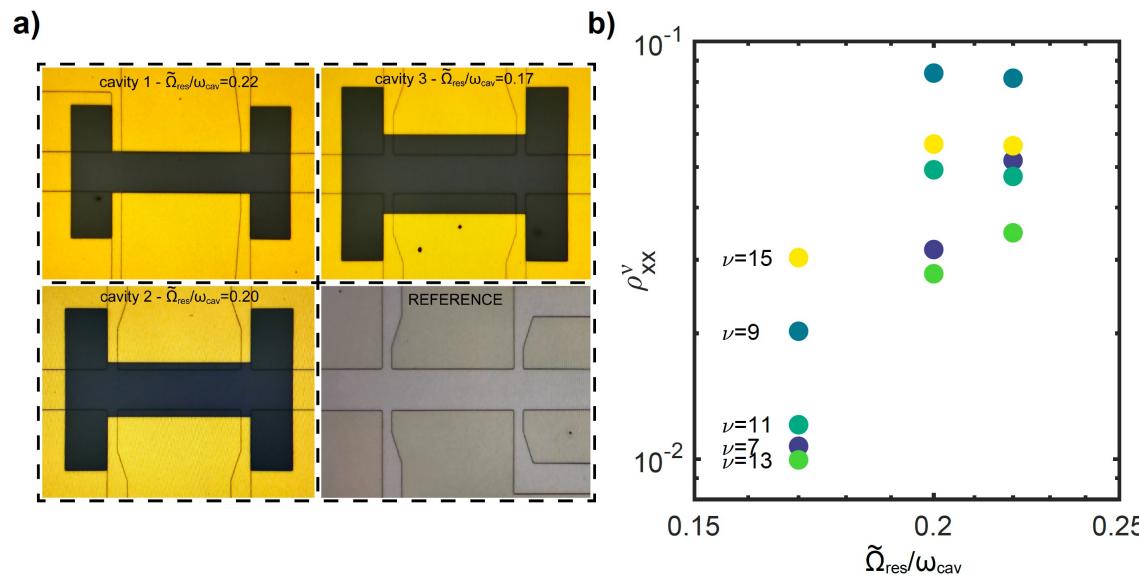
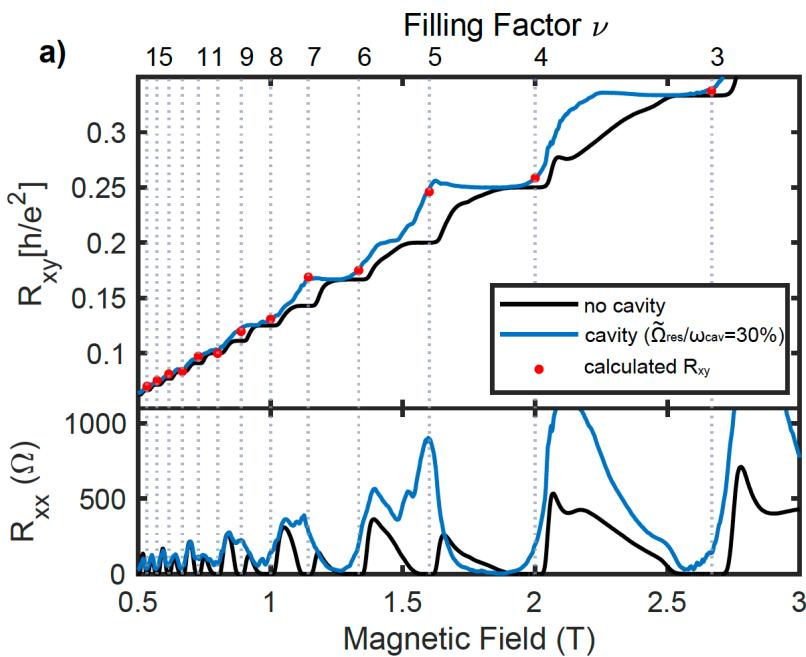
Application of the network model at integer filling factors



Knowing the longitudinal resistance, we can get the inter-edge coupling

With no adjustable parameters, we can then calculate the Hall resistance and find excellent agreement with experimental values

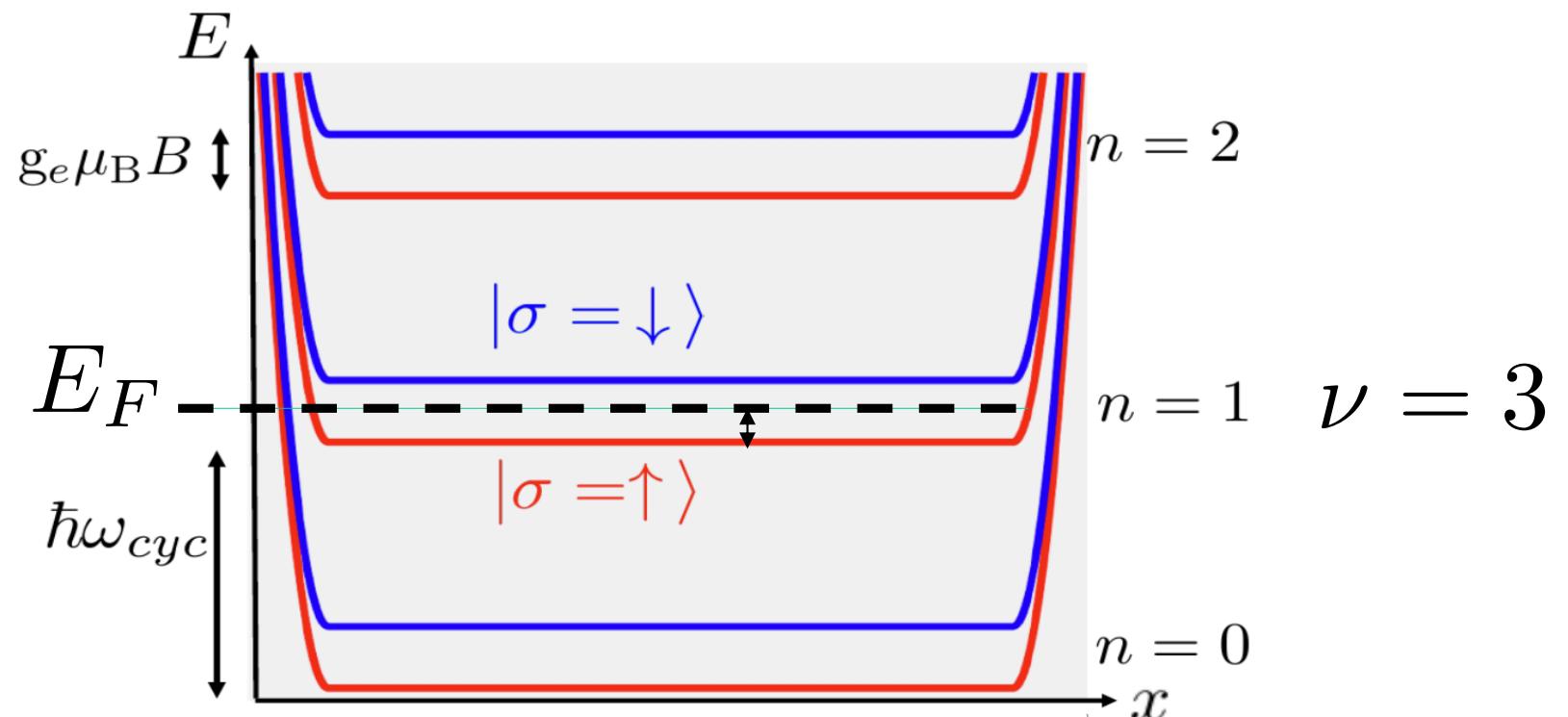
Effect increase with increasing vacuum Rabi frequency



Why odd/even strong asymmetry?

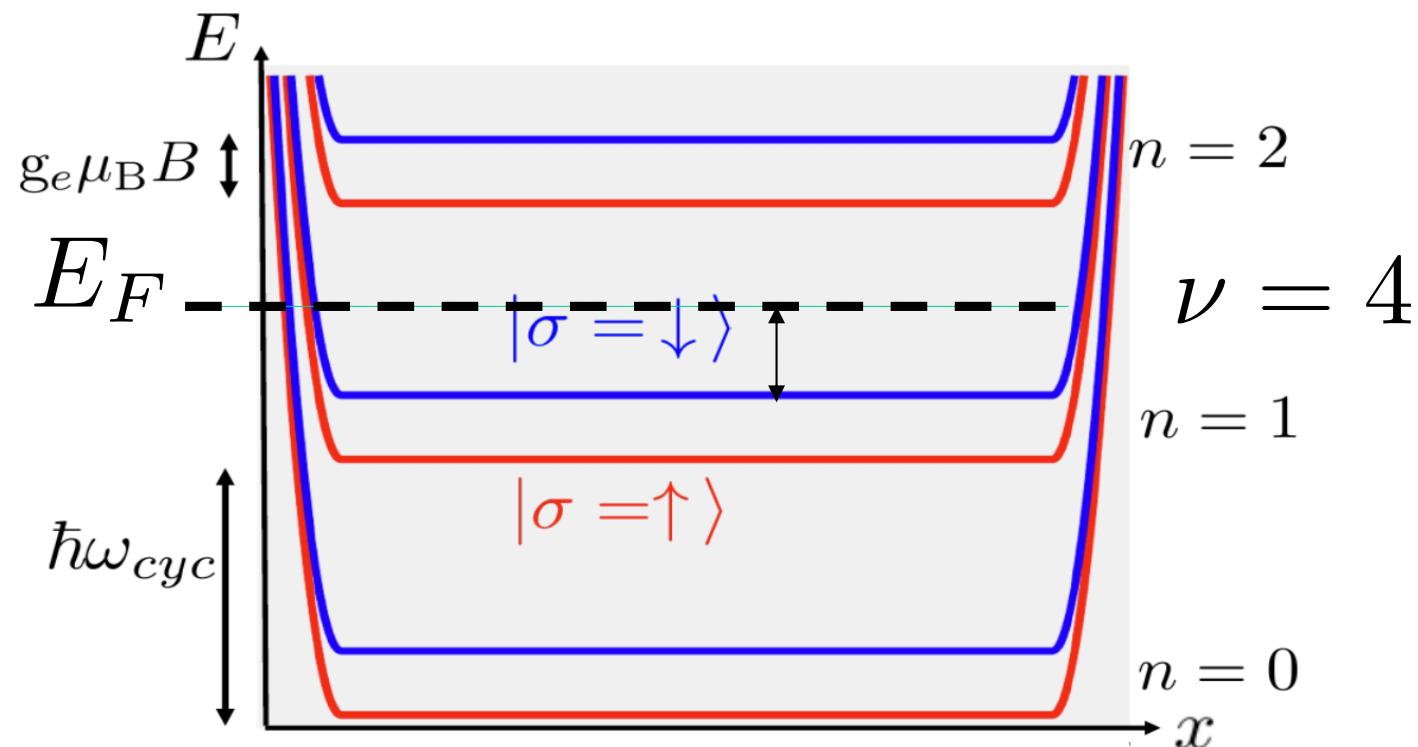
Cavity-mediated hopping is spin-independent but

- i) Cyclotron splitting much larger than Zeeman splitting
- ii) EDGE states at **ODD** integer filling factors are **CLOSER TO BULK** states



Why odd/even strong asymmetry?

EDGE states at EVEN integer filling factors
are energetically more distant from bulk states



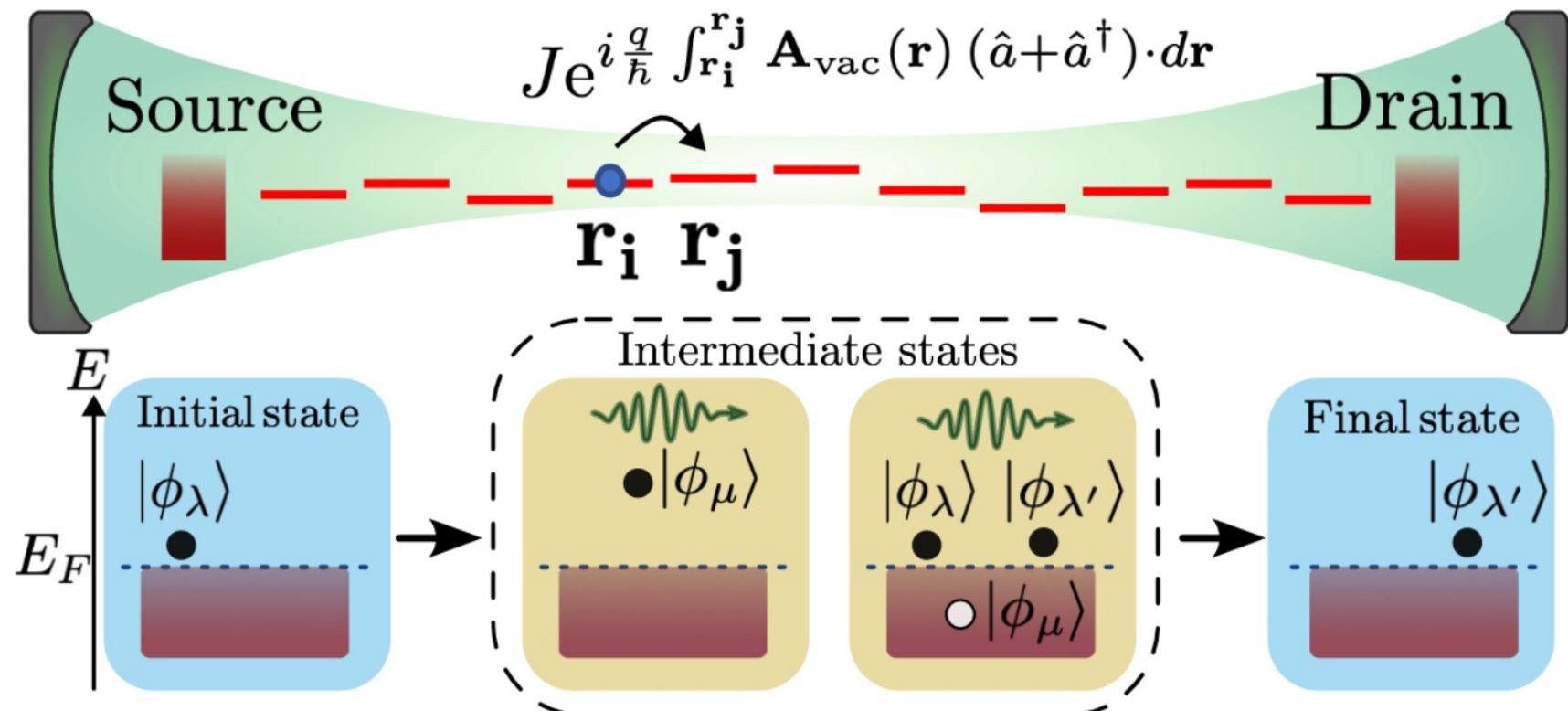
A general theoretical framework for coherent quantum electron transport controlled by cavity vacuum fields



G. Arwas and CC, arXiv:2206.13432

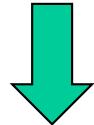
Geva Arwas

A microscopic quantum electron transport theory



Tight-binding model

$$\hat{\mathcal{H}} = \sum_{\mathbf{i}} E_{\mathbf{i}} \hat{d}_{\mathbf{i}}^\dagger \hat{d}_{\mathbf{i}} - \sum_{\langle \mathbf{i}, \mathbf{j} \rangle} J e^{i \frac{q}{\hbar} \int_{\mathbf{r}_i}^{\mathbf{r}_j} \hat{\mathbf{A}}(\mathbf{r}) \cdot d\mathbf{r}} \hat{d}_{\mathbf{i}}^\dagger \hat{d}_{\mathbf{j}} + \hbar \omega_{cav} \hat{a}^\dagger \hat{a}$$



$$g_{ij} = \frac{q}{\hbar} \int_{\mathbf{r}_i}^{\mathbf{r}_j} \mathbf{A}_{\text{vac}}(\mathbf{r}) \cdot d\mathbf{r}$$

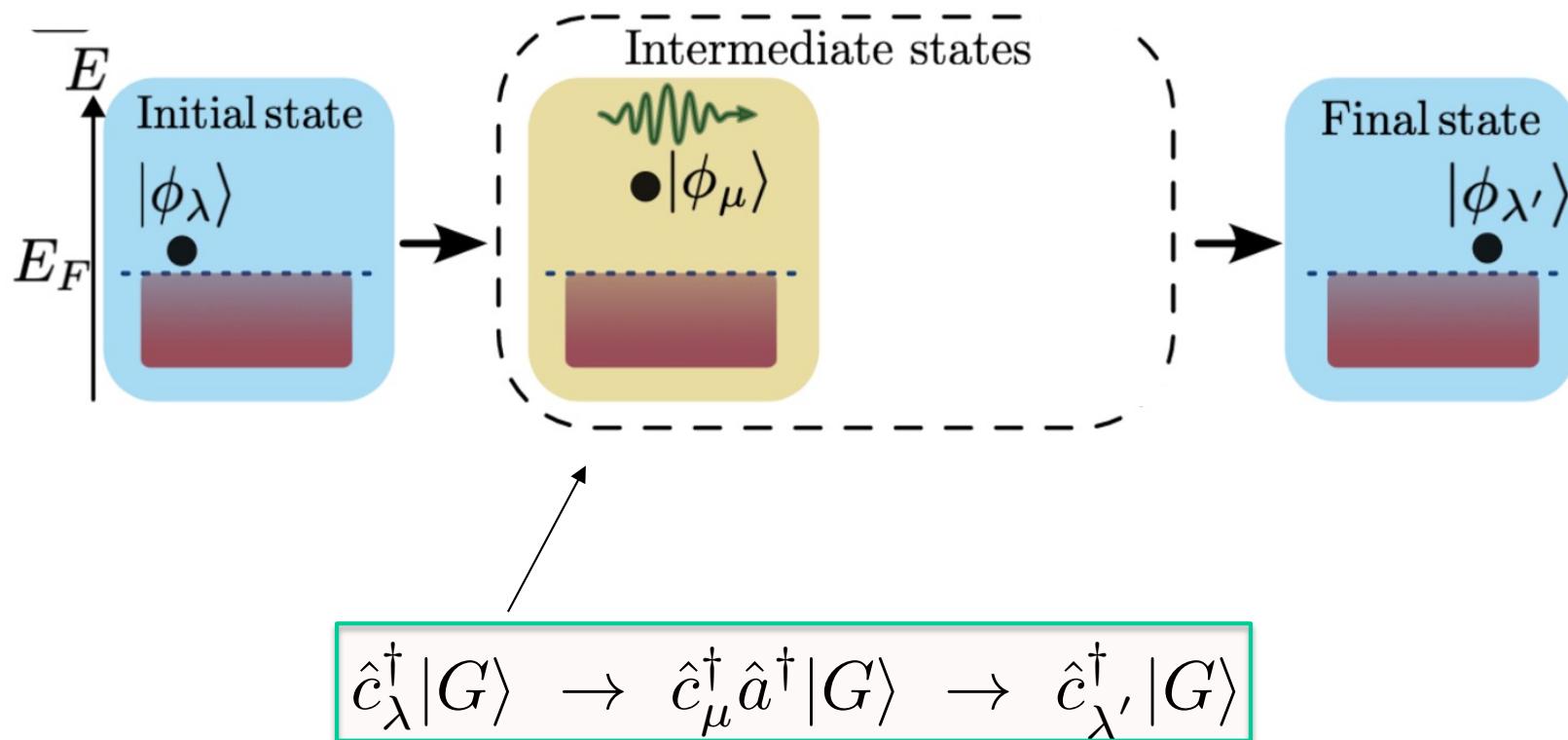
$$\hat{\mathcal{H}} = \hat{\mathcal{H}}_0 + \hbar \omega_{\text{cav}} \hat{a}^\dagger \hat{a} + \hat{V}$$

$$\hat{\mathcal{H}}_0 = \sum_{\mathbf{i}} E_{\mathbf{i}} \hat{d}_{\mathbf{i}}^\dagger \hat{d}_{\mathbf{i}} - J \sum_{\langle \mathbf{i}, \mathbf{j} \rangle} \hat{d}_{\mathbf{i}}^\dagger \hat{d}_{\mathbf{j}} = \sum_{\lambda} \epsilon_{\lambda} \hat{c}_{\lambda}^\dagger \hat{c}_{\lambda}$$

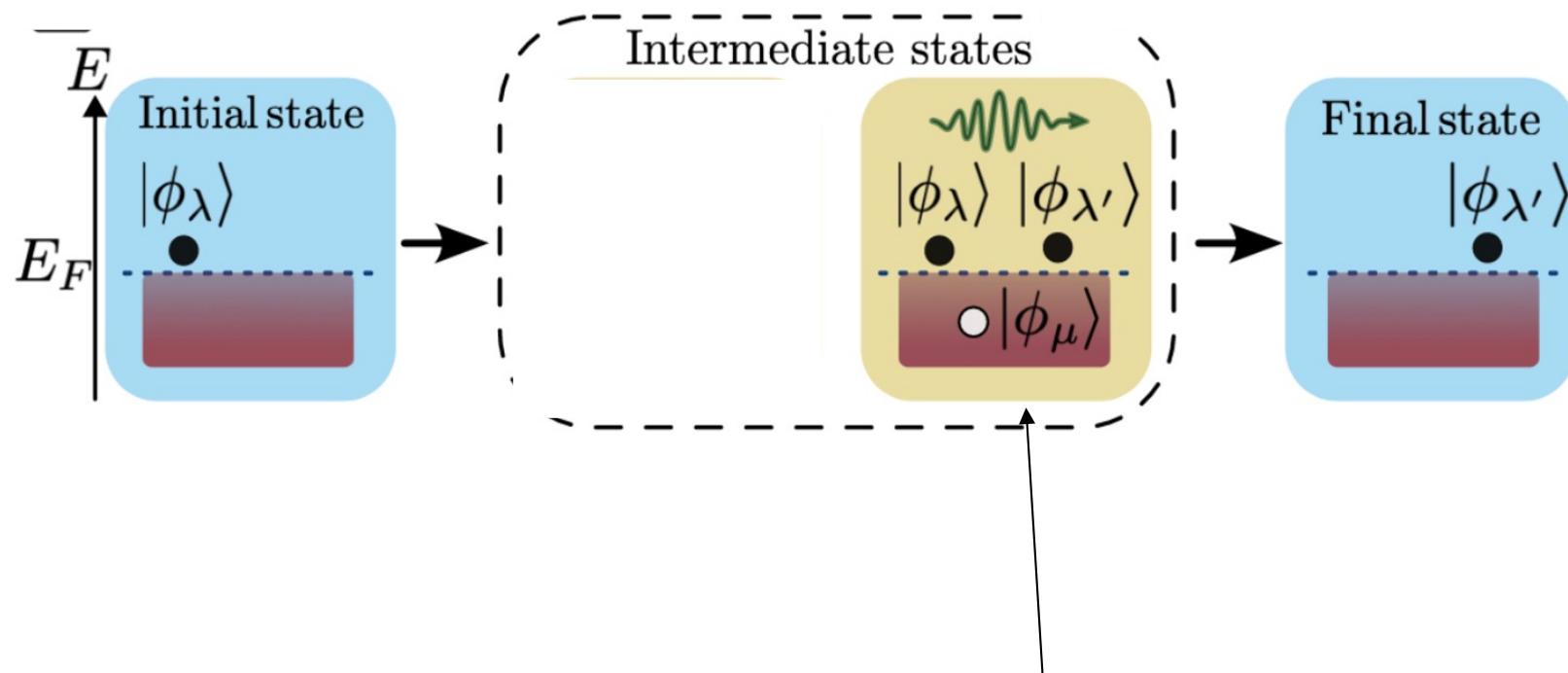
$$\hat{V} = -J \sum_{\lambda, \lambda'} \sum_{n=1}^{\infty} \frac{i^n}{n!} \tilde{g}_{\lambda, \lambda'}^{(n)} (\hat{a} + \hat{a}^\dagger)^n \hat{c}_{\lambda}^\dagger \hat{c}_{\lambda'}$$

$$\tilde{g}_{\lambda \lambda'}^{(n)} = \sum_{\langle \mathbf{i}, \mathbf{j} \rangle} g_{\mathbf{i}\mathbf{j}}^n \langle \phi_{\lambda} | \mathbf{i} \rangle \langle \mathbf{j} | \phi_{\lambda'} \rangle$$

Effective interaction mediated by intermediate states

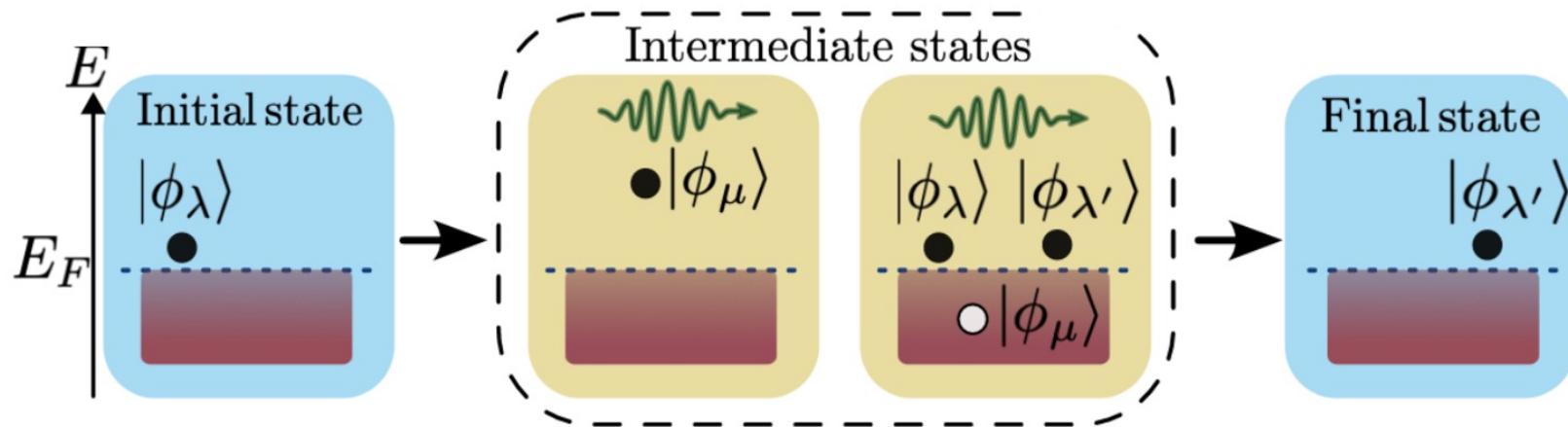


Effective interaction mediated by intermediate states



$$\hat{c}_\lambda^\dagger |G\rangle \rightarrow \hat{c}_\lambda^\dagger \hat{c}_{\lambda'}^\dagger \hat{c}_\mu \hat{a}^\dagger |G\rangle \rightarrow \hat{c}_{\lambda'}^\dagger |G\rangle$$

Effective interaction mediated by intermediate states



$$\tilde{\Gamma}_{\lambda,\lambda'} \simeq \sum_{\epsilon_\mu \geq E_F} \frac{J^2 \tilde{g}_{\lambda,\mu} \tilde{g}_{\mu,\lambda'}}{\epsilon_\mu - \epsilon_\lambda + \hbar\omega_{cav}} - \sum_{\epsilon_\mu < E_F} \frac{J^2 \tilde{g}_{\lambda,\mu} \tilde{g}_{\mu,\lambda'}}{\epsilon_{\lambda'} - \epsilon_\mu + \hbar\omega_{cav}}$$

$$\hat{\mathcal{H}}_{\text{eff}} = \sum_{\lambda} \epsilon_{\lambda} |\phi_{\lambda}\rangle\langle\phi_{\lambda}| + \sum_{\lambda,\lambda'} \frac{\tilde{\Gamma}_{\lambda,\lambda'} + \tilde{\Gamma}_{\lambda',\lambda}^*}{2} |\phi_{\lambda}\rangle\langle\phi_{\lambda'}|.$$

Quantum conductance in terms of transmission coefficients

$$G(E_F) = \frac{e^2}{h} \sum_{j \in \mathcal{S}, j' \in \mathcal{D}} T_{j,j'}(E_F)$$

Transmission matrix between contacts calculated with effective Hamiltonian

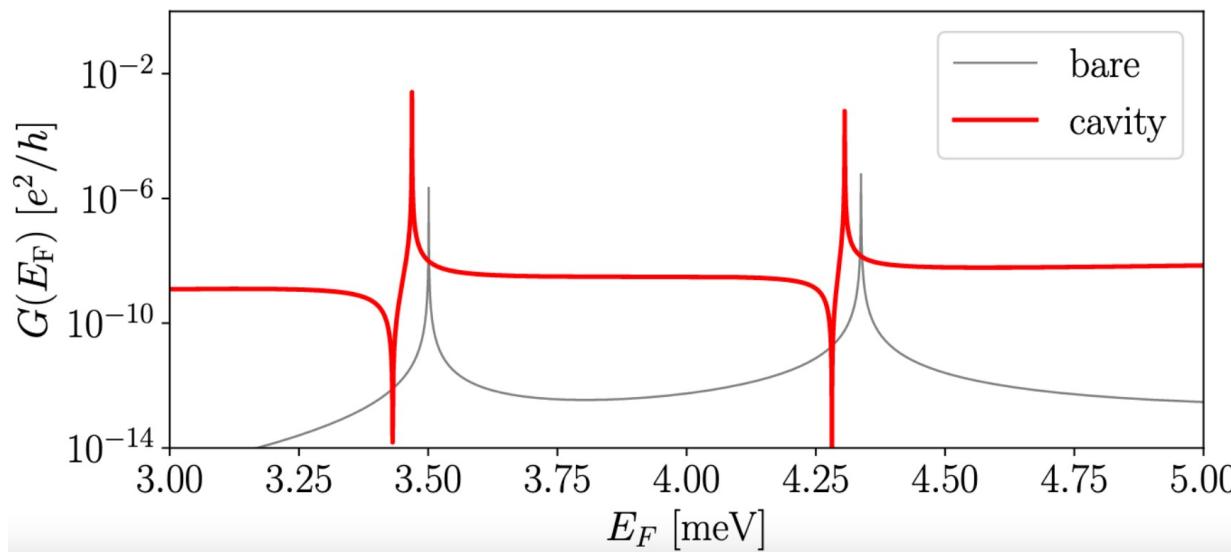
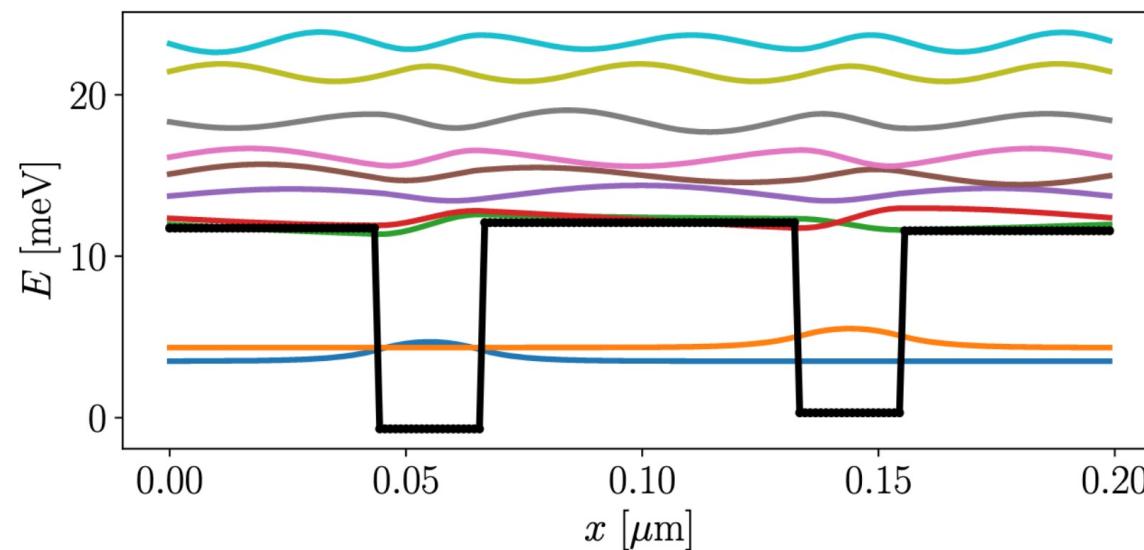
See e.g.

ELECTRONIC TRANSPORT IN MESOSCOPIC SYSTEMS

SUPRIYO DATTA
Professor of Electrical Engineering
Purdue University

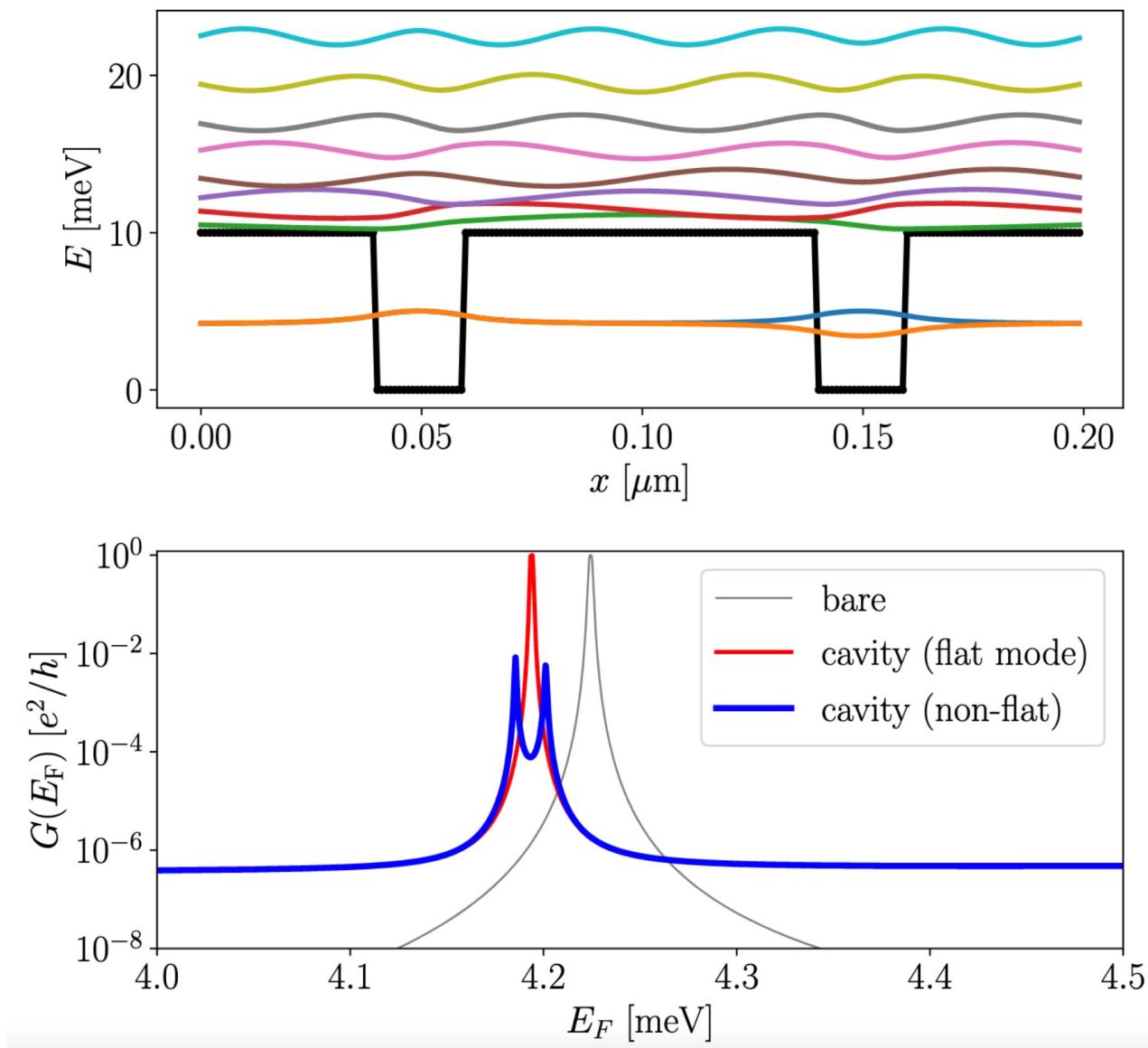


Example of 1D system: asymmetric double quantum well



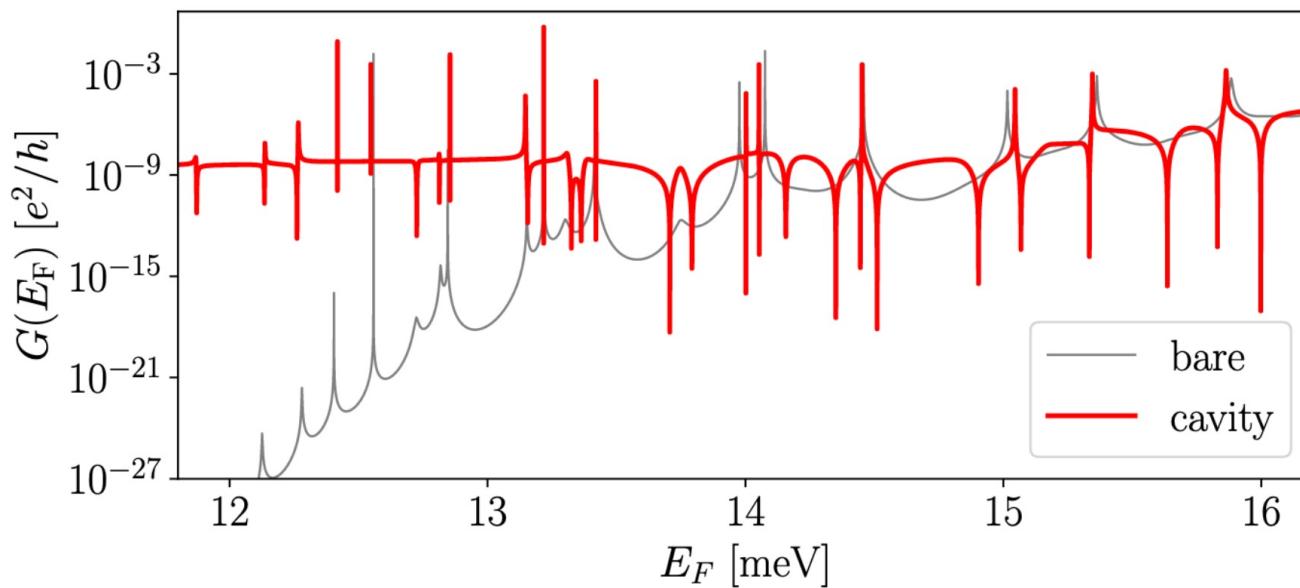
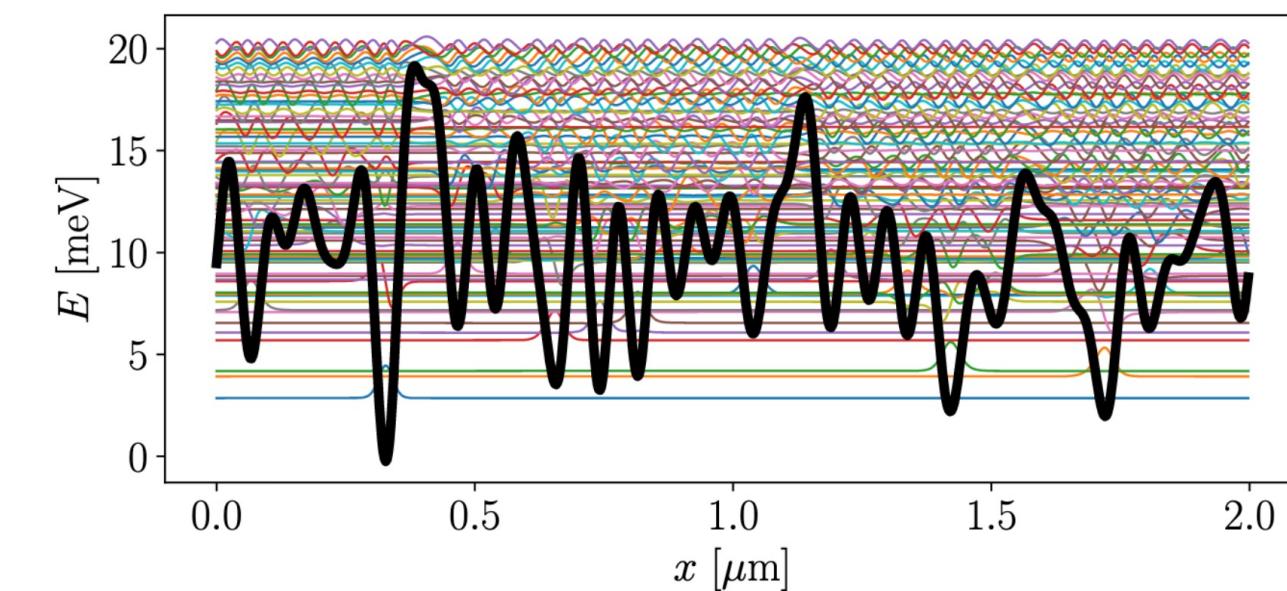
Conductance enhancement

Example of 1D system: symmetric double well

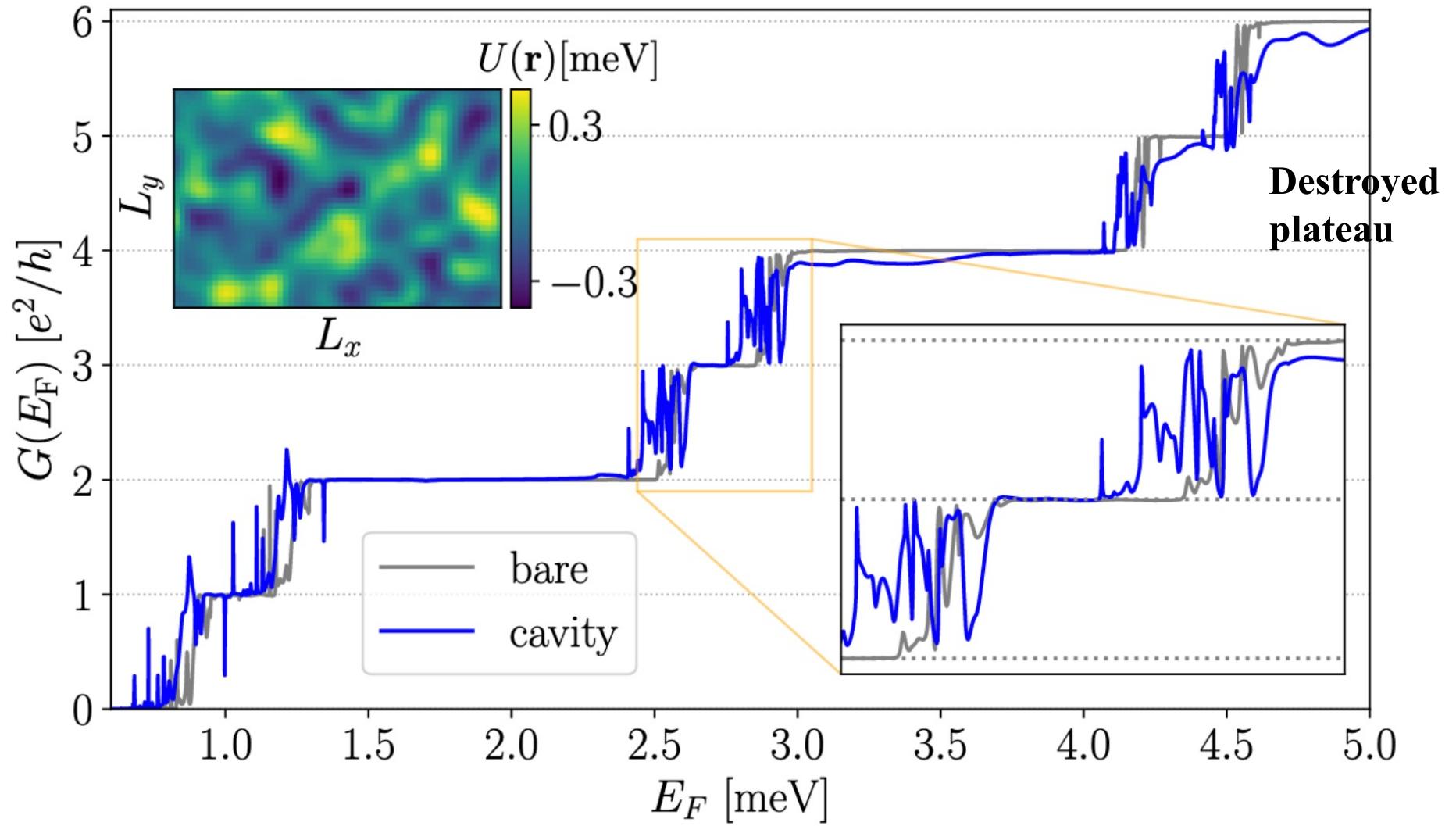


Conductance suppression

Example of 1D system: smooth disordered potential



Example of 2D system: disordered quantum Hall system



Take-home message

Electromagnetic vacuum fluctuations cannot be generally overlooked in mesoscopic systems

Cavity-mediated long-range interactions alter quantum transport

Topological conductors not immune to cavity-mediated interactions

Challenge: we might try this physics as a tool to control