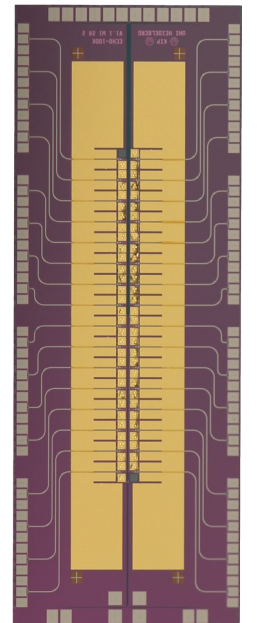
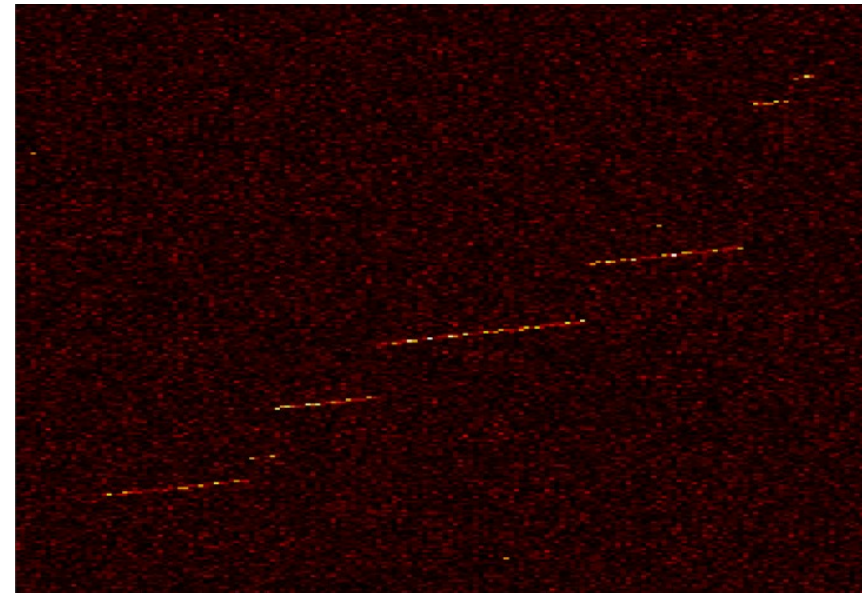
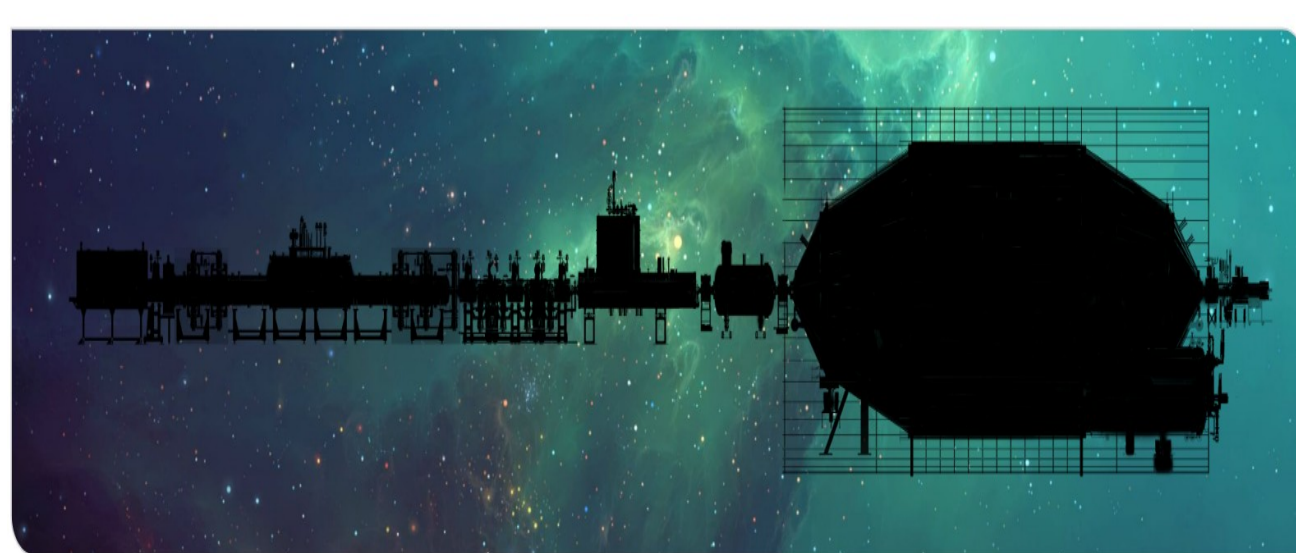


Neutrino mass determination – Part I

International School on Astroparticle Physics (ISAPP 2023) – Varenna, Italy
Alexey Lokhov



Outline

What do we know
so far about
neutrino masses?

What are the three
approaches to
neutrino mass?

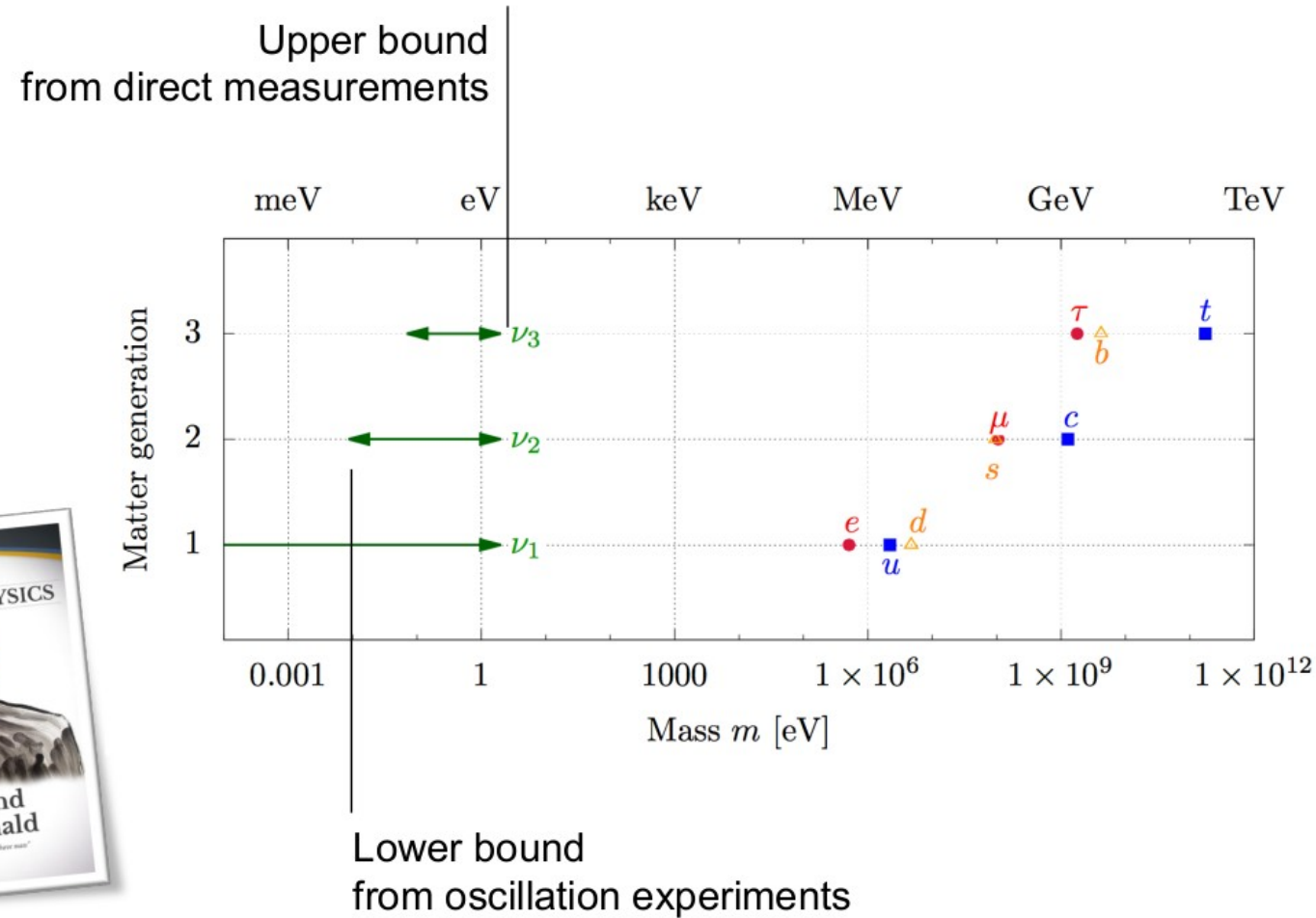
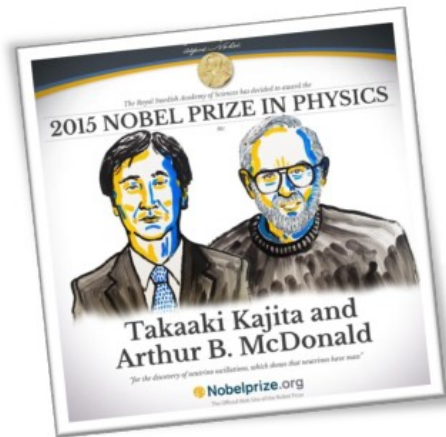
How to measure
the mass without
model
dependencies?

What other physics
can we probe in
the direct mass
measurements?

Status of direct
neutrino mass
measurements

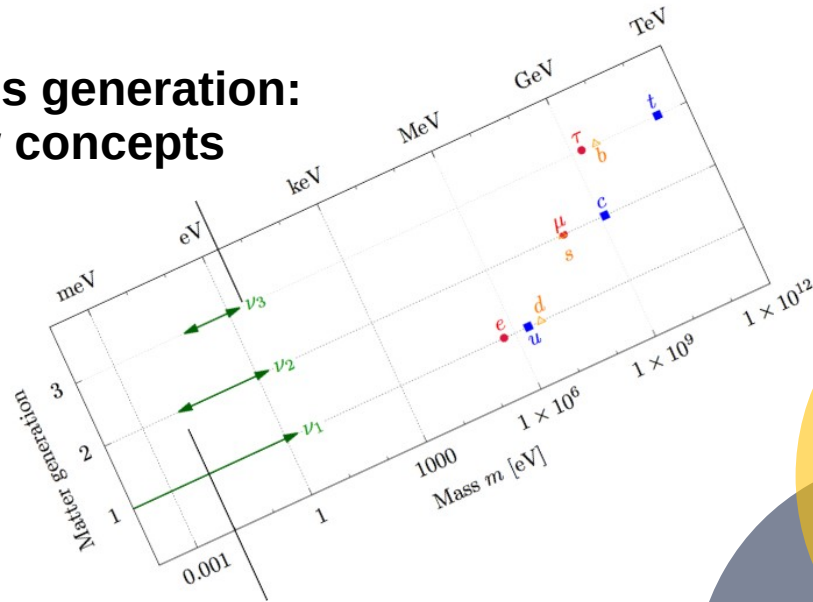
Next generation of
experiments

Neutrino mass

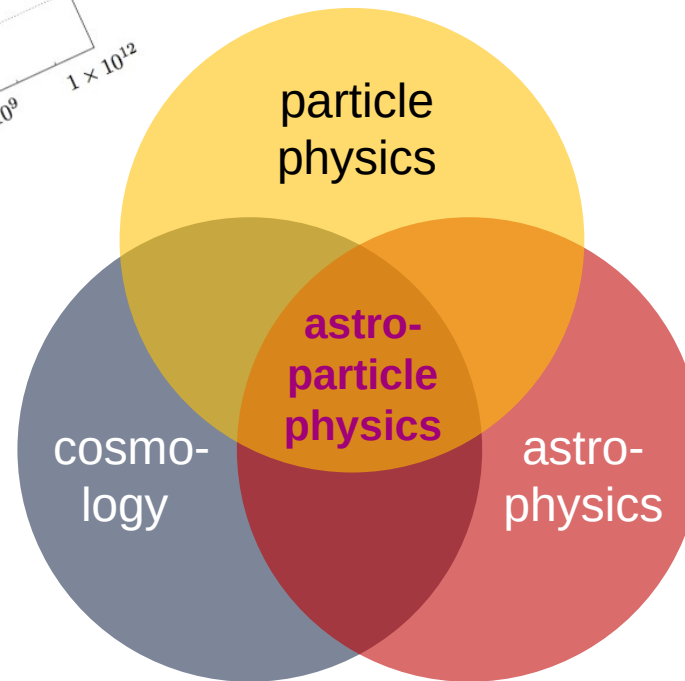
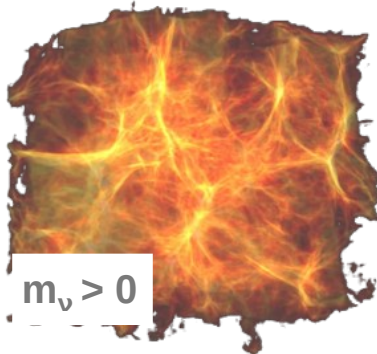
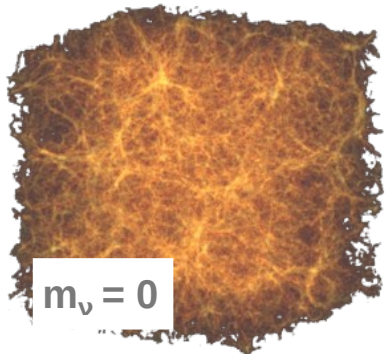


Role of massive neutrinos

Mass generation:
new concepts



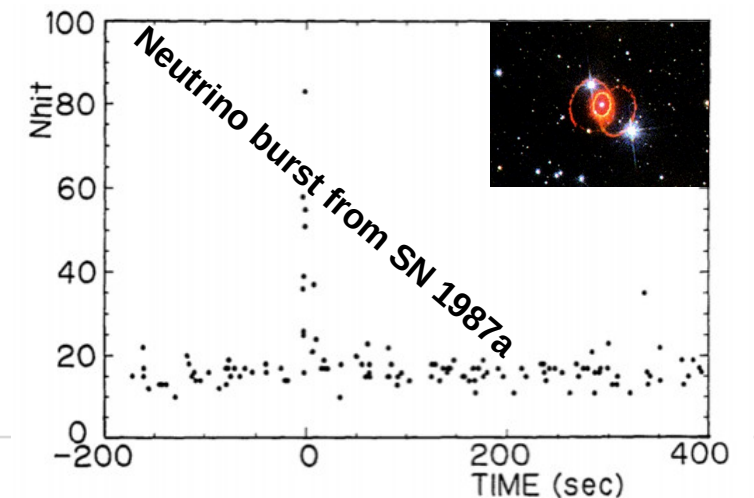
Massive neutrinos as
“cosmic architects”



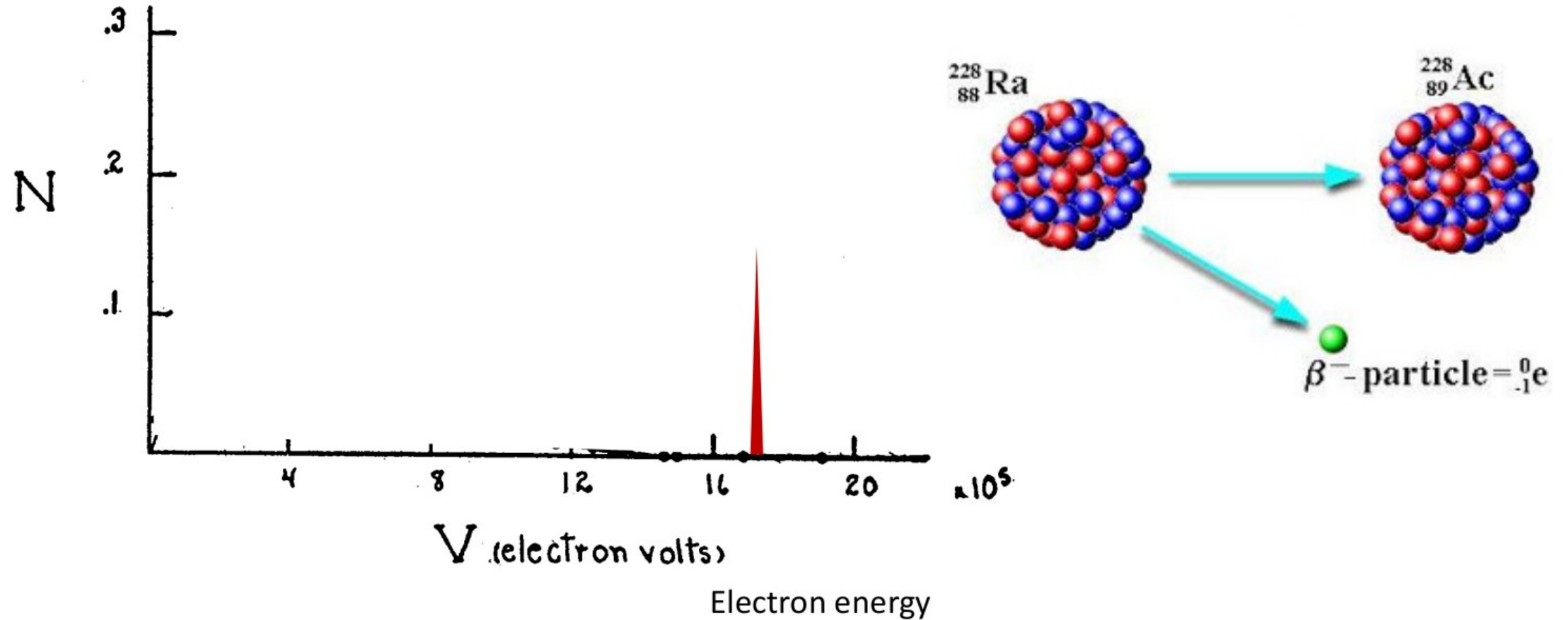
Mass measurement:
new concepts



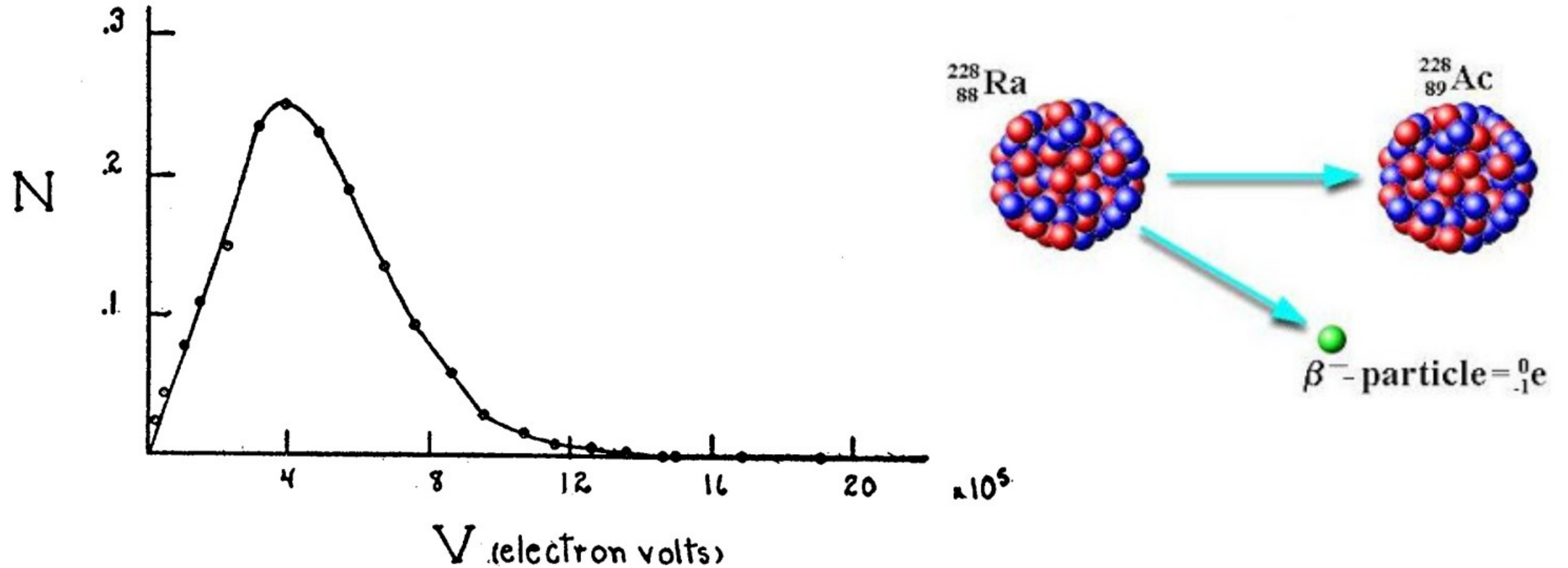
Understanding
astrophysical processes



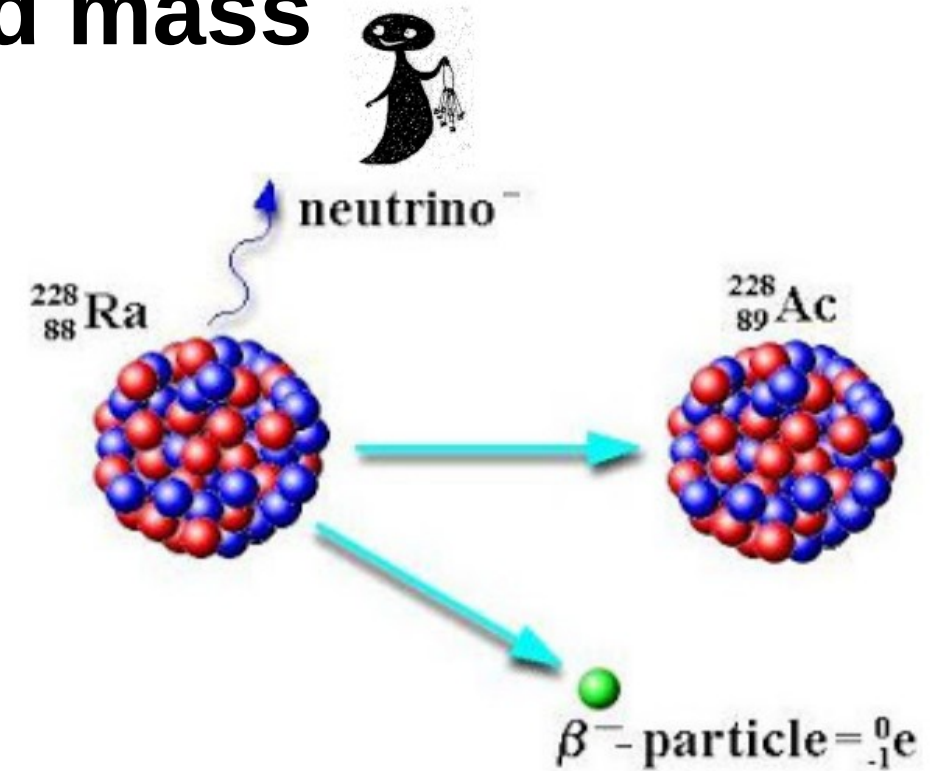
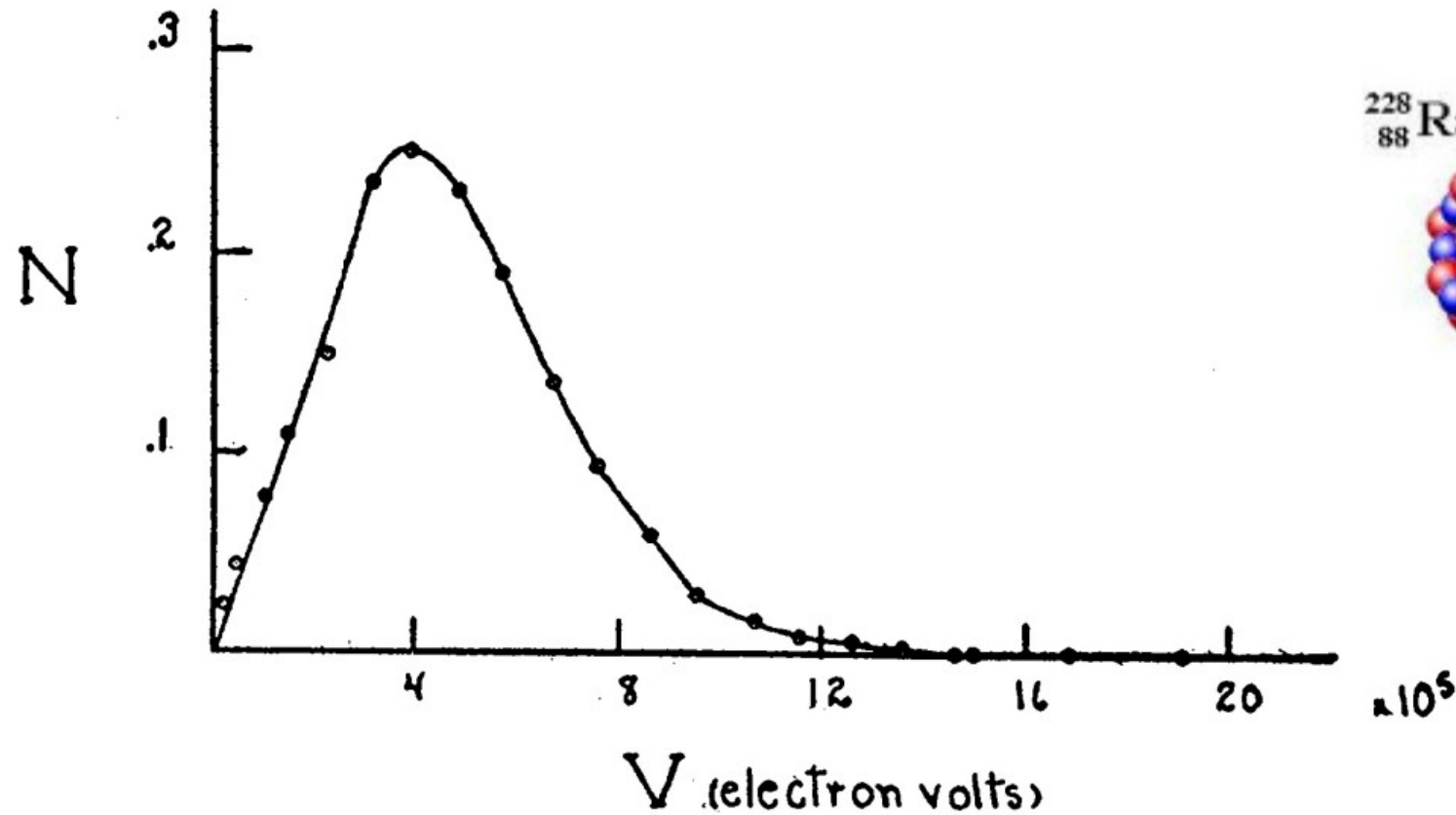
1930: Neutrino postulation and mass



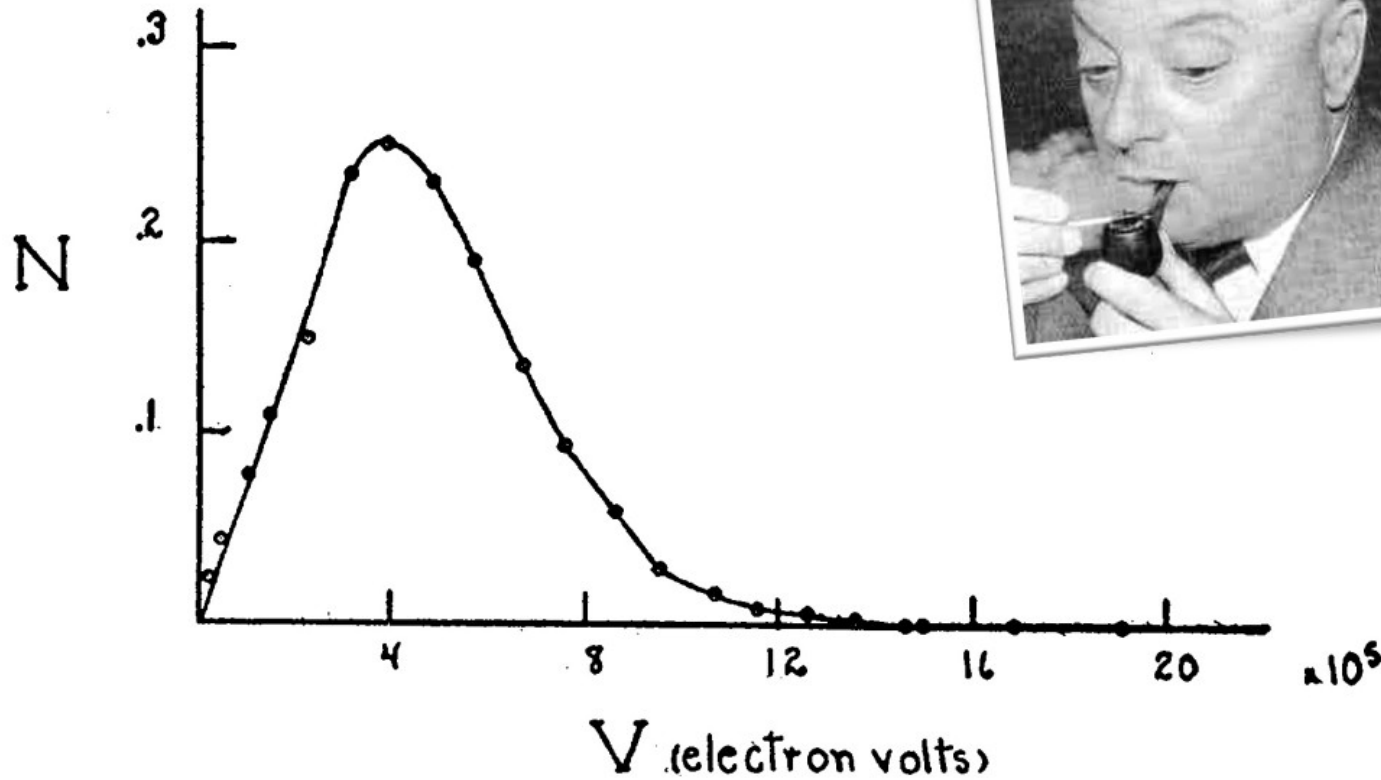
1930: Neutrino postulation and mass



1930: Neutrino postulation and mass



1930: Neutrino postulation and mass



Original - Photocopy of PLC 0393
Abschrift/15.12.56 PM

Offener Brief an die Gruppe der Radioaktiven bei der
Gauvereins-Tagung zu Tübingen.

Abschrift

Physikalisches Institut
der Eidg. Technischen Hochschule
Zürich

Zürich, 4. Dez. 1930
Gloriastrasse

Liebe Radioaktive Damen und Herren,

Wie der Ueberbringer dieser Zeilen, den ich huldvollst
ansuhören bitte, Ihnen des näheren auseinandersetzen wird, bin ich
angesichts der "falschen" Statistik der N- und Li-6 Kerne, sowie
des kontinuierlichen beta-Spektrums auf einen verzweifelten Ausweg
verfallen um den "Wechselsatz" (1) der Statistik und den Energiesatz
zu retten. Nämlich die Möglichkeit, es könnten elektrisch neutrale
Teilchen, die ich Neutronen nennen will, in den Kernen existieren,
welche den Spin 1/2 haben und das Ausschliessungsprinzip befolgen und
sich von Lichtquanten ausserdem noch dadurch unterscheiden, dass sie
nicht mit Lichtgeschwindigkeit laufen. Die Masse der Neutronen
müsste von derselben Grössenordnung wie die Elektronenmasse sein und
jedenfalls nicht grösser als 0,01 Protonenmasse. Das kontinuierliche
beta-Spektrum wäre dann verständlich unter der Annahme, dass beim
beta-Zerfall mit dem Elektron jeweils noch ein Neutron emittiert
wird, derart, dass die Summe der Energien von Neutron und Elektron
konstant ist.

$$m_\nu < 0.01 m_p \sim 10 \text{ MeV}$$

Neutrino in the Standard Model

Standard Model of Elementary Particles

| three generations of matter (elementary fermions) | | | | | | three generations of antimatter (elementary antifermions) | | | | | | interactions / force carriers (elementary bosons) | |
|--|--|--|--|--|--|--|--|----|--|-----|--|--|---|
| I | | II | | III | | I | | II | | III | | | |
| mass | $\approx 2.2 \text{ MeV}/c^2$ | $\approx 1.28 \text{ GeV}/c^2$ | $\approx 173.1 \text{ GeV}/c^2$ | $\approx 2.2 \text{ MeV}/c^2$ | $\approx 1.28 \text{ GeV}/c^2$ | $\approx 173.1 \text{ GeV}/c^2$ | | | | | | 0 | $\approx 124.97 \text{ GeV}/c^2$ |
| charge | $\frac{2}{3}$ | $\frac{2}{3}$ | $\frac{2}{3}$ | $-\frac{2}{3}$ | $-\frac{2}{3}$ | $-\frac{2}{3}$ | | | | | | 0 | 0 |
| spin | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | | | | | | 1 | 0 |
| | u up | c charm | t top | \bar{u} antiup | \bar{c} anticharm | \bar{t} antitop | | | | | | g gluon | H higgs |
| | d down | s strange | b bottom | \bar{d} antidown | \bar{s} antistrange | \bar{b} antibottom | | | | | | γ photon | |
| | e electron | μ muon | τ tau | e^+ positron | $\bar{\mu}$ antimuon | $\bar{\tau}$ antitau | | | | | | Z Z ⁰ boson | |
| | ν_e electron neutrino | ν_μ muon neutrino | ν_τ tau neutrino | $\bar{\nu}_e$ electron antineutrino | $\bar{\nu}_\mu$ muon antineutrino | $\bar{\nu}_\tau$ tau antineutrino | | | | | | W^+ W ⁺ boson | W^- W ⁻ boson |

QUARKS

LEPTONS

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

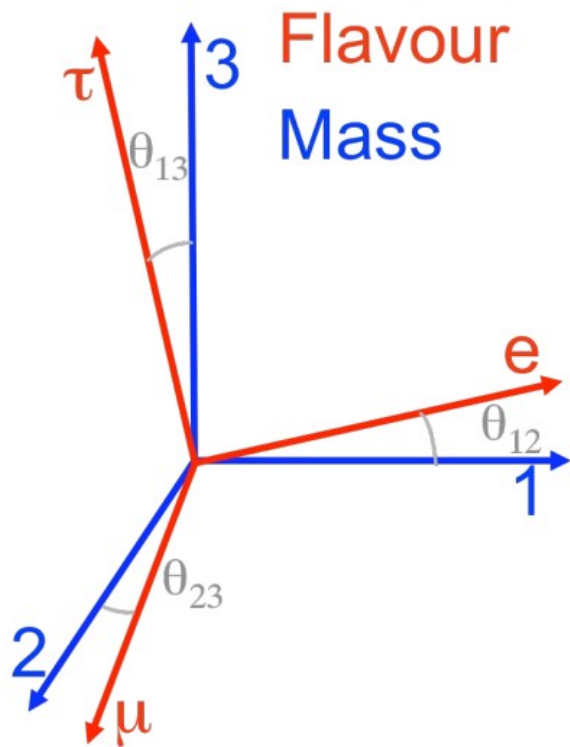
QUARKS

LEPTONS

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

Neutrino mixing, masses and oscillations



PMNS matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

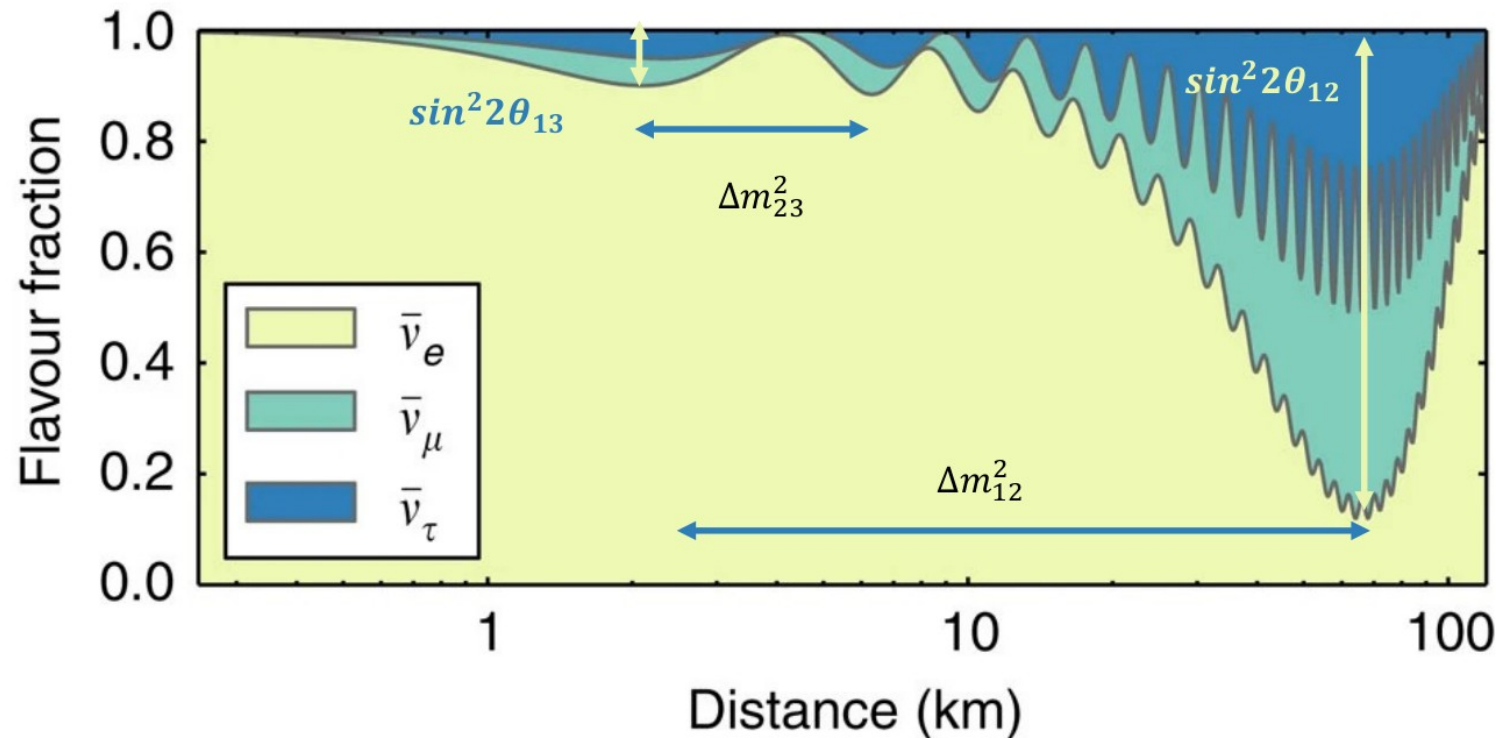
→ Eligio Lisi
Marco Pallavicini



Neutrino oscillations

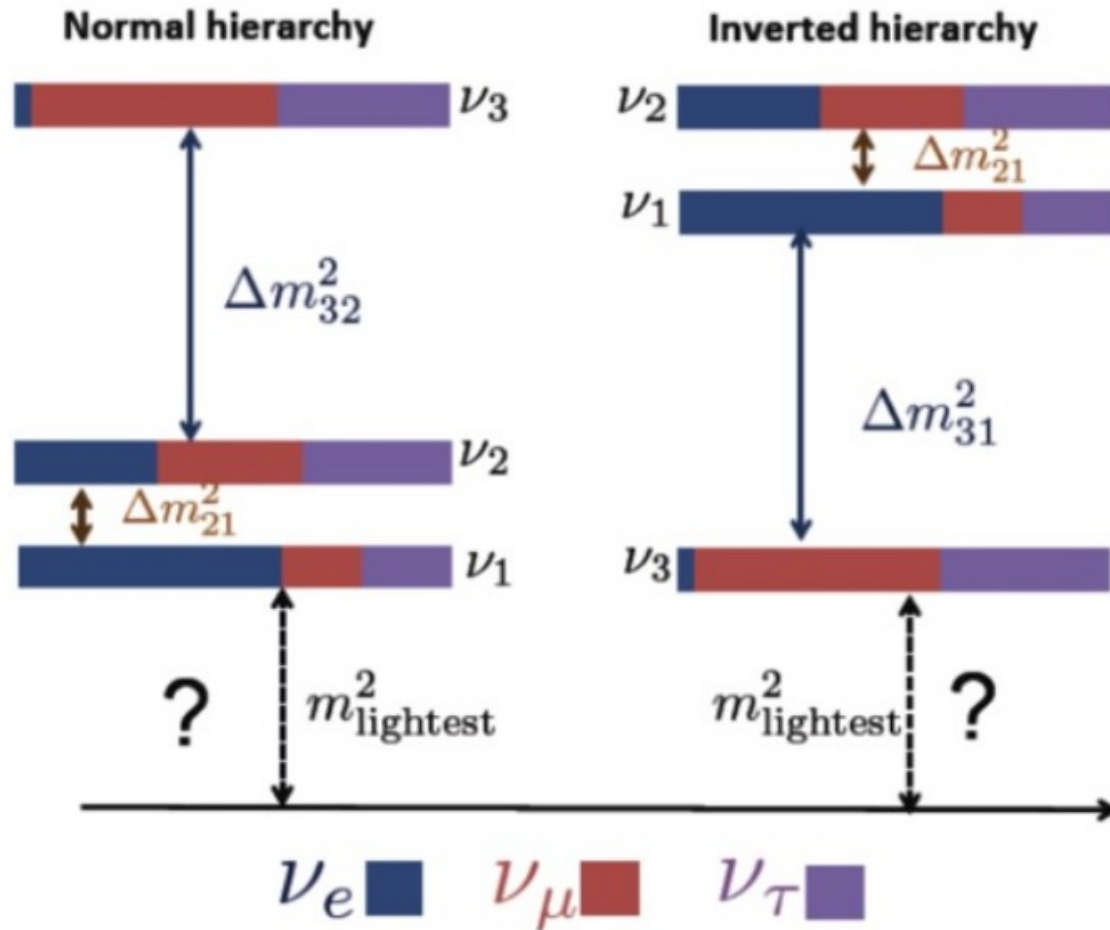
For two flavors:

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\theta \cdot \sin^2 \left(\Delta m^2 \cdot \frac{L}{E_\nu} \right)$$



- 3 mixing angles: θ_{12} , θ_{23} , θ_{13}
- 1 Dirac phase: δ
 - possibly 2 Majorana phases $\alpha_{1,2}$
- 2 independent “splittings”
 Δm^2 and lightest mass m_{lightest}

What have we learned from oscillation data?



- At least two neutrinos have mass
- $\Delta m_{21}^2 = 8 \cdot 10^{-5} \text{ eV}^2$, $\Delta m_{32}^2 = 2.5 \cdot 10^{-3} \text{ eV}^2$
- ν_1 is lighter than ν_2 (matter effects)
- Which neutrino is the lightest?
- What is the mass of the lightest neutrino?

Outline

What do we know
so far about
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Neutrinos are
massive

The squared mass
differences are
known

The absolute scale
is unknown

What are the three
approaches to
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How to measure
the mass without
model
dependencies?

What other physics
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the direct mass
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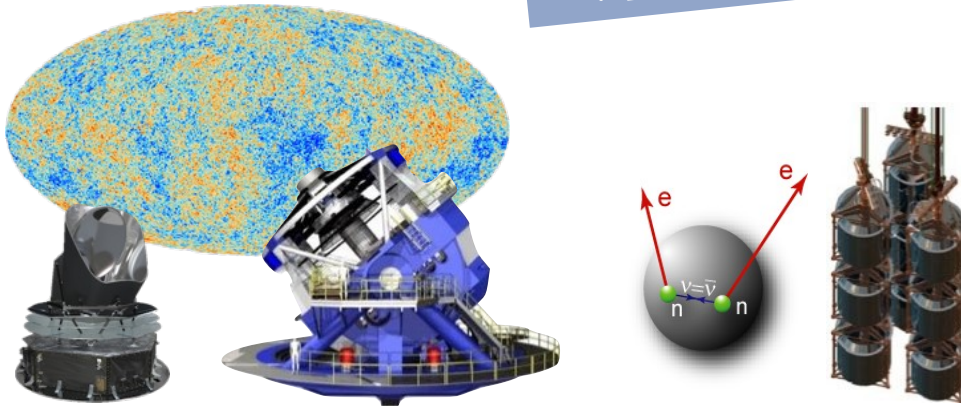
How can we measure the neutrino masses?

Indirect (model-dependent) probes:

- Observational cosmology
- Search for $0\nu\beta\beta$

→ Matteo Viel
Enzo Branchini
Douglas Scott
Nicola Bartolo

→ Ezio Previtali



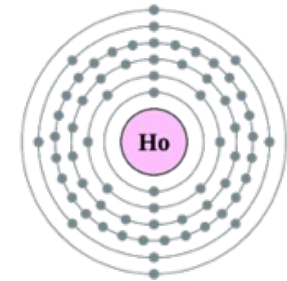
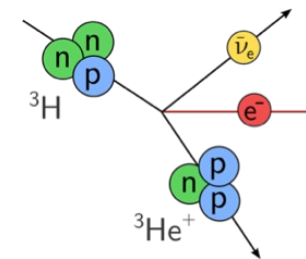
Direct probes:

- Supernova ν time-of-flight
- Kinematics of weak decays (^3H β -decay, ^{163}Ho electron capture)

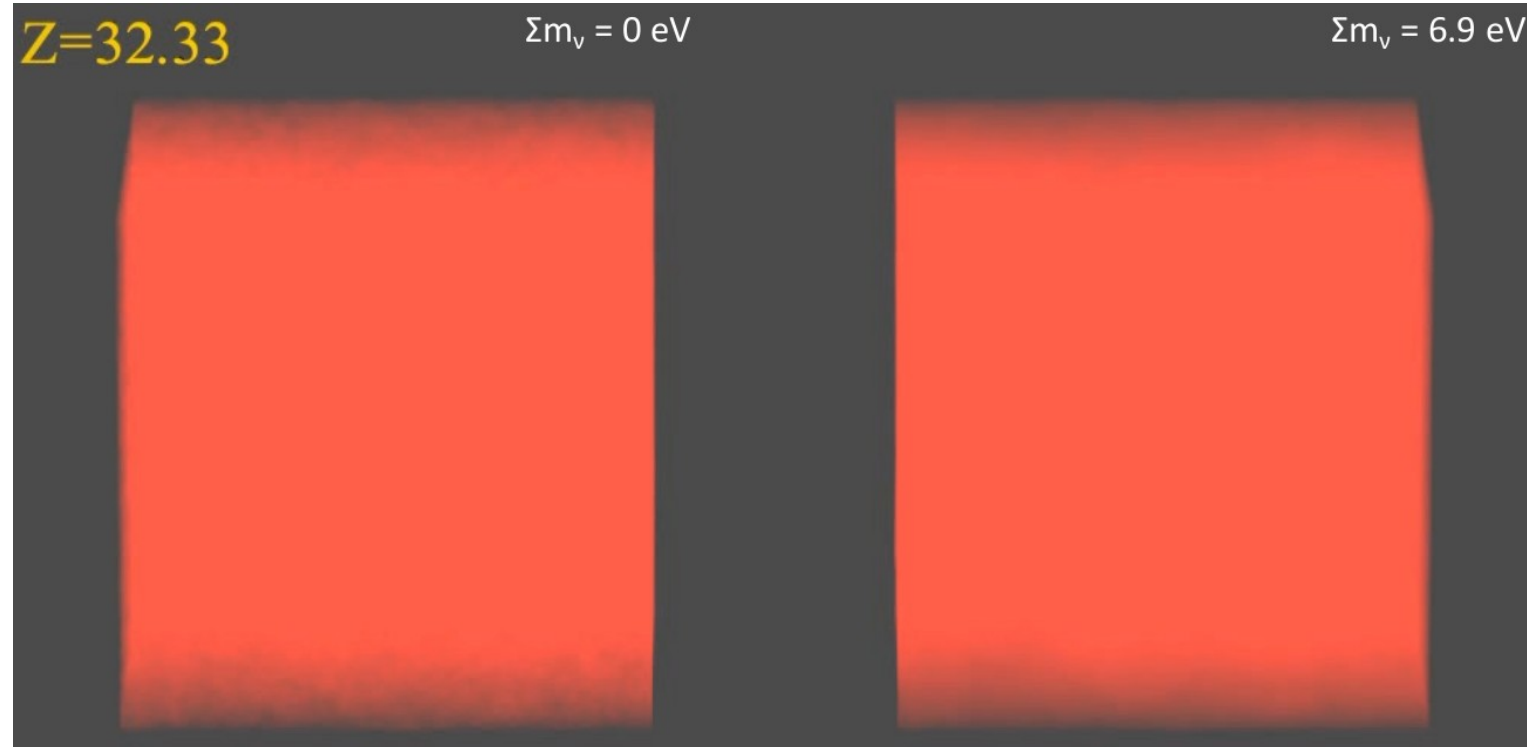
→ Aldo Ianni



→ this lecture

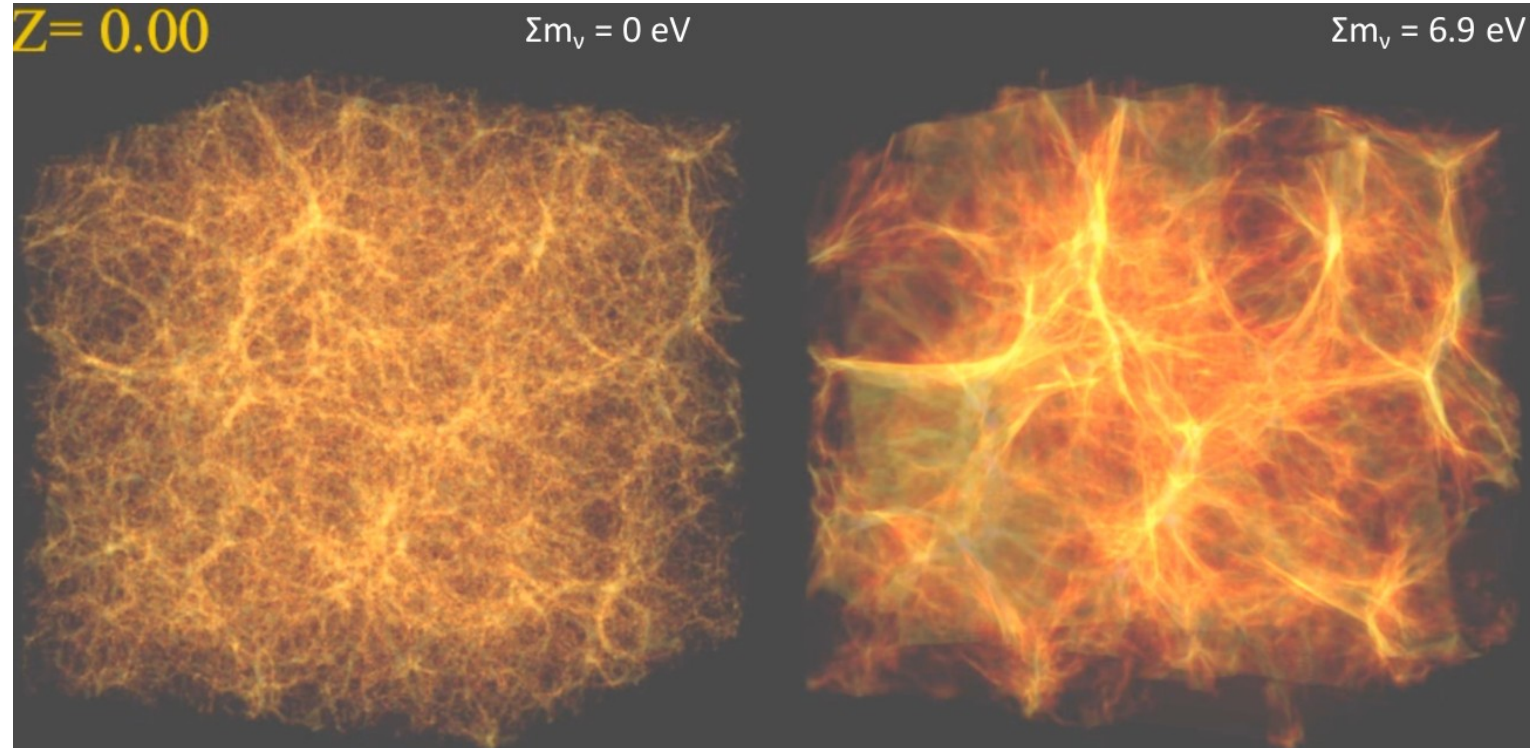


Observational cosmology



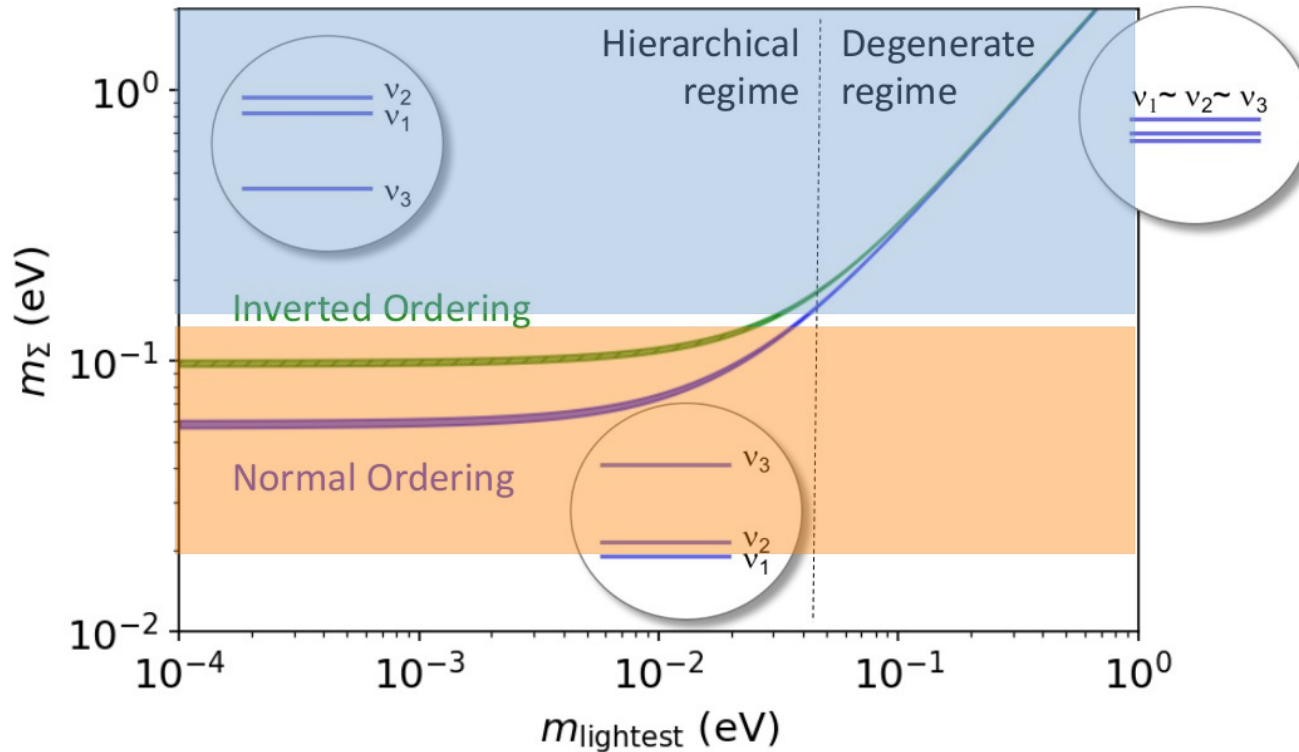
- Neutrinos are the most abundant matter particle in the universe
- Even if light they can impact the structure formation

Observational cosmology



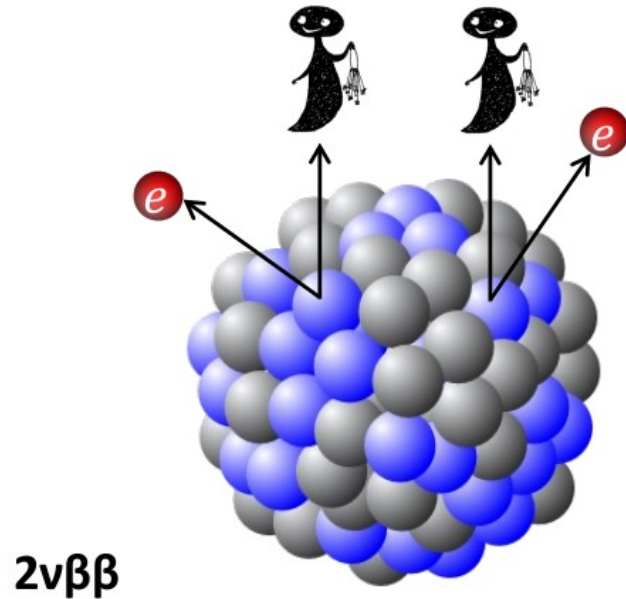
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Observational cosmology



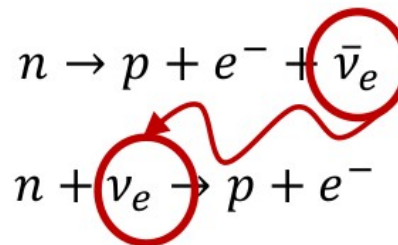
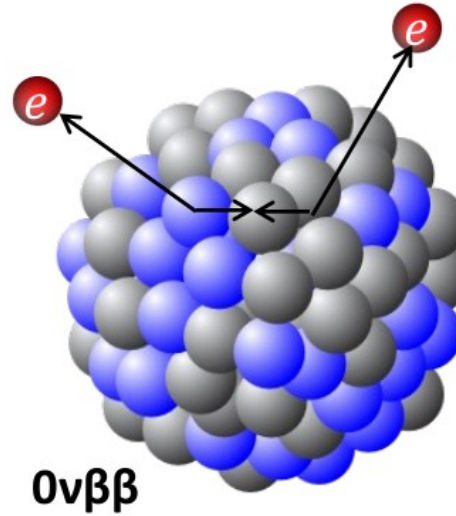
- $\sum m_\nu < 120$ meV (Planck)
- Future missions
 - 10 meV precision
- Various ways to relax the limits:
 - Beyond Λ CDM
 - New neutrino physics

Search for $0\nu\beta\beta$ decay



$$n \rightarrow p + e^- + \bar{\nu}_e$$

$$n \rightarrow p + e^- + \bar{\nu}_e$$



- Proof that neutrinos are Majorana particles and that Lepton number is violated
- Depends on the nuclear matrix calculation
- $m_{\beta\beta} < 79\text{--}180 \text{ meV}$ (90% CL)

GERDA collaboration

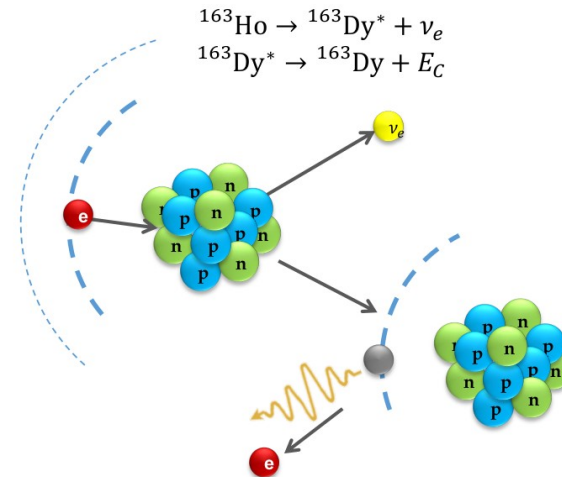
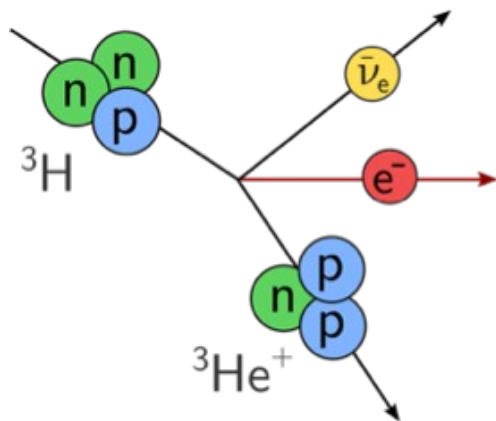
Science 365, 1445 (2019)

PRL. 125, 252502 (2020)

$$\frac{1}{T_{1/2}^{0\nu}} = G_{0\nu}(Q, Z) \cdot |M^{0\nu}|^2 \cdot m_{\beta\beta}^2$$

Direct neutrino mass measurement

- No further assumptions needed, use $E^2 = p^2c^2 + m^2c^4$
 $\Rightarrow m_\nu^2$
- Time-of-flight measurements (ν from supernova)
- Kinematics of weak decays / beta decays, e.g. T, ^{163}Ho



Overview: neutrino mass observables

Cosmology

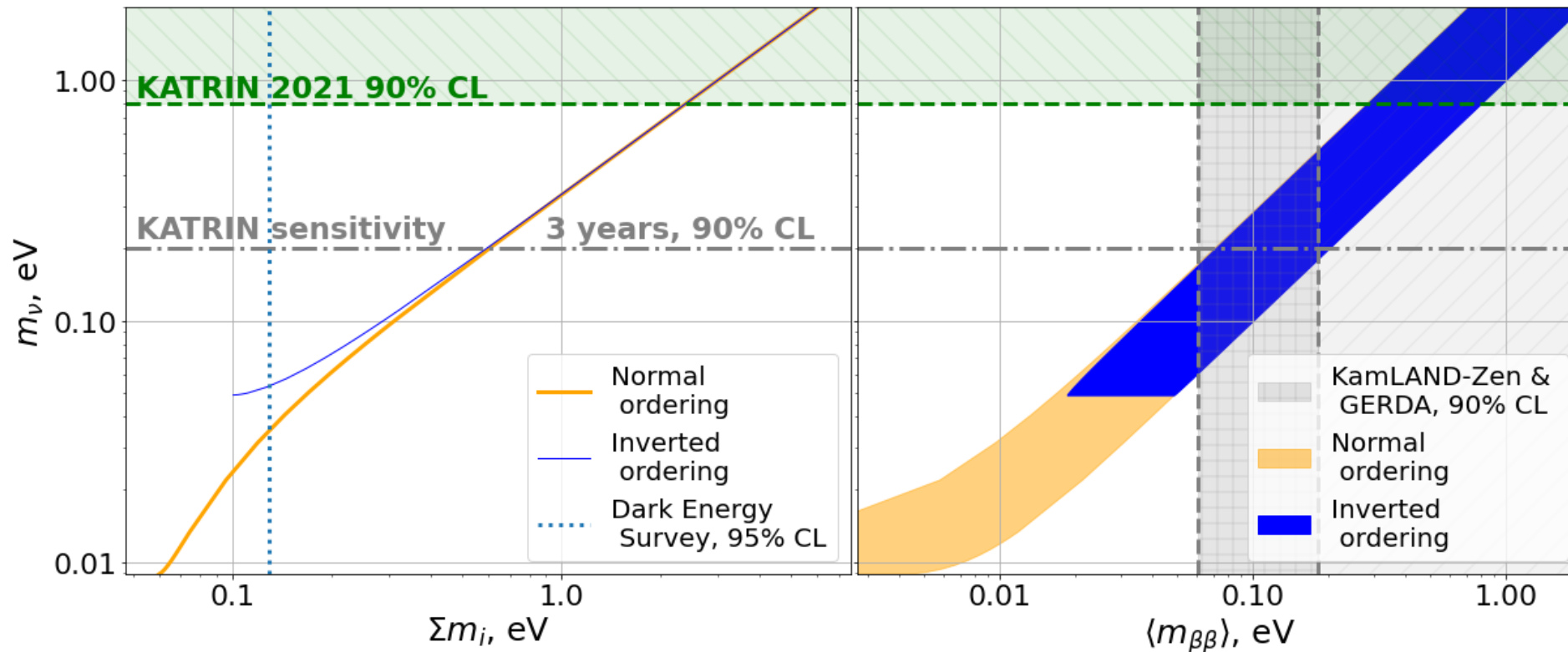
$$M_\nu = \sum_i m_i$$

$0\nu\beta\beta$ decay

$$m_{\beta\beta}^2 = \left| \sum_i U_{ei}^2 m_i \right|^2$$

β decay and EC

$$m_\beta^2 = \sum_i |U_{ei}|^2 m_i^2$$



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What are the three
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neutrino mass?

Cosmology, $0\nu 2\beta$ -
decay, direct
searches

Complementary
observables

Direct laboratory
measurements –
least model
dependent

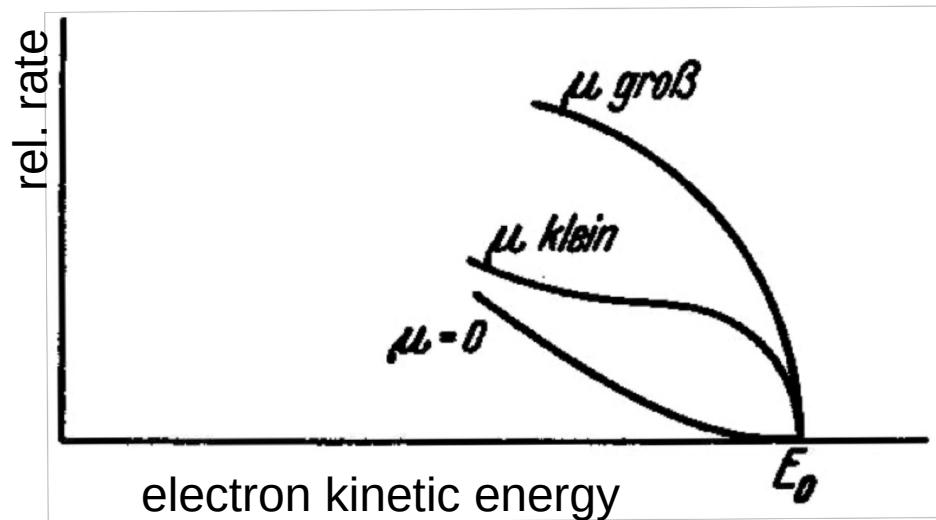
How to measure
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Neutrino mass from β -decay kinematics

Theory: Starting from Fermi's seminal paper (Z. Phys., 1934)

Experiment: Tritium identified early on as most suitable β -emitter



NATURE

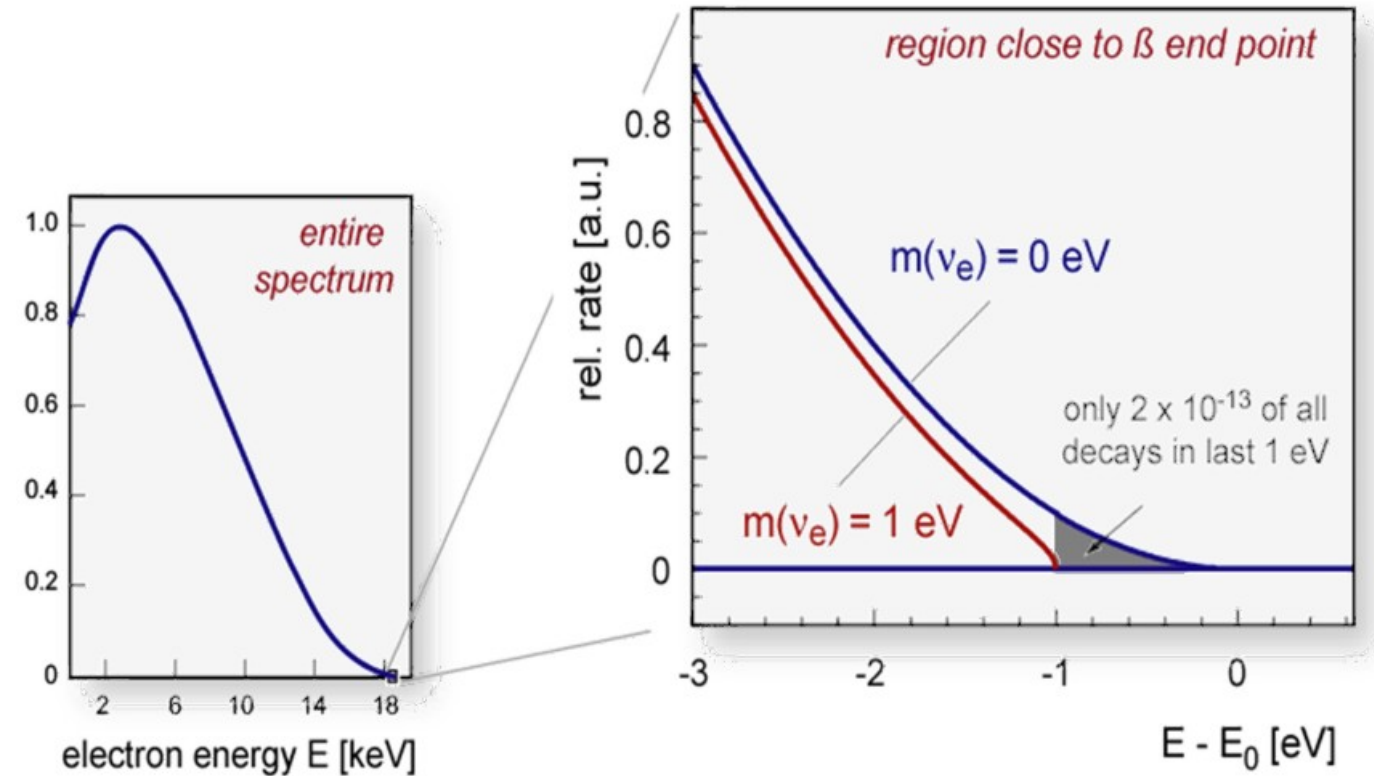
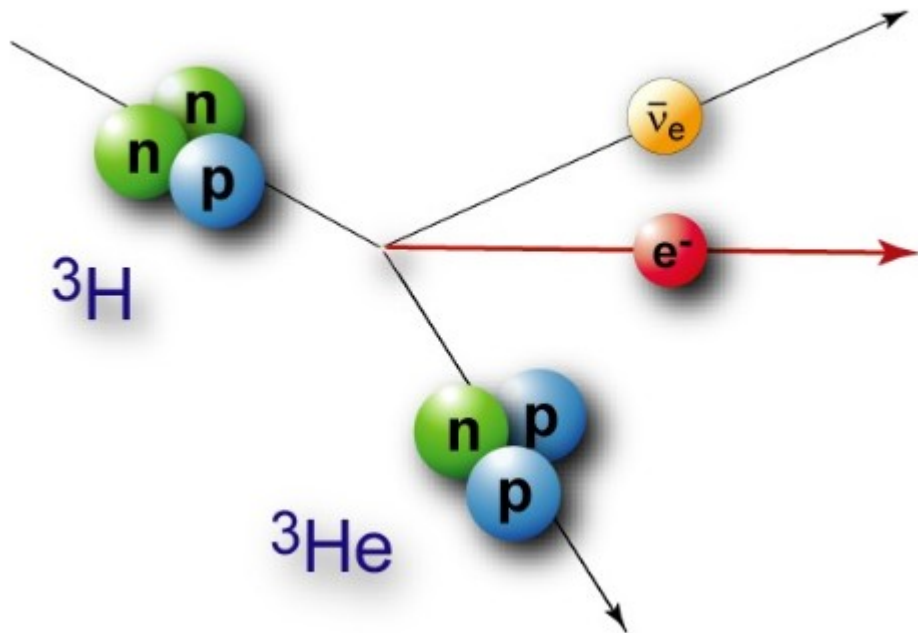
August 21, 1948 Vol. 162

Beta Spectrum of Tritium

THE β -spectrum of tritium (${}^3_1\text{H}$) is of particular interest because : (1) the relatively simple structure of the ${}^3_1\text{H}$ nucleus makes it well suited to a test of the Fermi theory of β -decay ; (2) the unusually low energy of the β -particles means that the shape of the spectrum near the upper limit is an extremely sensitive function of the rest mass of the neutrino if the Fermi theory is confirmed ; (3) a theoretical discrepancy¹ exists between the half-life² and the upper energy limit, as recently measured³ ; (4) the mass difference (${}^3_1\text{H} - {}^3_2\text{He}$) can be accurately determined.

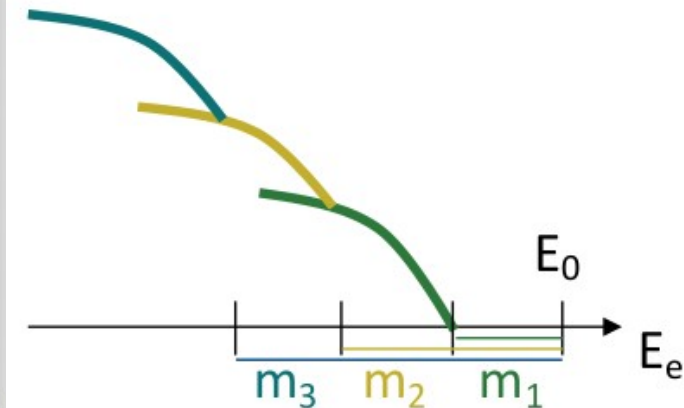
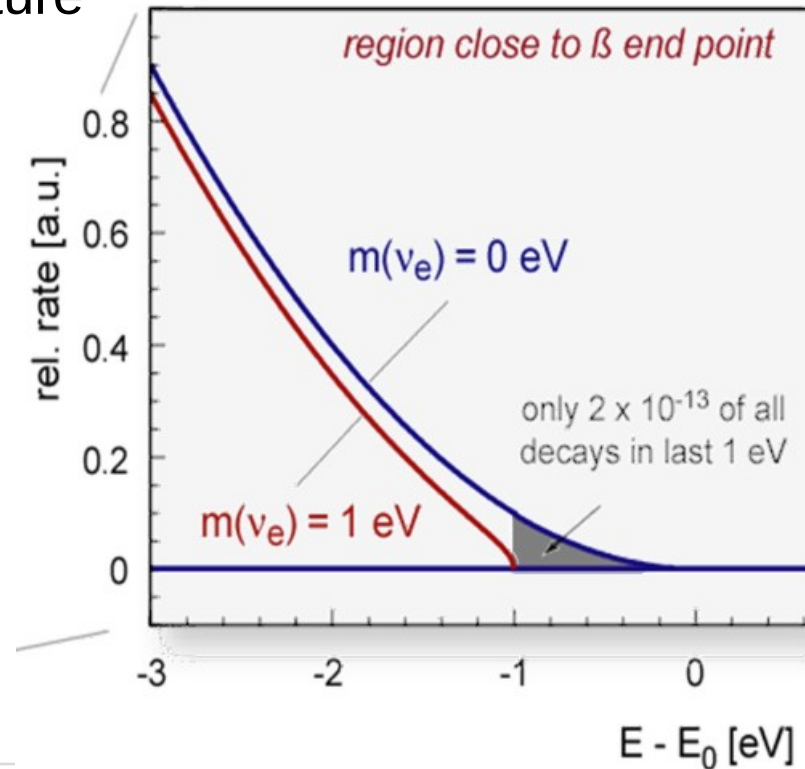
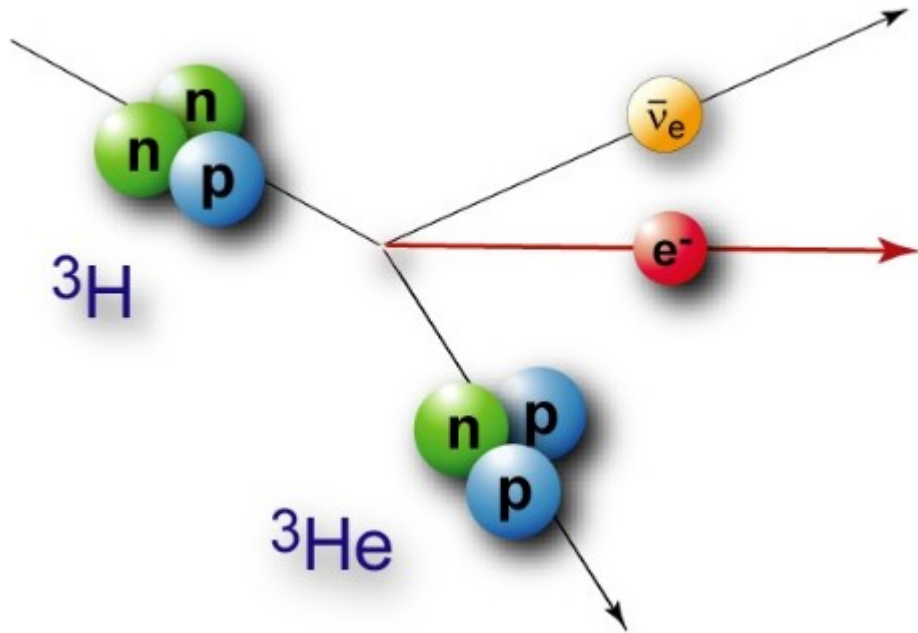
Neutrino mass from β -decay kinematics

- Non-zero neutrino mass distorts the spectrum of electrons
 - Independent from cosmology
 - Independent from neutrino nature



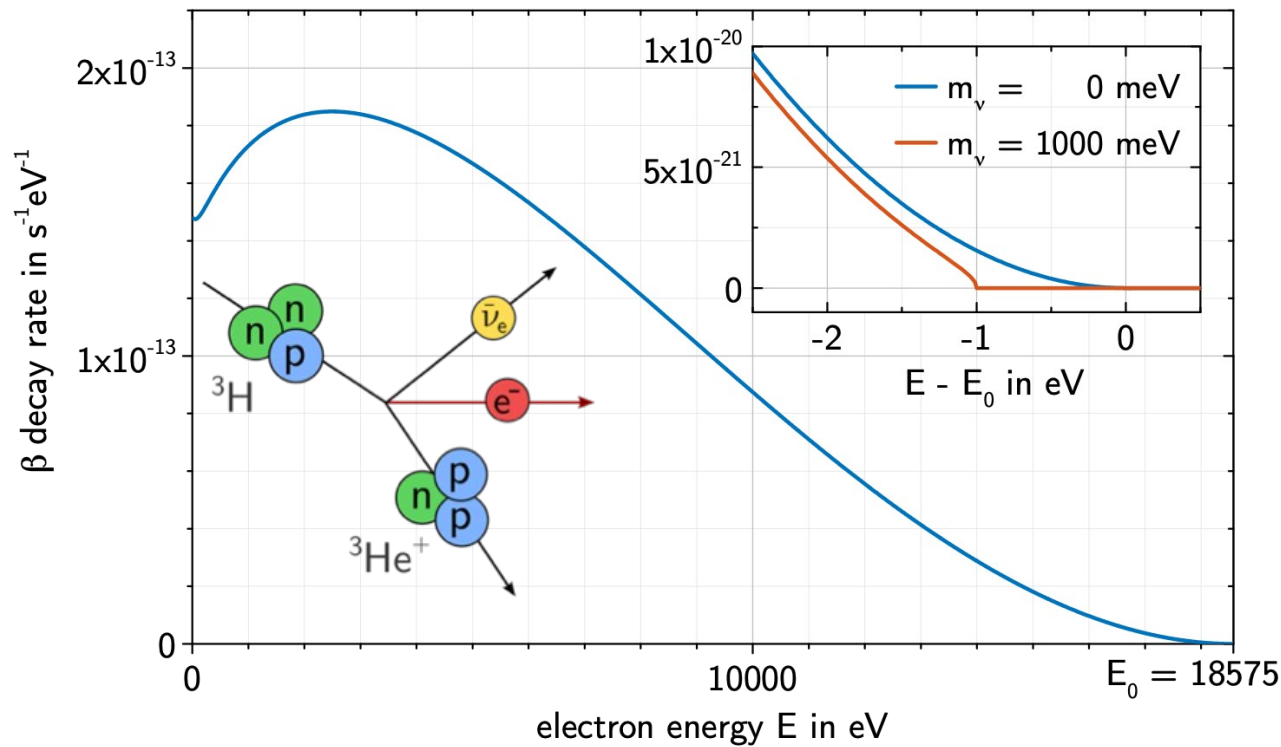
Neutrino mass from β -decay kinematics

- Non-zero neutrino mass distorts the spectrum of electrons
 - Independent from cosmology
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Neutrino mass from β -decay kinematics

$$\frac{d\Gamma}{dE} = K \cdot F(Z, E) \cdot \underbrace{p}_{p_e} \cdot \underbrace{E_{\text{tot}}}_{E_e} \cdot \underbrace{(E_0 - E)}_{E_\nu} \cdot \underbrace{\sum_i |U_{ei}|^2 \sqrt{(E_0 - E)^2 - m_i^2}}_{p_\nu}$$



Key requirements & technologies

- Low-endpoint β/EC nuclide:
 $E_0 = 18.6 \text{ keV}$ for ^3H
- High-activity source:
 $T_{1/2} = 12.3 \text{ yr}$ for ^3H
- Excellent energy resolution

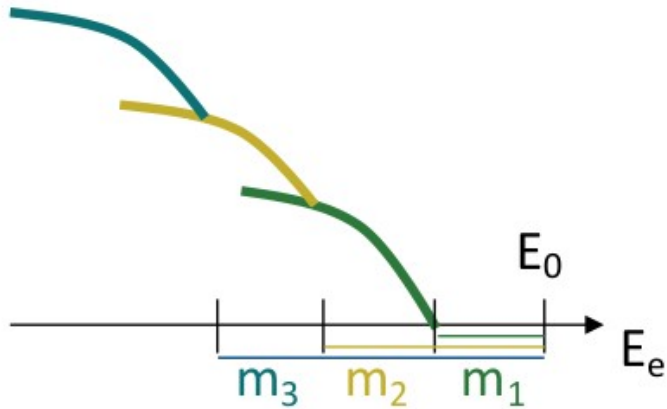
Spectral distortion measures
“effective” mass square:

$$m^2(\nu_e) := \sum_i |U_{ei}|^2 m_i^2$$

Effective neutrino mass parameter

$$\frac{d\Gamma}{dE} = \sum_i |U_{ei}|^2 C \cdot F(E, Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - m_i^2}$$

- Assume that we are measuring “far away” from E_0



$$\begin{aligned} & \sum_i |U_{ei}|^2 \cdot (E_0 - E) \cdot \sqrt{1 - \frac{m_i^2}{(E_0 - E)^2}} \\ & \approx \sum_i |U_{ei}|^2 \cdot (E_0 - E) \cdot \left(1 - \frac{1}{2} \cdot \frac{m_i^2}{(E_0 - E)^2}\right) \\ & = (E_0 - E) \cdot \left(1 - \frac{1}{2} \cdot \frac{\sum_i |U_{ei}|^2 \cdot m_i^2}{(E_0 - E)^2}\right) \\ & \approx \sqrt{(E_0 - E)^2 - \sum_i |U_{ei}|^2 \cdot m_i^2} \end{aligned}$$

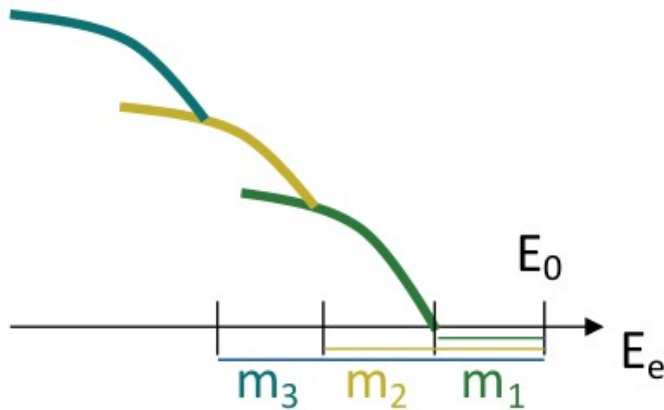
Effective neutrino mass parameter

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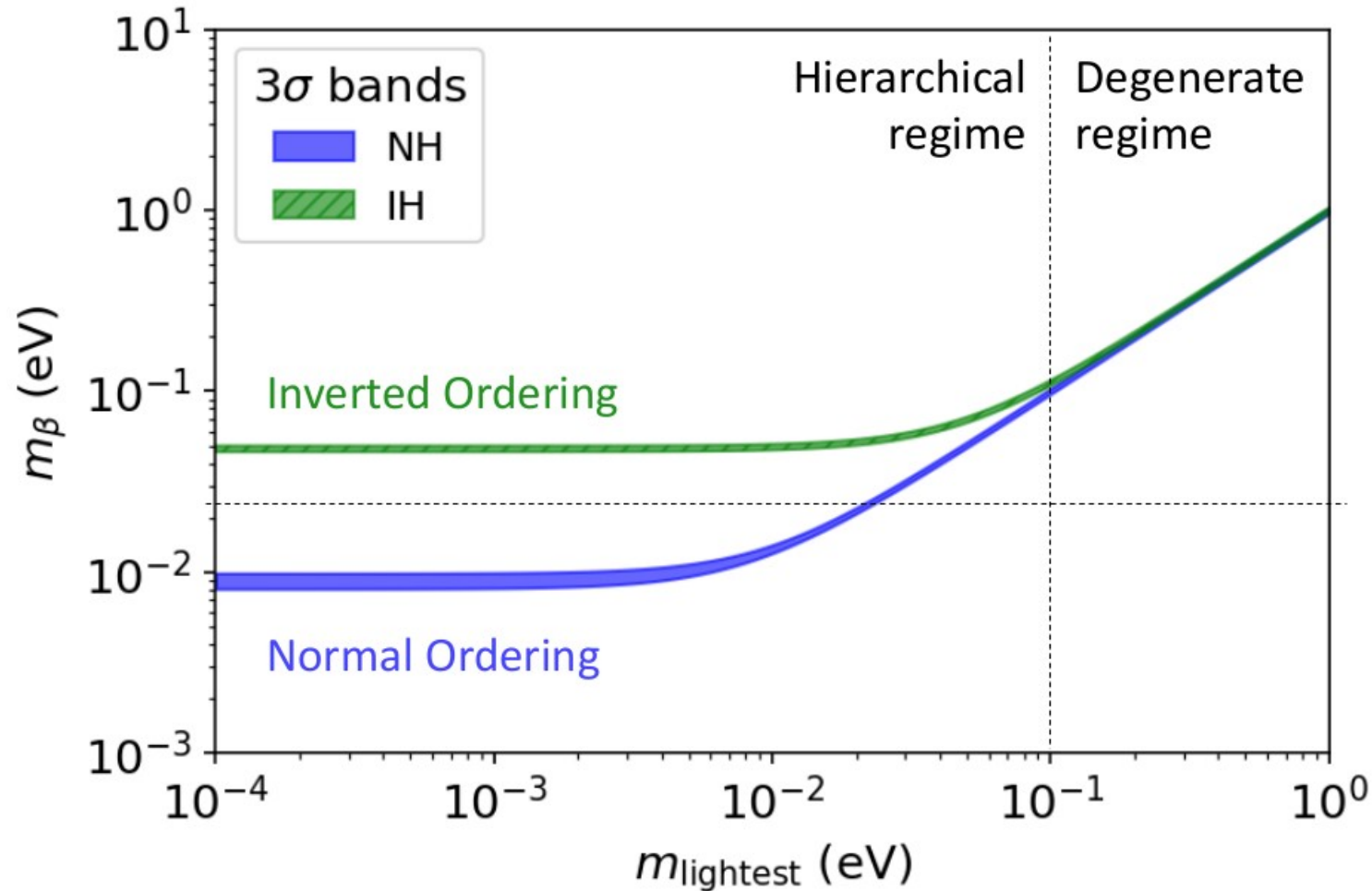
$$\frac{d\Gamma}{dE} = C \cdot F(E, Z) \cdot (E + m_e) \cdot (E_0 - E) \cdot \sqrt{(E + m_e)^2 - m_e^2} \cdot \sqrt{(E_0 - E)^2 - \sum_i |U_{ei}|^2 \cdot m_i^2}$$

$$m_v^2 = \sum_i |U_{ei}|^2 \cdot m_i^2$$

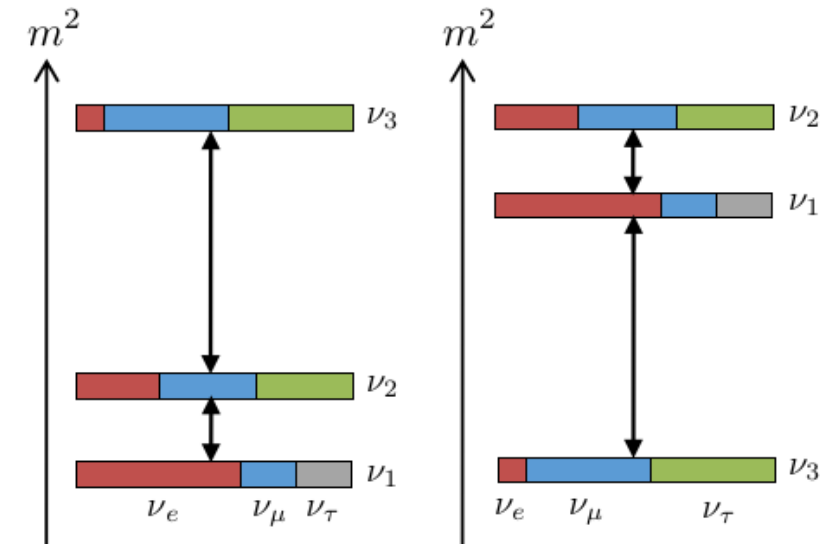


- Incoherent sum of neutrino masses
- Effective squared mass of electron antineutrino

Effective neutrino mass

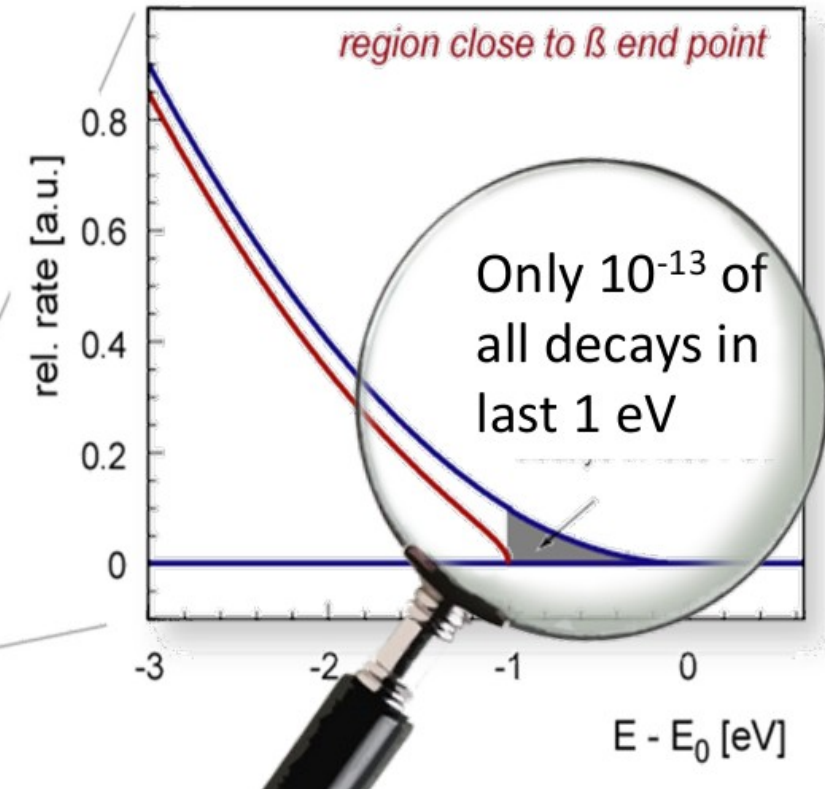
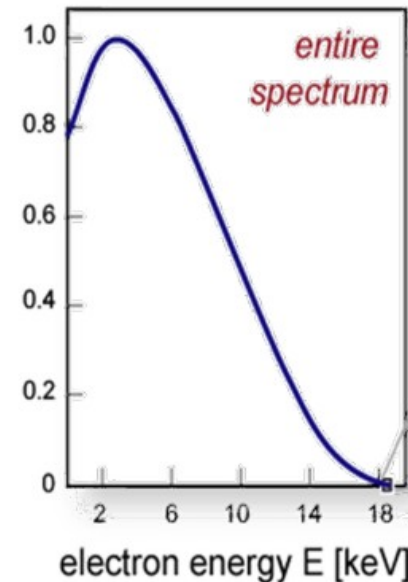


$$m_\beta = \sqrt{\sum_i |U_{ei}|^2 \cdot m_i^2}$$

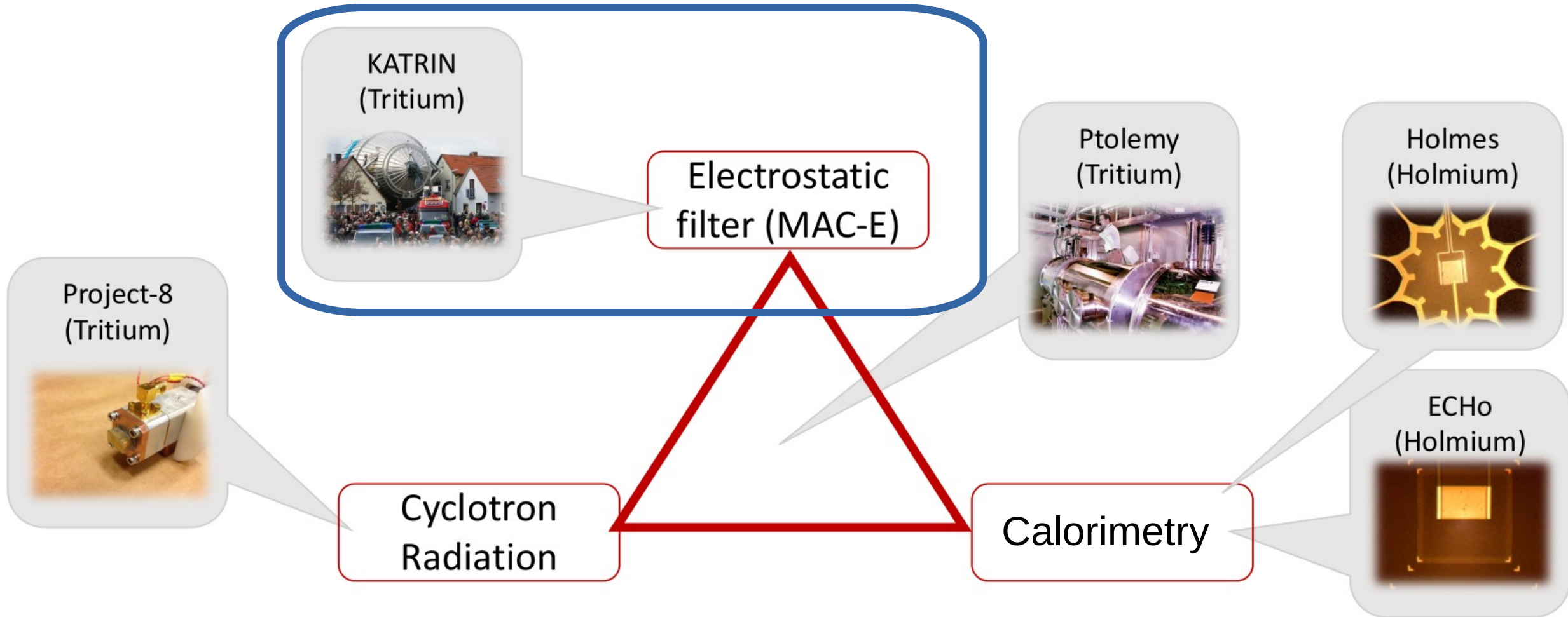


Experimental challenges

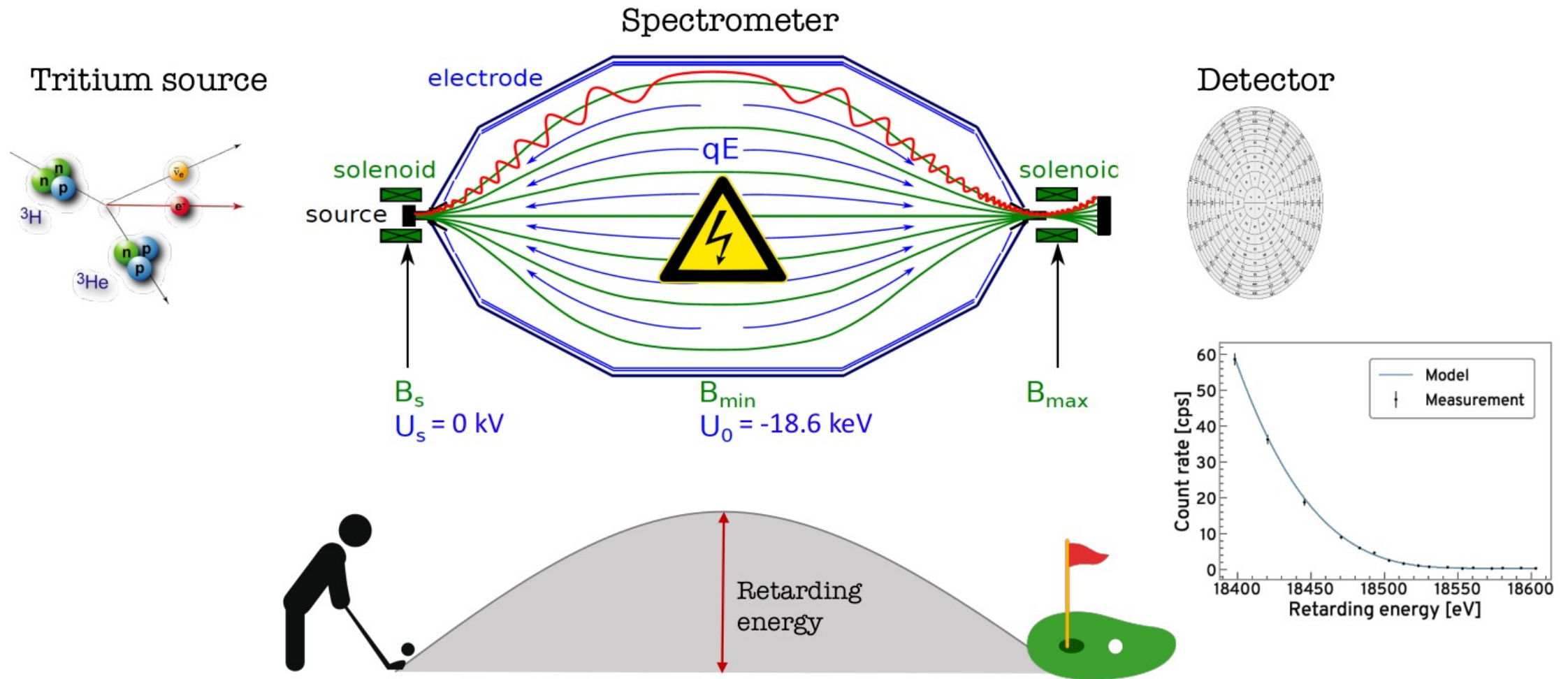
- How to realize such experiment?
 - Ultra-strong radioactive source (10^{11} decays/s)
 - Excellent energy resolution (~ 1 eV, 0.005%)
 - Low background (< 100 mcps)



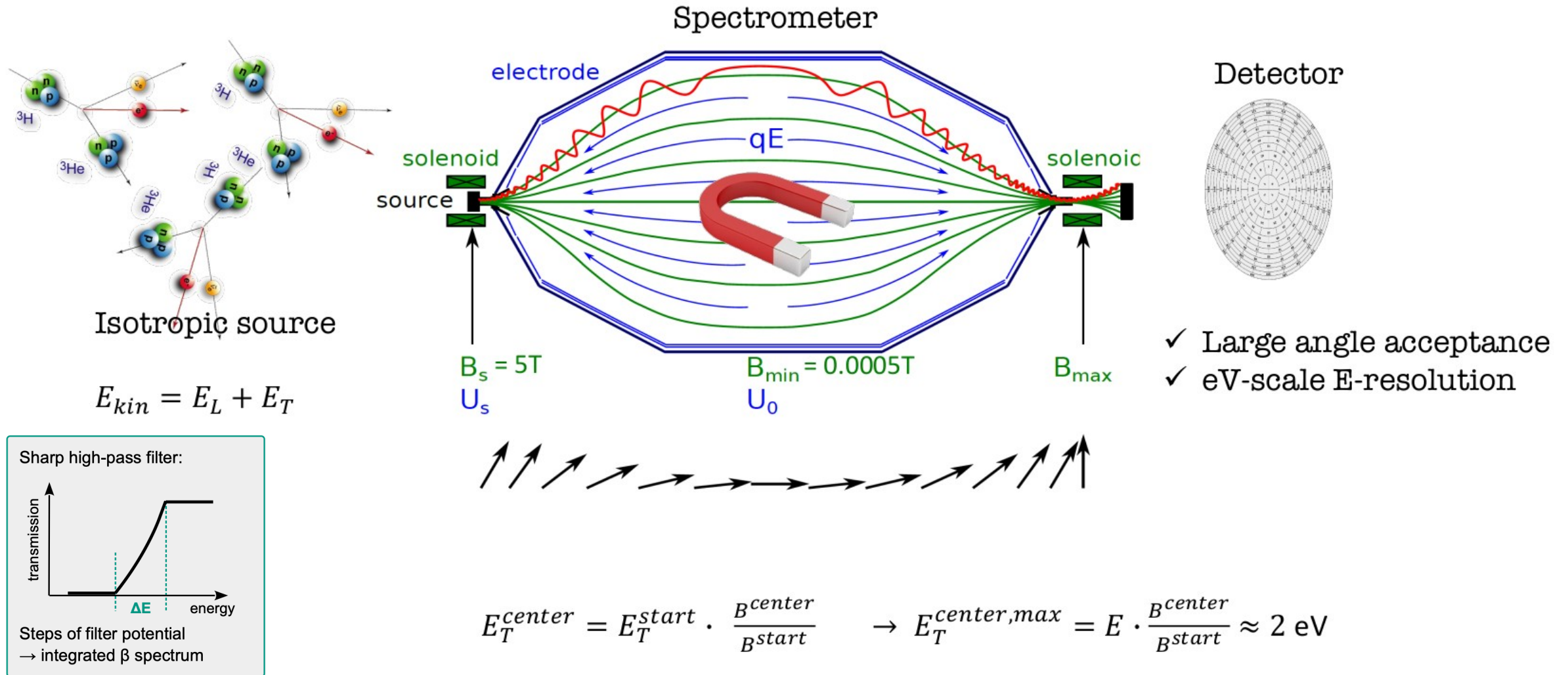
Experimental techniques for direct ν -mass measurement



MAC-E filter technique



MAC-E filter technique



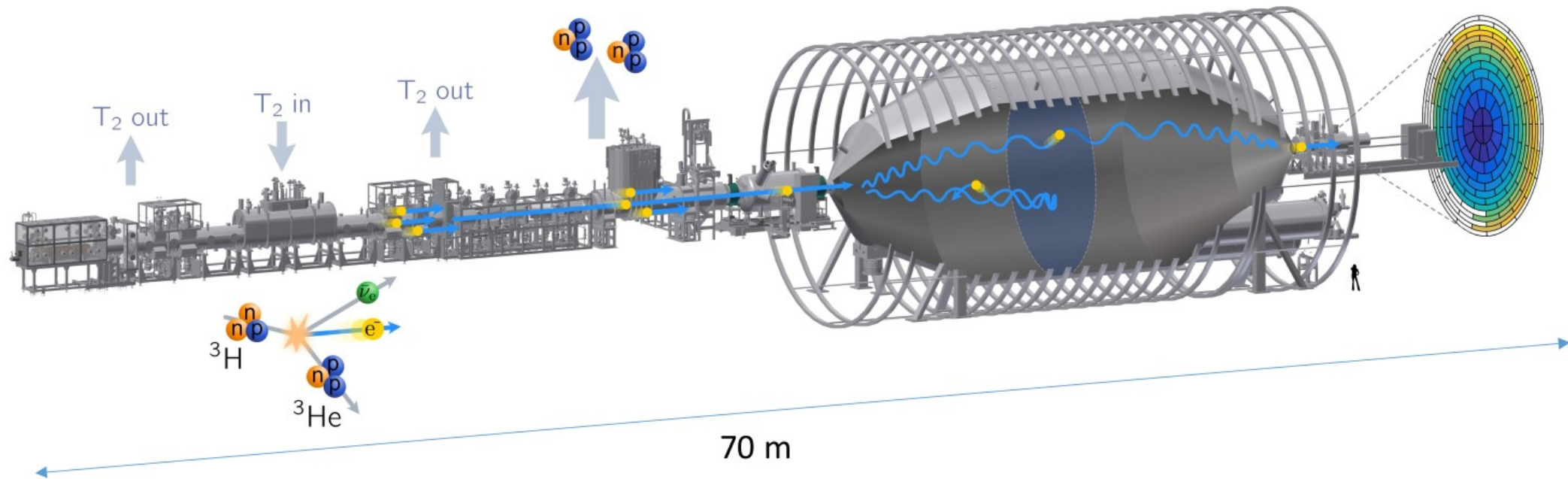
KATRIN: Karlsruhe Tritium Neutrino Experiment



KATRIN's epic voyage



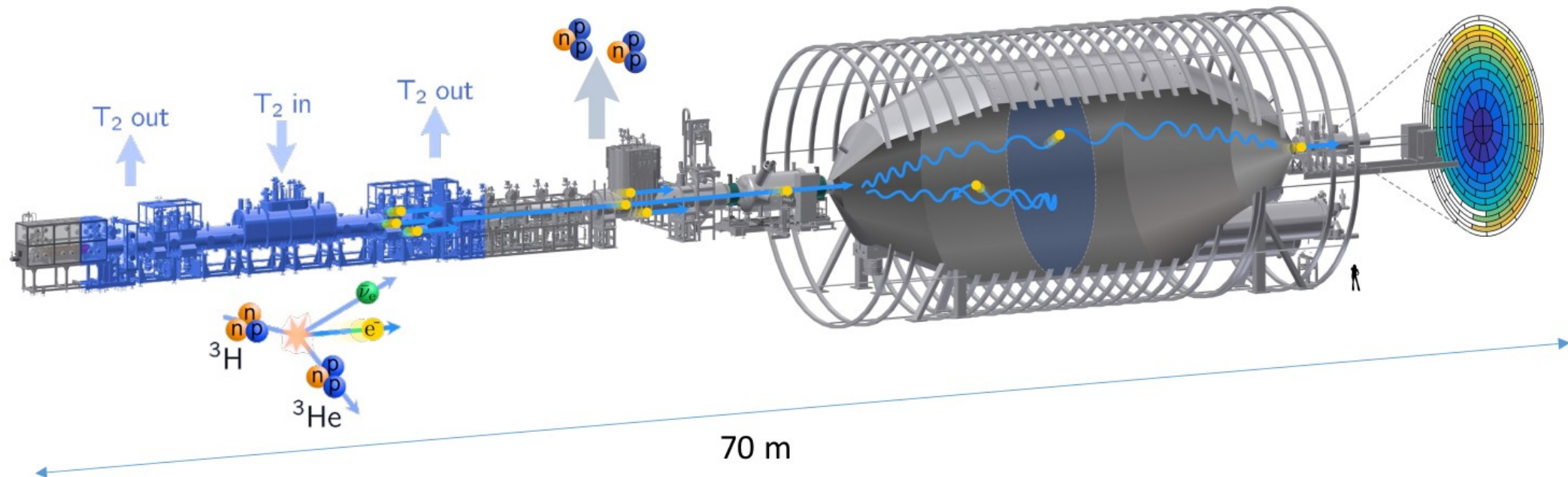
Measurement principle of KATRIN



Measurement principle of KATRIN

Tritium source

- 100 μg of gaseous T_2
- 10^{11} T_2 decays/s



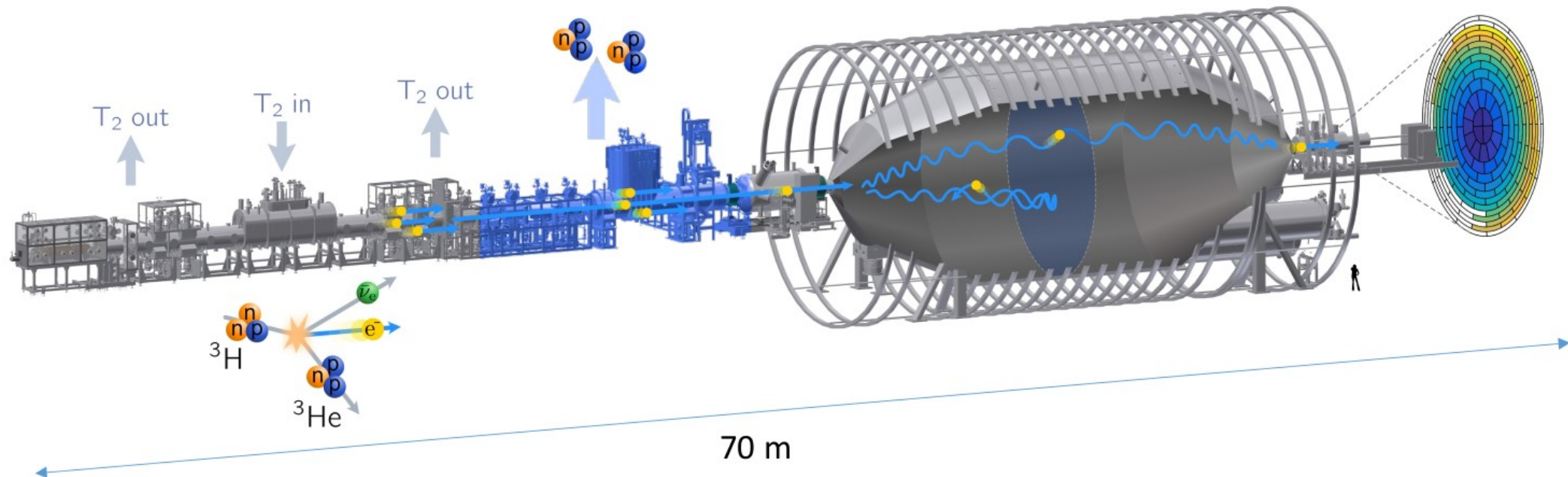
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- 100 μg of gaseous T_2
- 10^{11} T_2 decays/s

Transport section

- Guidance of electrons
- Removal of tritium



Measurement principle of KATRIN

Tritium source

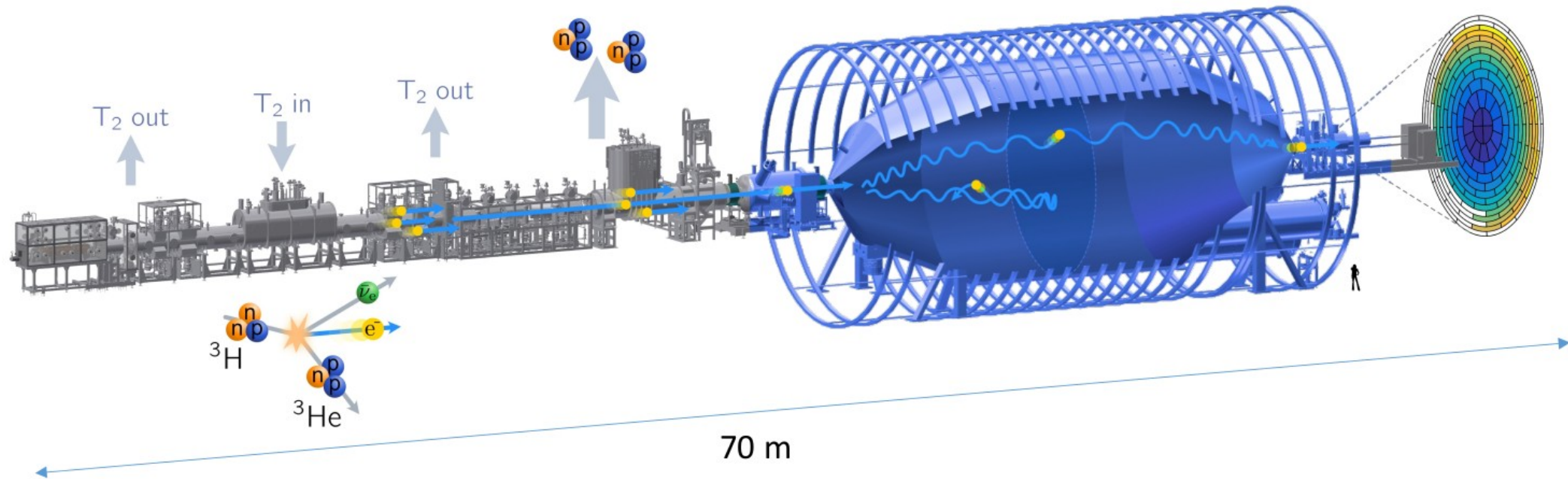
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Spectrometer

- Electrostatic filter
- MAC-E filter principle



Measurement principle of KATRIN

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- 10^{11} T_2 decays/s

Transport section

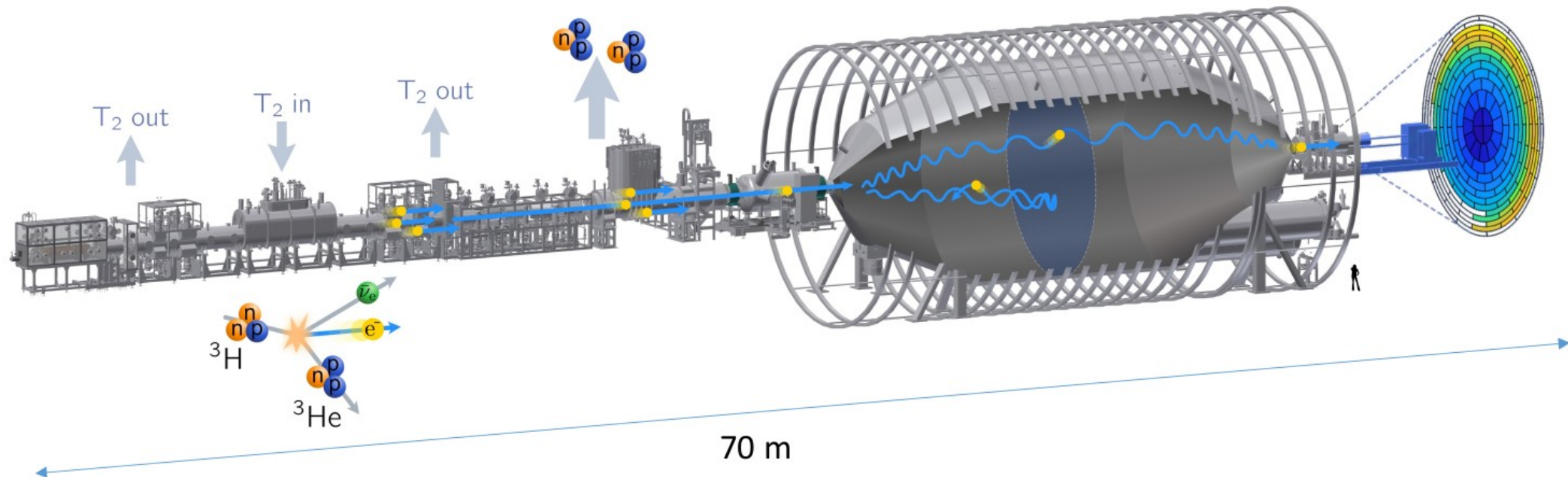
- Guidance of electrons
- Removal of tritium

Spectrometer

- Electrostatic filter
- MAC-E filter principle

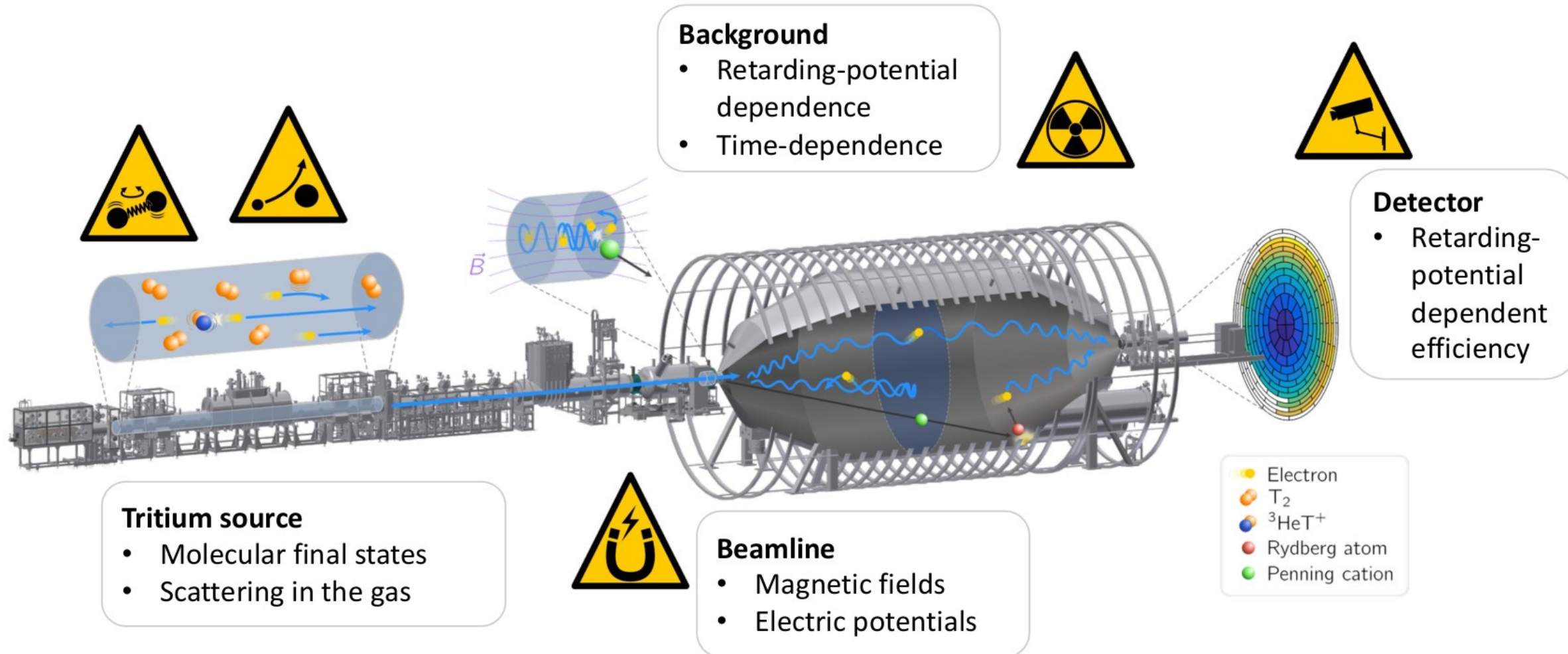
Detector

- Counts electrons
- Rate vs potential

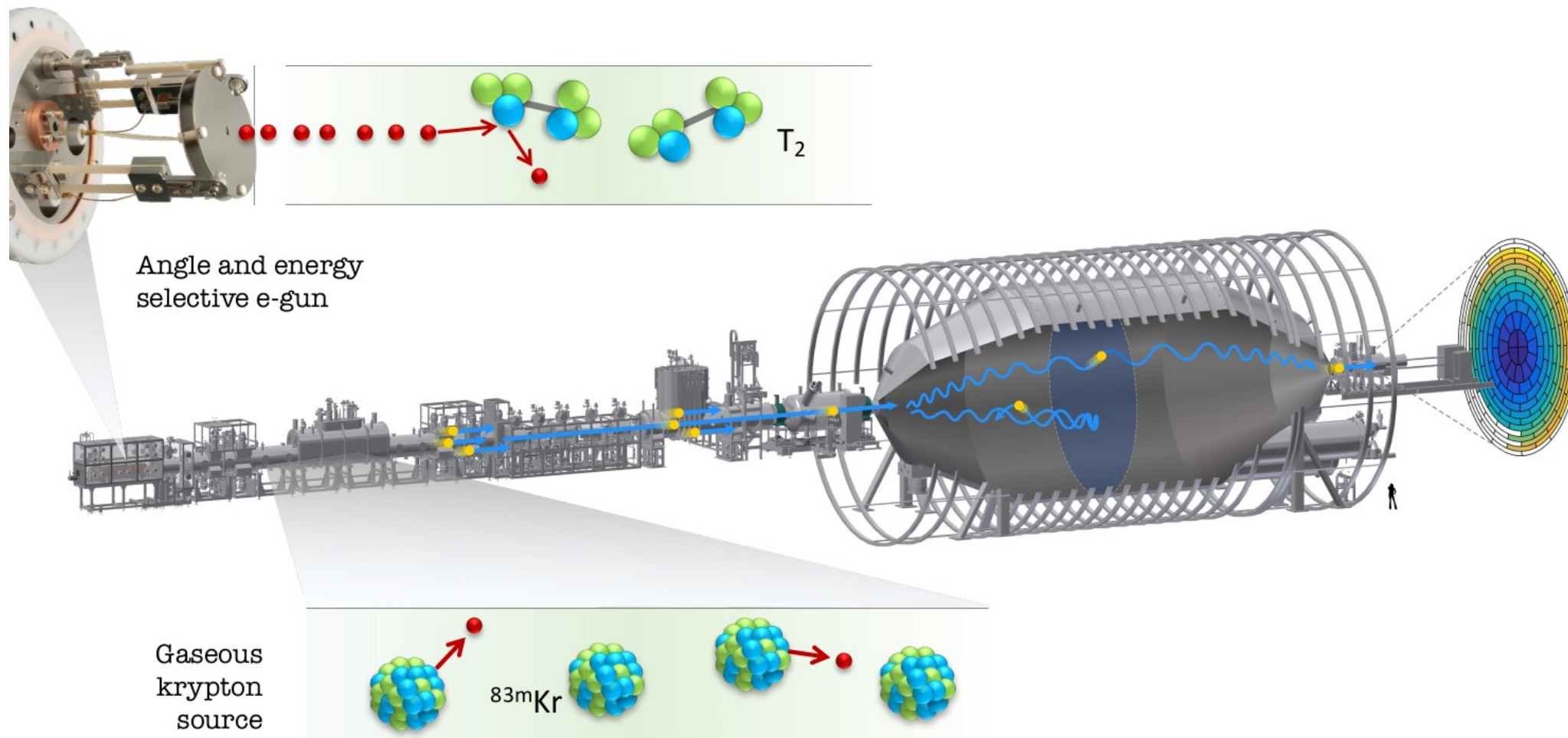


Full system description & commissioning, [JINST 16 \(2021\) T08015](#)

Systematic effects

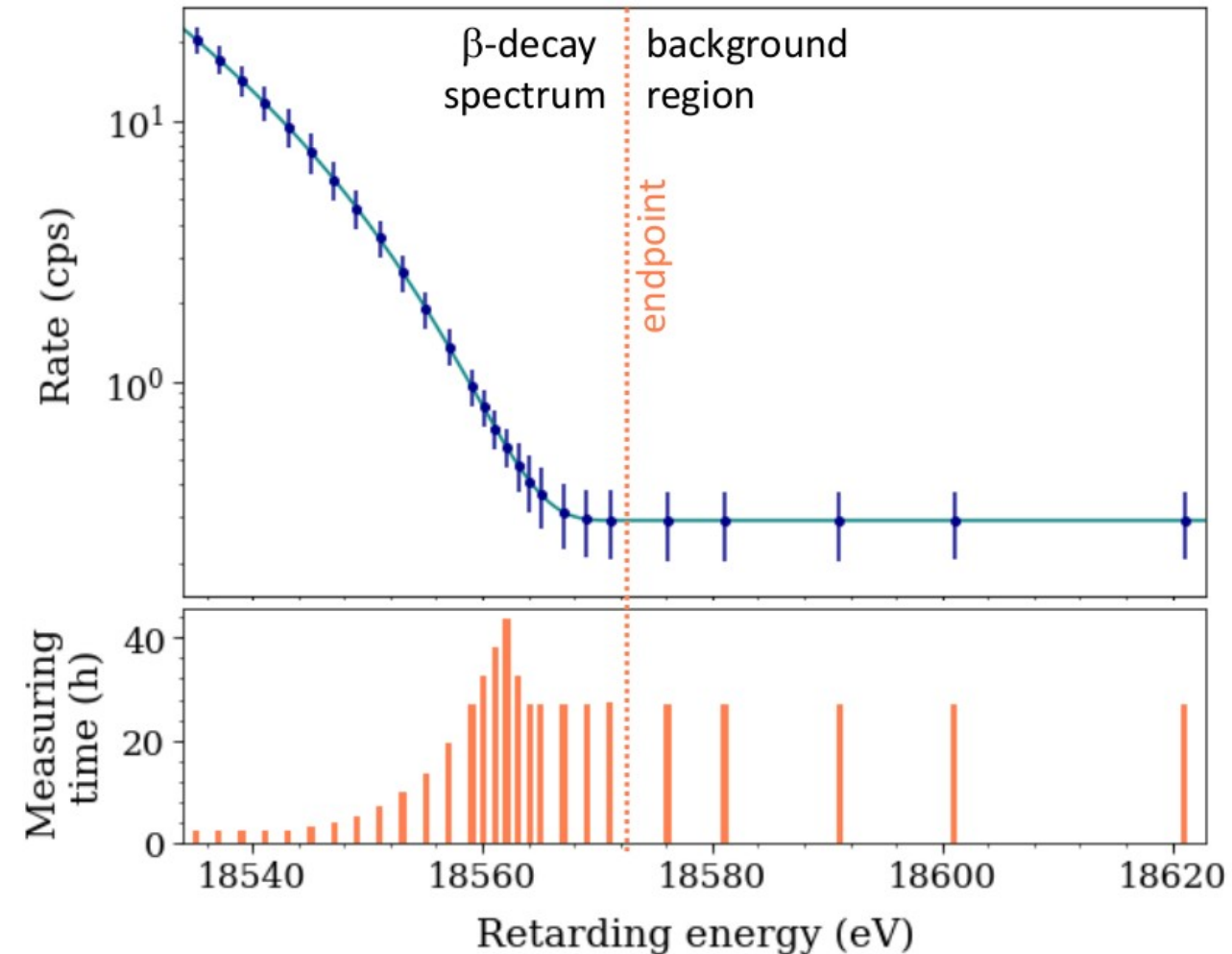


Calibration sources



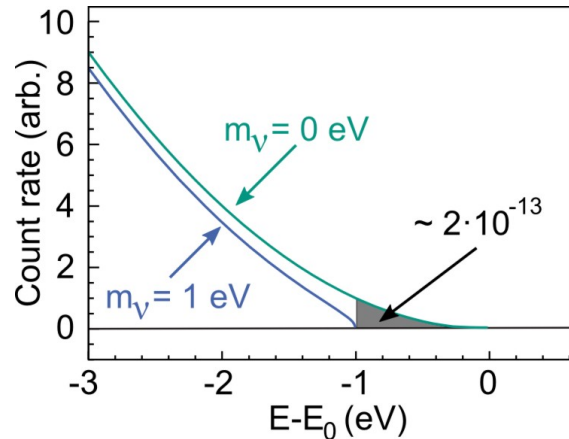
Measurement strategy

- Scan: ~ 40 HV set points
- Scan length: 2-3 hours
- Analysis interval:
 - $E_0 - 40$ eV, $E_0 + 135$ eV
- Hundreds of scans per campaign

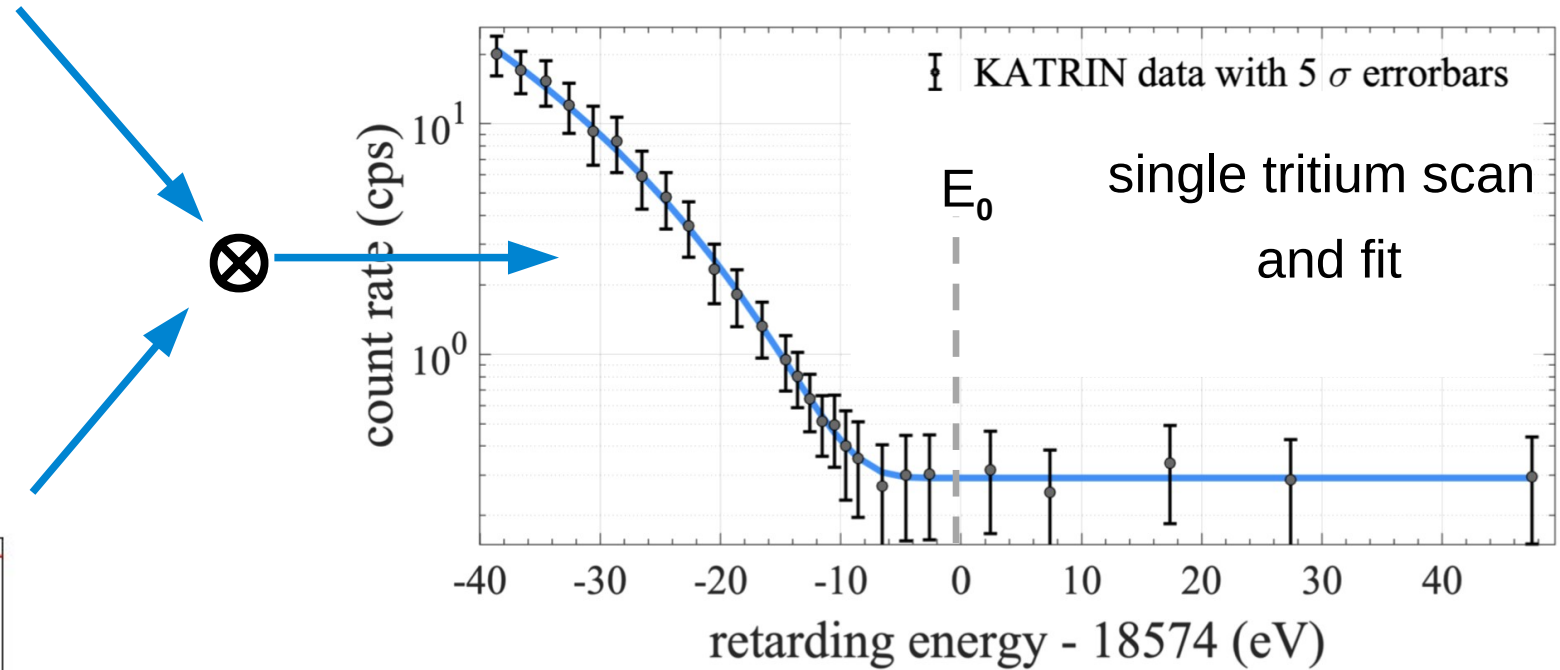
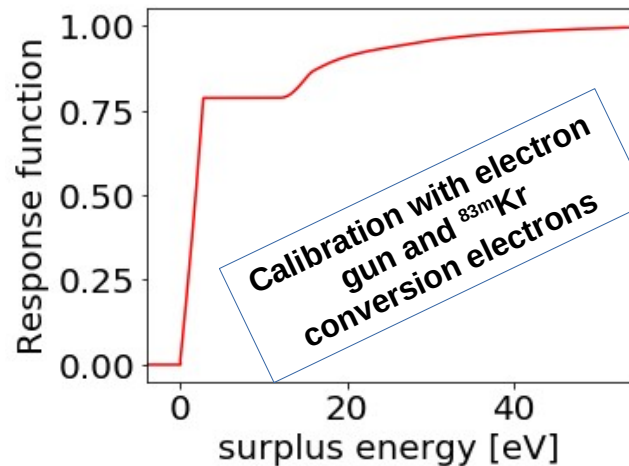


Beta-spectrum and neutrino mass

Beta spectrum: $R_\beta(E, m^2(\nu_e))$

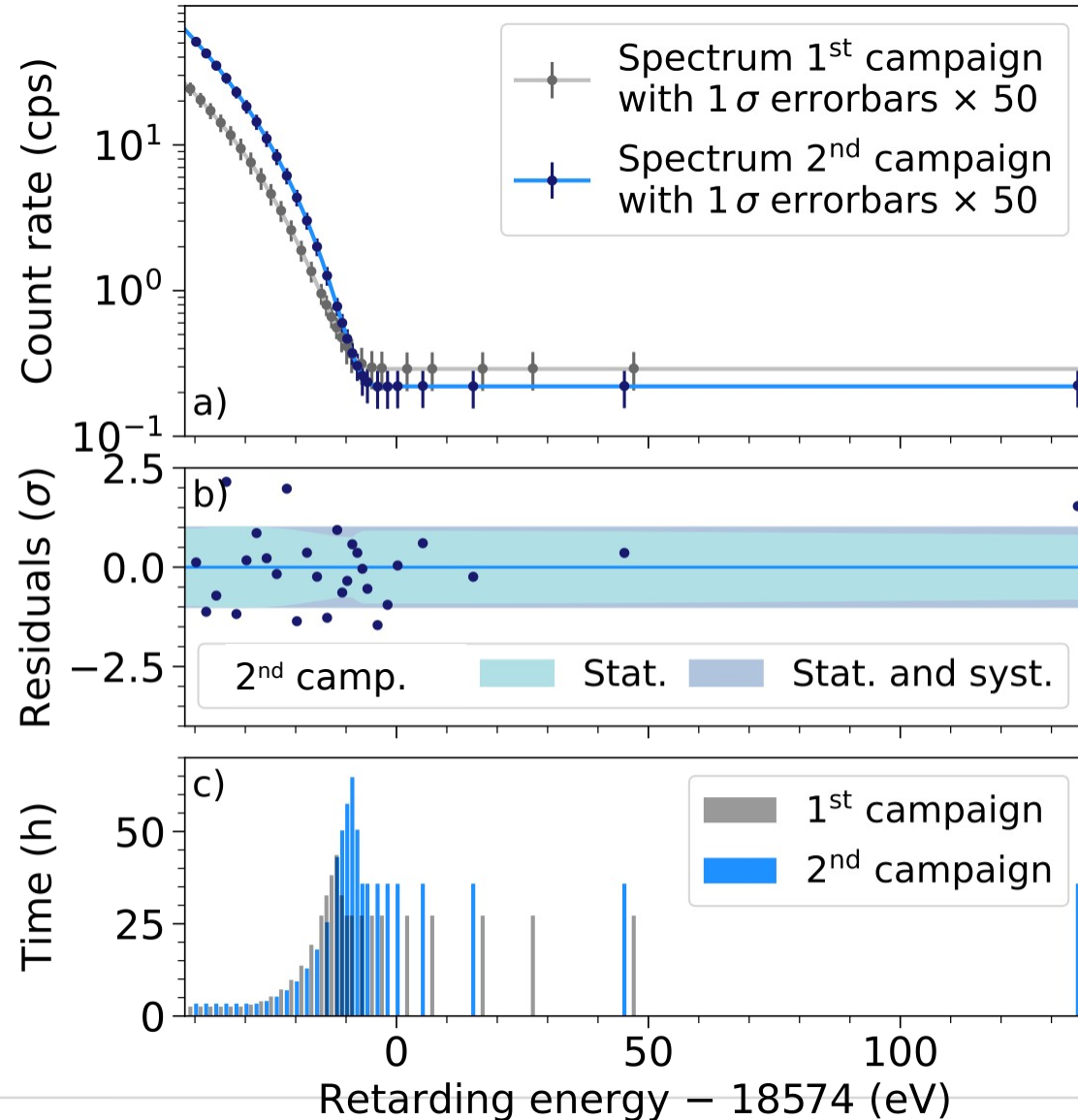


Experimental response: $f(E - qU)$



$$R(qU) = A_s \cdot N_T \int_{qU}^{E_0} R_\beta(E, m^2(\nu_e)) \cdot f(E - qU) dE + R_{bg}$$

Recent ν -mass results



First campaign (spring 2019):

✓ total statistics: 2 million events

✓ best fit: $m_\nu^2 = (-1.0^{+0.9}_{-1.1}) \text{ eV}^2 \text{ (stat. dom.)}$

✓ limit: $m_\nu < 1.1 \text{ eV (90\% CL)}$



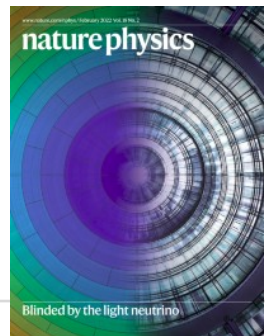
Second campaign (autumn 2019):

✓ total statistics: 4.3 million events

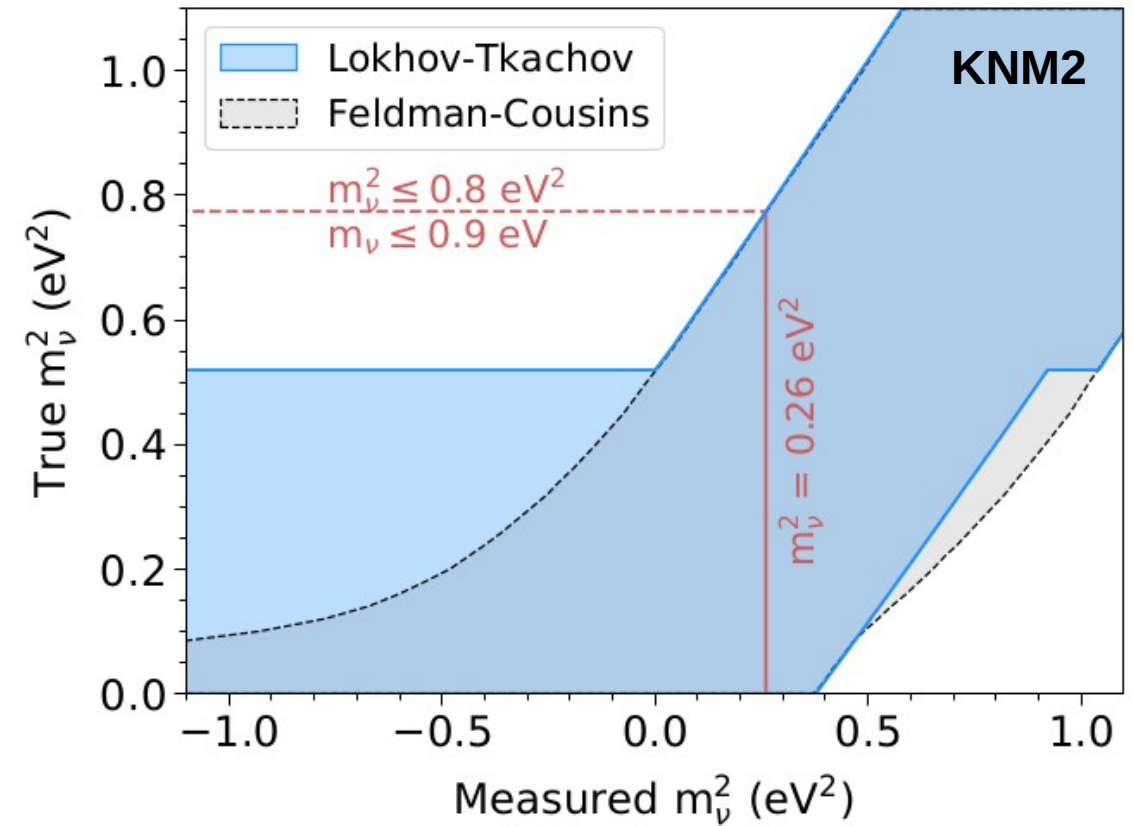
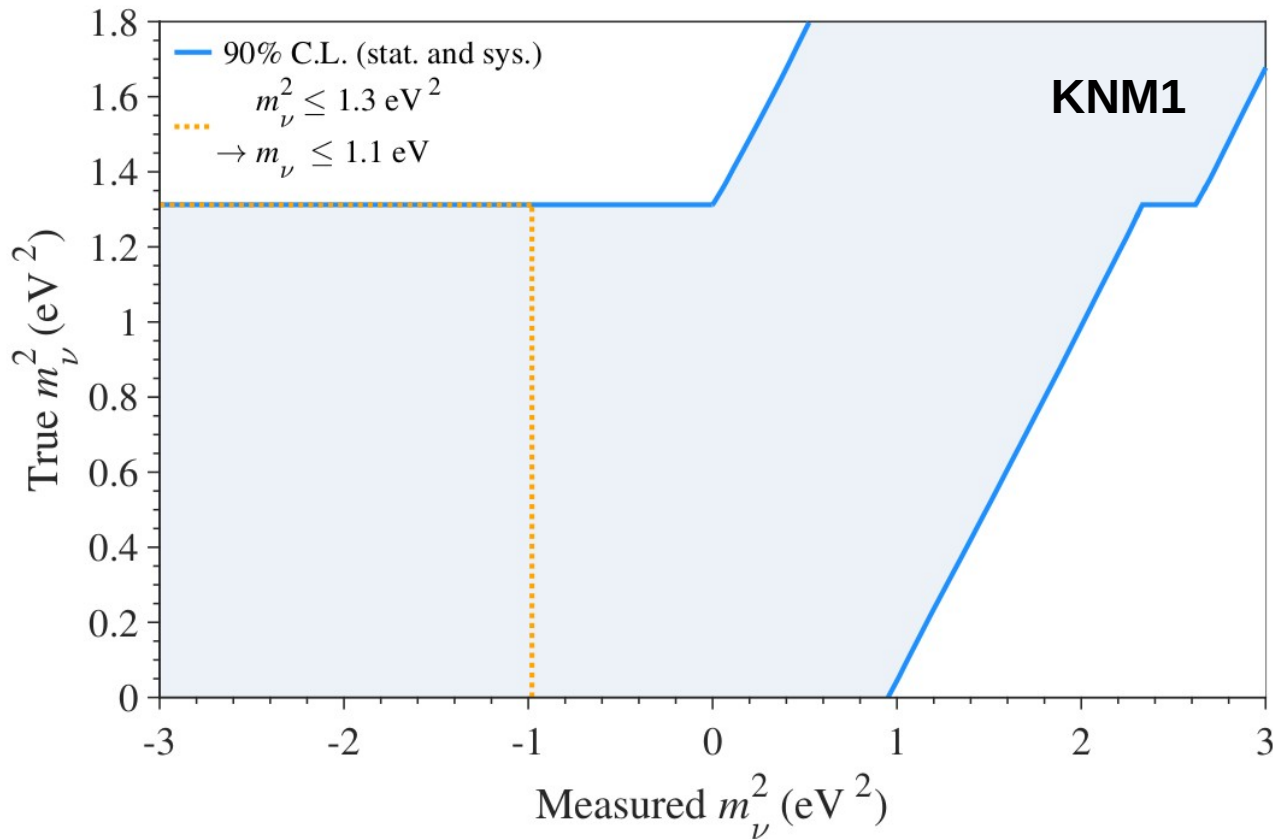
✓ best fit: $m_\nu^2 = (0.26^{+0.34}_{-0.34}) \text{ eV}^2 \text{ (stat. dom.)}$

✓ limit: $m_\nu < 0.9 \text{ eV (90\% CL)}$

Combined result: $m_\nu < 0.8 \text{ eV (90\% CL)}$



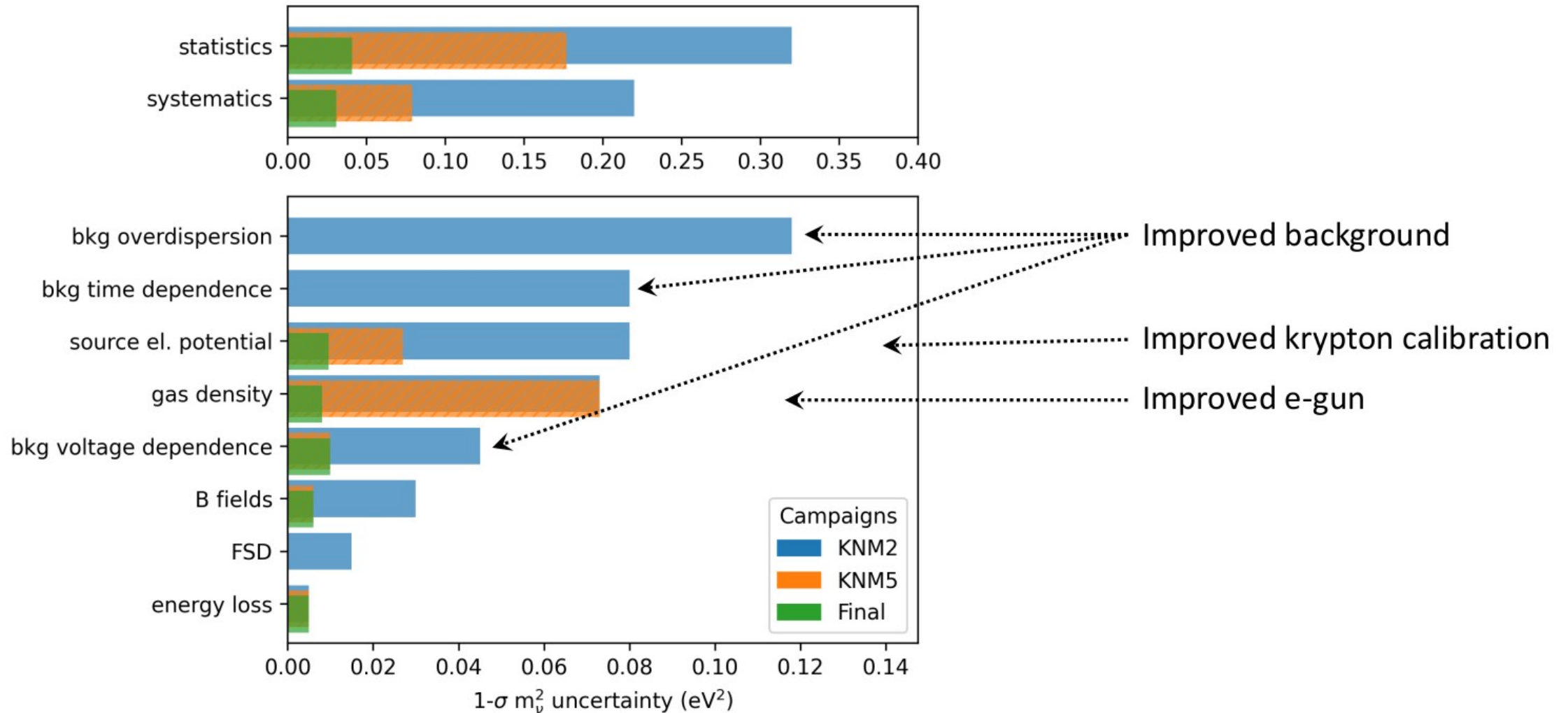
Confidence intervals construction



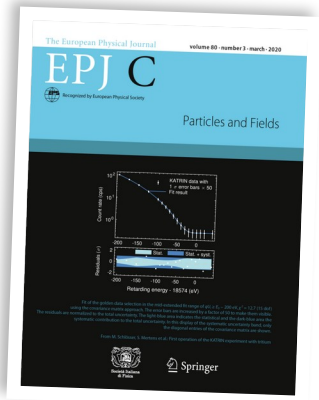
Phys. Part. Nucl. 46, 347–365

Phys. Rev. D 57, 3873–3889

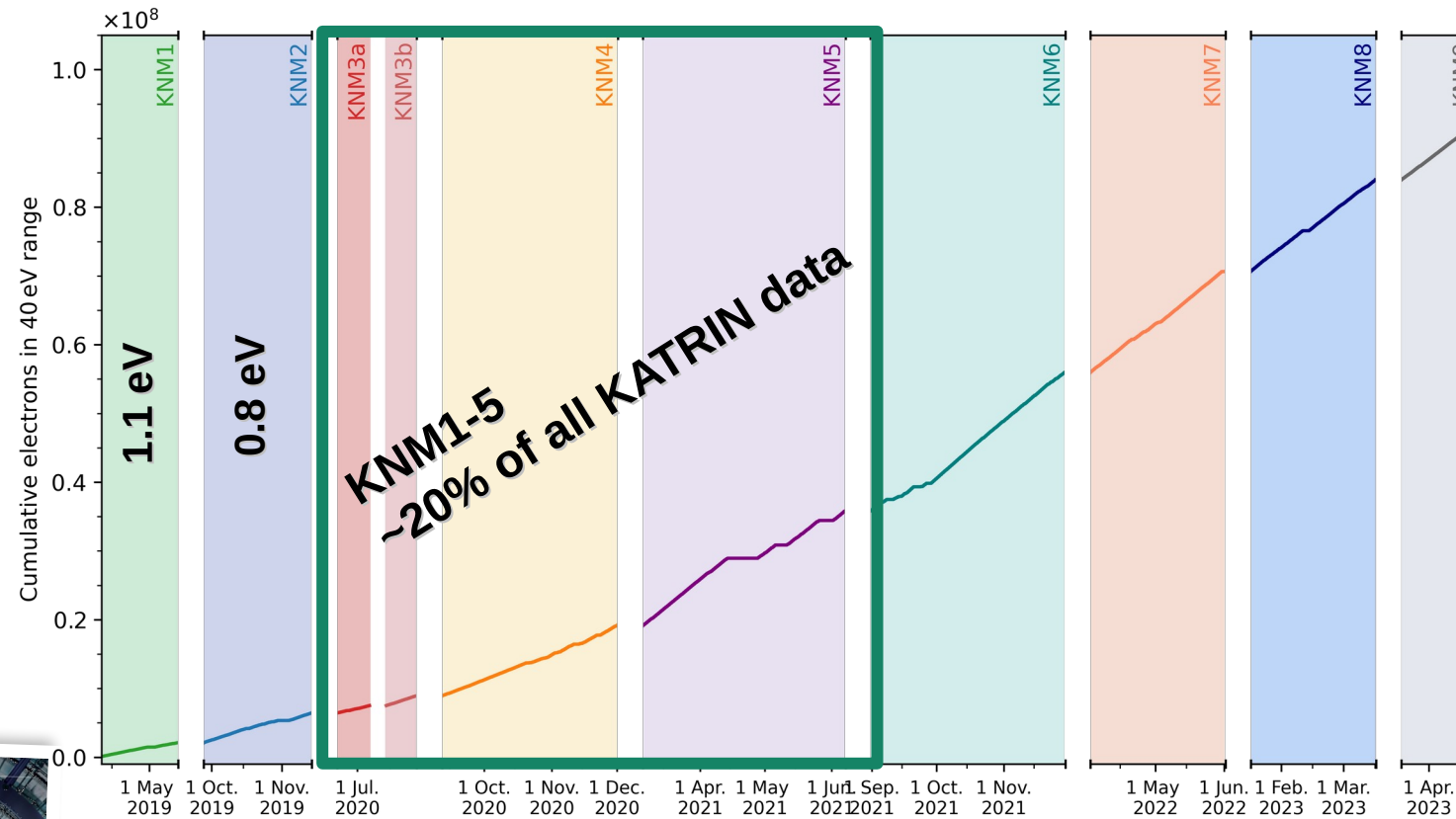
Systematics



KATRIN Data taking



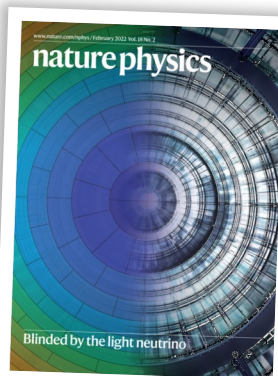
EPJ C 80, 264 (2020)



Analysis of 5 scientific runs → to be published soon

Statistical sensitivity ~ 0.5 eV (90% CL)

Nature Phys. 18 (2022) 160



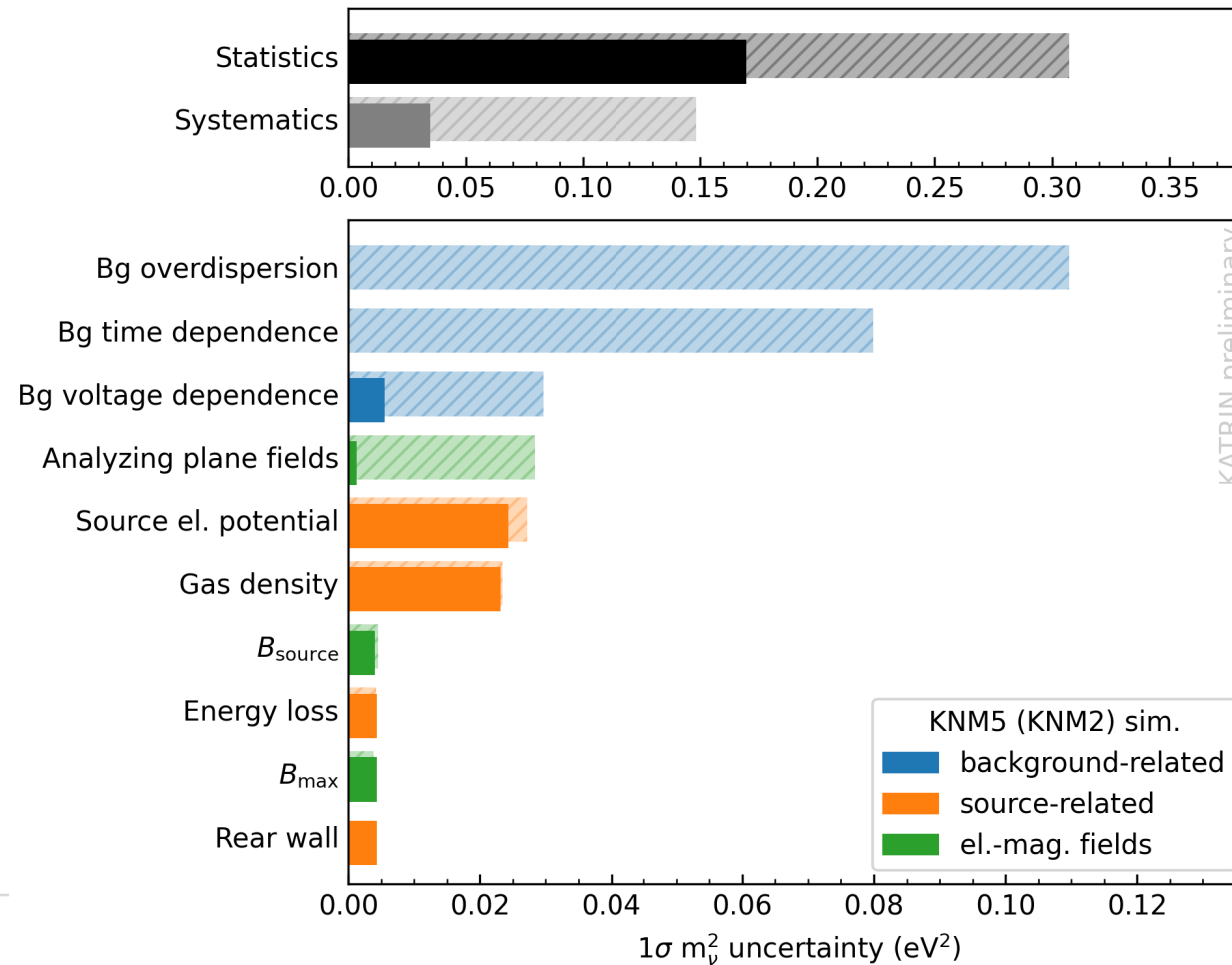
Nature Phys. 18 (2022) 160



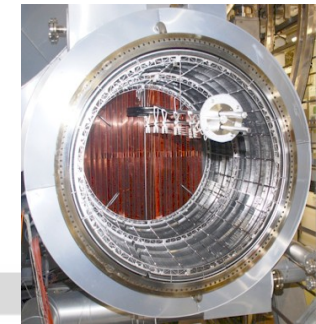
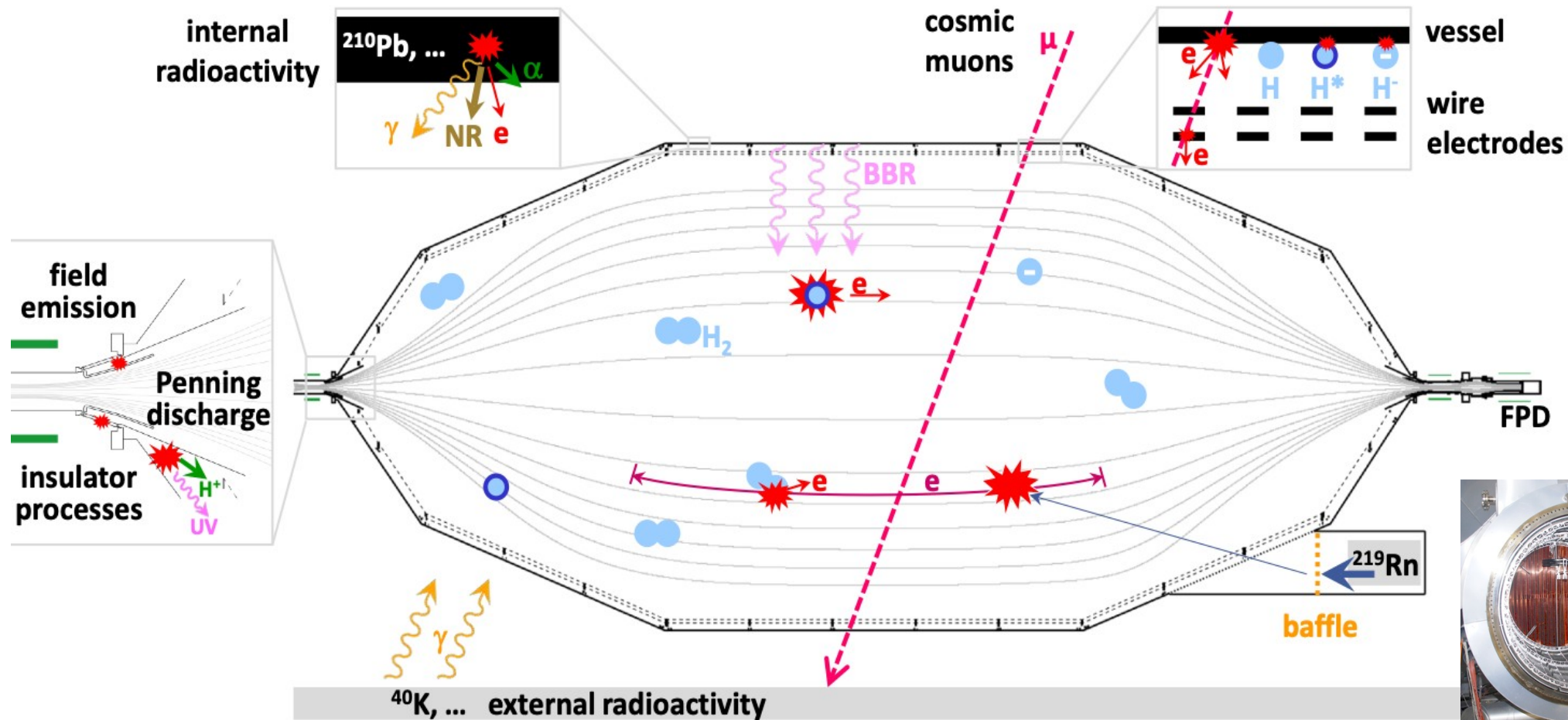
PRL 123 (2019) 221802
PRD 104 (2021) 012005

New data

- More statistics and lower systematics



Challenge: Background

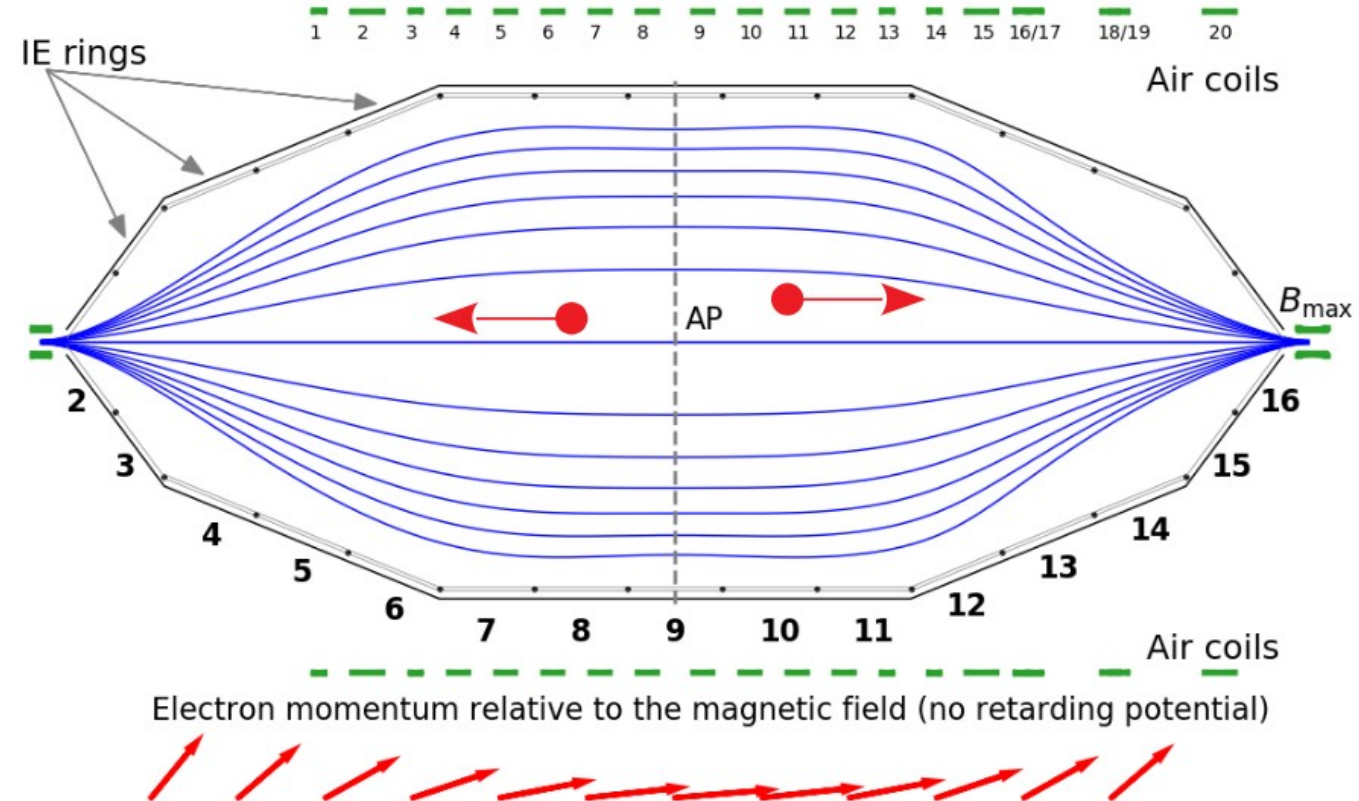


- Various sources of backgrounds identified

- All but one known sources are suppressed

Background reduction

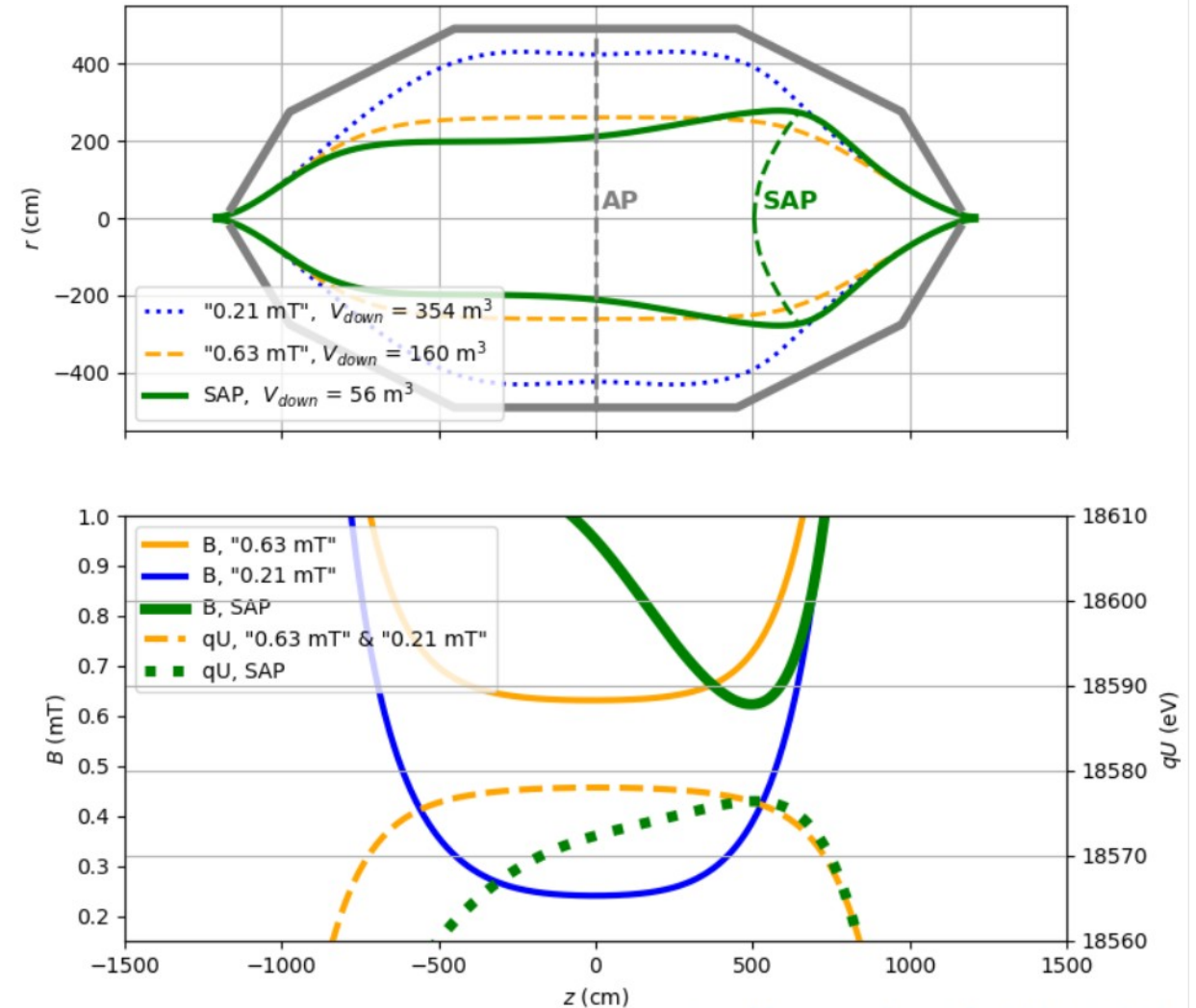
- Main component:
 - Highly excited (Rydberg) atoms
 - Uniformly distributed in the spectrometer
- Reducing volume → reducing background
 - Shifted analysing plane mode



$$\Delta E = \frac{B_{\min}}{B_{\max}} \cdot E$$

Background reduction

- Main component:
 - Highly excited (Rydberg) atoms
 - Uniformly distributed in the spectrometer
- Reducing volume → reducing background
 - **Shifted analysing plane** mode
- Factor 2 reduction of the background rate



Historical overview

2022:

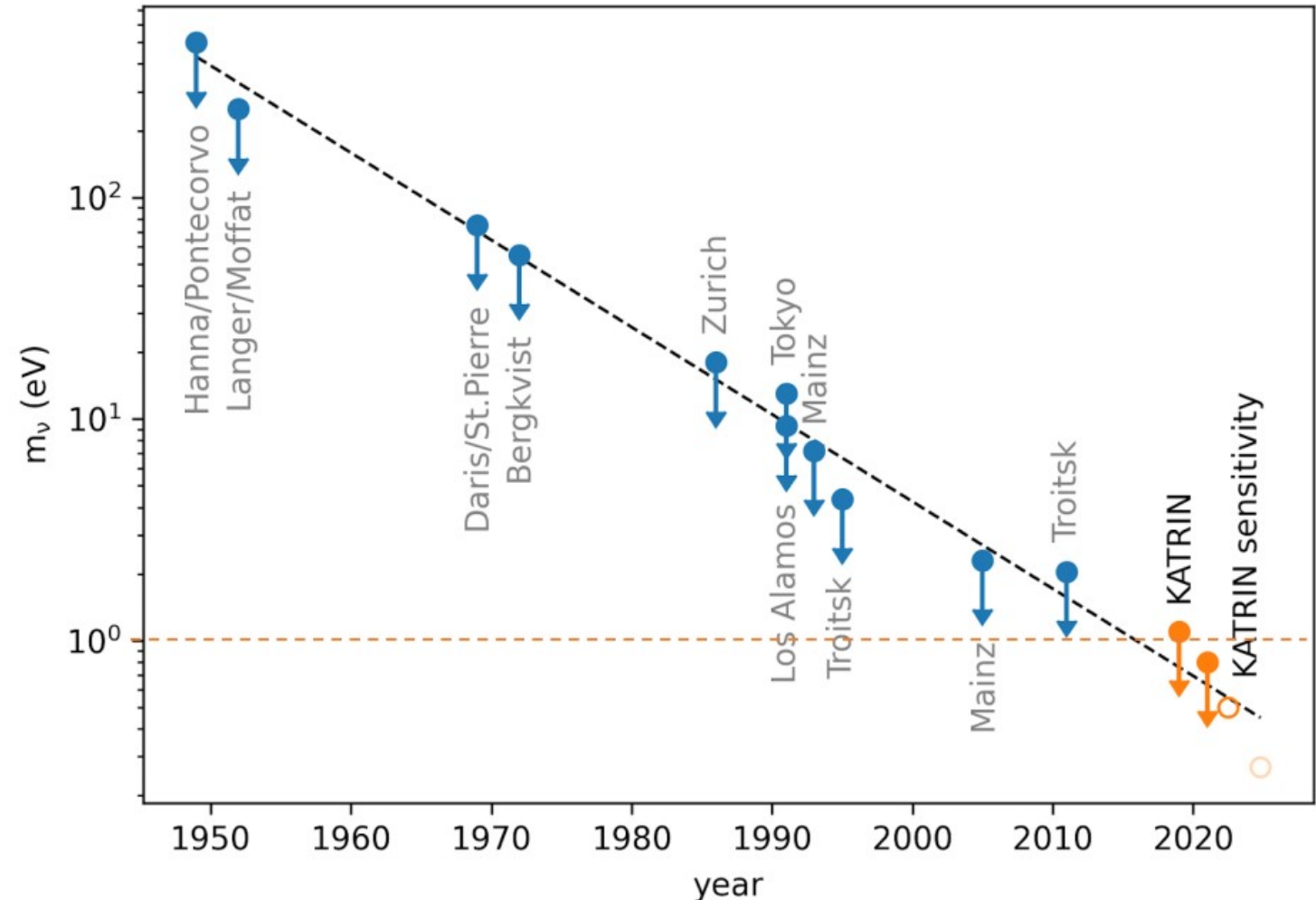
- first direct neutrino-mass experiment to reach sub-eV sensitivity and limit
- $m_\nu < 0.8 \text{ eV}$ (90% CL)
KATRIN Collab. Nat. Phys. 18, 160–166 (2022)

2023:

- Sensitivity: $m_\nu < 0.5 \text{ eV}$ (90% CL)

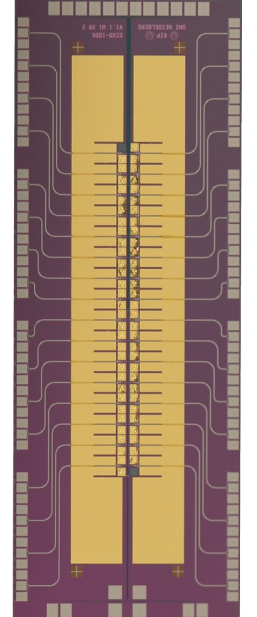
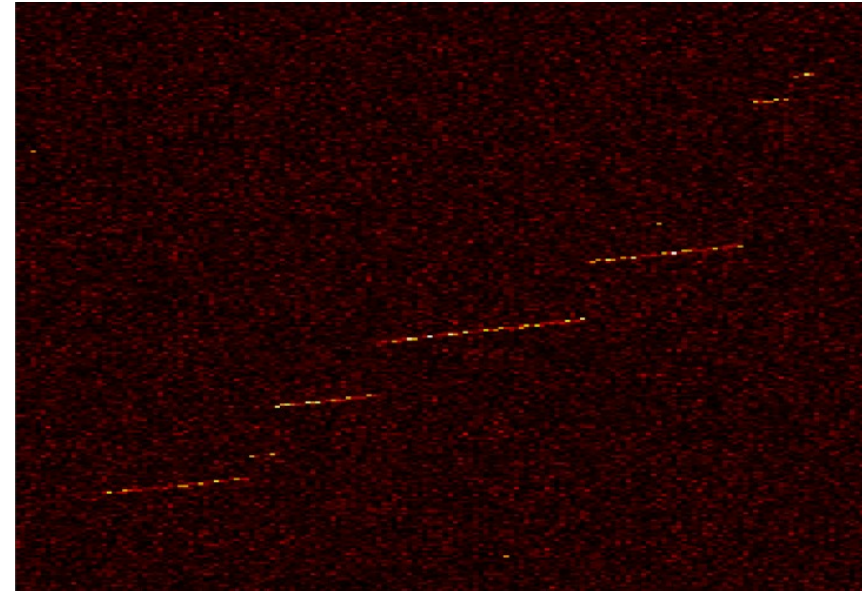
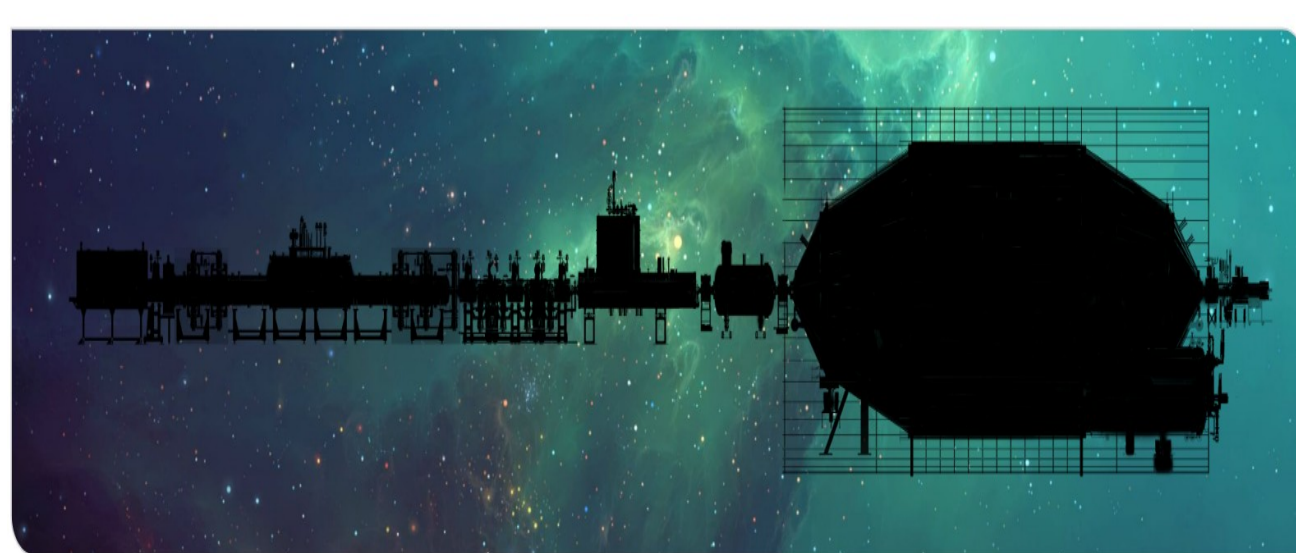
2025:

- Final goal: $m_\nu < 0.3 \text{ eV}$ (90% CL)



Neutrino mass determination – Part II

International School on Astroparticle Physics (ISAPP 2023) – Varenna, Italy
Alexey Lokhov



Outline

What do we know
so far about
neutrino masses?

Neutrinos are
massive

The squared mass
differences are
known

The absolute scale
is unknown

What are the three
approaches to
neutrino mass?

Cosmology, $0\nu 2\beta$ -
decay, direct
searches

Complementary
observables

Direct laboratory
measurements –
least model
dependent

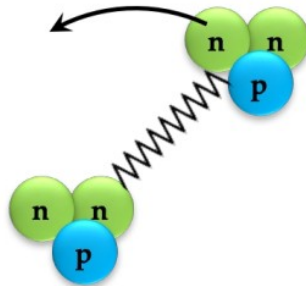
How to measure
the mass without
model
dependencies?

Current limit from
KATRIN
(MAC-E-Filter):
 < 0.8 eV (90% CL)

What other physics
can we probe in
the direct mass
measurements?

What type of limitations are there?

- Better statistics: more tritium
 - More scatterings → “Opaque” source
- “Different” tritium: atomic



- Differential measurement
 - Better use of statistics
 - Intrinsically less background

