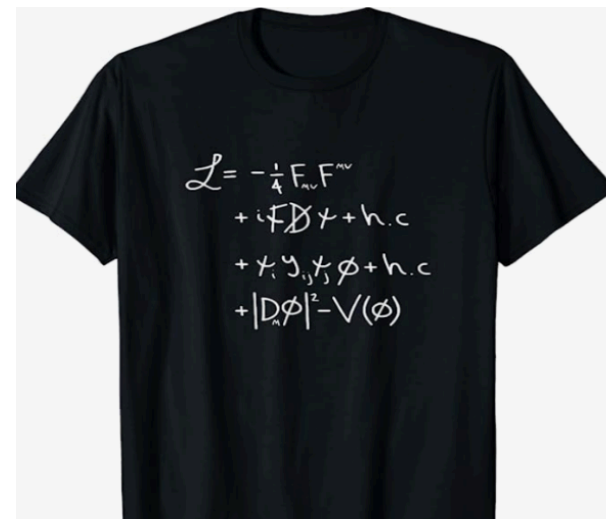


**MICRO-COSMOS**



# Basics on particle physics.

Structure of the

## Standard Model of particle physics

Antonio Masiero

University of Padua and INFN

- By the end of the 20<sup>th</sup> century ...  
**we have a comprehensive,  
fundamental theory of all  
observed forces of nature which  
has been tested and might be  
valid from the Planck length  
scale [ $10^{-33}$  cm.] to the edge of  
the universe [ $10^{+28}$  cm.]**

**D. Gross 2007**

# LECTURES I – II

- Where the **two infinities** touch each other: a bird's-eye view of the **Standard Models (SM) of particle physics and of cosmology**
- **Symmetries** and fundamental interactions
- The **QED** and **QCD** lessons
- **Spontaneous breaking** of a (gauge) symmetry and the **Higgs mechanism**. The appearance of the **electroweak energy scale**.
- The structure of the **SM of particle physics**.
- **Masses** and **mixings** of the SM **fermions**. **CP violation** in the SM
- The exceptional **points of strength** of the SM

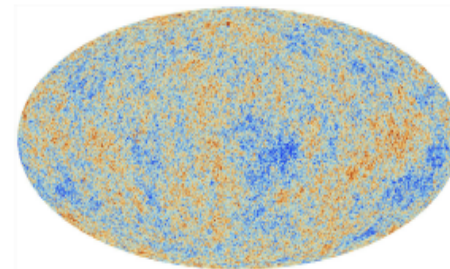
# In this last decade → the triumph of the STANDARD

- PARTICLE STANDARD MODEL
- COSMOLOGY STANDARD MODEL

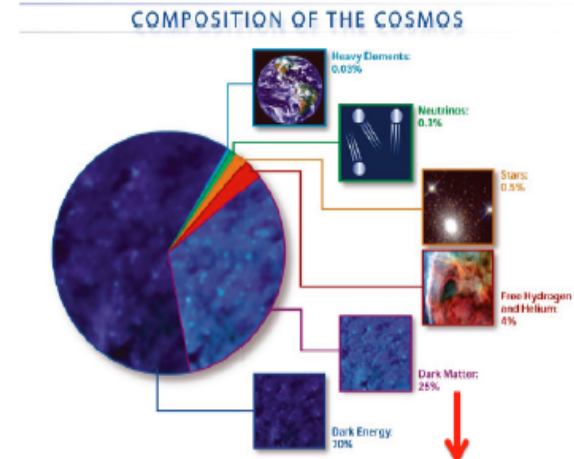
Three Generations of Matter (Fermions) spin  $\frac{1}{2}$

	I	II	III	
mass →	2.4 MeV	1.27 GeV	173.2 GeV	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
name →	u up	c charm	t top	g gluon
	Left Right	Left Right	Left Right	
	Left Right	Left Right	Left Right	
Quarks	4.8 MeV $-\frac{1}{3}$ d down	104 MeV $-\frac{1}{3}$ s strange	4.2 GeV $-\frac{1}{3}$ b bottom	$\gamma$ photon
	Left Right	Left Right	Left Right	
	Left Right	Left Right	Left Right	
	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	126 GeV Higgs boson spin 0
	Left Right	Left Right	Left Right	
	Left Right	Left Right	Left Right	
Leptons	0.511 MeV -1 e electron	105.7 MeV -1 $\mu$ muon	1.777 GeV -1 $\tau$ tau	91.2 GeV Z weak force
	Left Right	Left Right	Left Right	
	Left Right	Left Right	Left Right	
				80.4 GeV W <sup>±</sup> weak force

Bosons (Force s) spin 1

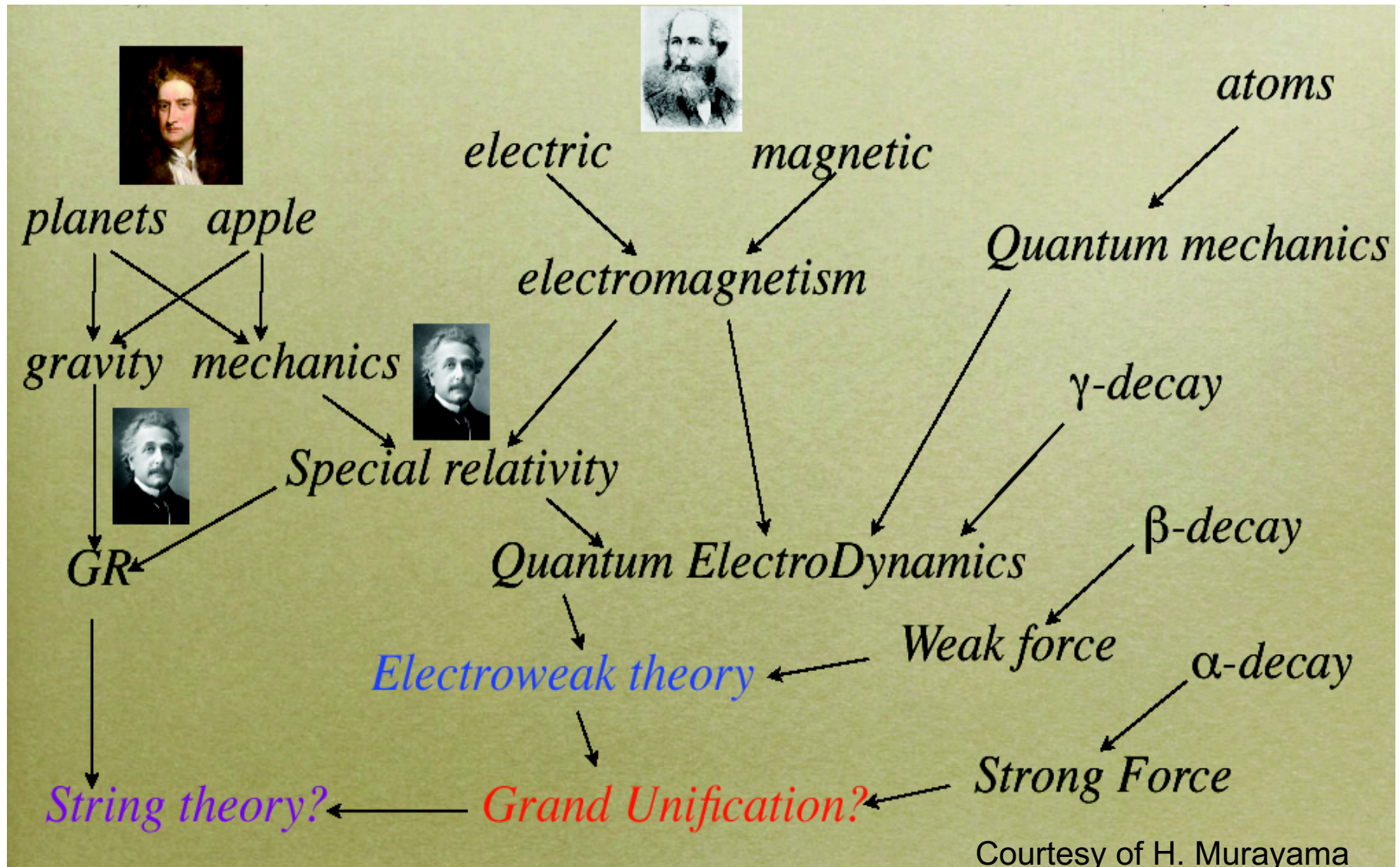


$\Lambda$ CDM + "SIMPLE" INFLATION

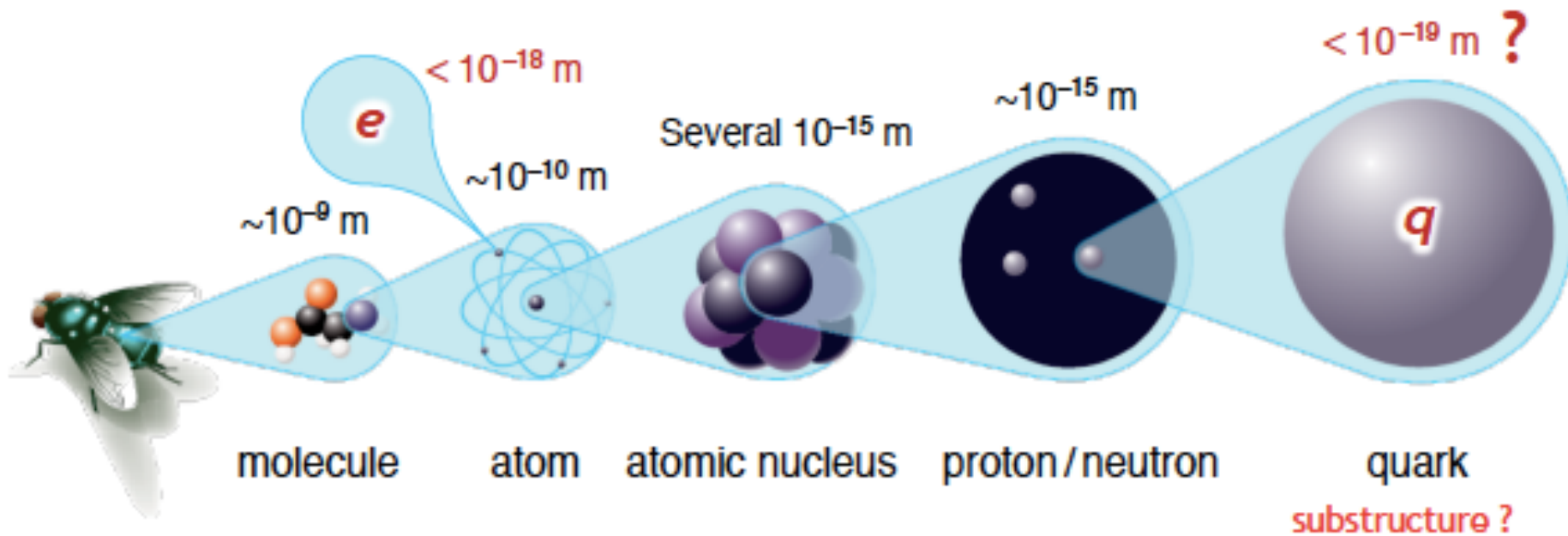




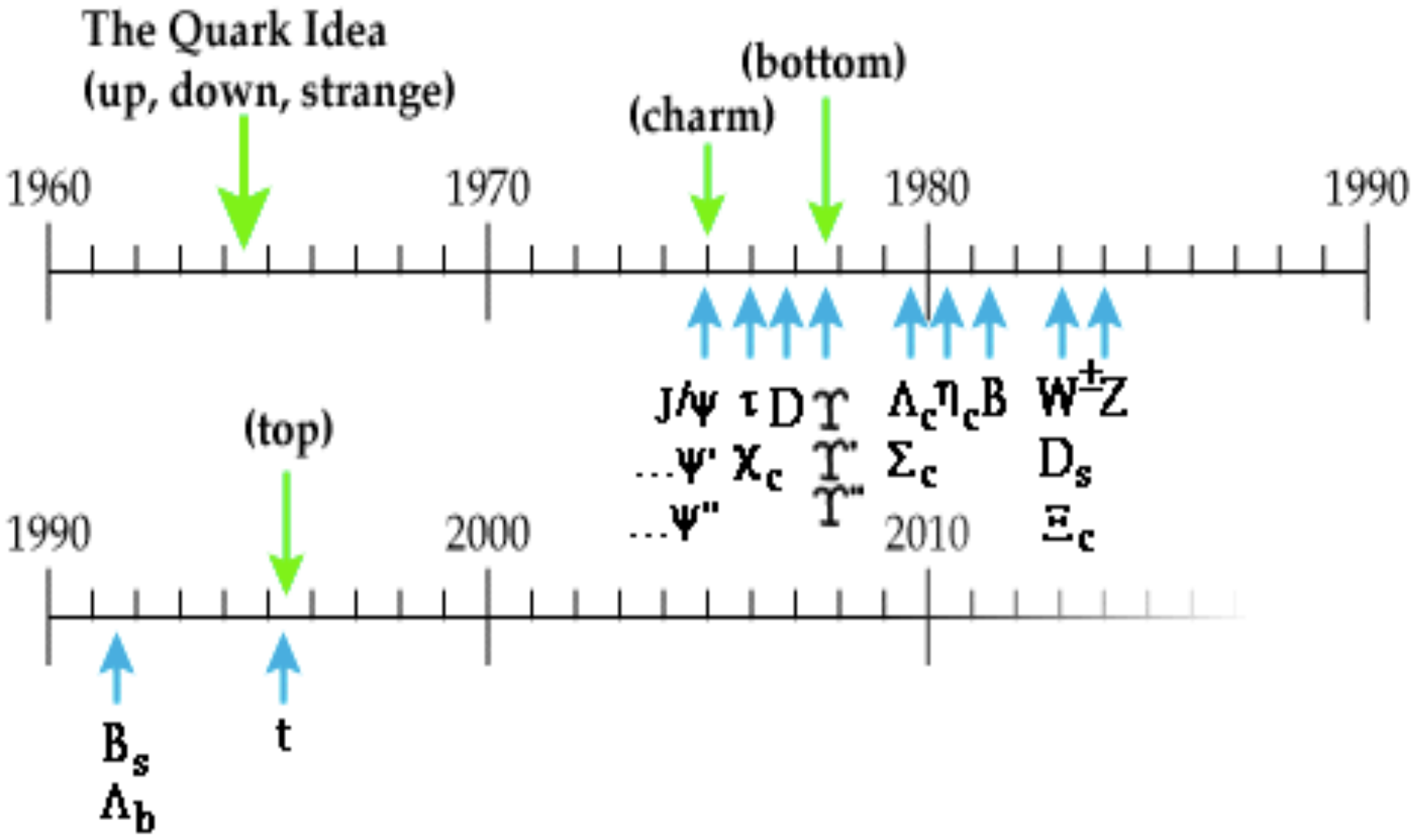
# UNIFICATION of FUNDAMENTAL INTERACTIONS



# MICRO-COSMOS



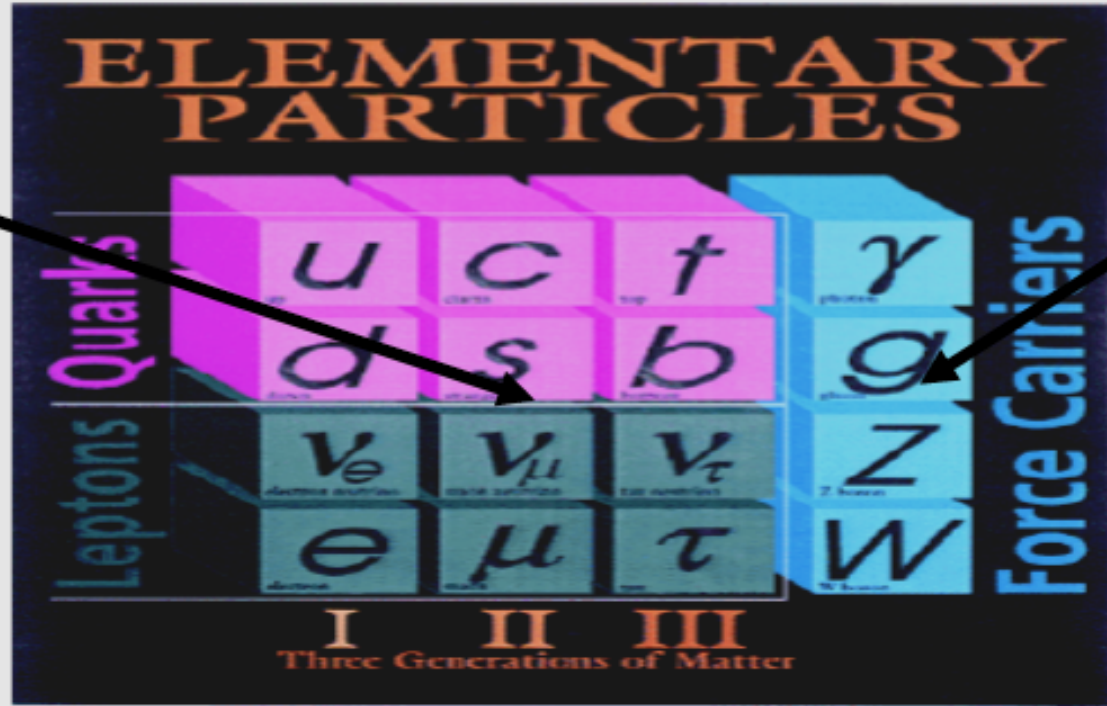
# HUNTING FOR THE QUARKS



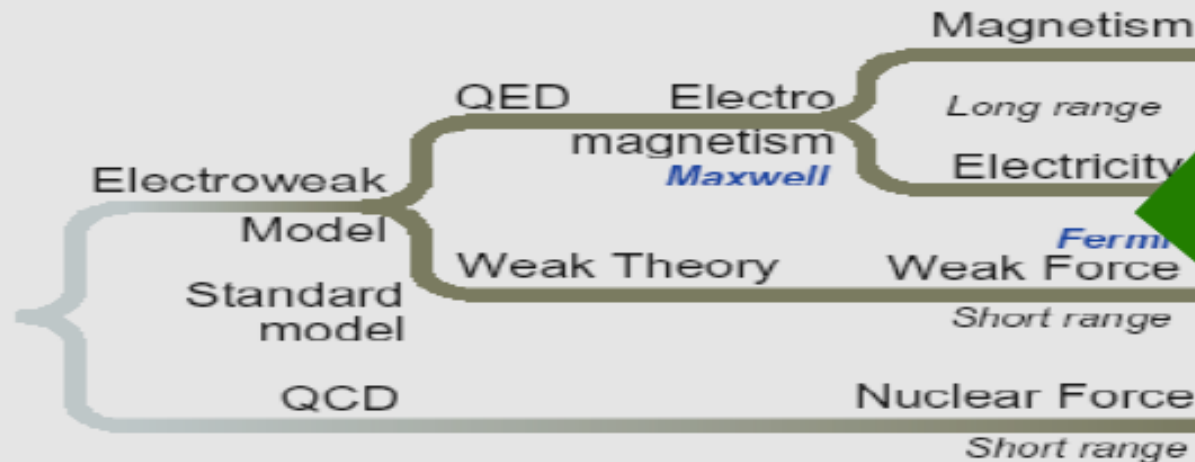
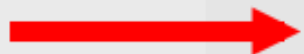
# SM OF ELEMENTARY PARTICLES AND FUNDAMENTAL INTERACTIONS

**MATTER**

**RADIATION**



**Grand  
Unified  
Theory  
GUT**



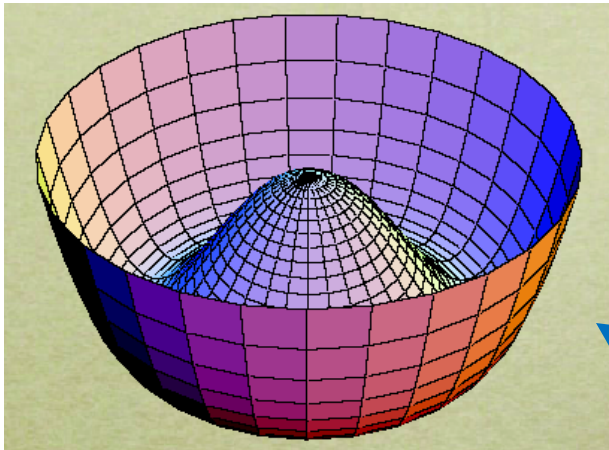
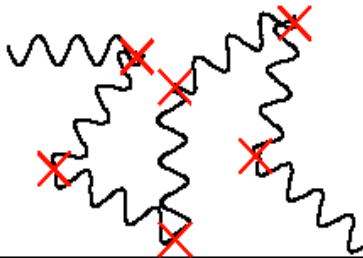


# The HIGGS BOSON CONDENSATE

gravity 

electric force 

weak force



- “SOMETHING” fills the Universe: it “disturbs” **Weak interactions** making them **SHORT-RANGED**, while it does **NOT** affect **gravity** or **electromagnetism**.
- WHAT IS IT?
- Analogy with **SUPERCONDUCTIVITY**: in a superconductor the magnetic field gets repelled (**Meissner effect**) and penetrates only over the “penetration length”, i.e. the magnetic field is short-ranged → source which disturbs are the **boson condensates**, **Cooper pairs**.
- We are “swimming” in **Higgs Boson Condensates** → its value at the minimum of its potential determines the masses of all particles!

# THE FERMION MASS PUZZLE

fermion masses

(large angle MSW)

$\nu_1$   $\nu_2$   $\nu_3$

$d$   $s$   $b$

$u$   $c$   $t$

$e$   $\mu$   $\tau$

$\mu\text{eV}$

$\text{meV}$

$\text{eV}$

$\text{keV}$

$\text{MeV}$

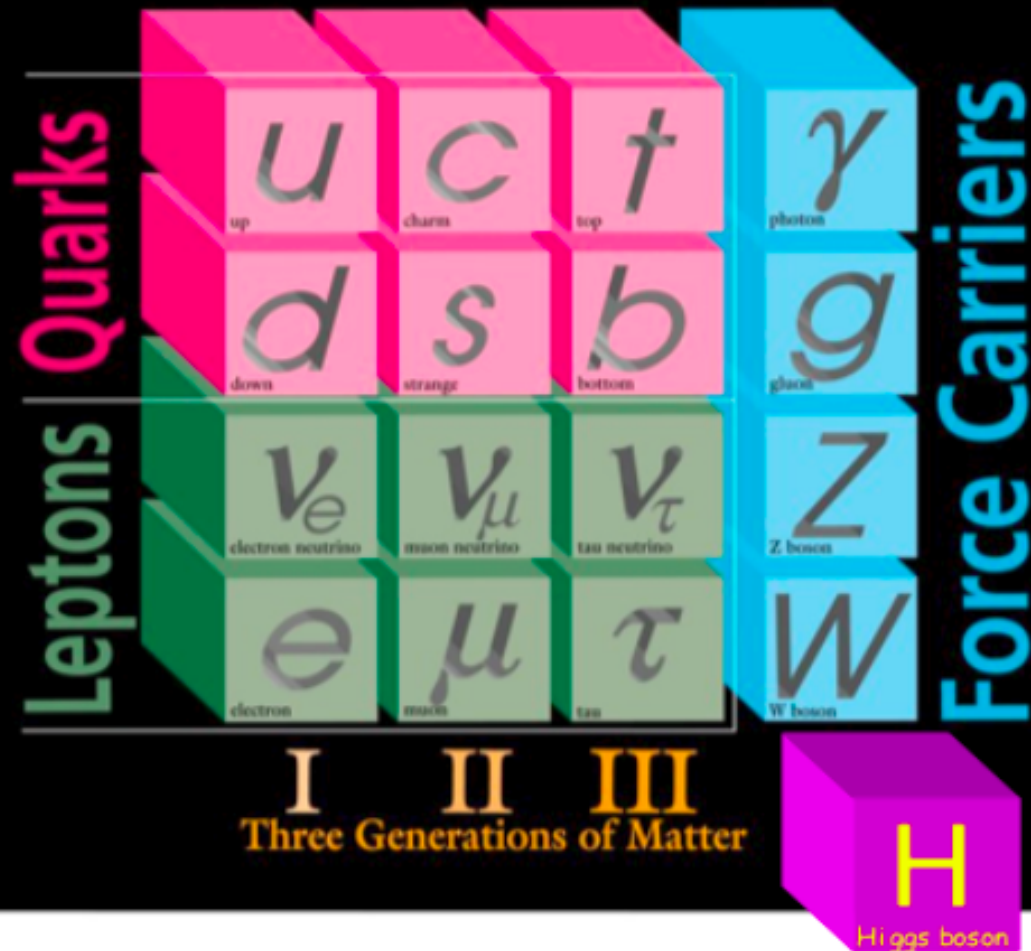
$\text{GeV}$

$\text{TeV}$



Gravity  
?

# The Standard Model



? →

EXP.  
2012

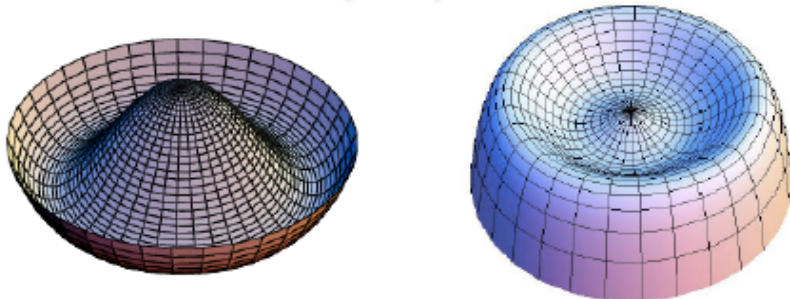


- PARTICLE STANDARD MODEL**

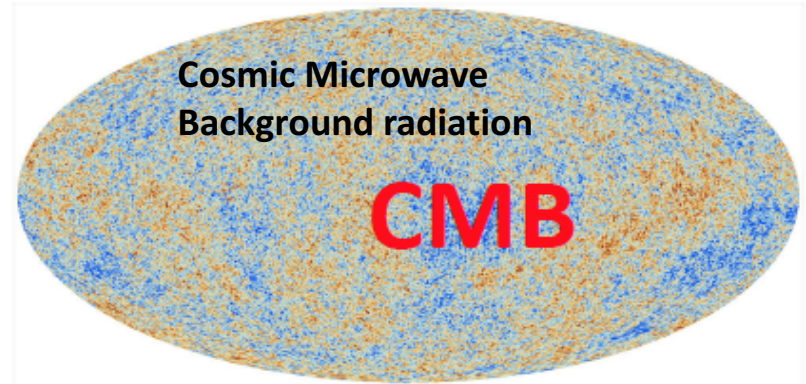


The **Higgs boson** and the destiny of the Universe

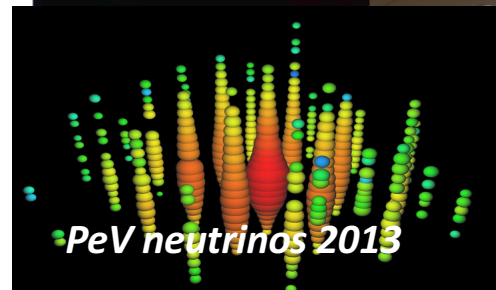
**STABILITY** ↔ **INSTABILITY**



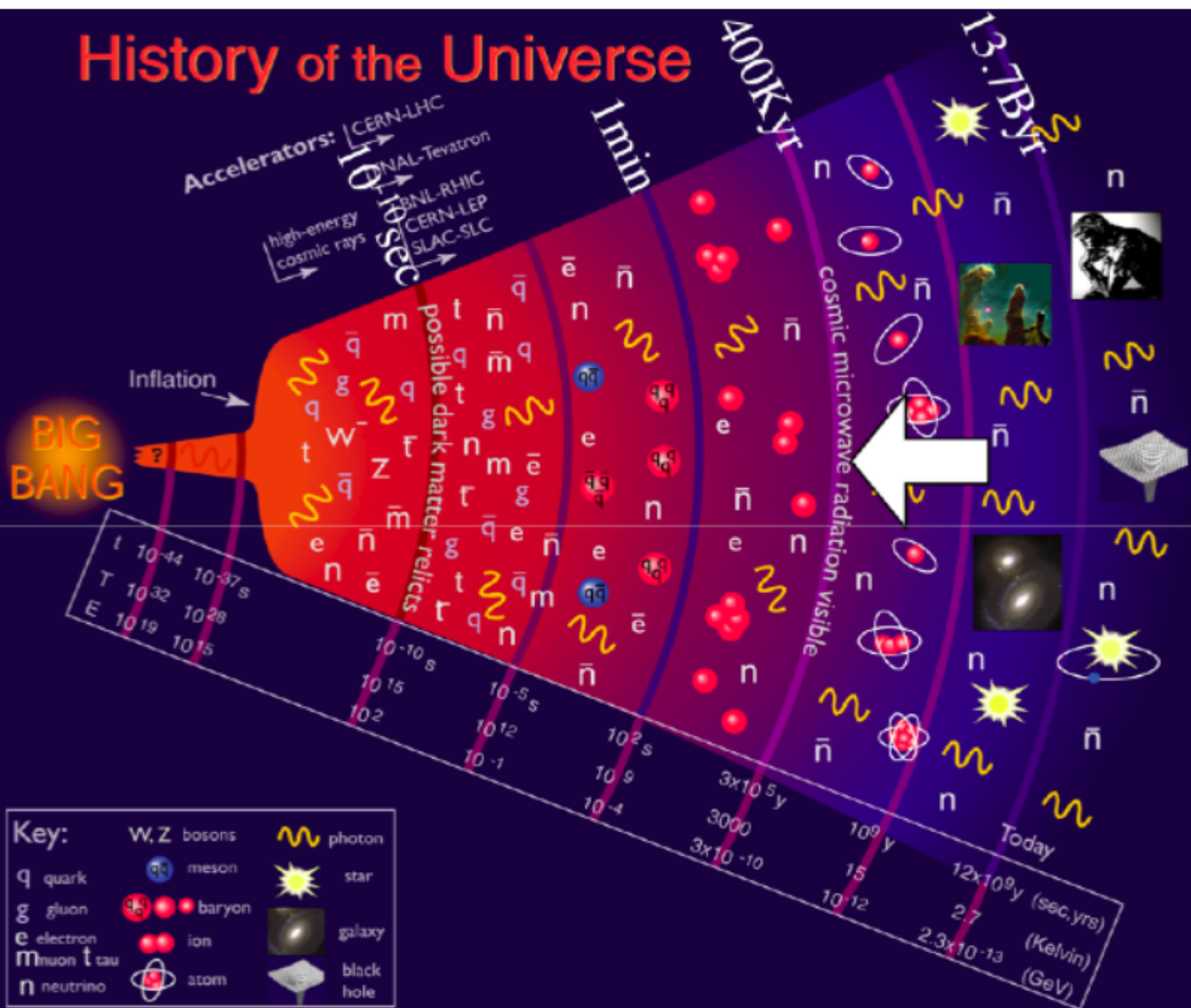
- COSMOLOGY STANDARD MODEL**



**GRAV. WAVES**



# History of the Universe



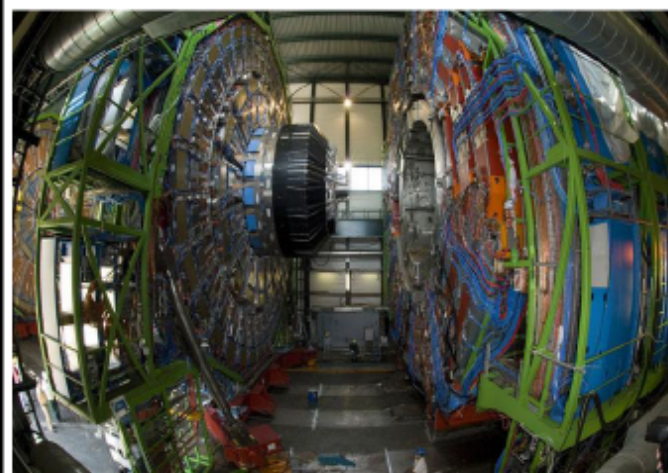
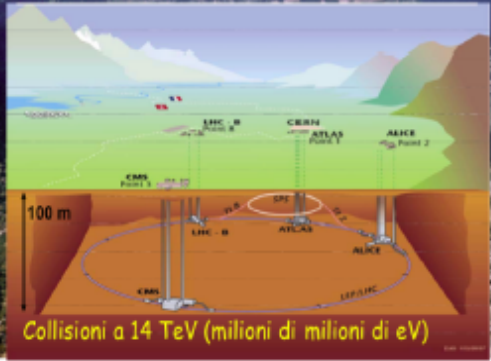


# History of the

Accelerators: CERN-LHC

high-energy cosmic rays

LHC at CERN



CMS



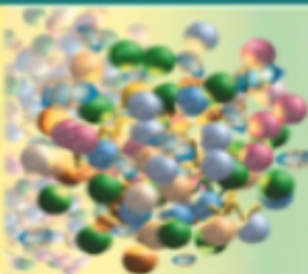



BIG BANG

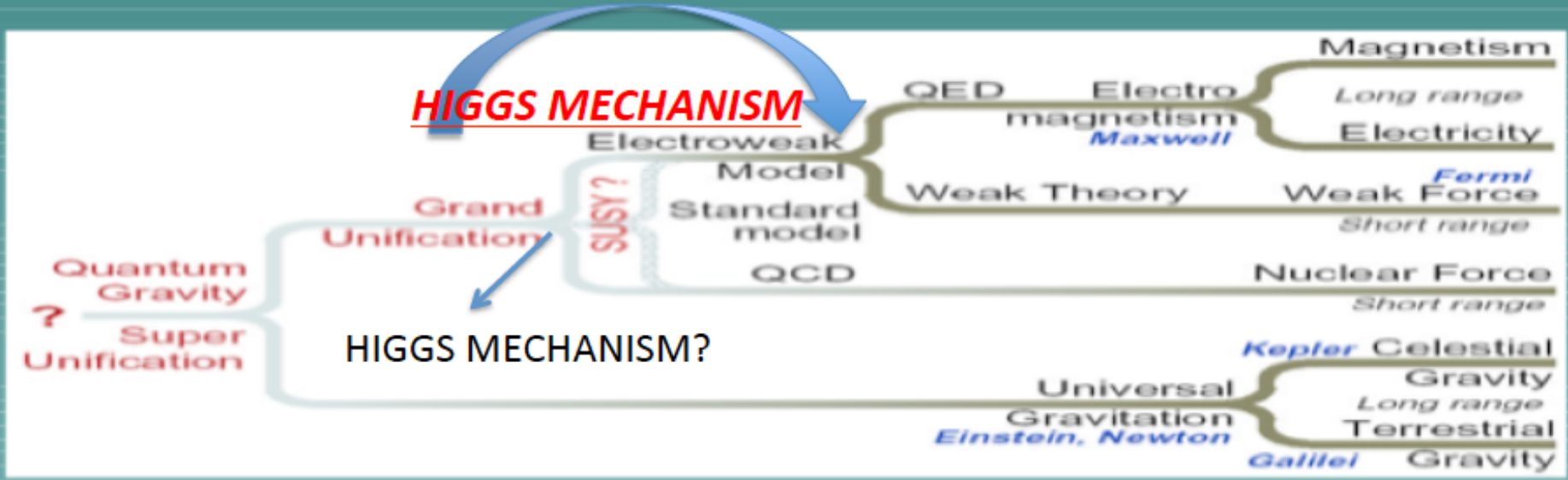
Inflation

$t$   $10^{-44}$   $10^{-37}$  s  
 $T$   $10^{32}$   $10^{28}$   
 $E$   $10^{19}$   $10^{16}$

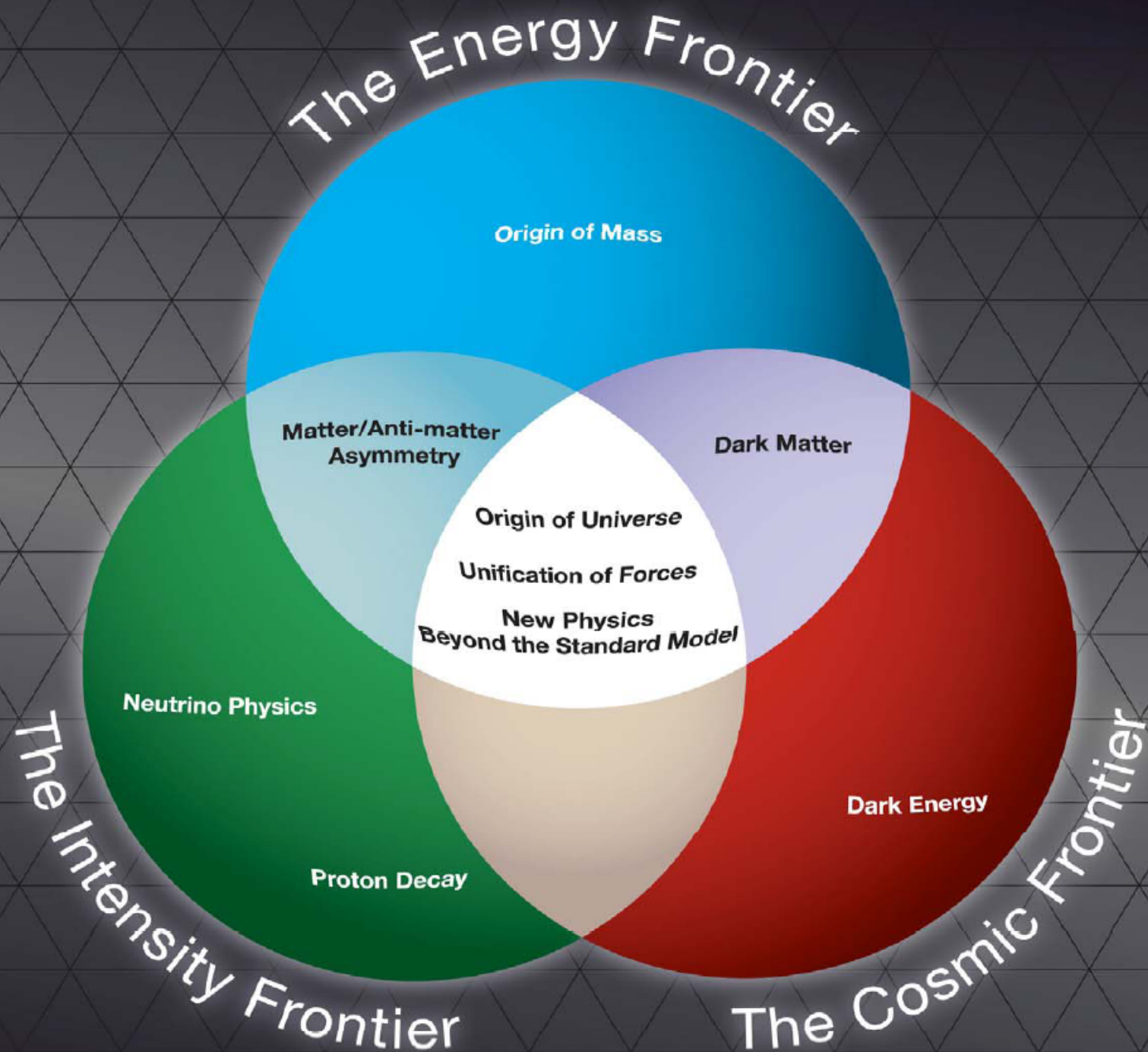
Key:

W, Z bosons  
 q quark  
 g gluon  
 e electron  
 $\mu$  muon  
 $\tau$  tau  
 n neutrino  
 meson  
 baryon  
 ion  
 atom  
 photon  
 star  
 galaxy  
 black hole

Big Bang	Quark-Gluon Plasma		Protoni e neutroni	Protoni e Nuclei leggeri	Atomi →Galassie →Molecole→DNA
<i>Gravità</i>	<i>Nucleare forte</i>	<i>Nucleare debole</i>			
					
$10^{-43}$ sec $10^{-35}$ m $10^{19}$ GeV	$10^{-32}$ sec $10^{-32}$ m $10^{16}$ GeV	$10^{-10}$ sec $10^{-18}$ m $10^2$ GeV	$10^{-4}$ sec $10^{-16}$ m 1 GeV	100 sec $10^{-15}$ m 1 MeV	300KY → 15GY $10^{-10}$ m 10 eV
???	LHC	LEP			As tronomia→

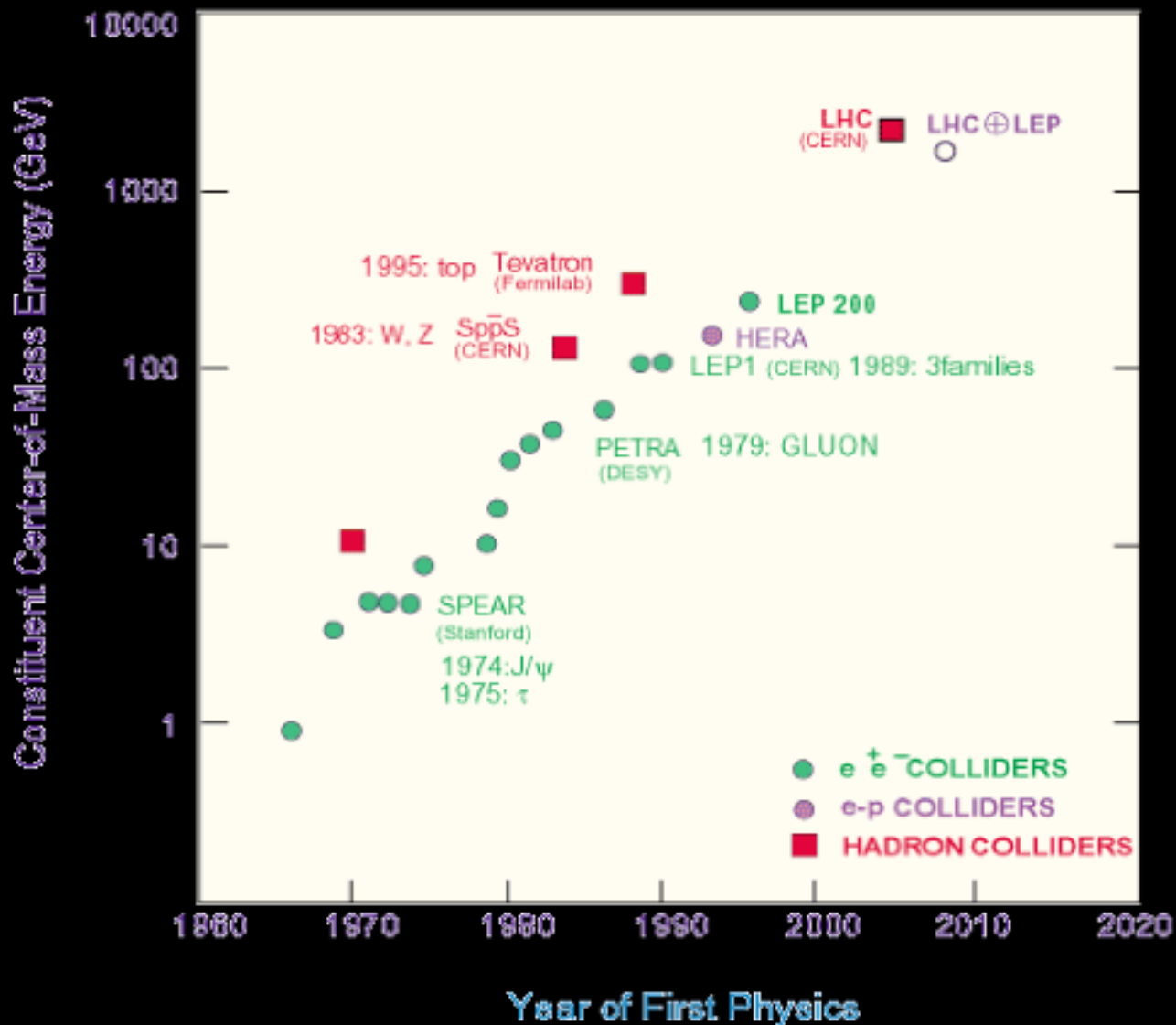


Theories:		
STRINGS?	RELATIVISTIC/QUANTUM	CLASSICAL

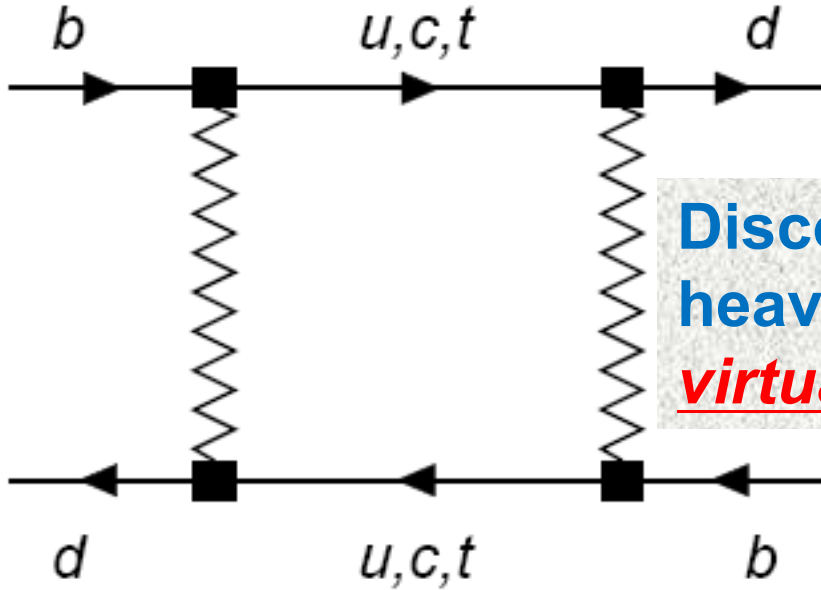




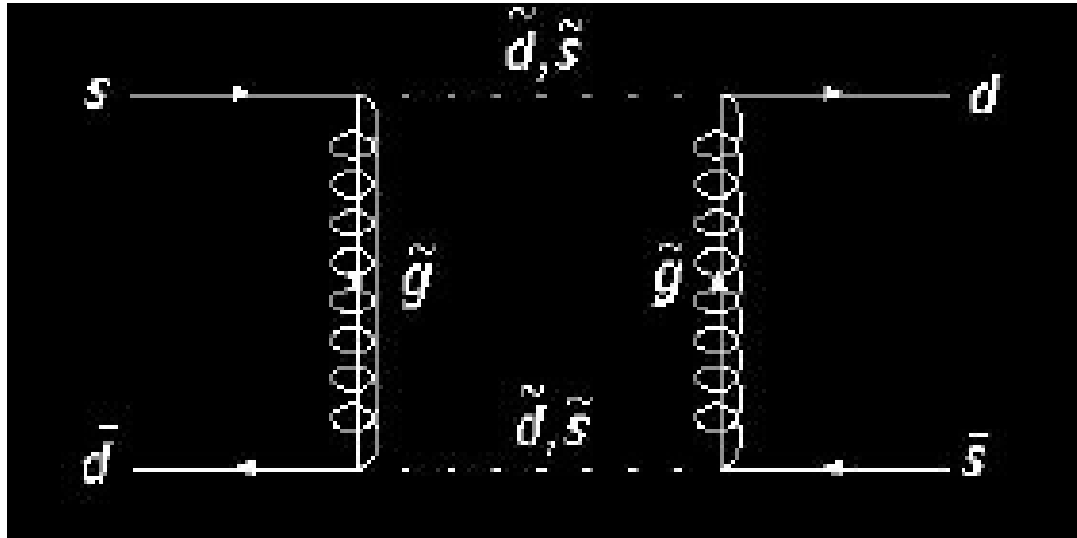
# THE HIGH-ENERGY ROAD



# THE HIGH-INTENSITY ROAD



Discovering the presence of the heavy up-type quarks through their virtual effects on physical processes

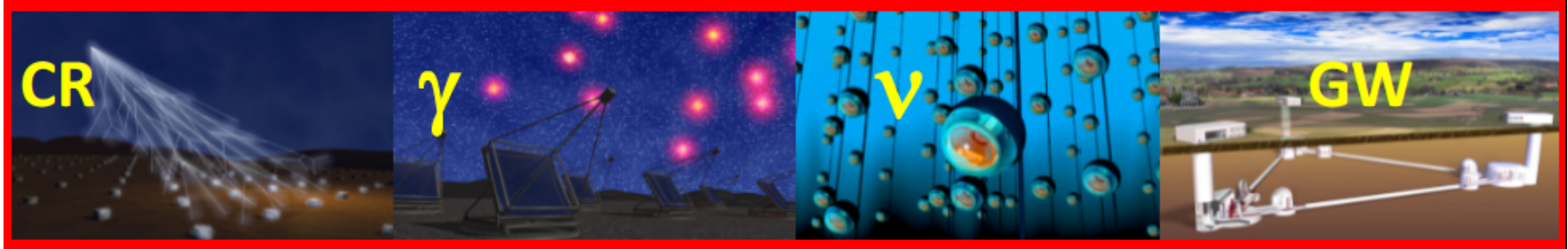


Looking for **NEW PARTICLES** through their virtual effects → **discrepancies** w.r.t. the **SM predictions**

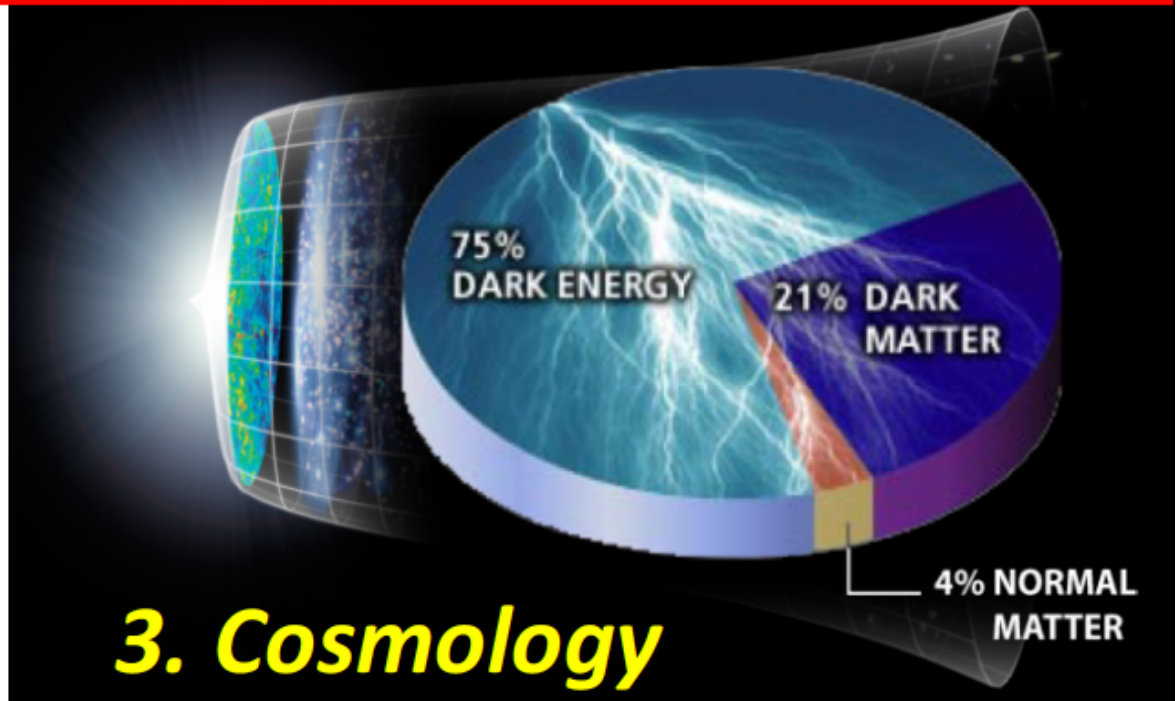


# THE ASTRO-PARTICLE PHYSICS ROAD

## 1. High-energy Universe: multi-messengers



## 2. Neutrino's



# 1. STANDARD MODEL

(2)

## SPONTANEOUSLY BROKEN GAUGE THEORY

BROKEN SYMMETRIES :

$\left\{ \begin{array}{l} \text{CONTINUOUS} \\ \text{DISCRETE} \\ \text{(e.g. PARITY)} \end{array} \right.$	$\left\{ \begin{array}{l} \text{GLOBAL} \\ \text{LOCAL (GAUGE)} \end{array} \right.$
	$\left\{ \begin{array}{l} \text{GLOBAL} \\ \text{LOCAL (GAUGE)} \end{array} \right.$

ex:  $(i\cancel{D} - m)\psi(x) = 0 \quad \cancel{D} \equiv \gamma^\mu \partial_\mu$

↓  
DIRAC EQ.  $\rightarrow$  free electron invariant

under:  $\psi(x) \rightarrow e^{i\alpha} \psi(x)$

$\alpha$  const.  $\rightarrow$  U(1) GLOBAL Symm.

U(1) LOCAL (GAUGE) Symm:

$\alpha$  const  $\rightarrow \alpha(x)$

$\uparrow$  param. of the U(1)  
rotation is a function of  $x(t, \vec{x})$

to enforce the local U(1) symm:

$\partial_\mu \rightarrow \cancel{D}_\mu \equiv \partial_\mu - ie A_\mu$   
 $\hookrightarrow$  covariant deriv.  $\hookrightarrow$  "compensating" vector (gauge) field

$A_\mu(x) \xrightarrow{U(1)} A_\mu(x) - \frac{i}{e} \partial_\mu \alpha(x)$

$(i\cancel{D} - m)\psi(x) = 0$  invar. under local U(1)

# QUANTUM ELECTRODYNAMICS

$$\begin{aligned}\mathcal{L} &= \bar{\psi} (i \gamma^\mu D_\mu - m) \psi \\ &= \bar{\psi} (i \gamma^\mu \partial_\mu - m) \psi - e Q A_\mu (\bar{\psi} \gamma^\mu \psi)\end{aligned}$$



Kinetic term:

$$\mathcal{L}_K = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \quad \longrightarrow \quad \partial_\mu F^{\mu\nu} = eQ (\bar{\psi} \gamma^\nu \psi) \quad \text{Maxwell}$$

Mass term:

$$[\text{exp: } m_\gamma < 1 \cdot 10^{-18} \text{ eV}]$$

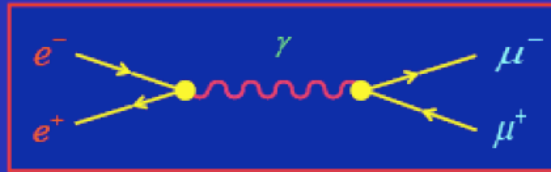
$$\mathcal{L}_M = \frac{1}{2} m_\gamma^2 A^\mu A_\mu \quad \text{Not Gauge Invariant} \quad \longrightarrow \quad m_\gamma = 0$$

Gauge Symmetry



QED Dynamics

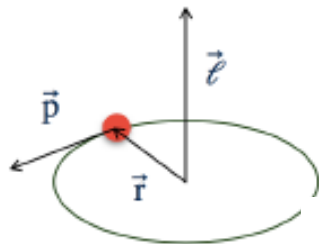
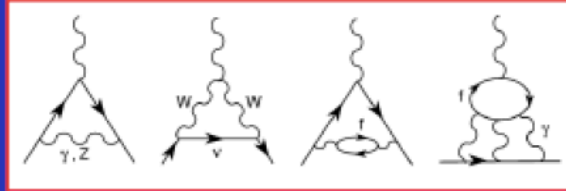
## Successful Theory



### Anomalous Magnetic Moment

$$\mu_l \equiv g_l \frac{e}{2m_l}$$

$$a_l \equiv \frac{1}{2} (g_l - 2)$$



- 1928: Dirac's equation unifies the two fields that revolutionized XX<sup>th</sup> century physics: special relativity and quantum mechanics.

The Dirac equation predicts that a unit of spin interacts with a magnetic field twice as much as a unit of orbital angular momentum: **g=2!**

Great triumph for the Dirac equation, but not the end of the story...

The motion of a classical particle of mass  $m$  and charge  $e$  with angular momentum

$$\vec{\ell} = \vec{r} \times \vec{p}$$

generates the (orbital) magnetic moment :

$$\vec{\mu}_\ell = \frac{e}{2m} \vec{\ell}$$

In 1925 Goudsmit & Uhlenbeck propose that the electron has an "internal rotation" characterised by a "spin"  $\vec{s}$  and an associated magnetic moment, like a tiny bar magnet:

$$\vec{\mu}_s = g \frac{e}{2m} \vec{s}$$

with **g = 2**, not 1! Very strange, but worked.





- 1948: With improvements in experimental techniques, Kusch & Foley measure  $g \neq 2$ ! The electron “magnetic moment anomaly” is:

$$a = (g-2)/2 = 0.00119(5)$$

What happened?? A relativistic **quantum field theory** of electromagnetism, ie Quantum ElectroDynamics (QED), is needed!

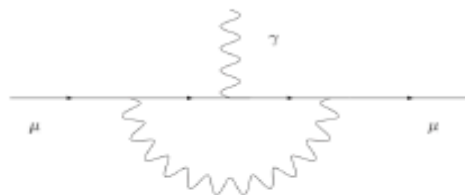
## QED contribution

- 1948: Schwinger, using Quantum ElectroDynamics (QED), predicts

$$a = (g-2)/2 = \alpha/(2\pi) = 0.00116$$

in perfect agreement with Kusch & Foley’s measurement

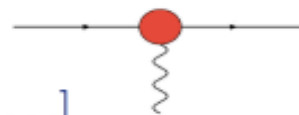
$$a = (g-2)/2 = 0.00119(5)$$



- Tremendous quantitative triumph for relativistic QFT (QED).
- Today we keep studying the lepton-photon vertex:

$$\Gamma^\mu = ie[\gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu}q_\nu}{2m}F_2(q^2) + \dots]$$

$$F_1(0) = 1 \quad F_2(0) = a$$



# "g – 2 is not an experiment: it is a way of life."

[John Adams (Head of the Proton Synchrotron at CERN (1954-1961))]

This statement also applies to many theorists! [Nyffeler '16]

$$a_{\mu}^{\text{QED}} = (1/2) (\alpha/\pi) \text{ [Schwinger, 1948]}$$

$$+ 0.765857426 (16) (\alpha/\pi)^2$$

[Sommerfield; Petermann; Suura&Wichmann '57; Elend '66]

$$+ 24.05050988 (28) (\alpha/\pi)^3$$

[Remiddi, Laporta, Barbieri...; Czarnecki, Skrzypek '99]

$$+ 130.8780 (60) (\alpha/\pi)^4$$

[Kinoshita et al. '81-'15; Steinhauser et al. '13-'16; Laporta '17]

$$+ 750.86 (88) (\alpha/\pi)^5 \text{ [Kinoshita et al. '90-'19]}$$

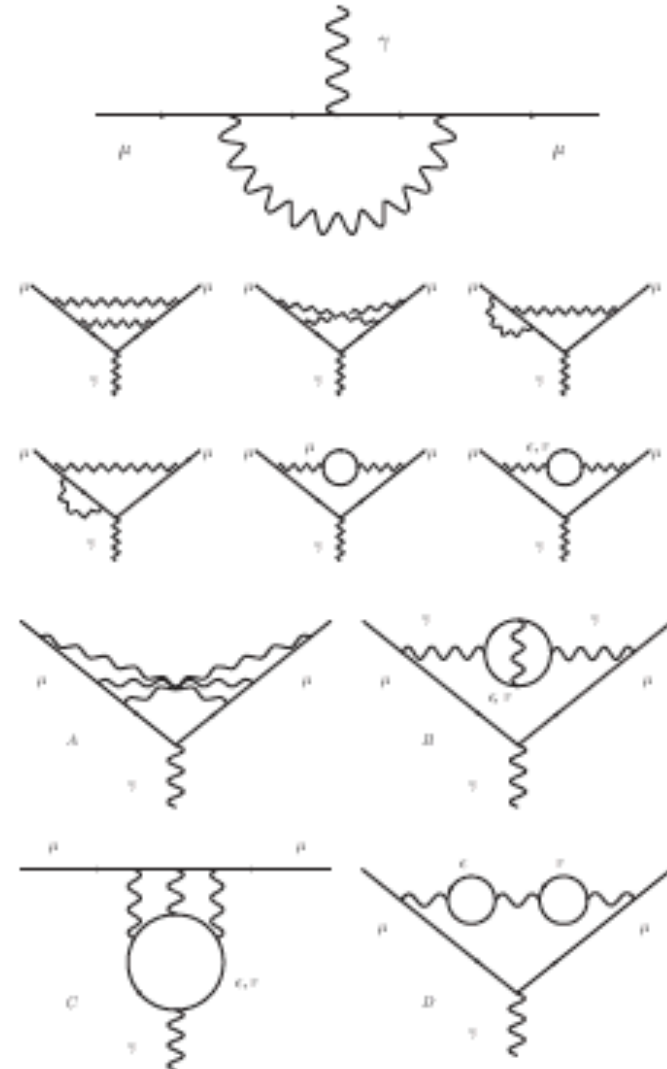
$$a_{\mu}^{\text{QED}} = 116584718.931 (19)(100)(23) \times 10^{-11}$$

mainly from 4-loop coeff. unc.  6-loop  from  $\alpha(\text{Ca})$

$\alpha = 1/137.035999046(27)$  [0.2ppb] Parker et al 2018

WP20 value

[WP20  $\equiv$  T. Aoyama et al., Phys. Rept. '20]



**NEW**

# Measurement of the Electron Magnetic Moment

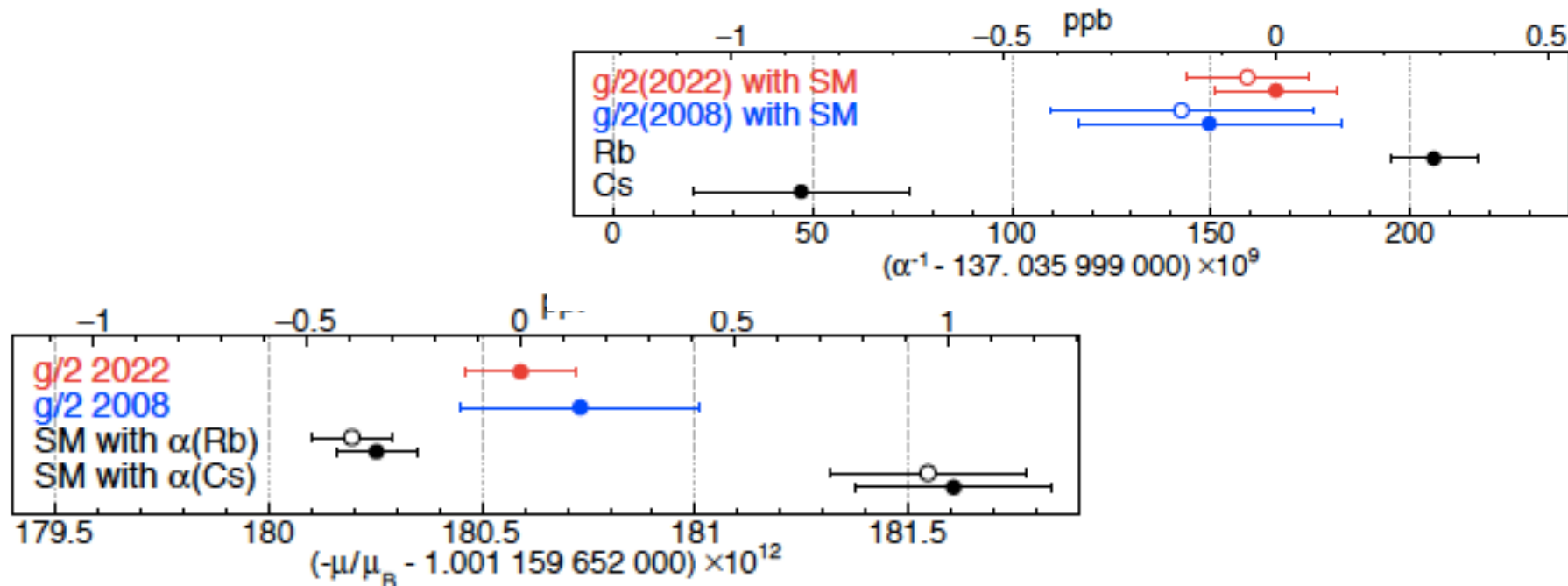
X. Fan,<sup>1,2,\*</sup> T. G. Myers,<sup>2</sup> B. A. D. Sukra,<sup>2</sup> and G. Gabrielse<sup>2,†</sup>

<sup>1</sup>*Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA*

<sup>2</sup>*Center for Fundamental Physics, Northwestern University, Evanston, Illinois 60208, USA*

(Dated: September 28, 2022)

The electron magnetic moment in Bohr magnetons,  $-\mu/\mu_B = 1.001\,159\,652\,180\,59(13)$  [0.13 ppt], is consistent with a 2008 measurement and is 2.2 times more precise. The most precisely measured property of an elementary particle agrees with the most precise prediction of the Standard Model (SM) to 1 part in  $10^{12}$ , the most precise confrontation of all theory and experiment. The SM test will improve further when discrepant measurements of the fine structure constant  $\alpha$  are resolved, since the prediction is a function of  $\alpha$ . The magnetic moment measurement and SM theory together predict  $\alpha^{-1} = 137.035\,999\,166(15)$  [0.11 ppb]





# QUANTUM CHROMODYNAMICS

$$\mathbf{q} \equiv \begin{pmatrix} \bar{q} \\ q \\ q \end{pmatrix}$$

**FREE QUARKS:**

$$\mathcal{L} = \bar{\mathbf{q}} [i \gamma^\mu \partial_\mu - m] \mathbf{q}$$

$$N_C = 3$$

**SU(3) Colour Symmetry:**

$$\mathbf{q} \rightarrow \mathbf{U} \mathbf{q} \quad ; \quad \bar{\mathbf{q}} \rightarrow \bar{\mathbf{q}} \mathbf{U}^\dagger$$

$$\mathbf{U} \mathbf{U}^\dagger = \mathbf{U}^\dagger \mathbf{U} = \mathbf{1} \quad ; \quad \det \mathbf{U} = 1 \quad ; \quad \mathbf{U} = \exp \left\{ i \frac{\lambda^a}{2} \theta_a \right\}$$

**Gauge Principle:**

Local Symmetry

$$\theta_a = \theta_a(x)$$

$$\mathbf{D}^\mu \mathbf{q} \equiv (\mathbf{I}_3 \partial^\mu + i g_s \mathbf{G}^\mu) \mathbf{q} \rightarrow \mathbf{U} \mathbf{D}^\mu \mathbf{q}$$

$$\mathbf{D}^\mu \rightarrow \mathbf{U} \mathbf{D}^\mu \mathbf{U}^\dagger \quad ; \quad \mathbf{G}^\mu \rightarrow \mathbf{U} \mathbf{G}^\mu \mathbf{U}^\dagger + \frac{i}{g_s} (\partial^\mu \mathbf{U}) \mathbf{U}^\dagger$$

$$[\mathbf{G}^\mu]_{\alpha\beta} \equiv \frac{1}{2} (\lambda^a)_{\alpha\beta} G_a^\mu(x)$$

**8 Gluon Fields**

## Kinetic Term:

$$\mathbf{G}^{\mu\nu} \equiv -\frac{i}{g_s} [\mathbf{D}^\mu, \mathbf{D}^\nu] = \partial^\mu \mathbf{G}^\nu - \partial^\nu \mathbf{G}^\mu + i g_s [\mathbf{G}^\mu, \mathbf{G}^\nu] \rightarrow \mathbf{U} \mathbf{G}^{\mu\nu} \mathbf{U}^\dagger$$

$$\mathbf{G}^{\mu\nu} \equiv \frac{\lambda^a}{2} G_a^{\mu\nu} \quad ; \quad G_a^{\mu\nu} = \partial^\mu G_a^\nu - \partial^\nu G_a^\mu - g_s f^{abc} G_b^\mu G_c^\nu$$

$$\mathcal{L}_K = -\frac{1}{2} \text{Tr} (\mathbf{G}^{\mu\nu} \mathbf{G}_{\mu\nu}) = -\frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a$$

## Mass Term:

$$\mathcal{L}_M = \frac{1}{2} m_G^2 G_a^\mu G_\mu^a$$

Not Gauge Invariant

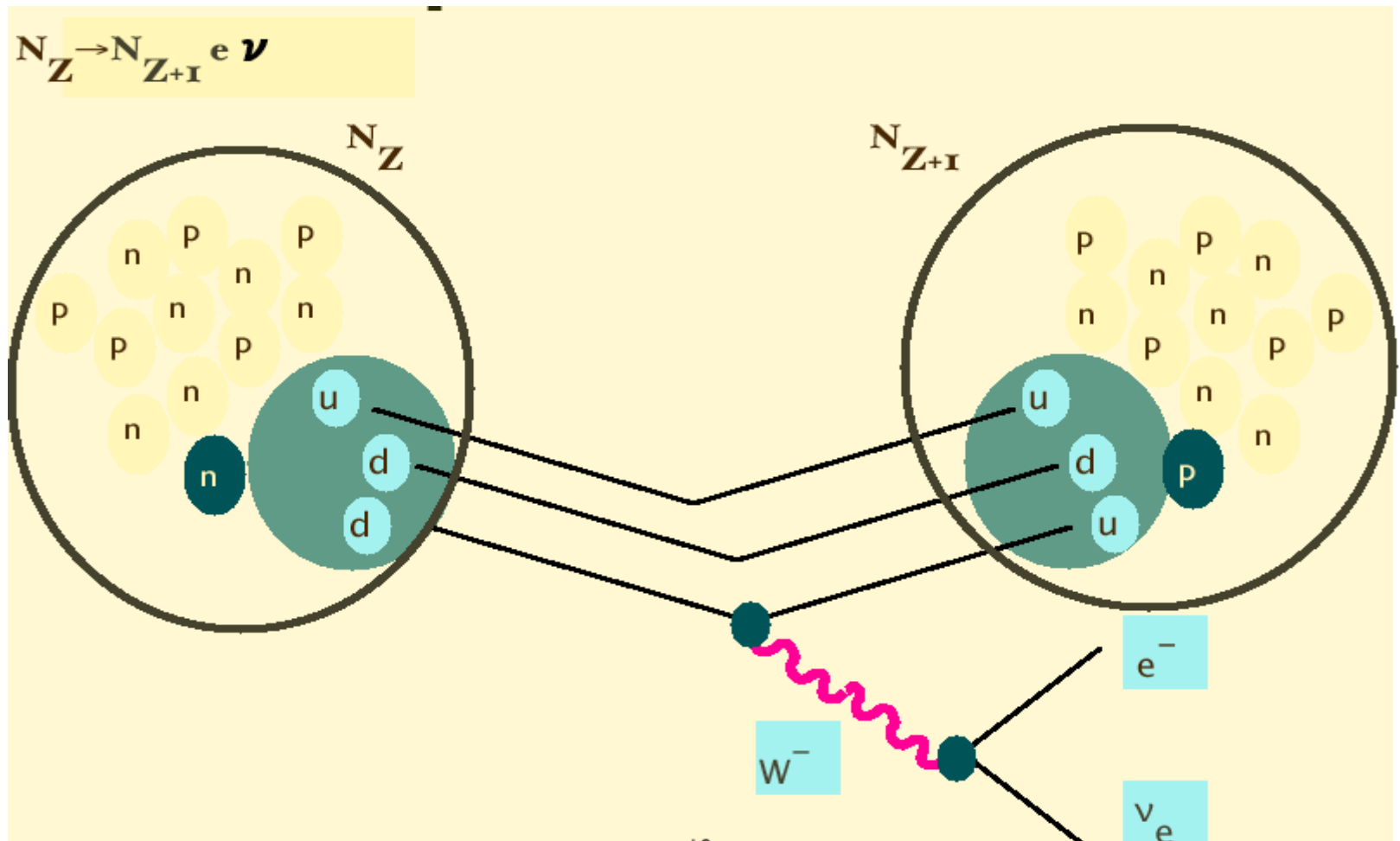


$$m_G = 0$$

Massless Gluons

# NUCLEUS $\beta$ -DECAY

(Nuclear) **WEAK** Interactions



# EXPERIMENTAL FACTS

Three Families

$$\begin{bmatrix} \nu_e & u \\ e^- & d' \end{bmatrix}, \quad \begin{bmatrix} \nu_\mu & c \\ \mu^- & s' \end{bmatrix}, \quad \begin{bmatrix} \nu_\tau & t \\ \tau^- & b' \end{bmatrix}$$

Family  
Structure

$$\begin{bmatrix} \nu_l & q_u \\ l^- & q_d \end{bmatrix} \equiv \left\{ \begin{pmatrix} \nu_l \\ l^- \end{pmatrix}_L, (\nu_l)_R, l_R^- \right\} ; \left\{ \begin{pmatrix} q_u \\ q_d \end{pmatrix}_L, (q_u)_R, (q_d)_R \right\}$$

Charged Currents

$$W^\pm \begin{cases} \text{Left-handed Fermions only} \\ \text{Flavour Changing: } \nu_l \Leftrightarrow l, q_u \Leftrightarrow q_d \end{cases}$$

Neutral currents

$$\gamma, Z \quad \text{Flavour Conserving}$$

Universality

(Family – Independent Couplings)

$$(\nu_l)_R \quad ?$$

$$SU(2)_L \otimes U(1)_Y$$

# GAUGE THEORY

Fields	$\psi_1(x)$	$\psi_2(x)$	$\psi_3(x)$
Quarks	$\begin{pmatrix} q_u \\ q_d \end{pmatrix}_L$	$(q_u)_R$	$(q_d)_R$
Leptons	$\begin{pmatrix} \nu_l \\ l^- \end{pmatrix}_L$	$(\nu_l)_R$	$(l^-)_R$

Free Lagrangian for Massless Fermions:

$$\mathcal{L}_0 = \sum_j i \bar{\psi}_j \gamma^\mu \partial_\mu \psi_j$$

$SU(2)_L \otimes U(1)_Y$  Flavour Symmetry:

$$U_L \equiv \exp \left\{ i \frac{\vec{\sigma}}{2} \vec{\alpha} \right\}$$

$$\begin{aligned} \psi_1 &\rightarrow e^{iy_1\beta} U_L \psi_1 & ; & \quad \psi_2 \rightarrow e^{iy_2\beta} \psi_2 & ; & \quad \psi_3 \rightarrow e^{iy_3\beta} \psi_3 \\ \bar{\psi}_1 &\rightarrow \bar{\psi}_1 U_L^\dagger e^{-iy_1\beta} & ; & \quad \bar{\psi}_2 \rightarrow \bar{\psi}_2 e^{-iy_2\beta} & ; & \quad \bar{\psi}_3 \rightarrow \bar{\psi}_3 e^{-iy_3\beta} \end{aligned}$$

## 4 Massless Gauge Bosons

$$W_\mu^\pm, W_\mu^3, B_\mu^0$$

## CHARGED CURRENTS

$$\mathbf{W}_\mu \equiv \frac{\vec{\sigma}}{2} \cdot \vec{W}_\mu = \frac{1}{2} \begin{pmatrix} W_\mu^3 & \sqrt{2} W_\mu^\dagger \\ \sqrt{2} W_\mu & -W_\mu^3 \end{pmatrix} ; \quad W_\mu \equiv \frac{1}{\sqrt{2}} (W_\mu^1 + i W_\mu^2)$$

$$\mathcal{L}_{\text{cc}} = -\frac{g}{2\sqrt{2}} W_\mu^\dagger \left[ \bar{q}_u \gamma^\mu (1-\gamma_5) q_d + \bar{\nu}_l \gamma^\mu (1-\gamma_5) l \right] + \text{h.c.}$$

**Quark / Lepton Universality ; Left-Handed Interaction**

## NEUTRAL CURRENTS

$$\begin{pmatrix} W_\mu^3 \\ B_\mu \end{pmatrix} \equiv \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} Z_\mu \\ A_\mu \end{pmatrix}$$

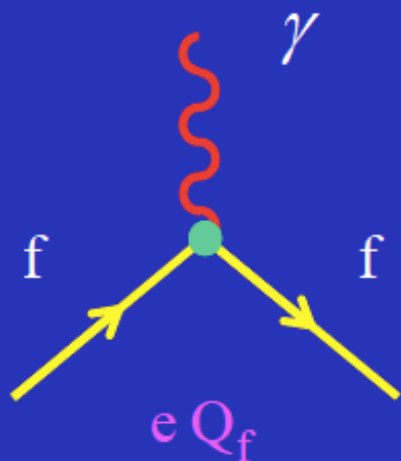
$$g \sin \theta_W = g' \cos \theta_W = e \quad ; \quad y_1 = Q_u - \frac{1}{2} = Q_d + \frac{1}{2} \quad ; \quad y_2 = Q_u \quad ; \quad y_3 = Q_d$$

$$\mathcal{L}_{\text{NC}} = -e A_\mu \sum_j \bar{\psi}_j \gamma^\mu Q_j \psi_j + \mathcal{L}_{\text{NC}}^Z$$

$$Q_1 = \begin{pmatrix} Q_u & 0 \\ 0 & Q_d \end{pmatrix} ; \quad Q_2 = Q_u \quad ; \quad Q_3 = Q_d$$

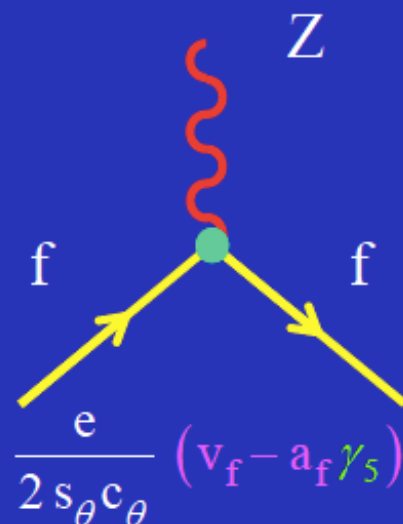
**Electroweak  
Unification**

## NEUTRAL CURRENTS

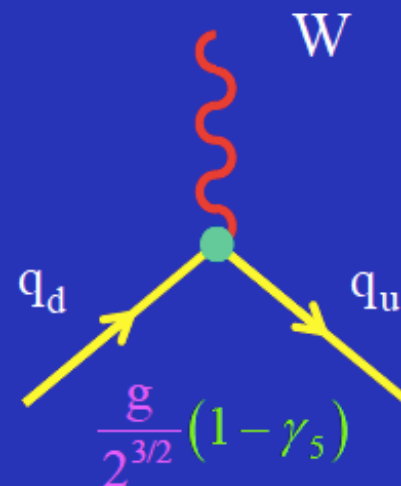
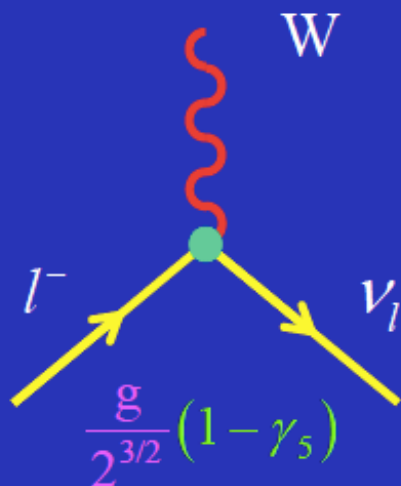


$$a_f = T_3^f = \pm \frac{1}{2}$$

$$v_f = T_3^f (1 - 4 |Q_f| \sin^2 \theta_w)$$



## CHARGED CURRENTS

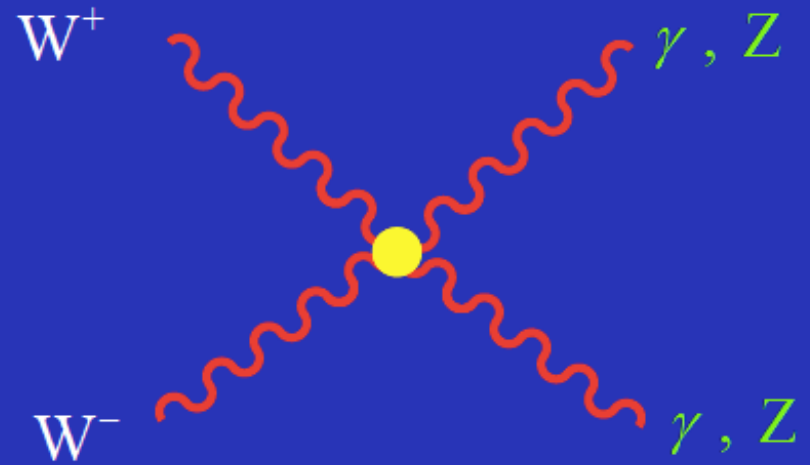
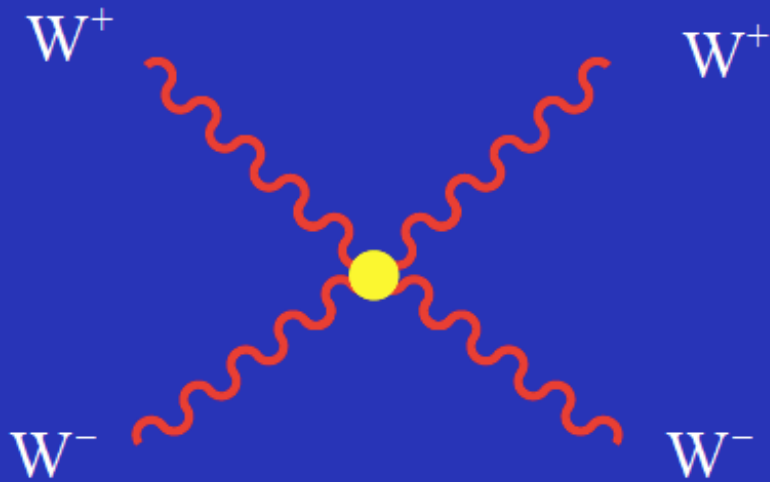
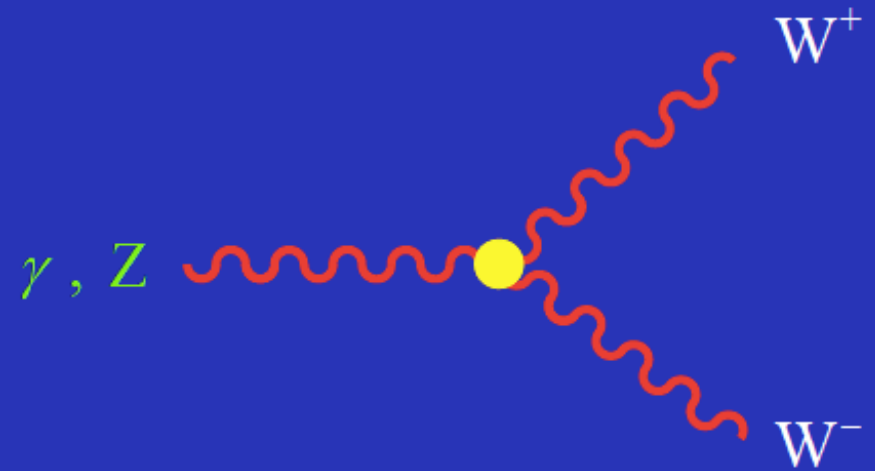


$y(\nu_R) = Q_\nu = 0 \Rightarrow$  No  $\nu_R$  Interactions

**Sterile Neutrinos**



# GAUGE SELF-INTERACTIONS



# PROBLEM WITH MASS SCALES

Gauge Symmetry



$$m_\gamma = 0$$

Good

$$M_W = M_Z = 0$$

Bad!



$$M_W = 80.40 \text{ GeV}$$

$$M_Z = 91.19 \text{ GeV}$$

Moreover

$$\mathcal{L}_{m_f} \equiv -m_f \bar{f} f = -m_f (\bar{f}_L f_R + \bar{f}_R f_L)$$

Also Forbidden by Gauge Symmetry



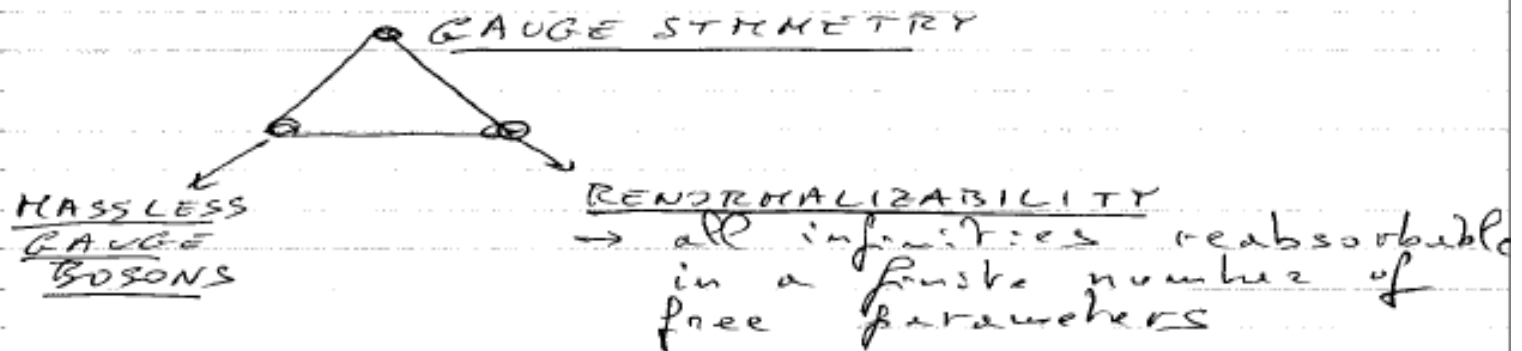
$$m_f = 0$$

$$\forall f$$

## All Particles Massless

⇒ interaction term:  $e \bar{\psi} \gamma^\mu \psi A_\mu$   
↑  
interaction electron-photon fields

$F_{\mu\nu} F^{\mu\nu} \rightarrow$  kinetic term for the photon



SPONTANEOUS SYMMETRY BREAKING

↓  $\mathcal{L}$  (Lagrangian) respects a symm.,  
but the vacuum of the theory  
does NOT respect it

ex:  $V = \mu^2 \phi \phi^* + \lambda (\phi \phi^*)^2$

$V$  invar. under  $\phi(x) \rightarrow e^{i\alpha} \phi(x)$

if  $\mu^2 < 0 \rightarrow \langle 0 | \phi | 0 \rangle \neq 0$

↓  
order param.  
of the phase transition

↘ vacuum is NOT  
 $U(1)$  invariant

(4)

$$G \xrightarrow[\text{spont. break.}]{} G'$$

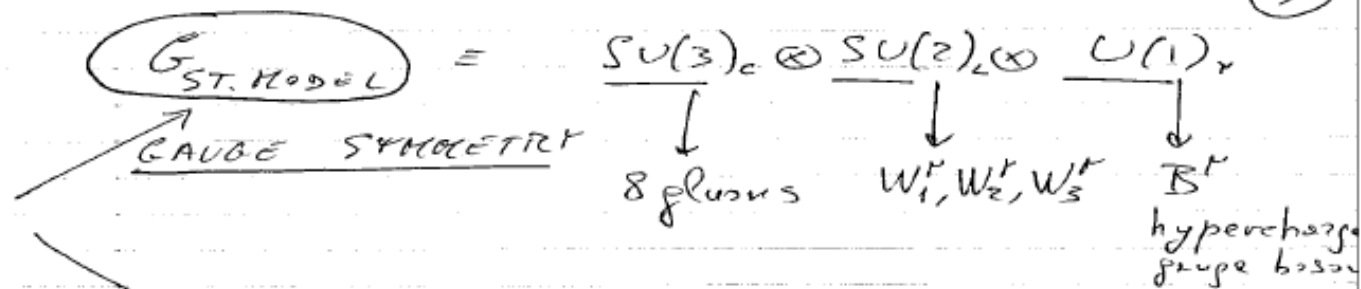
if  $G$  global  $\rightarrow$  generators of  $G/G'$   
 $\hookrightarrow$  Goldstone bosons  
 (massless scalars)

if  $\boxed{G \text{ LOCAL}} \rightarrow \boxed{\text{HIGGS MECHANISM}}$

Goldstone bosons "eaten up" by  
 the gauge bosons of  $G/G'$   
 to become their longitudinal  
 components

$\Rightarrow$  gauge bosons of  $G/G'$   
 become MASSIVE, their  
 mass being  $\propto \langle \phi / \phi \rangle = v$   
 and to their gauge coupl. const.

5



MATTER  
 FERMIONS

	$\begin{pmatrix} u \\ d \end{pmatrix}_L$	$(u^c)_L$	$(d^c)_L$	$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$(e^c)_L$
$SU(3)_c$	3	$\bar{3}$	$\bar{3}$	1	1
$SU(2)_L$	2	1	1	2	1
$U(1)_Y$	1/6	-2/3	+1/3	-1/2	1/2

$$Q = T_3 + Y$$

$$L_{\text{int}} = g_1 J^r B_r + g_2 J_i^r W_{r,i} + g_3 J_a^r A_{r,a}$$

$i = 1, 2, 3$        $a = 1, \dots, 8$

$$J_r^i = (\bar{u} \vec{\tau})_L \gamma_r \left( \frac{\tau_i}{2} \right) \begin{pmatrix} u \\ d \end{pmatrix}_L + (\bar{\nu}_e \vec{\tau})_L \gamma_r \left( \frac{\tau_i}{2} \right) \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$$

$$W_{\pm}^r = \frac{1}{\sqrt{2}} (W_1^r \mp i W_2^r)$$

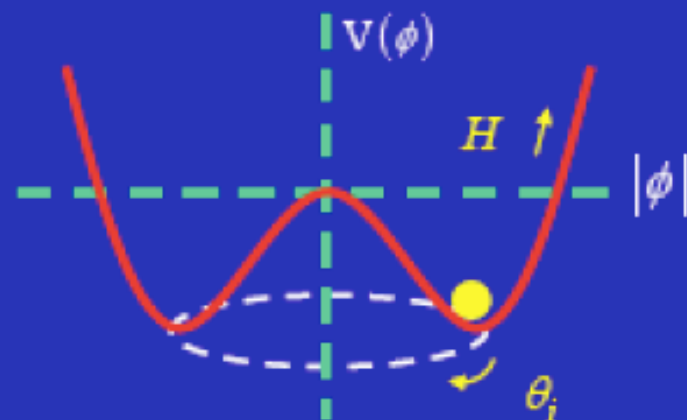
As long as  $G_{\text{SM}}$  unbroken

$\Rightarrow$  all gauge bosons + fermions  
 are MASSLESS



# Spontaneous Symmetry Breaking

$$\phi(x) \equiv \begin{pmatrix} \phi^{(+)}(x) \\ \phi^{(0)}(x) \end{pmatrix} = \exp \left\{ i \frac{\vec{\tau}}{2} \cdot \vec{\theta}(x) \right\} \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix}$$



$$\mathcal{L}(\phi) = (\mathbf{D}_\mu \phi)^\dagger \mathbf{D}^\mu \phi - \mu^2 \phi^\dagger \phi - h (\phi^\dagger \phi)^2 \quad ; \quad \mu^2 < 0$$

$$\mathbf{D}^\mu \phi = \left[ \partial^\mu - i g \mathbf{W}^\mu - i g' y_\phi B^\mu \right] \phi \quad ; \quad \mathbf{W}^\mu = \frac{\vec{\tau}}{2} \cdot \vec{W}^\mu$$

$$|\langle 0 | \phi^{(0)} | 0 \rangle| = \sqrt{\frac{-\mu^2}{2h}} \equiv \frac{v}{\sqrt{2}}$$

$$y_\phi = Q_\phi - T_3 = \frac{1}{2}$$

**Unitary Gauge:**  $(\mathbf{D}_\mu \phi)^\dagger \mathbf{D}^\mu \phi \xrightarrow{\vec{\theta} \rightarrow 0} \frac{1}{2} \partial_\mu H \partial^\mu H + \frac{g^2}{4} (v + H)^2 \left\{ W_\mu^\dagger W^\mu + \frac{1}{2 \cos^2 \theta_W} Z_\mu Z^\mu \right\}$



$$M_Z \cos \theta_W = M_W = \frac{1}{2} v g$$

**HIGGS MECHANISM**

# Bosonic Degrees of Freedom

Massless  $W^\pm, Z$

$$3 \times 2 \text{ polarizations} = 6$$

$\pm$

3 Goldstones  $\tilde{\theta}$

SSB



Massive  $W^\pm, Z$

$$3 \times 3 \text{ polarizations} = 9$$

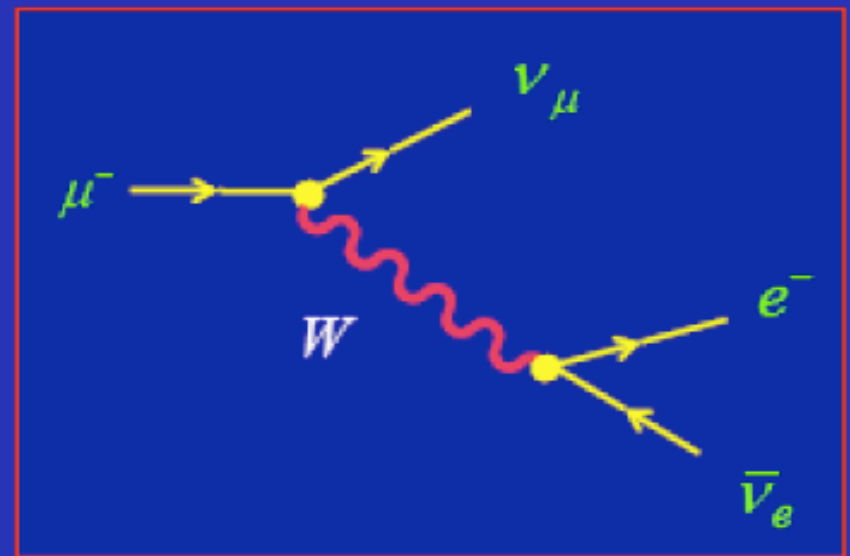
**SAME  
PHYSICS**

$$M_Z \cos \theta_W = M_W = \frac{1}{2} v g$$

$$M_Z = 91.1875 \text{ GeV} > M_W = 80.399 \text{ GeV} \Rightarrow \sin^2 \theta_W = 1 - \frac{M_W^2}{M_Z^2} = 0.223$$

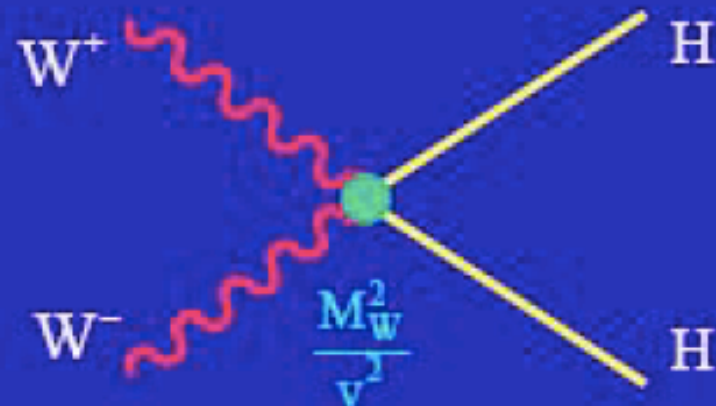
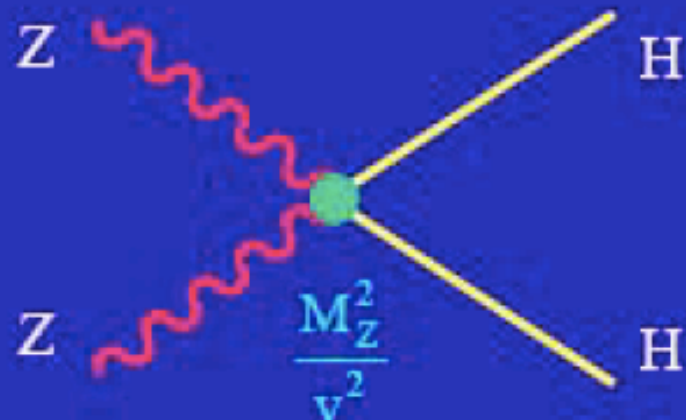
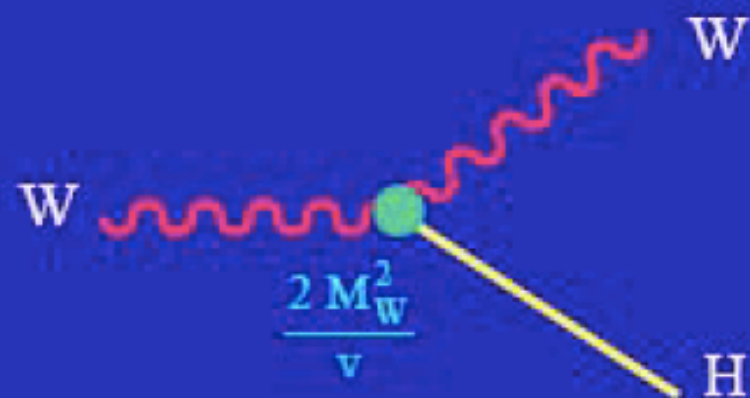
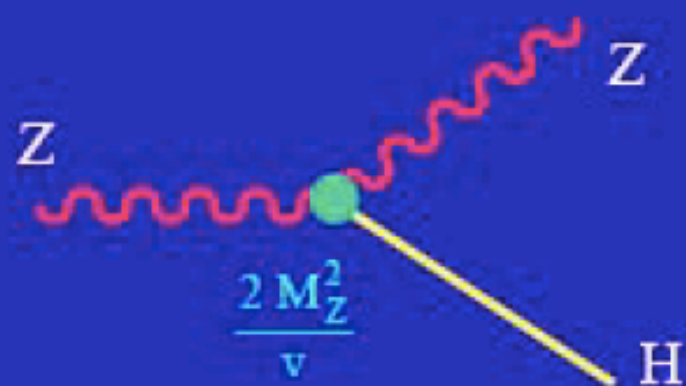
$$\frac{g^2}{M_W^2 - q^2} \approx \frac{g^2}{M_W^2} \equiv 4\sqrt{2} G_F$$

$$\frac{1}{\tau_\mu} \equiv \Gamma = \frac{G_F^2 m_\mu^5}{192 \pi^3}$$



$$\left. \begin{aligned} G_F &= 1.16637 \times 10^{-5} \text{ GeV}^{-2} \\ g &= \frac{e}{\sin \theta_W}, \quad M_W \end{aligned} \right\} \Rightarrow \begin{aligned} \sin^2 \theta_W &= 0.215 \\ v &= (\sqrt{2} G_F)^{-1/2} = 246 \text{ GeV} \end{aligned}$$

# Higgs Couplings $\propto$ Masses



$$v = \left( \sqrt{2} G_F \right)^{-1/2} = 246 \text{ GeV}$$

# FERMION MASSES

Scalar – Fermion Couplings allowed by Gauge Symmetry

$$\mathcal{L}_Y = (\bar{q}_u, \bar{q}_d)_L \left[ c^{(d)} \begin{pmatrix} \phi^{(+)} \\ \phi^{(0)} \end{pmatrix} (q_d)_R + c^{(u)} \begin{pmatrix} \phi^{(0)\dagger} \\ -\phi^{(+)\dagger} \end{pmatrix} (q_u)_R \right] + (\bar{\nu}_l, \bar{l})_L c^{(l)} \begin{pmatrix} \phi^{(+)} \\ \phi^{(0)} \end{pmatrix} l_R + \text{h.c.}$$

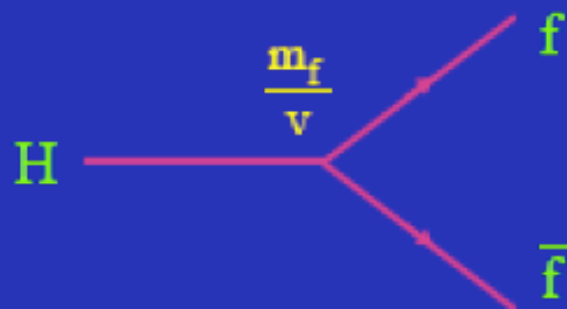


**SSB**

$$\mathcal{L}_Y = - \left( 1 + \frac{H}{v} \right) \left\{ m_{q_d} \bar{q}_d q_d + m_{q_u} \bar{q}_u q_u + m_l \bar{l} l \right\}$$

**Fermion Masses are  
New Free Parameters**

$$[m_{q_d}, m_{q_u}, m_l] = - [c^{(d)}, c^{(u)}, c^{(l)}] \frac{v}{\sqrt{2}}$$



**Couplings Fixed:**

$$g_{Hf\bar{f}} = \frac{m_f}{v}$$

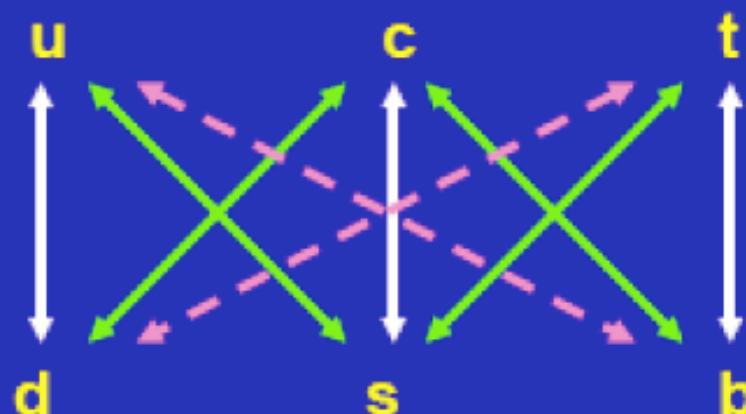
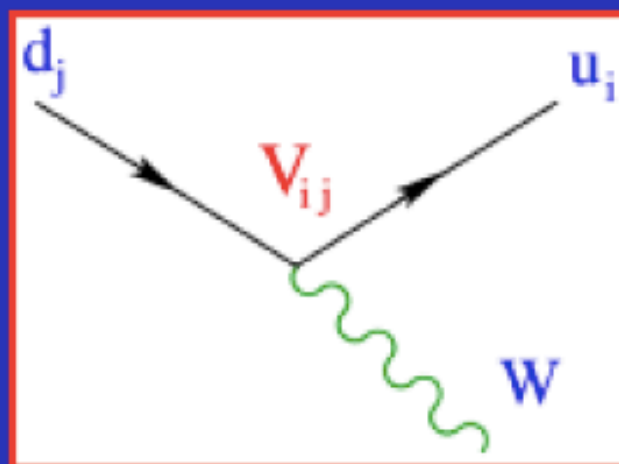


$$\mathcal{L}_{\text{NC}}^Z = - \frac{e}{2 \sin \theta_W \cos \theta_W} Z_\mu \sum_f \bar{f} \gamma^\mu [v_f - a_f \gamma_5] f$$

## Flavour Conserving Neutral Currents

$$\mathcal{L}_{\text{CC}} = - \frac{g}{2\sqrt{2}} W_\mu^\dagger \left[ \sum_{ij} \bar{u}_i \gamma^\mu (1-\gamma_5) \mathbf{V}_{ij} d_j + \sum_l \bar{\nu}_l \gamma^\mu (1-\gamma_5) l \right] + \text{h.c.}$$

## Flavour Changing Charged Currents



# QUARK MIXING MATRIX

- **Unitary**  $N_G \times N_G$  **Matrix:**  $N_G^2$  **parameters**

$$\mathbf{V} \cdot \mathbf{V}^\dagger = \mathbf{V}^\dagger \cdot \mathbf{V} = \mathbf{1}$$

- $2 N_G - 1$  **arbitrary phases:**

$$u_i \rightarrow e^{i\phi_i} u_i \quad ; \quad d_j \rightarrow e^{i\theta_j} d_j \quad \longrightarrow \quad V_{ij} \rightarrow e^{i(\theta_j - \phi_i)} V_{ij}$$



$V_{ij}$  **Physical Parameters:**

$$\frac{1}{2} N_G (N_G - 1) \quad \text{Moduli} \quad ; \quad \frac{1}{2} (N_G - 1) (N_G - 2) \quad \text{phases}$$

- $N_f = 2$  : 1 angle, 0 phases (Cabibbo)

$$V = \begin{bmatrix} \cos \theta_c & \sin \theta_c \\ -\sin \theta_c & \cos \theta_c \end{bmatrix} \quad \longrightarrow \quad \text{No } \cancel{CP}$$

- $N_f = 3$  : 3 angles, 1 phase (CKM)

$$c_{ij} \equiv \cos \theta_{ij} \quad ; \quad s_{ij} \equiv \sin \theta_{ij}$$

$$V = \begin{bmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i\delta_{13}} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i\delta_{13}} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i\delta_{13}} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta_{13}} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i\delta_{13}} & c_{23} c_{13} \end{bmatrix}$$

$$\approx \begin{bmatrix} 1 - \lambda^2/2 & \lambda & A \lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A \lambda^2 \\ A \lambda^3 (1 - \rho - i\eta) & -A \lambda^2 & 1 \end{bmatrix} + \mathcal{O}(\lambda^4)$$

$$\lambda \approx \sin \theta_c \approx 0.225 \quad ; \quad A \approx 0.81 \quad ; \quad \sqrt{\rho^2 + \eta^2} \approx 0.37$$

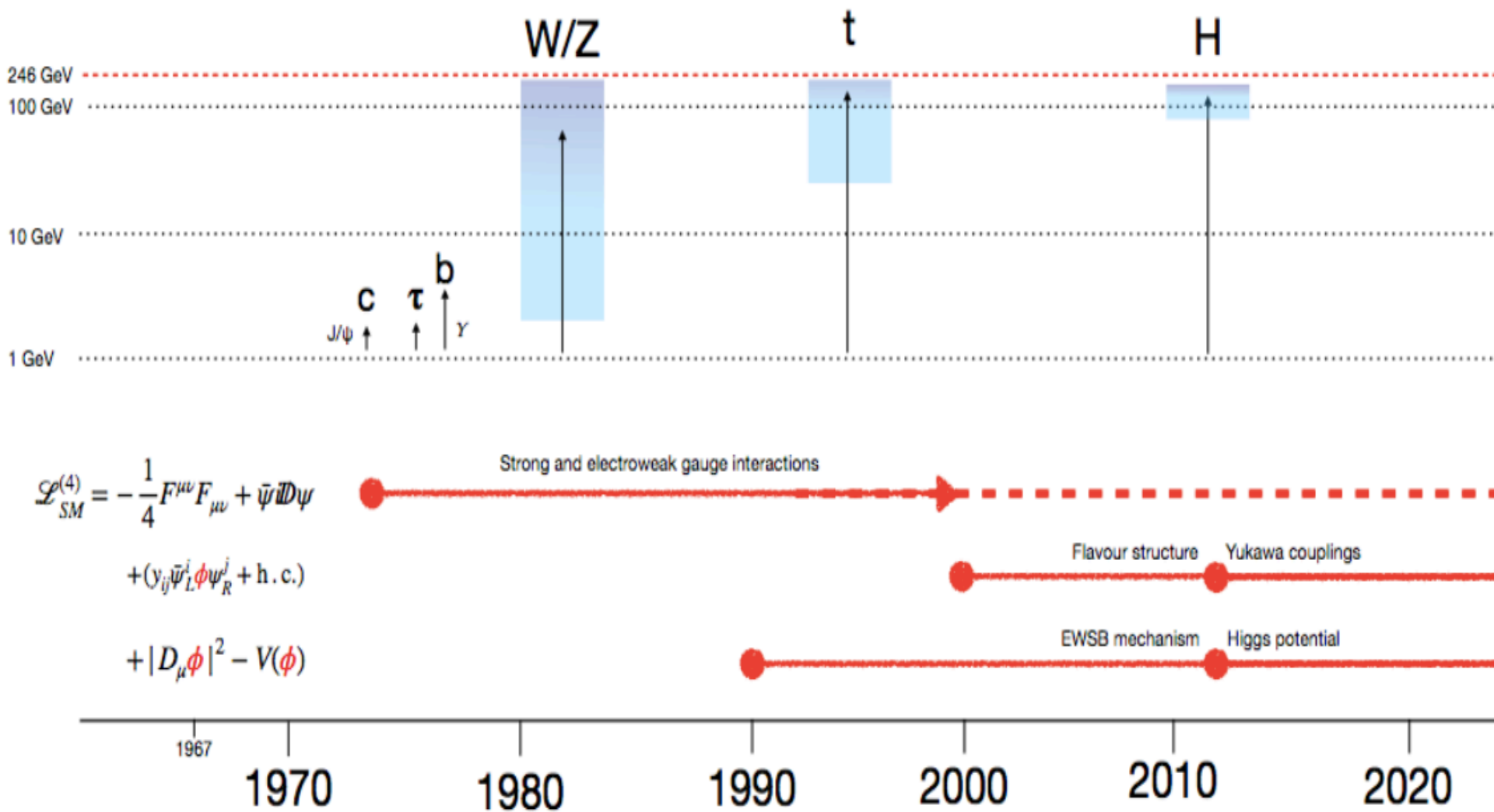
$$\delta_{13} \neq 0 \quad (\eta \neq 0) \quad \longrightarrow \quad \cancel{CP}$$

- $\mathcal{C}, \mathcal{P}$ : Violated maximally in weak interactions
- $\mathcal{CP}$ : Symmetry of nearly all observed phenomena
- Slight ( $\sim 0.2\%$ )  $\mathcal{CP}$  in  $K^0$  decays (1964)
- Sizeable  $\mathcal{CP}$  in  $B^0$  decays (2001)
- Huge Matter—Antimatter Asymmetry  
in our Universe  $\longrightarrow$  Baryogenesis

**$\mathcal{CPT}$  Theorem:**  $\mathcal{CP} \longleftrightarrow \mathcal{T}$

Thus,  $\mathcal{CP}$  requires:

- Complex Phases
- Interferences



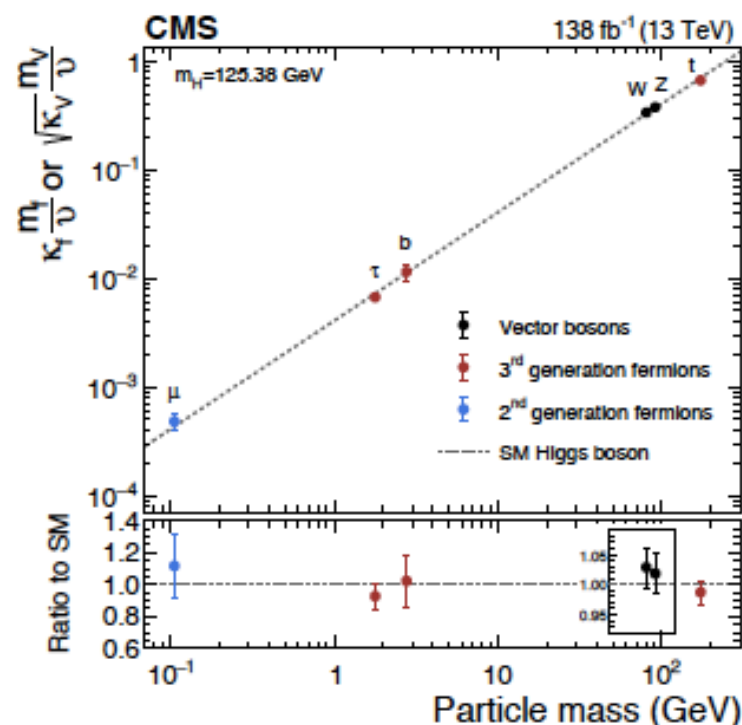
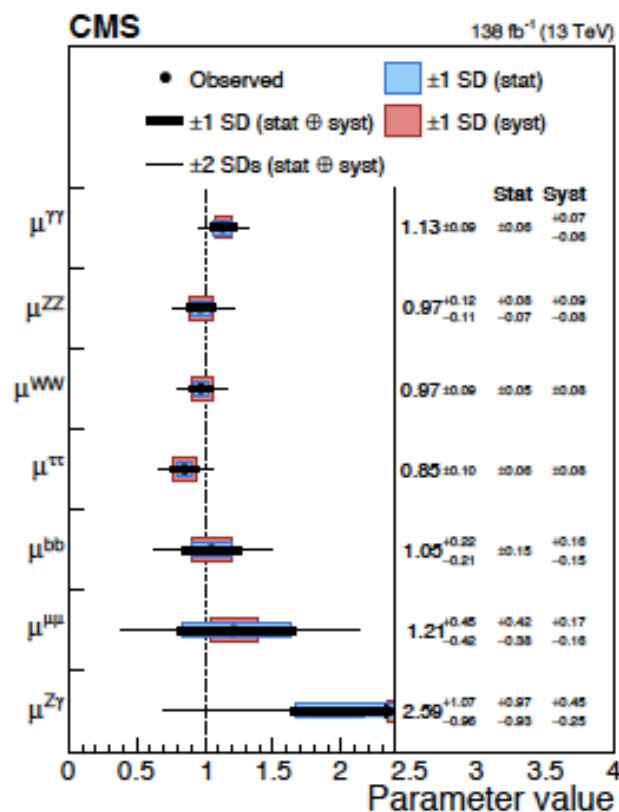


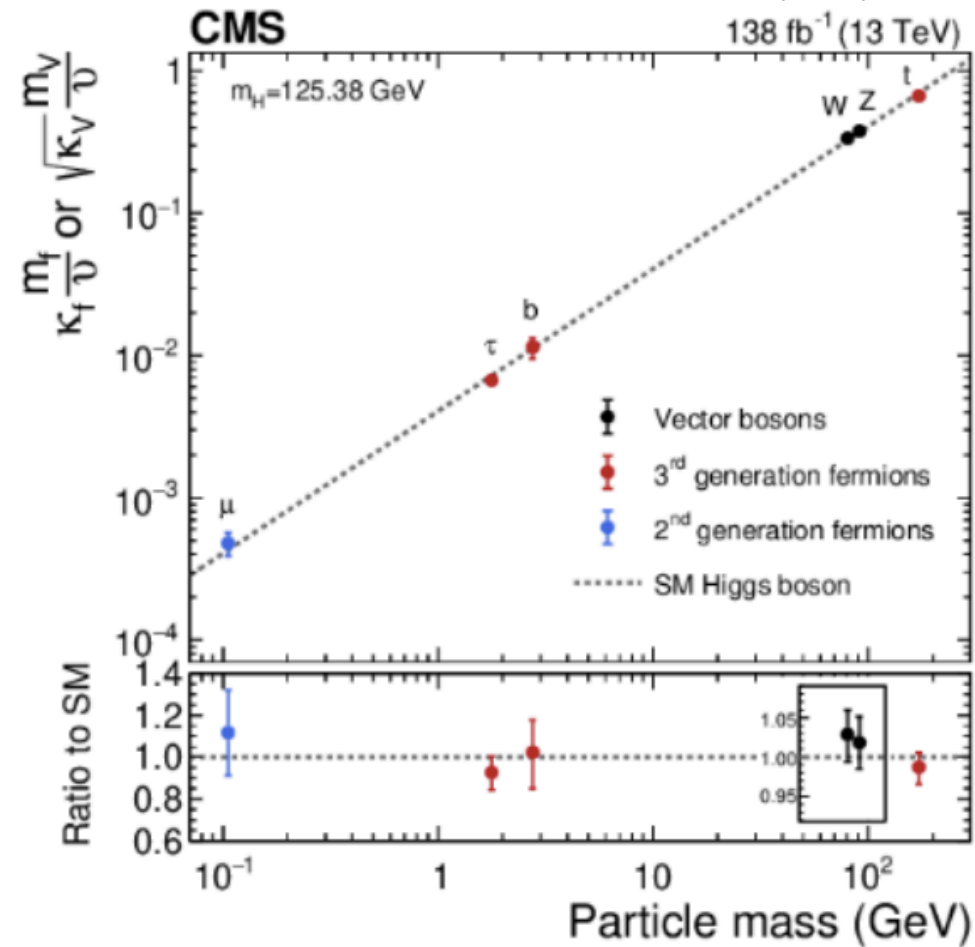
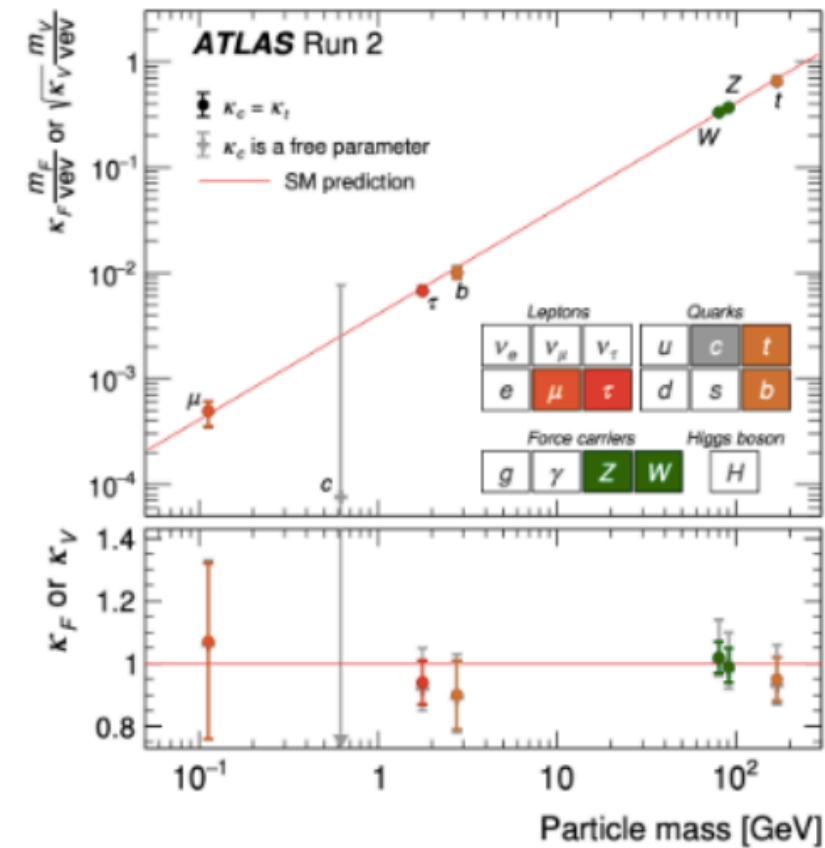
## The LHC legacy (so far)

- **Higgs Boson mass** (combined LHC Run 1 + 2 results of ATLAS and CMS)

$$m_H = 124.94 \pm 0.17 \text{ (stat.)} \pm 0.03 \text{ (syst.) GeV}$$

- **Higgs Boson couplings**  $\mu_i^f = \frac{\sigma_i \times BR^f}{(\sigma_i \times BR^f)_{SM}}$  (signal strengths)

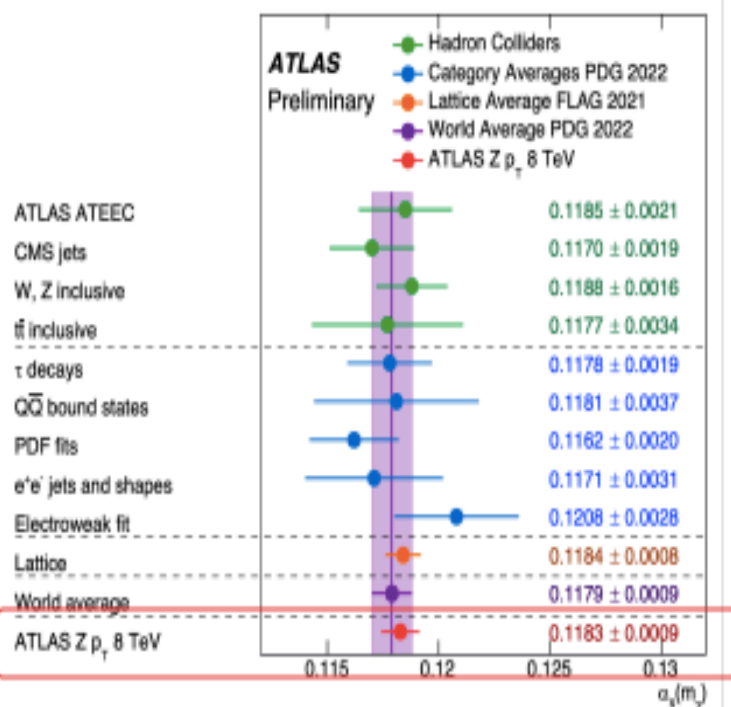




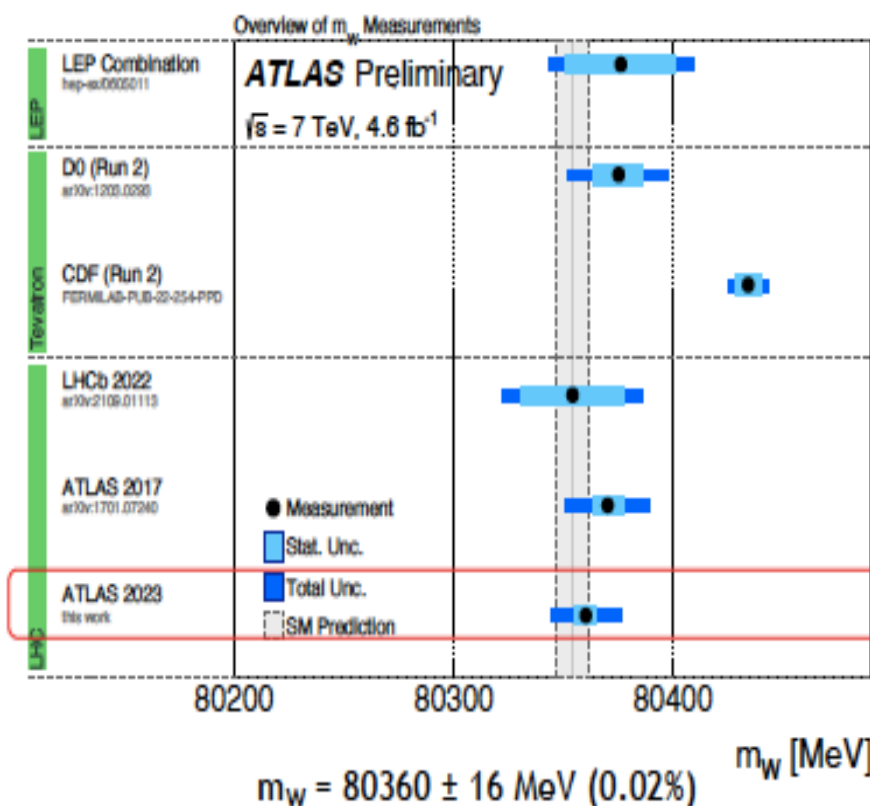
# Hadron colliders are **precision** machines

New precise measurement of strong coupling strength

New precise W mass measurement

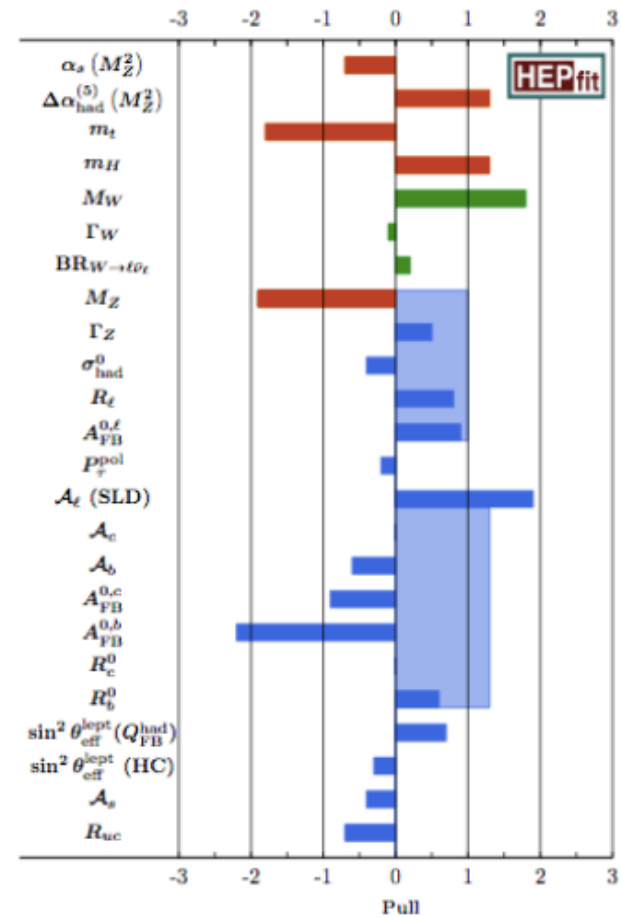
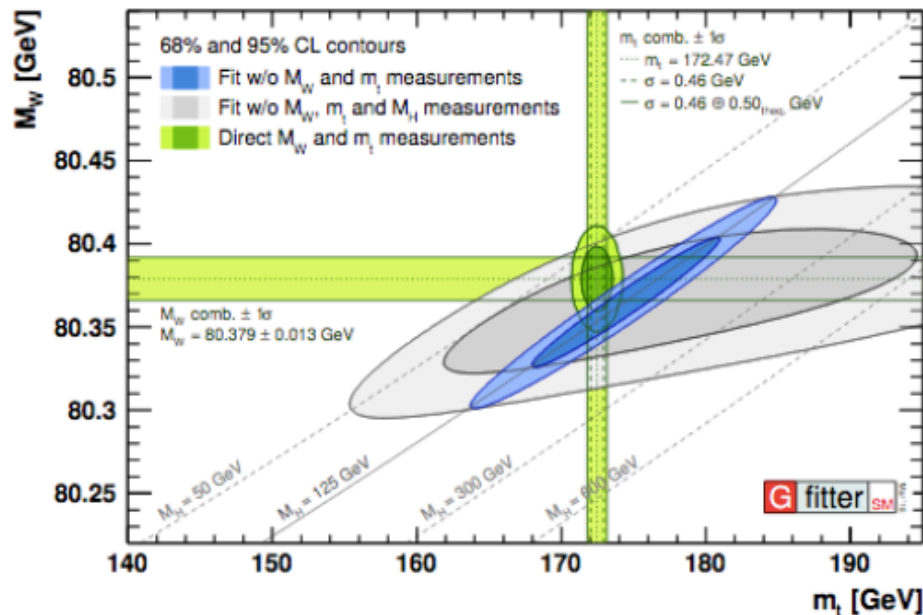


$$\alpha_s(m_Z) = 0.1183 \pm 0.0009 \quad (0.76 \%)$$

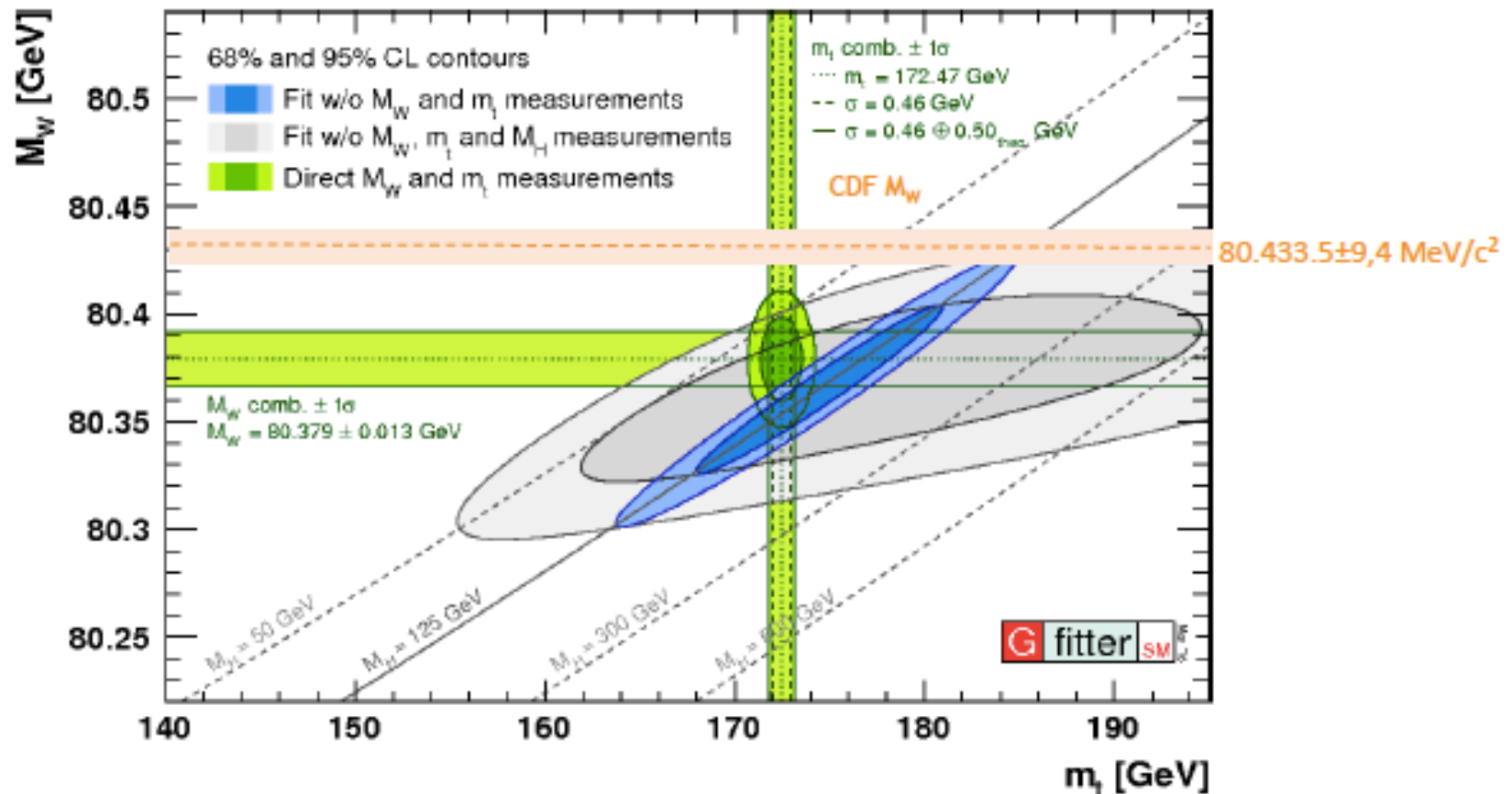


# Precision Observables

## ELW. PRECISION PHYSICS



# Standard Model Fit



EW Precision fit from 2018

<http://project-gfitter.web.cern.ch/project-gfitter/>



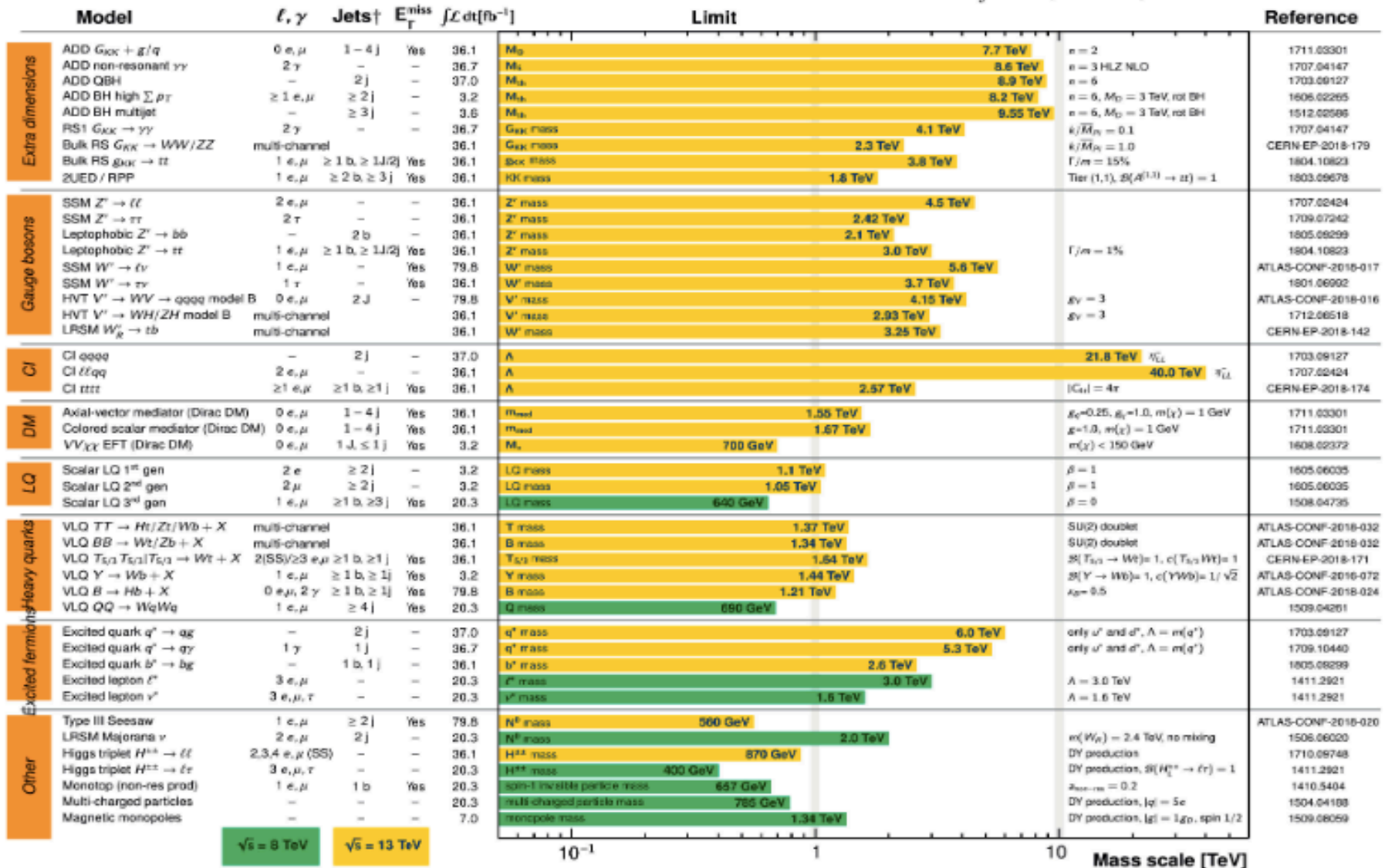
# BSM Direct Searches

High-Energy Frontier → produce and observe BSM new **heavy** particles

## ATLAS Exotics Searches\* - 95% CL Upper Exclusion Limits

Status: July 2018

ATLAS Preliminary  
 $\int \mathcal{L} dt = (3.2 - 79.8) \text{ fb}^{-1}$   
 $\sqrt{s} = 8, 13 \text{ TeV}$



\*Only a selection of the available mass limits on new states or phenomena is shown

# Several EXOTIC models ruled out!

March 2023



Resonances

Contact Interactions

Dark matter

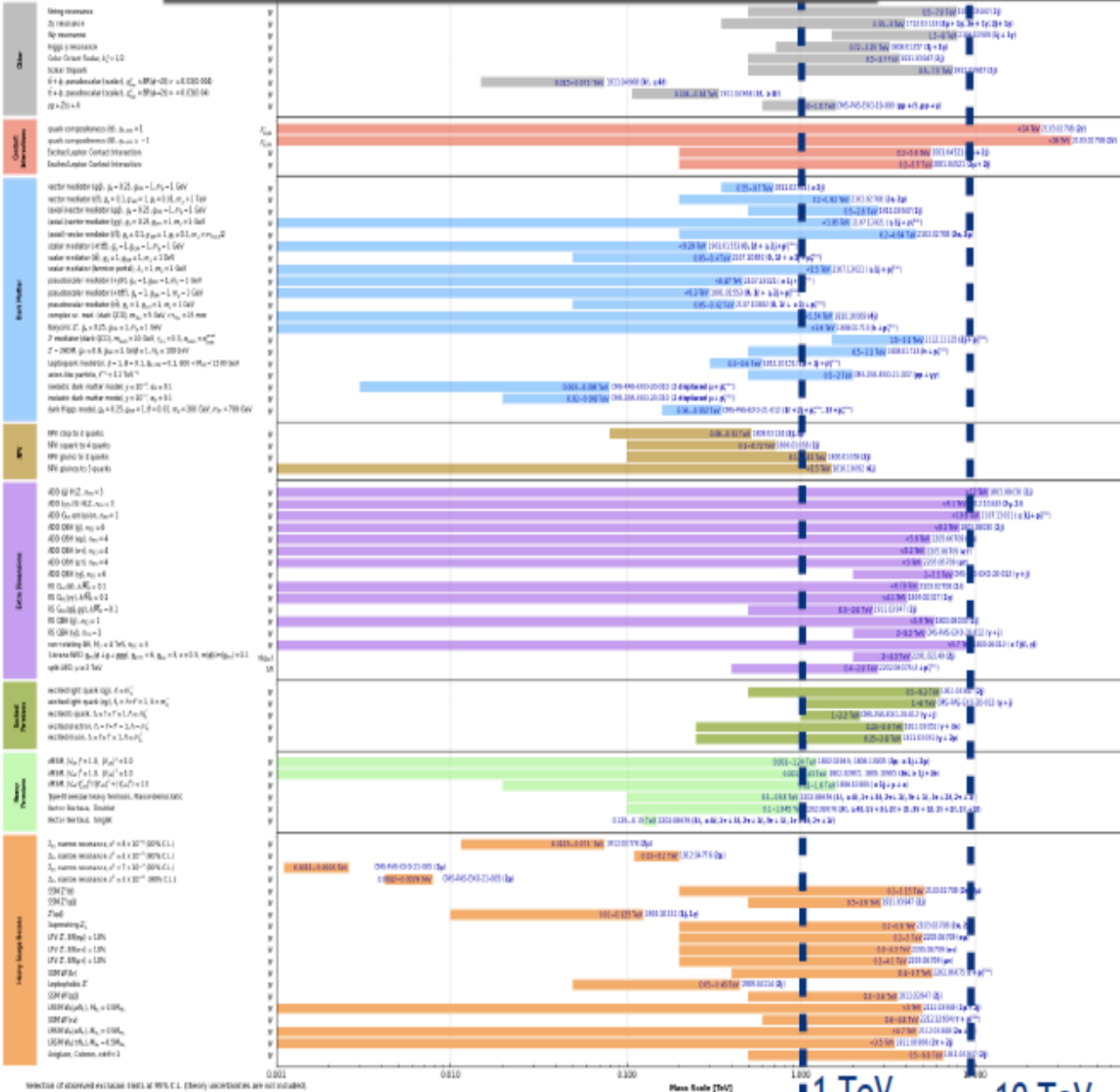
RPV

Extra Dimensions

Excited Fermions

Heavy Fermions

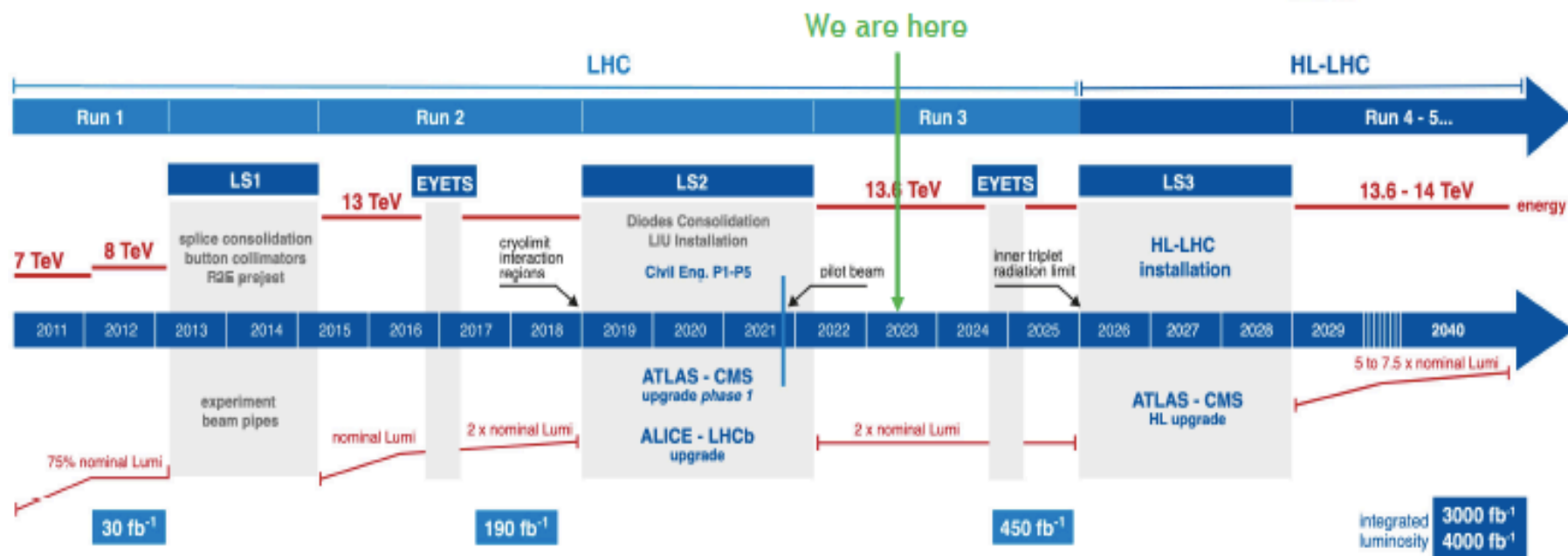
Heavy Bosons



# The LHC Schedule - Preparing for the future



## LHC / HL-LHC Plan



### HL-LHC TECHNICAL EQUIPMENT:



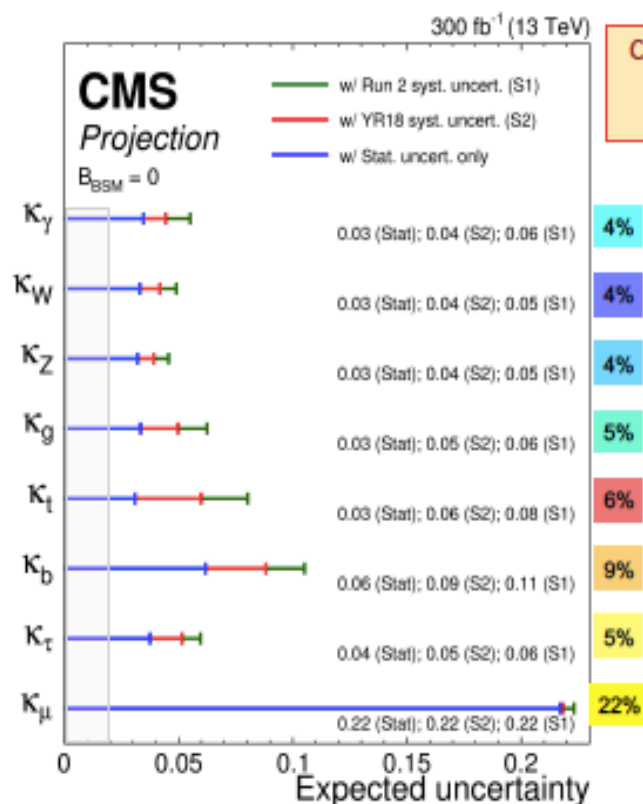
### HL-LHC CIVIL ENGINEERING:



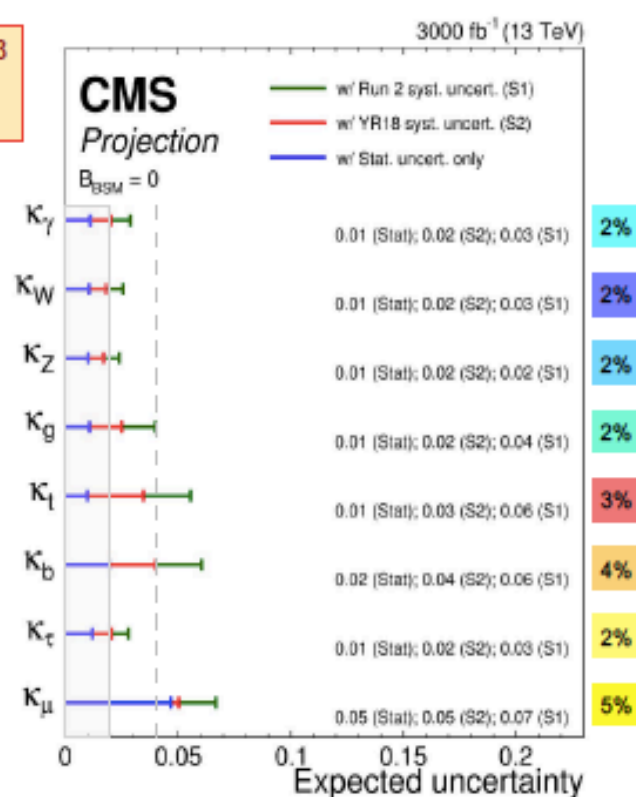
**New HL-LHC schedule updated to take into account current situation and delays in Run3 start.**

**So far LHC has delivered ~ 6% of the total planned integrated luminosity!**

# HL-LHC: expectations on Higgs



CMS End of Run-3  
13 TeV  
300 fb<sup>-1</sup>



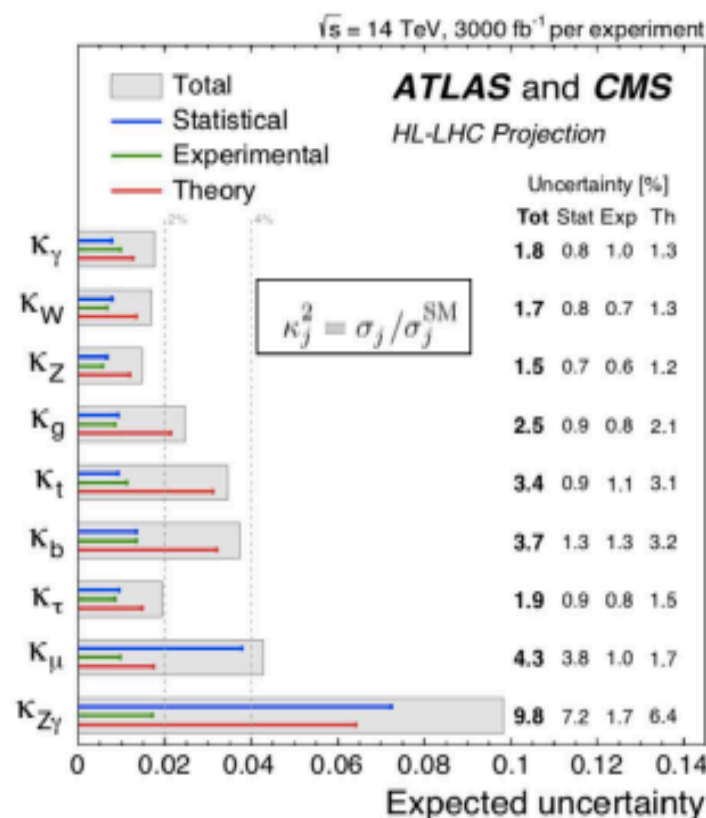
CMS HL-LHC  
13 TeV  
3 ab<sup>-1</sup>

Most Higgs couplings known to better than 4%, dominated by systematic uncertainties

# Physics potential of HL-LHC 1

Factor ~ 10 in data sample and improved detectors → significant increase in sensitivity for new physics and precise measurements

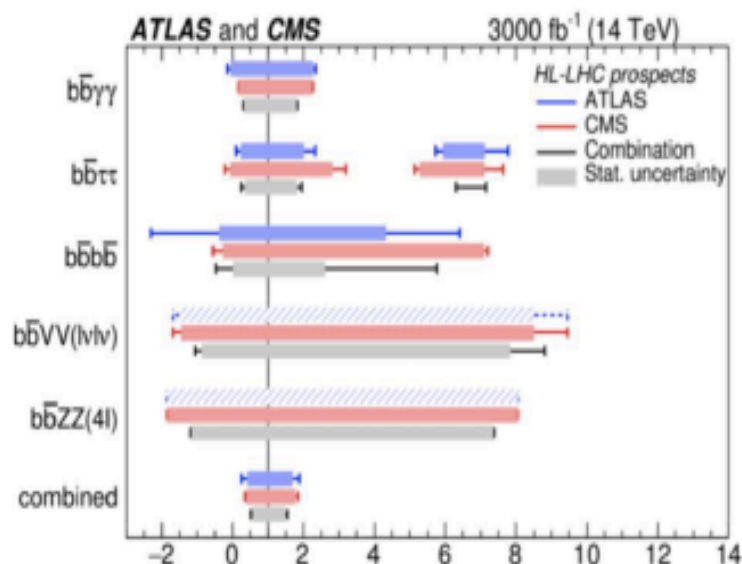
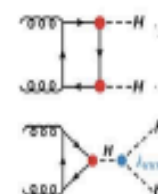
## Higgs couplings measurements



## First observation of HH production (~ 5σ level)

But only measure  $\lambda_3$  to +/-50%

$$\mathcal{L}_h = \frac{1}{2} m_H^2 H^2 + \lambda_3 H^3 + \lambda_4 H^4$$



Global fit assuming no BSM contributions to  $\Gamma_H$

- 2-3 more precise than at end of LHC
  - first 5σ observation of  $H \rightarrow Z$
- Experimental precision challenges theory!

$$0.52 < k_\lambda < 1.5 \text{ 95\% C.L.}$$

$k_\lambda = \lambda_{HHH} / \lambda_{HHH}^{SM}$



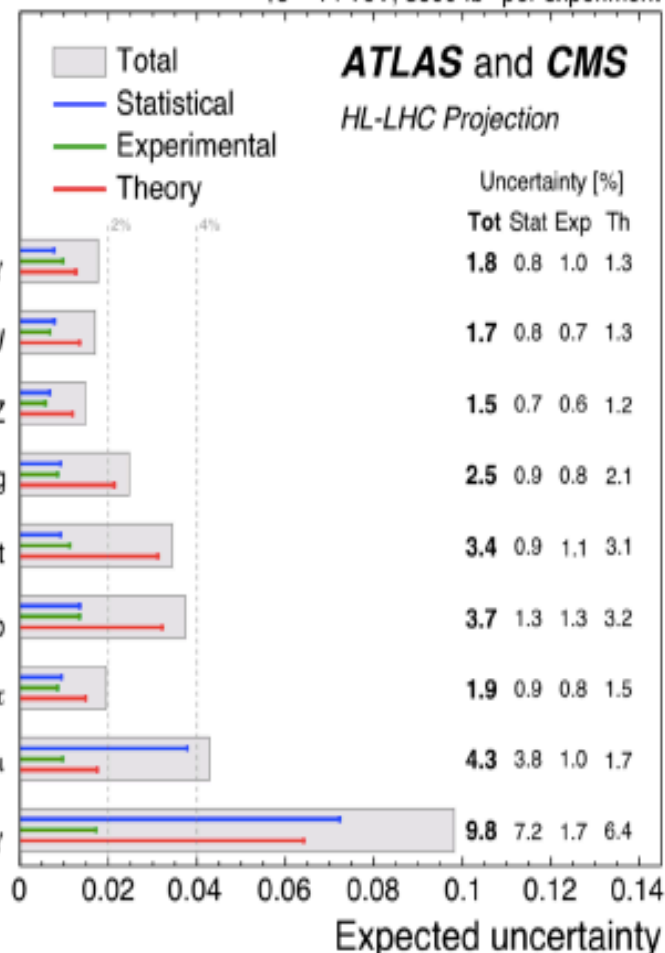
# Higgs @ (HL)-LHC

$\sqrt{s} = 14 \text{ TeV}$ , 3000 fb<sup>-1</sup> per experiment

	ATLAS - CMS Run 1 combination	ATLAS Run 2	CMS Run 2	Current precision	HL-LHC
$\kappa_\gamma$	13%	$1.04 \pm 0.06$	$1.10 \pm 0.08$	6%	1.8%
$\kappa_W$	11%	$1.05 \pm 0.06$	$1.02 \pm 0.08$	6%	1.7%
$\kappa_Z$	11%	$0.99 \pm 0.06$	$1.04 \pm 0.07$	6%	1.5%
$\kappa_g$	14%	$0.95 \pm 0.07$	$0.92 \pm 0.08$	7%	2.5%
$\kappa_t$	30%	$0.94 \pm 0.11$	$1.01 \pm 0.11$	11%	3.4%
$\kappa_b$	26%	$0.89 \pm 0.11$	$0.99 \pm 0.16$	11%	3.7%
$\kappa_\tau$	15%	$0.93 \pm 0.07$	$0.92 \pm 0.08$	8%	1.9%
$\kappa_\mu$	-	$1.06^{+0.25}_{-0.30}$	$1.12 \pm 0.21$	20%	4.3%
$\kappa_{Z\gamma}$	-	$1.38^{0.31}_{-0.36}$	$1.65 \pm 0.34$	30%	9.8%
$B_{inv}$		< 11 %	< 16 %	11%	2.5%

Nature 607,  
52-59 (2022)

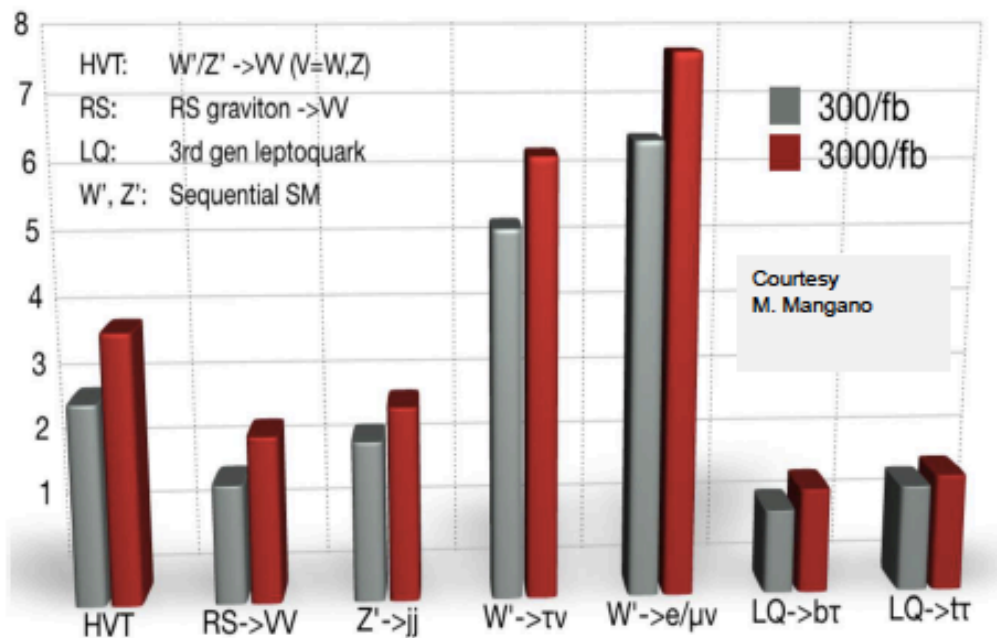
Nature 607,  
60-68 (2022)



TH Uncertainties dominant  
(assumed to be 1/2 of Run 2)

## Physics potential of HL-LHC 2

**5 $\sigma$  discovery mass reach (TeV) for new particles:**



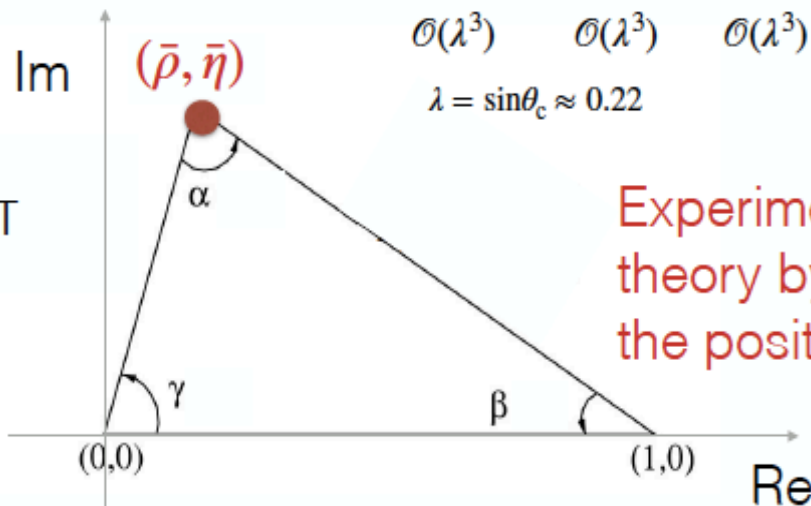
# Consistency tests of the CKM paradigm

- Unitarity of CKM matrix implies relations of the form  $\sum_i V_{ij} V_{ik}^* = \delta_{j,k}$ , with  $j \neq k$
- Each of these 6 unitarity constraints can be seen as the sum of 3 complex numbers closing a triangle in the complex plane

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\mathcal{O}(\lambda^3) \quad \mathcal{O}(\lambda^3) \quad \mathcal{O}(\lambda^3)$$

$$\lambda = \sin\theta_c \approx 0.22$$



Experiments test the theory by constraining the position of the apex

- $N_f = 2$  : 1 angle, 0 phases (Cabibbo)

$$V = \begin{bmatrix} \cos \theta_c & \sin \theta_c \\ -\sin \theta_c & \cos \theta_c \end{bmatrix} \quad \longrightarrow \quad \text{No } \cancel{CP}$$

- $N_f = 3$  : 3 angles, 1 phase (CKM)

$$c_{ij} \equiv \cos \theta_{ij} \quad ; \quad s_{ij} \equiv \sin \theta_{ij}$$

$$V = \begin{bmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i\delta_{13}} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i\delta_{13}} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i\delta_{13}} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta_{13}} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i\delta_{13}} & c_{23} c_{13} \end{bmatrix}$$

$$\longrightarrow \approx \begin{bmatrix} 1 - \lambda^2/2 & \lambda & A \lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A \lambda^2 \\ A \lambda^3 (1 - \rho - i\eta) & -A \lambda^2 & 1 \end{bmatrix} + \mathcal{O}(\lambda^4)$$

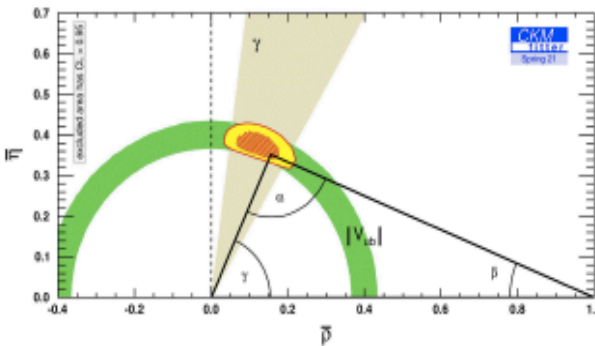
$$\lambda \approx \sin \theta_c \approx 0.225 \quad ; \quad A \approx 0.81 \quad ; \quad \sqrt{\rho^2 + \eta^2} \approx 0.37$$

$$\delta_{13} \neq 0 \quad (\eta \neq 0) \quad \longrightarrow \quad \cancel{CP}$$

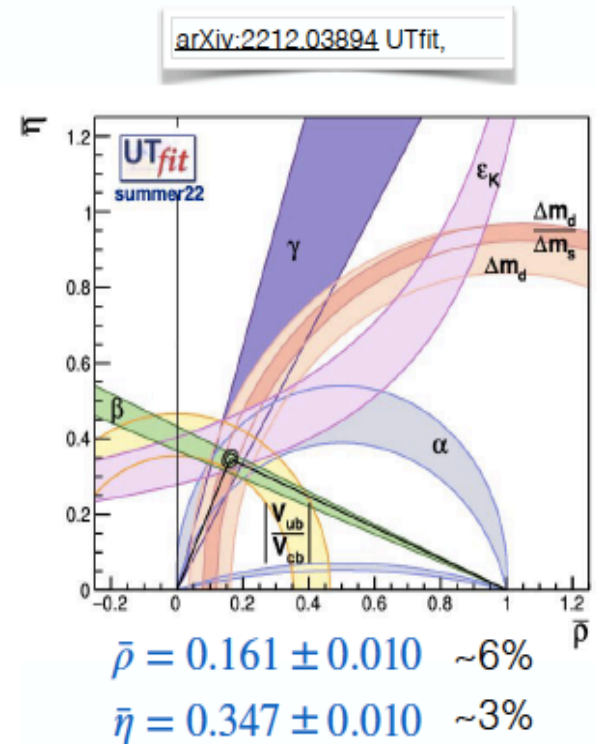
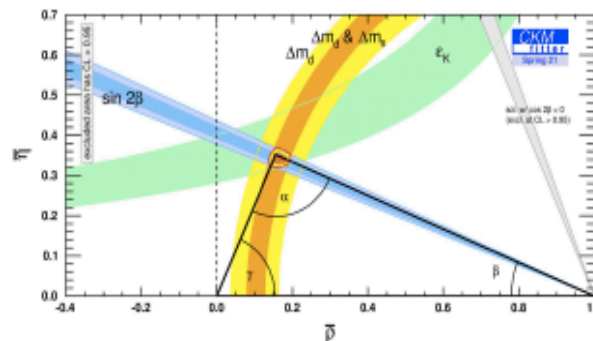
# Consistency tests of the CKM matrix

- At the current level of precision ( $\sim\%$ ), all measurements are consistent and intersect in the apex of the UT
- What is particularly noteworthy is the consistency of the tree-level determinations of CKM elements, with those obtained from meson-anti meson mixing

Tree-level observables



Loop observables



- New Physics effects (if there) are small!
- But... past examples show that it is unwise to think that few % is good enough

# On the peculiar value of $M_H$

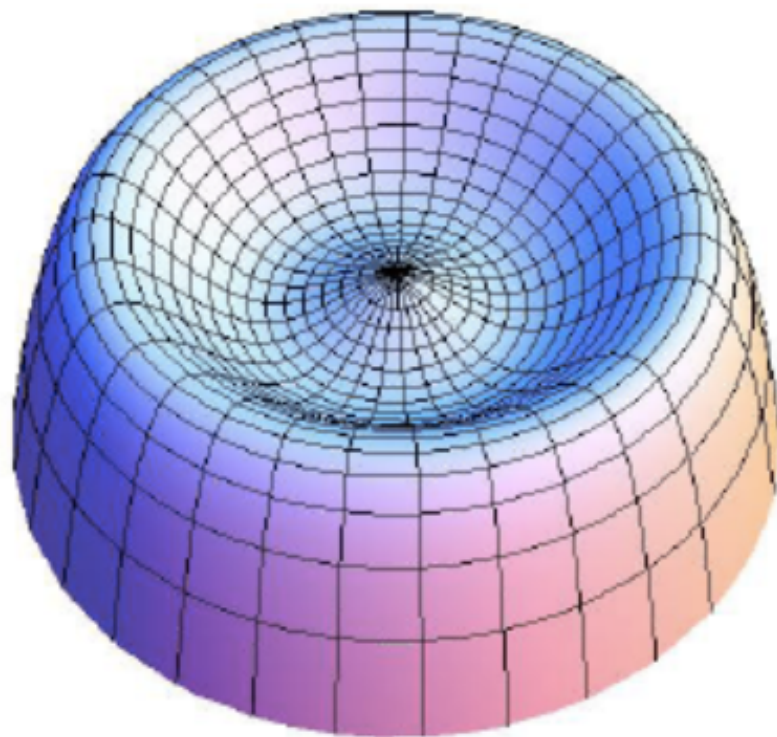
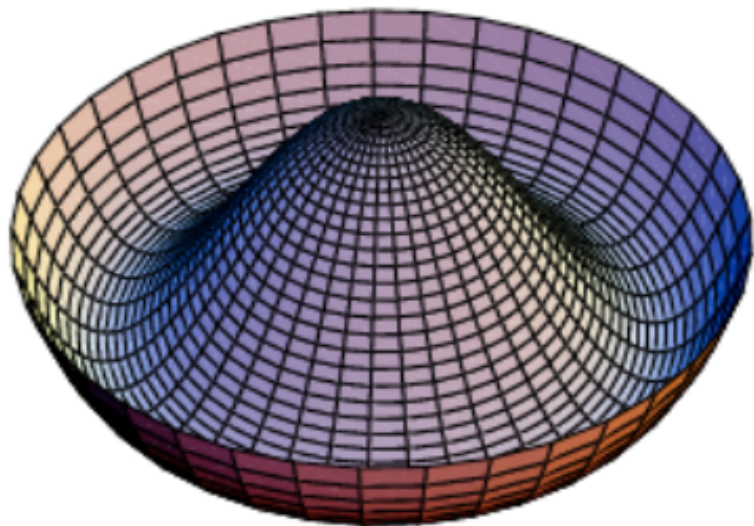
- For the SM to survive up to a very large scale,  $M_{\text{GUT}}$  or  $M_{\text{Planck}}$  :  $M_H$  in the fork 125 – 180 GeV, with  $\sim 125$  GeV just on the verge between stability and instability of the vacuum state where the SM sits
- For the existence of a (minimal) supersymmetric extension of the SM at the elw. scale, the lightest SUSY Higgs must have  $M_h < 130$  GeV ( for  $M_h > 120$  GeV, the radiative correction to  $M_h$  is  $\sim 50\%$  of the tree-level value)



**STABILITY**



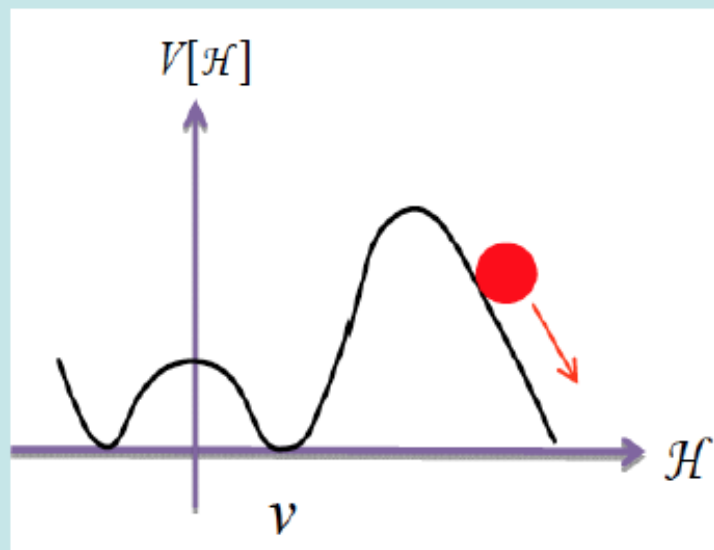
**INSTABILITY**



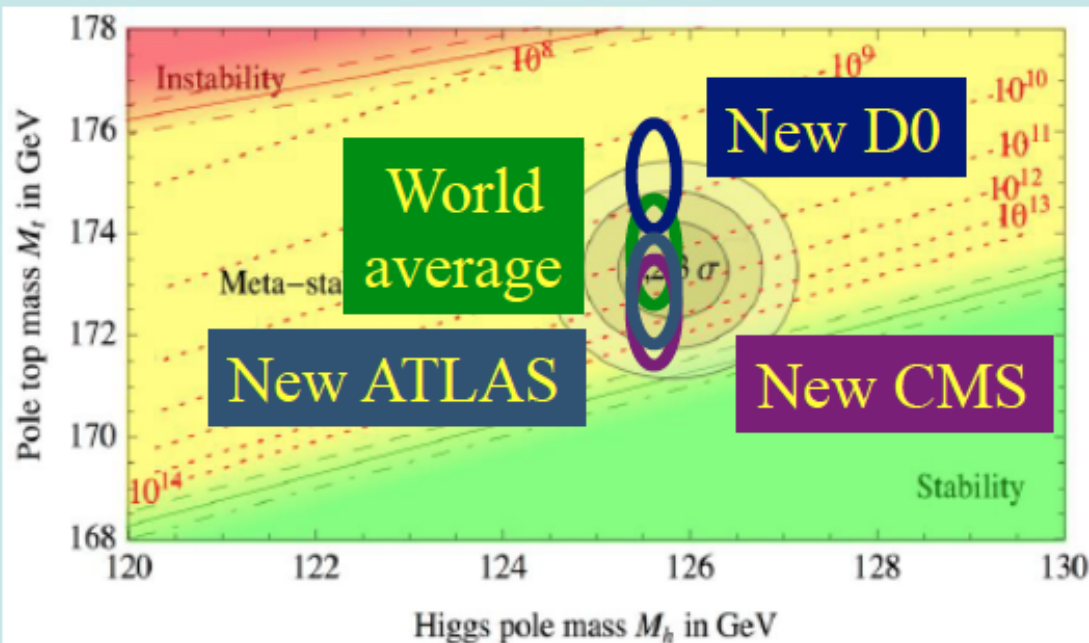
**ON THE IMPORTANCE OF PRECISELY  
MEASURING HIGGS and TOP MASSES**

# Vacuum Instability in the Standard Model

- Very sensitive to  $m_t$  as well as  $M_H$



J. Ellis, LP 2015

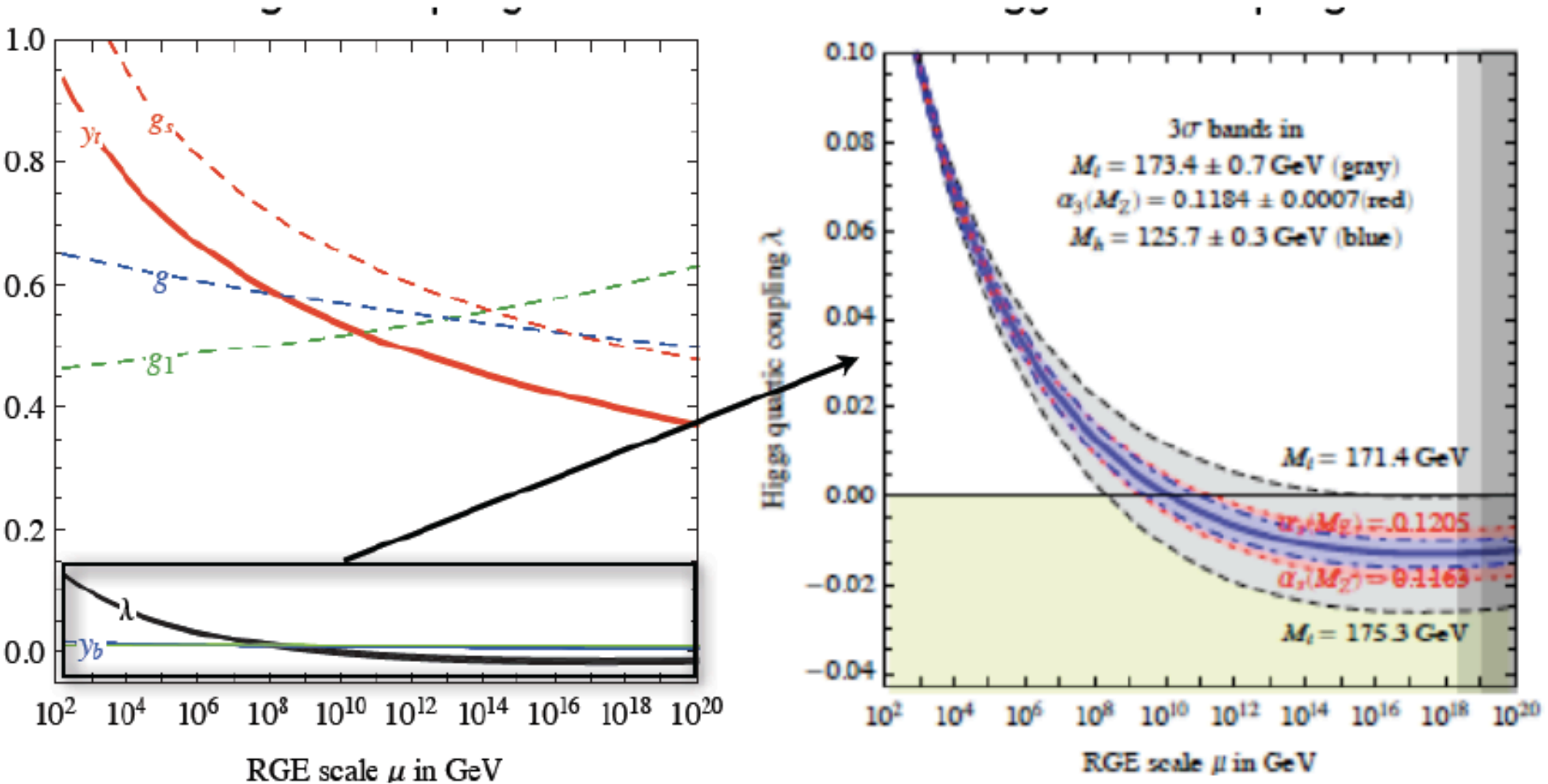


Buttazzo, Degrandi, Giardinò, Giudice, Sala, Salvio & Strumia, arXiv:1307.3536

- Instability scale.

$$\log_{10} \frac{\Lambda_I}{\text{GeV}} = 11.3 + 1.0 \left( \frac{M_h}{\text{GeV}} - 125.66 \right) - 1.2 \left( \frac{M_t}{\text{GeV}} - 173.10 \right) + 0.4 \frac{\alpha_3(M_Z) - 0.1184}{0.0007}$$

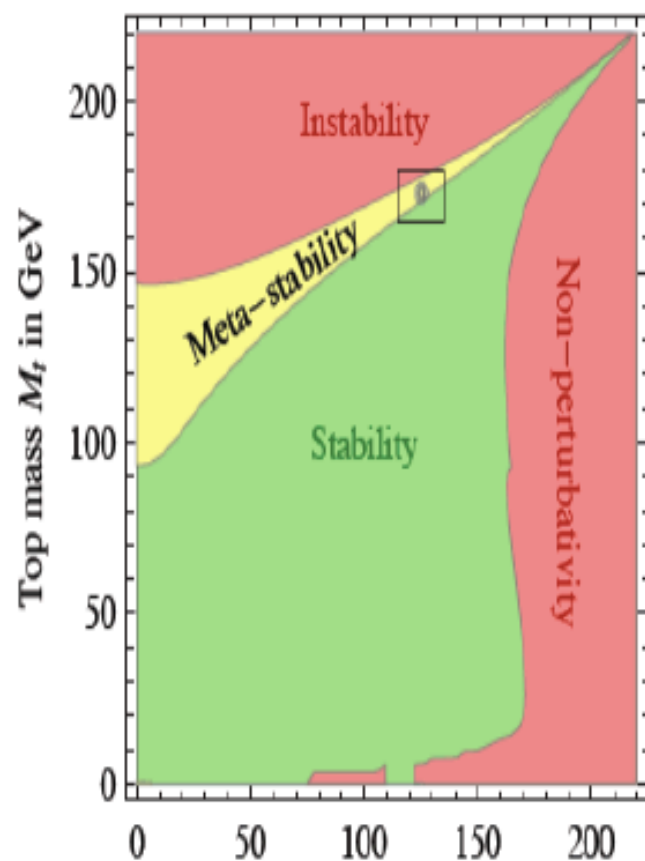
$$m_t = 173.3 \pm 1.0 \text{ GeV} \Rightarrow \log_{10}(\Lambda/\text{GeV}) = 11.1 \pm 1.3$$



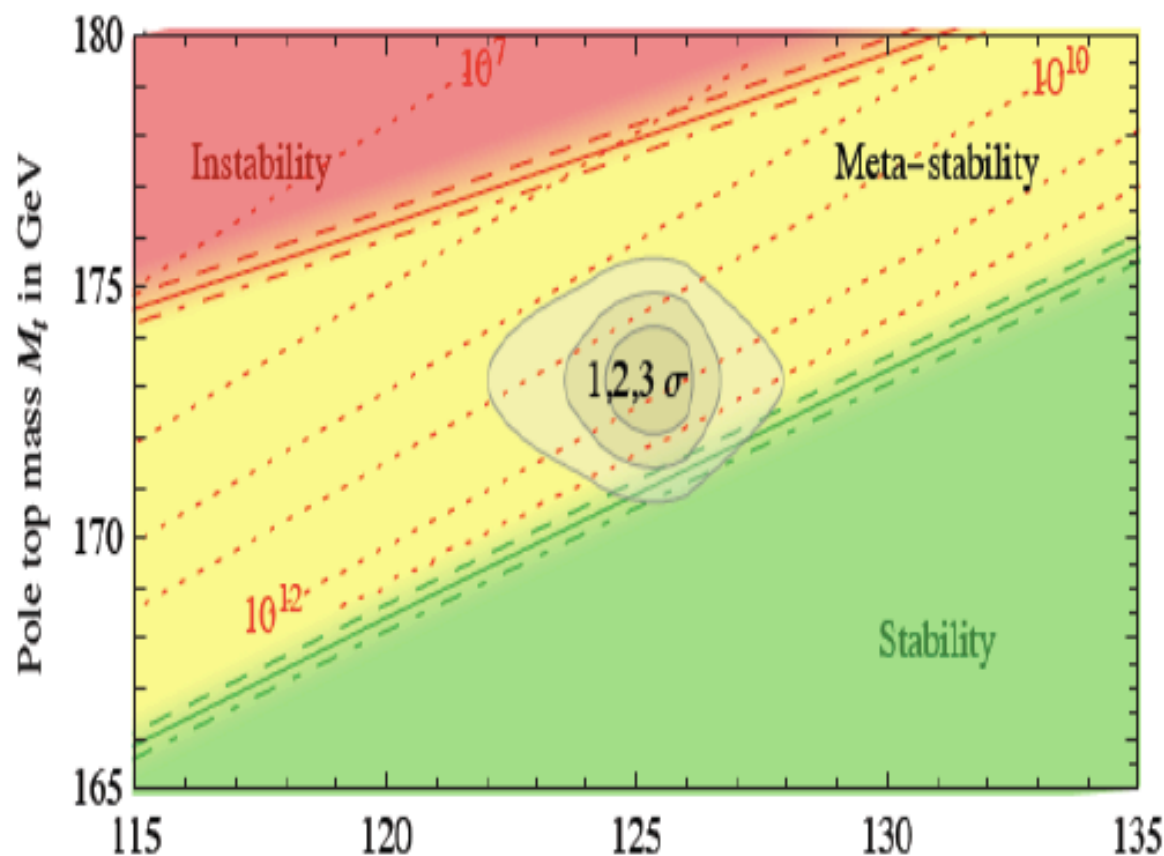
Buttazzo, Degrassi, Giardino, Giudice, Sala, Salvio, Strumia 2013

**For previous works:** Krive, Linde '76; Krasnikov '78; Maiani, Parisi, Petronzio '78; Cabibbo et al '79; Lindner '86; Altarelli, Isidori '96; Ellis et al 2009; Shaposhnikov et al '12; Elias-Miro' 'et a ''12; .....  
 Degrassi, Di Vita, Elias-Miro, Espinosa, Giudice, Isidori, Strumia '12

# LIVING DANGEROUSLY IN A “PROBABLE” METASTABLE UNIVERSE



Higgs mass  $M_h$  in GeV



Higgs mass  $M_h$  in GeV

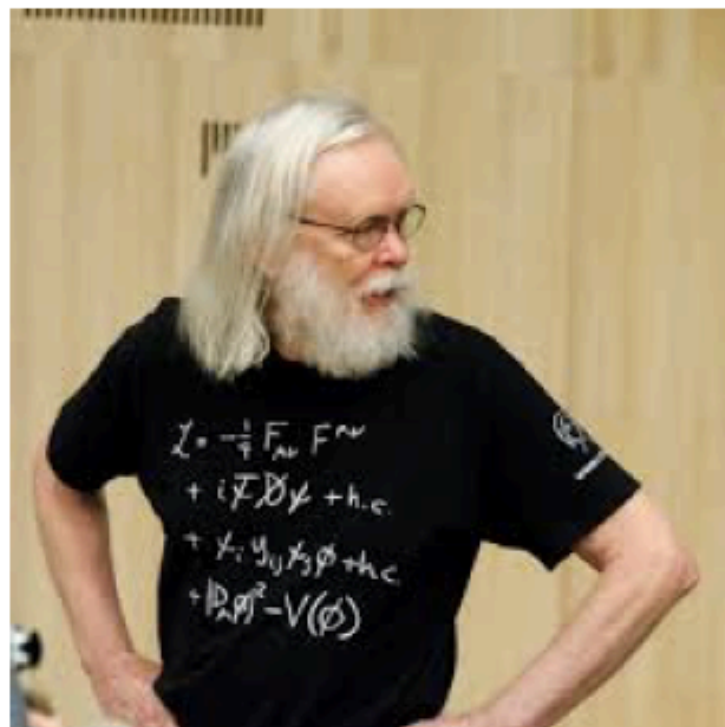
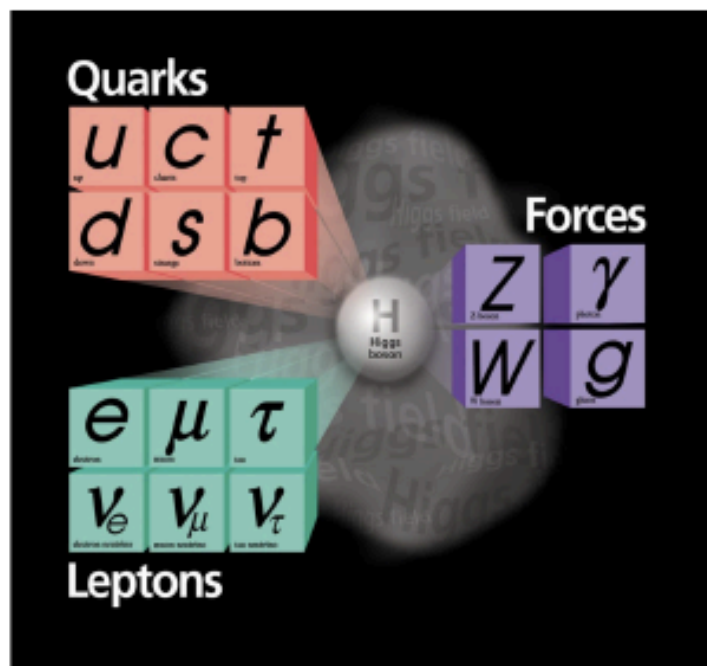
BEZUKOV, KALMIKOV, KNIEHL, SHAPOSHNIKOV 2012;

DEGRASSI, DI VITA, ELIAS-MIRO', ESPINOSA, GIUDICE, ISIDORI, STRUMIA 2012

**FIRST COMPLETE ANALYSIS NNLO OF THE SM HIGGS POTENTIAL**



The Standard Model (**SM**) is a remarkably simple Quantum Field Theory (**QFT**) that describes well all microscopic phenomena that we observe in **Nature**



The SM describes fundamental interactions among elementary particles

“This is short enough to write on a T-shirt!”

[John Ellis]